



From Halos to Galaxies. X. Decoding Galaxy SEDs with Physical Priors and Accurate Star Formation History Reconstruction

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Abstract

The spectral energy distribution (SED) of galaxies is essential for deriving fundamental properties like stellar mass and star formation history (SFH). However, conventional methods, including both parametric and nonparametric approaches, often fail to accurately recover the observed cosmic star formation rate (SFR) density due to oversimplified or unrealistic assumptions about SFH and their inability to account for the complex SFH variations across different galaxy populations. To address this issue, we introduce a novel approach that improves galaxy broadband SED analysis by incorporating physical priors derived from hydrodynamical simulations. Tests using IllustrisTNG simulations demonstrate that our method can reliably determine galaxy physical properties from broadband photometry, including stellar mass within 0.05 dex, current SFR within 0.3 dex, and fractional stellar formation time within 0.2 dex, with a negligible fraction of catastrophic failures. When applied to the Sloan Digital Sky Survey (SDSS) main photometric galaxy sample with spectroscopic redshift, our estimates of stellar mass and SFR are consistent with the widely used MPA-JHU and GSWLC catalogs. Notably, using the derived SFHs of individual SDSS galaxies, we estimate the cosmic SFR density and stellar mass density with remarkable consistency to direct observations up to $z \sim 6$. This demonstrates a significant advancement in deriving SFHs from SEDs that closely align with observational data. Consequently, our method can reliably recover observed spectral indices such as $D_n(4000)$ and $H\delta_A$ by synthesizing the full spectra of galaxies using the estimated SFHs and metal enrichment histories, relying solely on broadband photometry as input. Furthermore, this method is extremely computationally efficient compared to conventional approaches.

Unified Astronomy Thesaurus concepts: [Galaxy evolution \(594\)](#); [Galaxy properties \(615\)](#); [Galaxy stellar content \(621\)](#); [Galaxy colors \(586\)](#); [Galaxy ages \(576\)](#); [Galaxy masses \(607\)](#); [Star formation \(1569\)](#); [Galaxy quenching \(2040\)](#)

1. Introduction

The spectral energy distribution (SED) of galaxies encodes valuable information on a number of astrophysical processes of galaxy evolution, including gas inflow, star formation, gas outflow, and chemical enrichment. Extracting this information effectively from galaxy SEDs is a central challenge in understanding galaxy formation and evolution (see C. Conroy 2013

for a review). Traditional approaches typically involve forward-modeling the synthesized SED and adjusting model parameters to fit the observed data of a galaxy.

Deriving accurate star formation history (SFH) is one of the holy grails in SED fitting. Currently, the most widely used tools for obtaining SFH through SED fitting are Bagpipes (A. C. Carnall et al. 2018, 2019) and Prospector (J. Leja et al. 2017; B. D. Johnson et al. 2021). Despite its utility, the SED alone often fails to tightly constrain SFHs due to degeneracies among the effects of different stellar ages, metallicities, and dust extinction (S. M. Faber 1972; R. W. O'Connell 2009; G. Worthey et al. 1994; A. C. Carnall et al. 2019; C. Papovich et al. 2001), and

the outshining problem (i.e., young stars outshine their older counterparts, making it hard to constrain the old stellar populations from SEDs; C. Papovich et al. 2001). Observational limitations such as restricted wavelength coverage and low signal-to-noise ratios further complicate this issue.

Strong priors have been implemented on the SFHs to mitigate these challenges. Common approaches include parametric models like the exponential model ($\propto e^{-(t-t_0)/\tau}$), which is also known as the τ model and was widely used, perhaps for being the result of the closed-box model in which the star formation rate (SFR) is proportional to the gas mass (M. Schmidt 1959), which is assumed to be all in place at the beginning. This is not what happens to real galaxies, which start from small seeds and grow secularly by merging and gas accretion. Moreover, a single function is incapable of capturing features from recent starbursts and, to cope with this, additional burst components were incorporated (G. Kauffmann et al. 2003; S.-K. Lee et al. 2009). In an attempt to use more realistic SFHs, exponentially rising ($\propto e^{(t-t_0)/\tau}$) and delayed-exponential ($\propto (t-t_0)e^{-(t-t_0)/\tau}$) relations were introduced (S.-K. Lee et al. 2010; C. Maraston et al. 2010). Motivated by the coverage of observational parameter space of spatially resolved spectra from the Calar Alto Legacy Integral Field Area survey (S. F. Sánchez et al. 2012), a library of SFHs modeled as double-Gaussians plus random bursts was also applied (see S. Zibetti et al. 2017, 2020, as well as a high-redshift application in preparation). Motivated by the shape of the cosmic SFR density (P. Madau & M. Dickinson 2014), the Γ function was also used in the SED fits (Z. Lu et al. 2015; S. Zhou et al. 2020);, with others preferring the log-normal function or a double power law (see M. D. Gladders et al. 2013; L. E. Abramson et al. 2016; B. Diemer et al. 2017; A. C. Carnall et al. 2018). Finally, to increase flexibility, the combination of different functions is sometimes also applied (e.g., A. C. Carnall et al. 2018; Y. Han et al. 2023).

Clearly, there is no guarantee that galaxies have evolved following any of these simple analytical functions, which introduce arbitrary nonphysical priors (V. Simha et al. 2014; A. C. Carnall et al. 2019). Consequently, models based on the nonparametric SFHs have also been employed (R. Cid Fernandes et al. 2005; P. Ocvirk et al. 2006; K. Iyer & E. Gawiser 2017; J. Leja et al. 2017; P. Chauke et al. 2018; K. G. Iyer et al. 2019). Regarding the limited ability to constrain the detailed shape of star formation histories, these nonparametric methods adopted broad step functions with additional continuity requirements (M. Cappellari 2012; C. J. Walcher et al. 2015; J. Leja et al. 2017, 2019a). Although these nonparametric methods can successfully recover simple, artificially input SFHs (J. Leja et al. 2019a), realistic SFHs of actual galaxies are still challenging. Moreover, nonparametric methods suffer from various degeneracies, are computationally demanding, and require high-quality data to constrain SFHs.

A promising solution to these limitations involves leveraging physical priors from realistic galaxy formation models. These models, including empirical models (e.g., C. Conroy & R. H. Wechsler 2009; B. P. Moster et al. 2010; X. Yang et al. 2012; P. Behroozi et al. 2019; Y. Chen et al. 2021), semi-analytic models (e.g., S. D. M. White & C. S. Frenk 1991; G. Kauffmann et al. 1993; R. S. Somerville & J. R. Primack 1999; Q. Guo et al. 2011), and hydrodynamical simulations (e.g., N. Katz et al. 1992; R. A. Crain et al. 2009; A. Pillepich et al. 2018a; J. Schaye et al. 2015, 2023), should be realistic in

the sense that they are capable of reproducing various distribution functions and scaling relations for observed galaxies. Using these models' star formation and metal enrichment histories, it is possible to establish more physically grounded priors for inferring real galaxy histories from SEDs. Similar approaches have been put into practice in C. Pacifici et al. (2012), where they use a semi-analytic galaxy formation model as a prior to infer the physical properties from galaxy observables (see also K. Finlator et al. 2007; C. Pacifici et al. 2016). Recently, S. Zhou et al. (2022) incorporate the semi-analytic model of galaxy evolution processes, including inflow, outflow, star formation, and chemical enrichment (R. J. J. Talbot & W. D. Arnett 1971; B. M. Tinsley 1974; C. Chiosi 1980; B. M. Tinsley 1980; C. G. Lacey & S. M. Fall 1985; N. Bouché et al. 2010; S. J. Lilly et al. 2013; A. Dekel et al. 2013; A. Dekel & N. Mandelker 2014; Y.-j. Peng & R. Maiolino 2014; J. Dou et al. 2021; E. Wang & S. J. Lilly 2021, 2022), into the modeling of galaxy spectra.

This work utilizes the SFHs and metal enrichment histories of realistic galaxies in state-of-the-art hydrodynamical simulations to infer the physical properties of observed galaxies from their broadband photometry. We demonstrate that our method accurately recovers stellar mass, current SFR, and comprehensive SFHs of the test galaxy sample. When applied to actual galaxies, our method can deliver realistic SFHs and metal enrichment histories that can not only reproduce the general trends including cosmic SFR density and cosmic stellar mass density, but also recover several observed spectral indices, despite relying solely on broadband photometry.

The paper is structured as follows. The data and method are introduced in Section 2 and Section 3, respectively. The test and validation of our method are presented in Section 4. Then, we apply it to the observed galaxies and show the results in Section 5. Finally, we present the summary in Section 6. Throughout this paper, we adopt the initial mass function from G. Chabrier (2003) and the cosmology from Planck Collaboration et al. (2016), with $\Omega_{m,0} = 0.3075$, $\Omega_{\Lambda,0} = 0.6910$, and $h = 0.6774$.

2. Data

2.1. Simulation

The IllustrisTNG project encompasses a series of cosmological hydrodynamical simulations (F. Marinacci et al. 2018; J. P. Naiman et al. 2018; D. Nelson et al. 2018, 2019; A. Pillepich et al. 2018a, 2018b; V. Springel et al. 2018), simulating the evolution of galaxies from $z \sim 127$ to $z = 0$ with the moving-mesh code AREPO (V. Springel 2010) across three distinct volumes: $35 h^{-1} \text{Mpc}$ for TNG50, $75 h^{-1} \text{Mpc}$ for TNG100, and $205 h^{-1} \text{Mpc}$ for TNG300. Subgrid recipes are adjusted so that the stellar mass function, the stellar mass–black hole mass relation, the mass–size relation, the cosmic SFR density, the intragroup medium, the mass–metallicity relation, and the galaxy quenching match the observational results under the resolution of TNG100. Therefore, we employ TNG100 in our study, which offers a mass resolution of $1.4 \times 10^6 h^{-1} M_{\odot}$ for dark matter particles and $2.6 \times 10^5 h^{-1} M_{\odot}$ for gas cells. This study focuses on galaxies above $10^9 h^{-1} M_{\odot}$, so that each galaxy is finely sampled with more than 3800 stellar particles.

Dark matter halos within the simulation are identified using the friends-of-friends (FoF) algorithm (M. Davis et al. 1985). In each FoF halo, substructures are identified using the SUBFIND

algorithm (V. Springel et al. 2001; K. Dolag et al. 2009) using dark matter particles with gas and star particles attached. Each baryonic substructure is designated as a galaxy, and its dark matter counterpart as a subhalo. The subhalo with the minimal gravitational potential is defined as the central subhalo, and the corresponding galaxy is defined as the central galaxy. Others are classified as satellites. The merger histories are tracked using the SUBLINK algorithm (V. Rodriguez-Gomez et al. 2015), and the main progenitor of each subhalo is defined as the most massive one among all its progenitors in the branching point. (G. De Lucia & J. Blaizot 2007).

Mock Sloan Digital Sky Survey (SDSS) photometry for each galaxy is synthesized from the stellar particles' mass, metallicity, and age, with dust attenuation modeled using the distribution of metal-enriched gas (see D. Nelson et al. 2018 for details). The stellar population synthesis is performed using the FSPS code (C. Conroy et al. 2009; C. Conroy & J. E. Gunn 2010; B. Johnson et al. 2022), incorporating Padova isochrones and the MILES stellar library (P. Marigo & L. Girardi 2007; P. Marigo et al. 2008; P. Sánchez-Blázquez et al. 2006), with an initial mass function from G. Chabrier (2003).

2.2. Observational Data

The observational data set for this study is sourced from the SDSS main galaxy sample of the seventh data release, comprising approximately 210,000 galaxies within the redshift range of $0.02 < z < 0.085$ (D. G. York et al. 2000; K. N. Abazajian et al. 2009). The detailed selection criteria can be found in Y.-j. Peng et al. (2010). Each galaxy has five broadband photometric magnitudes (u, g, r, i, z) and a spectroscopic redshift. The rest-frame magnitudes are obtained by applying the K-correction procedure with the Python package KCORRECT (M. R. Blanton & S. Roweis 2007). We also calculate the V_{\max} factor (M. Schmidt 1968) for each galaxy using the KCORRECT package, assessing the maximum redshift at which it can be detected, given the survey's magnitude limits and fiber collision corrections from the NYU-VAGC catalog (M. R. Blanton et al. 2005).¹⁸

The galaxies are cross-matched with the MPA-JHU¹⁹ (G. Kauffmann et al. 2003; J. Brinchmann et al. 2004; S. Salim et al. 2007) and GSWLC (S. Salim et al. 2007, 2016, 2018), using a unique ID tuple (MJD, PLATE, FIBERID). From the MPA-JHU catalog, we obtain two critical spectral indices, $D_n(4000)$ and $H\delta_A$, as well as estimates of stellar mass and SFRs. It is important to note that these spectral indices are adjusted for sky-line contamination by fitting the continuum using the model outlined in G. Bruzual & S. Charlot (2003). It is also noteworthy that the spectral indices are only used for comparison in Section 5.3 and *not* an input in the SED-fitting procedure.

The estimation of stellar mass in the MPA-JHU catalog involves a two-part methodology: the central region covered by the fiber is evaluated using various spectral indices, while the outer region's mass is derived from five broadband magnitudes. SFRs in the MPA-JHU catalog are determined using $H\alpha$ luminosity for star-forming galaxies, and the SFR upper limits are provided by the $D_n(4000)$ index for quiescent galaxies and those with active galactic nuclei. Adjustments are made to convert the initial mass function from P. Kroupa (2001) to that

of G. Chabrier (2003), applying a conversion factor from P. Madau & M. Dickinson (2014) (-0.034 dex for stellar mass and -0.027 dex for SFR). In GSWLC, both the stellar mass and SFR for each galaxy are obtained by simultaneously fitting the multiband photometry from the IR to UV using the CIGALE code (S. Noll et al. 2009; M. Boquien et al. 2019) with the synthesis model from G. Bruzual & S. Charlot (2003) and the initial mass function in G. Chabrier (2003).

3. Method

We propose a novel method to infer the SFHs, metal enrichment histories, and stellar mass-to-light ratios of galaxies using broadband photometry, with simulated galaxies from hydrodynamical galaxy formation simulations as a prior. To begin with, we consider the broadband magnitudes and the corresponding colors for the i th simulated galaxy as

$$\begin{aligned} \tilde{\mathbf{m}}_i &= (\tilde{m}_{i,1}, \tilde{m}_{i,2}, \dots, \tilde{m}_{i,n}) \\ \tilde{\mathbf{c}}_i &= (\tilde{c}_{i,1}, \tilde{c}_{i,2}, \dots, \tilde{c}_{i,n-1}), \quad \tilde{c}_{i,j} \equiv \tilde{m}_{i,j+1} - \tilde{m}_{i,j} \end{aligned} \quad (1)$$

and similarly for the i th observed galaxy:

$$\begin{aligned} \mathbf{m}_i &= (m_{i,1}, m_{i,2}, \dots, m_{i,n}) \\ \mathbf{c}_i &= (c_{i,1}, c_{i,2}, \dots, c_{i,n-1}), \quad c_{i,j} \equiv m_{i,j+1} - m_{i,j}. \end{aligned} \quad (2)$$

We first consider the inference of the SFH of observed galaxies, as the metal enrichment history and the stellar mass-to-light ratio can be derived similarly. To proceed, we need to assume that the star formation histories and metal enrichment histories for real galaxies in our Universe are drawn from the same distributions as those of the simulated galaxies. This assumption is supported by the TNG100 simulation's ability to replicate key observational statistics, including the stellar mass function (see A. Pillepich et al. 2018a), the magnitude-color joint distribution function (see D. Nelson et al. 2018), the cosmic SFR density (see R. A. Crain & F. van de Voort 2023), the quiescent fraction of galaxies (see M. Donnari et al. 2021), and the star-forming main sequence (see M. Donnari et al. 2019). However, we emphasize that our method does not require the TNG100 simulation to be strictly correct, as in practice we use it as a set of template SFHs from which to choose the one that best reproduces the observables of individual galaxies. The likelihood model is then formulated as:

$$\mathcal{P}(\mathcal{H}|\mathbf{c}_i) \propto \mathcal{P}(\mathcal{H}) \times \mathcal{P}(\mathbf{c}_i|\mathcal{H}) = \mathcal{P}(\tilde{\mathcal{H}}) \times \mathcal{P}(\mathbf{c}_i|\tilde{\mathcal{H}}),$$

where \mathcal{H} and $\tilde{\mathcal{H}}$ represent the SFHs of observed and simulated galaxies, respectively. Here \mathbf{c}_i is the multiband color of the i th observed galaxy. We estimate the SFH for the i th observed galaxy as:

$$\begin{aligned} \hat{\mathcal{H}}_i(t) &= \frac{\sum_{j=1}^N w_{i,j} \tilde{\mathcal{H}}_j(t)}{\sum_{j=1}^N w_{i,j}} \\ w_{i,j} &\propto \prod_{k=1}^{n-1} \frac{1}{\sigma_k} \exp\left(-\frac{1}{2} \frac{(c_{i,k} - \tilde{c}_{j,k})^2}{\sigma_k^2}\right) \end{aligned} \quad (3)$$

where N represents the number of simulated galaxies and σ_k the uncertainty of the k th color. Similar methods can be employed to estimate the metal enrichment history and the stellar mass-to-light ratio. A similar approach has been applied to strong emission lines to infer the abundances and electron

¹⁸ <http://sdss.physics.nyu.edu/vagc/>

¹⁹ <https://wwwmpa.mpa-garching.mpg.de/SDSS/DR7/>

temperatures in H II regions (the counterpart method proposed by L. S. Pilyugin et al. 2012).

To assess the reliability of our estimates, we calculate the weighted standard deviation of the prior physical properties as the uncertainty, effectively treating this as the probability density function.

However, as TNG simulations may not perfectly represent the observed galaxies' distribution, minor discrepancies may lead to biases in physical properties for outliers in the color space. To quantify this, we define a weighted distance metric:

$$\mathcal{D}_i = \frac{\sum_j w_{i,j} \sum_{k=1}^{n-1} (c_{i,k} - \tilde{c}_{j,k})^2}{\sum_j w_{i,j}} \quad (4)$$

This parameter quantifies the weighted average distance between the i th observed galaxy and the surrounding simulated galaxies in the color space. Galaxies with $\mathcal{D}_i \geq 0.19$ are considered poorly sampled and are excluded from further analysis, affecting approximately 5% of galaxies in our SDSS DR7 sample. This empirical threshold is chosen because it is the highest \mathcal{D}_i in the self-consistency test; thus, it can somehow be used to describe the limitation of our method.

4. Testing on the IllustrisTNG Simulation

We first test the performance of our method on the simulated galaxies in the IllustrisTNG simulation before we apply it to the observational galaxy sample. For each simulated galaxy, it is possible to obtain its SFH, metal enrichment history, and stellar mass-to-light ratio from the stellar particles it contains. We then apply a self-consistency test with all other simulated galaxies as priors to estimate these properties for the i th galaxy. The accuracy of our method was quantified by comparing these estimates to the properties derived directly from the galaxies' stellar particles.

We first estimate the r -band mass-to-light ratio and derive the stellar mass. The results, shown in Figure 1, indicate that our method reliably estimates stellar masses, with the majority of galaxies exhibiting less than 0.3 dex deviation from their true values, and a scatter of less than 0.05 dex. We also test another approach based on the z -band mass-to-light ratio, which provides similar results.

Similarly, Figure 2 illustrates the method's robustness in accurately estimating the SFRs averaged over three different timescales, which correspond to different observation probes: 10 Myr for indicators based on the H α emission, 100 Myr for indicators based on the UV luminosity or IR and far-IR luminosities, and 1 Gyr for indicators based on $D_n(4000)$ index. Note that we only present the SFR estimates for galaxies that are classified as star-forming, defined as those with $\log \text{SFR} > \log M_* \times 0.76 - 8.1$. This threshold is derived by shifting the best-fit star-forming main sequence from A. Renzini & Y. Peng (2015) downward by approximately 0.5 dex. Here, one can see that the standard deviation is about 0.3 dex for the SFR smoothed on these three timescales. Notably, the resolution limit of TNG100 ($\sim 10^9 M_\odot$ for baryonic mass) suggests a minimally detectable SFR of approximately $0.1 M_\odot \text{ yr}^{-1}$ over a 10 Myr timescale for particle-based methods.

Finally, Figures 3 and 4 show the comparison of star formation histories. The SFHs are parameterized with the

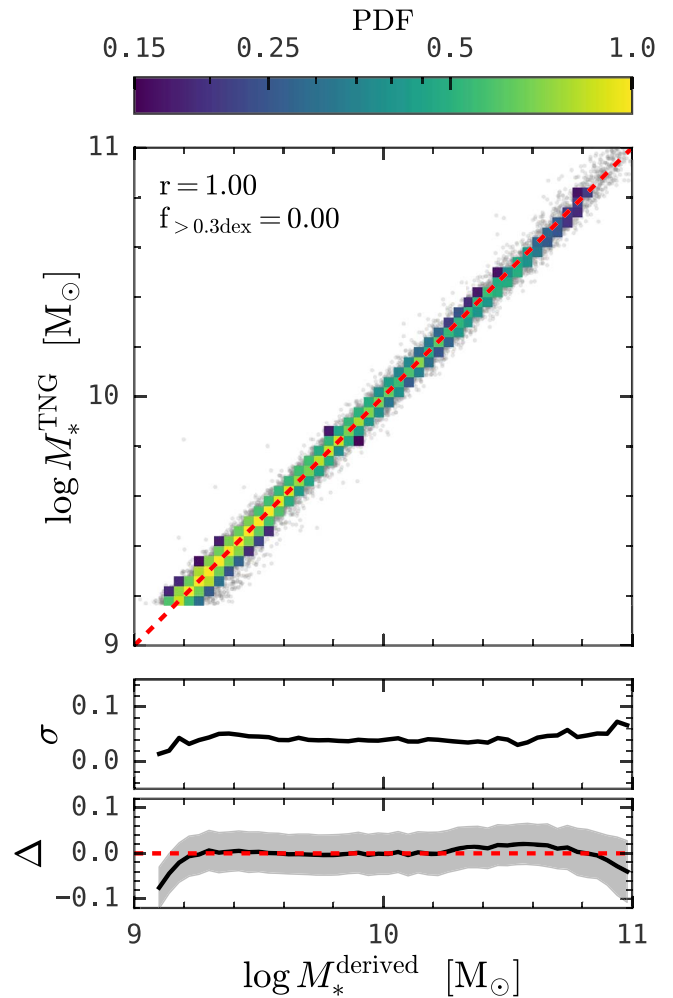


Figure 1. Comparison of estimated stellar mass using our method against actual values in TNG100. Individual galaxies are represented by gray dots, and the heat map illustrates the normalized probability distribution. The one-to-one reference line is shown as a red dashed line. Spearman's rank correlation coefficient (r) and the fraction of outliers ($f_{>0.3 \text{ dex}}$) are presented in the top-left corner. The lower two panels show the standard deviation and the systematic bias as a function of estimated stellar mass. The gray-shaded region in the bottom panel shows the median uncertainty. This figure demonstrates our method's accuracy (≈ 0.05 dex) and negligible systematic bias in estimating stellar masses from broadband optical photometry.

method described in Appendix A. From the SFH residual shown in Figure 3, the SFHs of individual galaxies can be recovered within 0.1 dex when the median is considered, and within 0.3–0.4 dex error when 1σ distribution is considered for both low-mass and high-mass galaxies. Note that the residual distribution of high-mass galaxies (red) is slightly broader than that of low-mass galaxies, possibly due to the better coverage of SFH space for low-mass galaxies since they are more abundant in simulations. Here, we also represent the SFH with the cosmic time that a certain fraction (50%, 70%, and 90%) of stars have formed in in Figure 4. Again, it is evident that our method can recover the SFH for individual galaxies quite well with scatter below ~ 0.2 dex.

5. The Application to SDSS

Following successful validation on the IllustrisTNG simulation, we apply our method to the SDSS main galaxy sample to

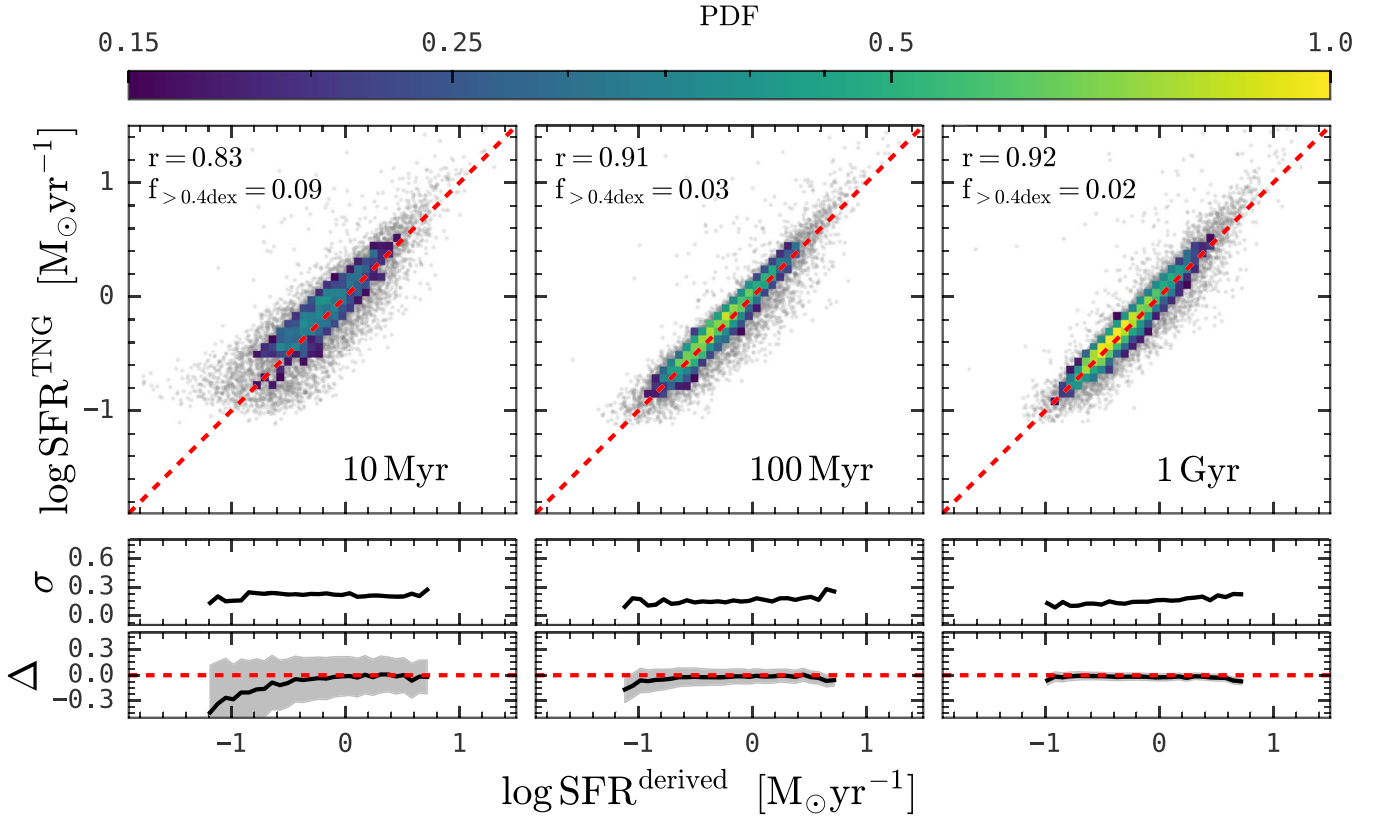


Figure 2. Similar to Figure 1, this figure displays the estimation accuracy of SFRs over three timescales: 10 Myr (left), 100 Myr (middle), and 1 Gyr (right). Gray dots represent individual star-forming galaxies in TNG100, and the heat map illustrates the normalized probability distribution. This figure demonstrates our method's effectiveness in recovering SFR with an accuracy of $\lesssim 0.3$ dex and negligible systematic bias.

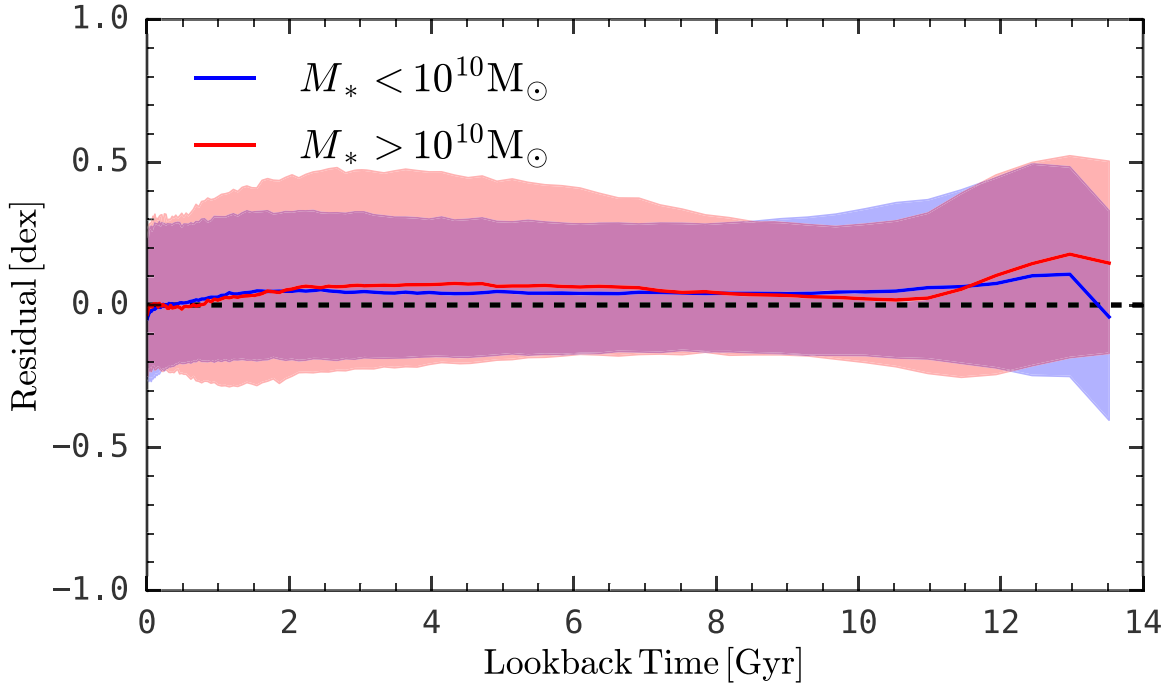


Figure 3. The distribution of SFH residuals (derived SFHs minus real SFHs in TNG100). The blue solid line shows the median residual for low-mass galaxies ($M_* > 10^{10} M_\odot$), with the blue-shaded region denoting a 1σ distribution. The high-mass counterparts are shown in red. This figure illustrates our method's capability to estimate galaxy SFHs with about 0.1 dex error for the median and 0.3–0.4 dex error when considering the 1σ distribution.

infer stellar mass, current SFR, and SFH from broadband photometry, utilizing the TNG100 galaxies as templates for mass-to-light ratio, SFH, and metal enrichment history.

5.1. Stellar Mass and SFR

Figure 5 shows the stellar mass recovered with our method in comparison with values in the MPA-JHU and GSWLC

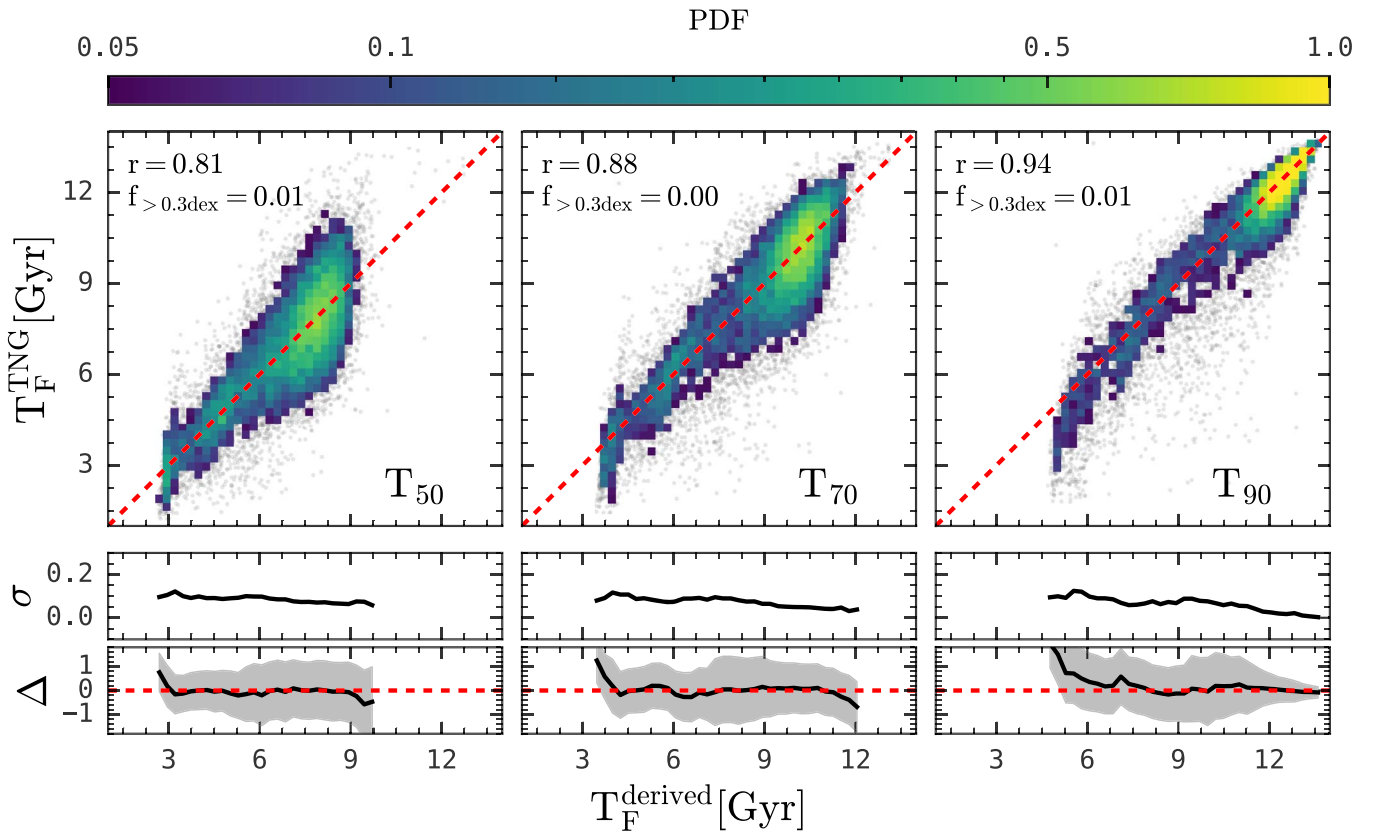


Figure 4. Similar to Figure 1, this figure extends the analysis to the cosmic time when 50% (left), 70% (middle), and 90% (right) of the stellar population has formed. Individual gray dots represent galaxies in TNG100, and the heat map illustrates the normalized probability distribution. This figure illustrates our method’s capability to estimate typical galaxy formation times with a fractional standard deviation of around 30% and negligible systematic bias.

catalog. Note that the MPA-JHU catalog derives stellar mass from the spectral indices for the central part covered by the fiber and from the broadband photometry for the outer part. Our result agrees with that of the MPA-JHU with the standard deviation $\lesssim 0.1$ dex, except that our stellar mass is systematically larger than theirs by about 0.13 dex. Note that we already corrected the difference caused by the initial mass function and cosmology. Such a systematic difference is also reported by S. Salim et al. (2016), where they attribute it to the different parametric function forms for the SFH. From the right panels of Figure 5, one can see that our result agrees with the GSWLC catalog (S. Salim et al. 2016) quite well with a standard deviation $\lesssim 0.1$ dex and negligible systematics, which suggests that the stellar mass in MPA-JHU is indeed biased by their nonphysical priors for SFH. Moreover, it is noteworthy that the GSWLC catalog derives the stellar mass from the UV-to-IR photometry, while we only use five optical broad bands of photometry.

Figure 6 shows the comparison of SFR for star-forming galaxies between our estimation and that of the MPA-JHU and GSWLC catalogs. For this figure, the star-forming galaxies are selected following the color–magnitude diagram criteria from I. K. Baldry et al. (2004), since there is no real SFR in observation. We also test the results with different criteria, including the color–stellar mass diagram (J. Cui et al. 2024) and stellar mass–SFR diagram ($\log \text{SFR} > \log M_* \times 0.76 - 0.81$; galaxies above the red dashed line in the upper right panel of Figure 7). There are no noticeable changes among these different definitions. For passive galaxies, their SFRs in MPA-JHU and GSWLC have high

uncertainties (S. Salim et al. 2016) and may even be upper limits, possibly due to the inaccurate photometry for GSWLC (Y. A. Li et al. 2023) and uncertainty in the D_n4000 –sSFR relation (J. Brinchmann et al. 2004). So, these passive galaxies are not considered for comparison. Note that the star formation rate in the MPA-JHU catalog is calibrated with the $H\alpha$ luminosity, which traces the star formation activity in the last 10 Myr, and that of GSWLC is estimated by smoothing the inferred SFH over 100 Myr. Thus, we choose to take the averaged SFR over 10 Myr and 100 Myr for a fair comparison with each catalog. Here, one can see that, for galaxies with $\text{SFR} > 0.1 M_\odot \text{yr}^{-1}$, our method produces consistent results with MPA-JHU and GSWLC with the standard deviation about 0.2–0.5 dex and negligible systematics. Finally, it should be emphasized that the GSWLC catalog uses additional information from the UV and IR emissions, and MPA-JHU uses the $H\alpha$ emission and $D_n(4000)$ spectral index, while our method only uses five optical broad bands of photometry. Still, we yield consistent results, indicating the superiority of our method.

We note that, for some galaxies, our model systematically provides lower SFR estimates than those from MPA-JHU and GSWLC. Although the true SFRs are unknown, these galaxies are all classified as star-forming; therefore, the measurements from MPA-JHU and GSWLC, which utilize $H\alpha$ emission and UV plus IR photometry, respectively, should theoretically be more accurate. It is also interesting to note that this discrepancy is almost nonexistent in the self-consistency test (Figure 2), suggesting that the issue likely does not originate from the link between SEDs and SFH or our method itself. One possible

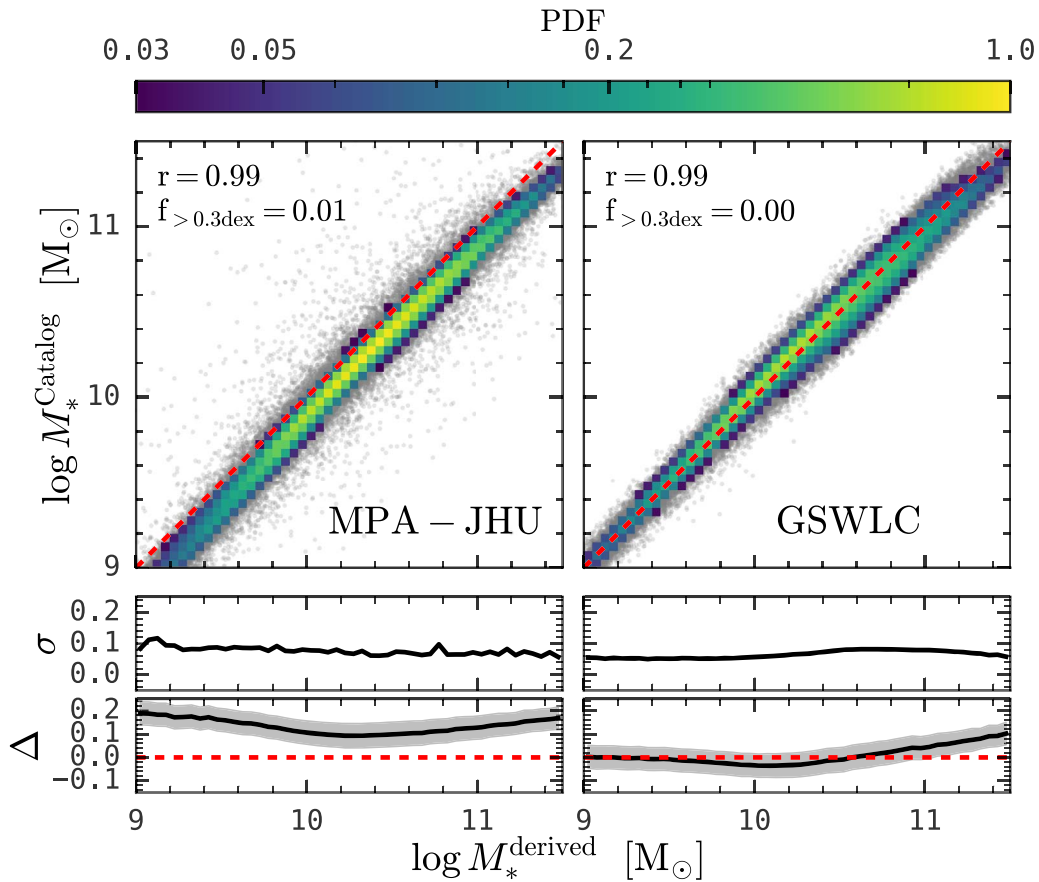


Figure 5. The top panels show the comparison of the stellar mass estimated by our method versus those in MPA-JHU (left; G. Kauffmann et al. 2003) and GSWLC (right; S. Salim et al. 2016). Individual galaxies in SDSS are represented by gray dots, and the heat map illustrates the normalized probability distribution. The bottom panels show the standard deviations and mean differences as functions of estimated stellar mass. Our method aligns closely with GSWLC values and consistently shows an approximate 0.13 dex systematic increase over MPA-JHU estimates.

explanation is the insufficient sampling of SFH space in the simulation. However, this problem does not significantly impact the results statistically, as the catastrophic failure rate is low (approximately 20%).

Before we step into the comparison of quiescent fraction and SFR bimodality, several technical considerations should be mentioned. First, we choose to compare with the MPA-JHU catalog rather than the GSWLC catalog, since the latter suffers from incompleteness due to the requirement of cross-matching with the UV and IR photometry catalog. Second, we note that TNG100 produces many quiescent galaxies with SFR equal to zero, which is not suitable for presentation, so we assign some small SFR to these galaxies for the sake of fair comparison with observational results. It is noteworthy that some work argues that the distribution of galaxies on the $\log M_*$ – \log SFR plane is unimodal: a star-forming peak and an extended tail toward low SFR (see A. Renzini & Y. Peng 2015; R. Feldmann 2017; S. Eales et al. 2017). Third, the calculation of SFR from the amount of stellar particles formed in the last period suffers from shot noise. We note that the baryon cell weighs about $10^6 M_\odot$ in TNG100, so the minimal SFR above zero in the last 10 Myr will be $0.1 M_\odot \text{ yr}^{-1}$, which corresponds to a specific SFR of 10^{-10} yr^{-1} for a $10^9 M_\odot$ galaxy and, hence, it will affect the calculation of the quiescent fraction. Therefore, we choose to smooth the SFR over 100 Myr to minimize this effect when we compare our results with TNG100.

Figure 7 shows the quiescent fraction for central and satellite galaxies, respectively, and the apparent bimodal distribution of

galaxies on the $\log M_*$ – \log SFR plane. Here, we employ the group catalog in X. Yang et al. (2007) to classify central and satellite galaxies. First, the quiescent fraction for central galaxies monotonically increases with stellar mass from about 10% at $10^9 M_\odot$ to almost 100% at $10^{11.5} M_\odot$, which is a manifestation of mass quenching. As reported in K. Wang et al. (2023), a large portion of low-mass quiescent central galaxies are backplash galaxies, which were previously satellite galaxies of other massive halos and got ejected out of their host halos. Second, the quiescent fraction of the central galaxies in TNG100 abruptly increases around $10^{10.2} M_\odot$, which is absent in observational data. The sharp transition may result from the problematic active galactic nucleus (AGN) feedback interpretation in TNG (see B. A. Terrazas et al. 2020 for more information). In addition, the result obtained from our method is consistent with MPA-JHU and previous results (I. K. Baldry et al. 2006; Y.-j. Peng et al. 2010; Y.-j. Peng et al. 2012; A. R. Wetzel et al. 2013; J. Trussler et al. 2020; A. R. Gallazzi et al. 2021) while significantly differing from the TNG100 simulation, thus confirming the robustness of our approach in applying physical priors without duplicating simulation results. Third, satellite galaxies are more quenched than central galaxies at a given stellar mass, since they are additionally subject to environmental effects. Finally, we found three components in the distribution of galaxies on the $\log M_*$ – \log SFR plane: one star-forming main sequence, one massive quiescent component contributed by mass quenching, and one low-mass quiescent component from

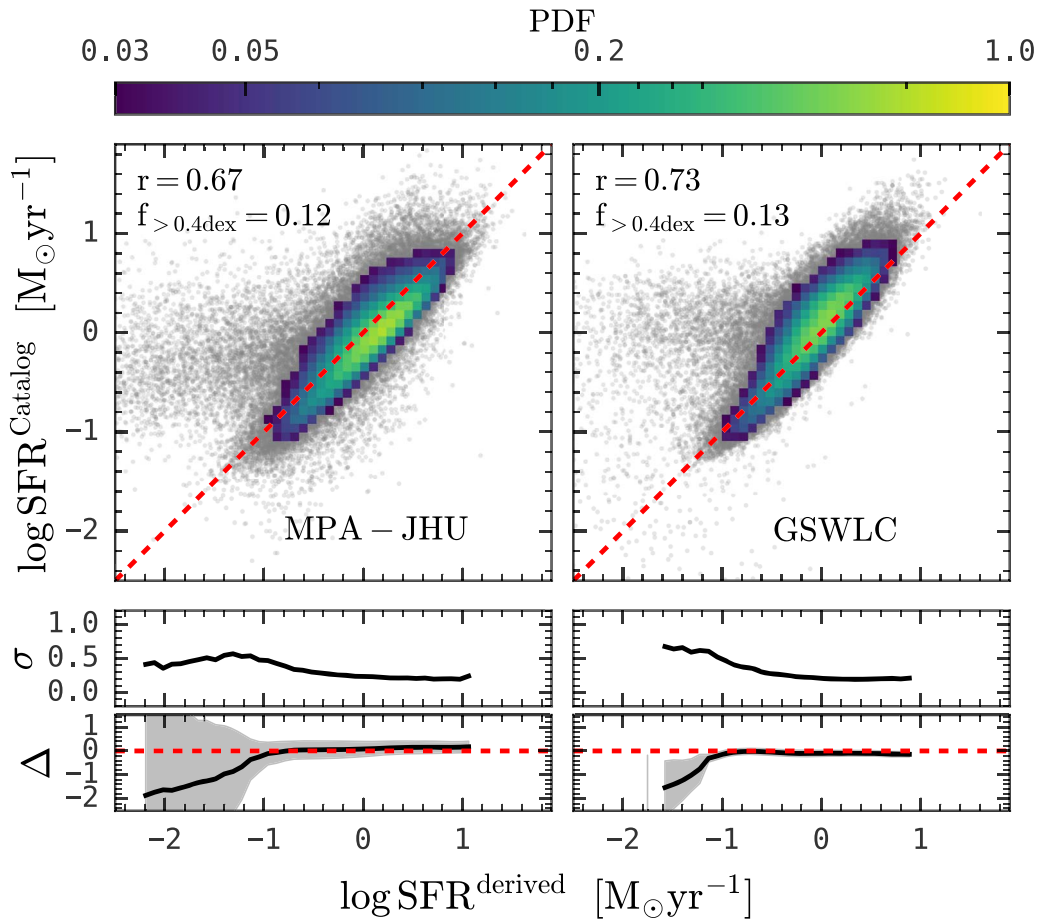


Figure 6. Similar to Figure 5, focusing on the SFR for star-forming galaxies. Individual star-forming SDSS galaxies are represented by gray dots, and the heat map illustrates the normalized probability distribution. Our estimates align well with MPA-JHU and GSWLC values above $0.1M_{\odot}\text{yr}^{-1}$.

environmental quenching (see A. Renzini & Y. Peng 2015). One notable thing is that we can accurately reproduce the star-forming main sequence exhibited in the MPA-JHU catalog, which is derived from $H\alpha$ luminosity, while our results are only based on five broad bands of photometry.

5.2. Cosmic SFR Density and Stellar Mass Density

As demonstrated in Section 3 and tested in Section 4, our method is able to recover the star formation history of each galaxy from their broadband photometry. By doing so for all galaxies in the SDSS main galaxy sample, the cosmic SFR density, i.e., the comoving SFR density as a function of redshift, can be recovered by aggregating individual SFHs of local galaxies and dividing it by the comoving volume occupied by these galaxies. This is known as the fossil record method and has been applied in many works (A. Heavens et al. 2004; A. Gallazzi et al. 2008; P. Madau & M. Dickinson 2014; A. C. Carnall et al. 2019; J. Leja et al. 2019a, 2019b; S. F. Sánchez et al. 2019), which should have similar results to direct observation (S. J. Lilly et al. 1996; P. Madau et al. 1996) in principle. It is noteworthy that, since SDSS is a flux-limited sample, the comoving volume occupied by observed galaxies is dependent on the intrinsic luminosity, which is commonly referred to as V_{max} (M. Schmidt 1968).

The top panel of Figure 8 shows the cosmic SFR density reconstructed from the individual 100 bins of SFH of local galaxies in the blue solid line. For comparison, we also present

the result from TNG100 in the red solid line, and the direct observational measurement results in gray symbols with the fitting function in the green solid line (D. B. Sanders et al. 2003; T. T. Takeuchi et al. 2003; D. Schiminovich et al. 2005; T. K. Wyder et al. 2005; T. Dahlen et al. 2007; N. A. Reddy & C. C. Steidel 2009; B. Magnelli et al. 2011; A. S. G. Robotham & S. P. Driver 2011; R. J. Bouwens et al. 2012a, 2012b; O. Cucciati et al. 2012; M. A. Schenker et al. 2013; B. Magnelli et al. 2013; C. Gruppioni et al. 2013; P. Madau & M. Dickinson 2014). Here, one can see that TNG100 slightly overpredicts the peak position by ≈ 1 Gyr, while our method, although using TNG100 as a prior, is a better match to the observational result from direct measurements. It is noteworthy that our method outperforms several previous parametric and nonparametric SFH methods (see A. C. Carnall et al. 2019; J. Leja et al. 2019a), which confirms the superiority of our method in delivering physical parameters from multiband photometry.

The three dashed lines in the top panel of Figure 8 show the cosmic star formation histories contributed by $z \sim 0$ descendant galaxies with different stellar masses. For massive galaxies, although their assembly is relatively recent, most of their stars were already formed more than 10 Gyr ago, which is known as the archeology downsizing effect (D. Thomas et al. 2005; J. E. Nelan et al. 2005; A. Heavens et al. 2004; R. Jimenez et al. 2005; E. Neistein et al. 2006; A. Renzini 2006). Meanwhile, stars formed in the recent several gigayears end up

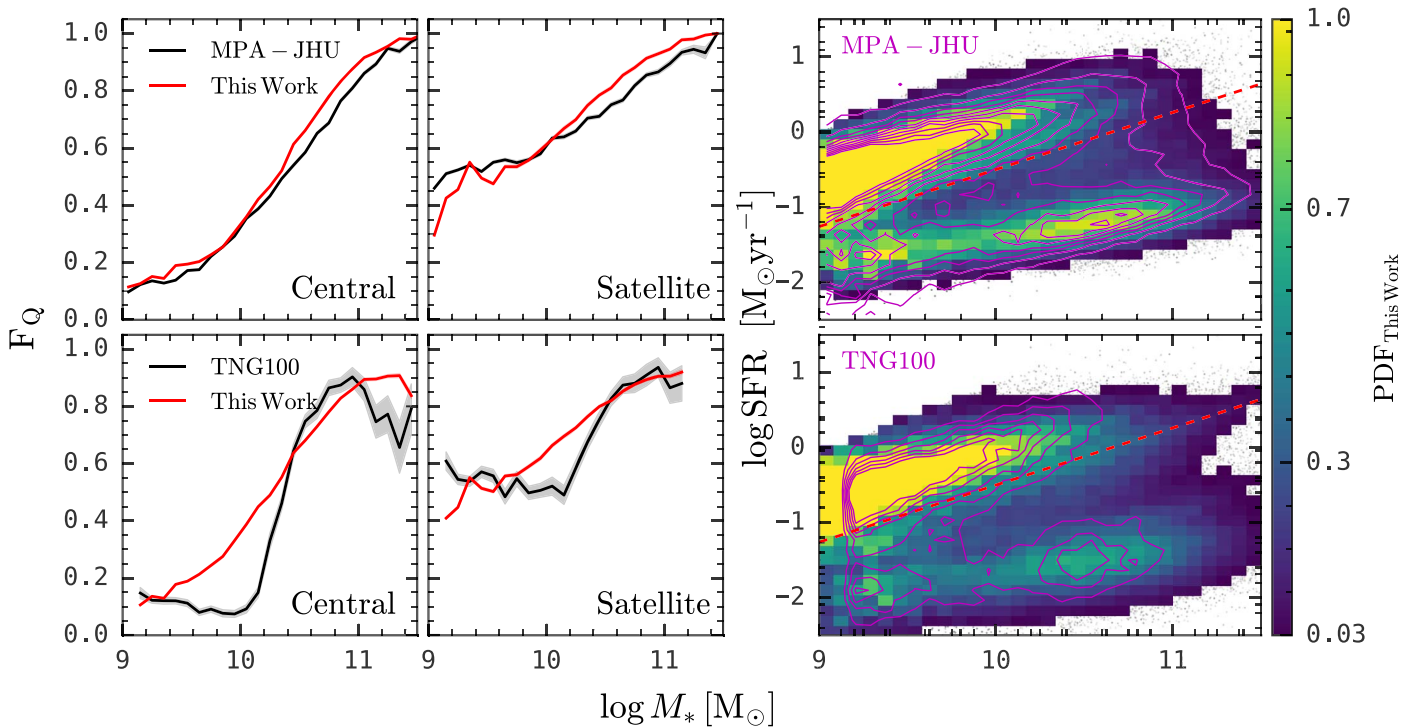


Figure 7. The left four panels show the quiescent galaxies fraction as a function of stellar mass for central (left) and satellite (right) galaxies. The red solid lines are our estimates smoothed over 10 Myr (top) and 100 Myr (bottom), in comparison with the results from the MPA-JHU catalog (top) and the TNG100 simulation (bottom). The right two panels show the distribution of galaxies on the $\log M_* - \log \text{SFR}$ plane. Individual galaxies are represented by gray dots, and the heat map illustrates the normalized probability distribution. The red dashed line ($\log \text{SFR} = 0.76 \times \log M_* - 8.1$) separates the star-forming and quiescent galaxies. The magenta solid contour lines are for our results with the SFR smoothed on 10 Myr (top) and 100 Myr (bottom), and the color maps are for the MPA-JHU result and the TNG100 simulation, respectively. Our method's results closely match the MPA-JHU observations in bimodality and show distinct deviations from TNG100 predictions, reinforcing the effectiveness of using TNG100 as a prior without replicating simulation biases.

in low-mass galaxies, which is expected since massive galaxies are quenched and stop producing new stars (see Figure 7).

By integrating the cosmic SFR density and assuming a return factor of 0.41 from the Chabrier initial mass function, we also derive the cosmic stellar mass density in the bottom panel of Figure 8. The results from direct SFR density estimates at different redshifts (P. Madau & M. Dickinson 2014) and TNG100 are also shown in green and red for comparison. Gray symbols are cosmic stellar mass density integrated from stellar mass function in the literature (K. I. Caputi et al. 2011; V. González et al. 2011; P. Santini et al. 2012; O. Ilbert et al. 2013; A. Muzzin et al. 2013; K. Duncan et al. 2014; A. Grazian et al. 2015; K. I. Caputi et al. 2015; A. H. Wright et al. 2018; S. Kikuchihara et al. 2020; D. J. McLeod et al. 2021; J. E. Thorne et al. 2021; J. R. Weaver et al. 2023). Our results agree with both P. Madau & M. Dickinson (2014) and stellar mass function results well, while TNG100 slightly exceeds most measurements at about 10 Gyr ago. When categorizing galaxies into descendant stellar mass bins, we again see the archeology downsizing effect: massive galaxies form their mass early and gradually cease star formation. By contrast, low-mass galaxies keep on creating new stars.

5.3. Reconstructing Spectral Indices

Previous studies found that the spectral indices of observed galaxies contain abundant information about the physical properties of galaxies, and these spectral indices are used to derive physical properties, such as stellar mass, SFH, and stellar metallicity (S. M. Faber 1972; G. Worthey & D. L. Ottaviani 1997; G. Kauffmann et al. 2003; A. Gallazzi et al. 2005), and are

incorporated into the full-spectrum fitting procedure to deliver more accurate property estimations. Thus, given the success of our method based on broadband photometry, it is pertinent to investigate the extent to which the spectral indices of observed galaxies can be reconstructed. Here, we focus on $D_n(4000)$ and $H\delta_A$. Here, $D_n(4000)$ quantifies the discontinuity around 4000 Å, which comes from the absorption of ionized metals, and it is defined as the ratio of the average flux density in the bands 3850–3950 and 4000–4100 Å (see M. L. Balogh et al. 1999; G. Kauffmann et al. 2003). $D_n(4000)$ is profoundly dependent on the stellar age and stellar metallicity: older and more metal-rich galaxies exhibit higher $D_n(4000)$. Particularly, $D_n(4000)$ is sensitive to the median stellar age. $H\delta_A$ quantifies the $H\delta$ absorption lines (G. Worthey & D. L. Ottaviani 1997), which are mainly contributed by late-B and early-F stars, and therefore $H\delta_A$ is a sensitive probe of star formation activities that occurred 0.1–1 Gyr ago (G. Kauffmann et al. 2004). Notice that the $D_n(4000)$ and $H\delta_A$ distributions of TNG100 galaxies are similar to observations (P.-F. Wu et al. 2018; P.-F. Wu et al. 2021), indicating that SFHs in TNG produce galaxy properties consistent with the observations. It is noteworthy that both spectral indices are not significantly affected by the presence of dust absorption (G. Kauffmann et al. 2003; L. A. MacArthur 2005; also see the test in Appendix C), allowing for the safe exclusion of this effect in the forward synthesis of these two spectral indices.

Here is the procedure to reconstruct the spectral indices ($D_n(4000)$ and $H\delta_A$) from the broadband photometry of observed SDSS galaxies. First, we derive the SFH and the metal enrichment history of each observed galaxy from its

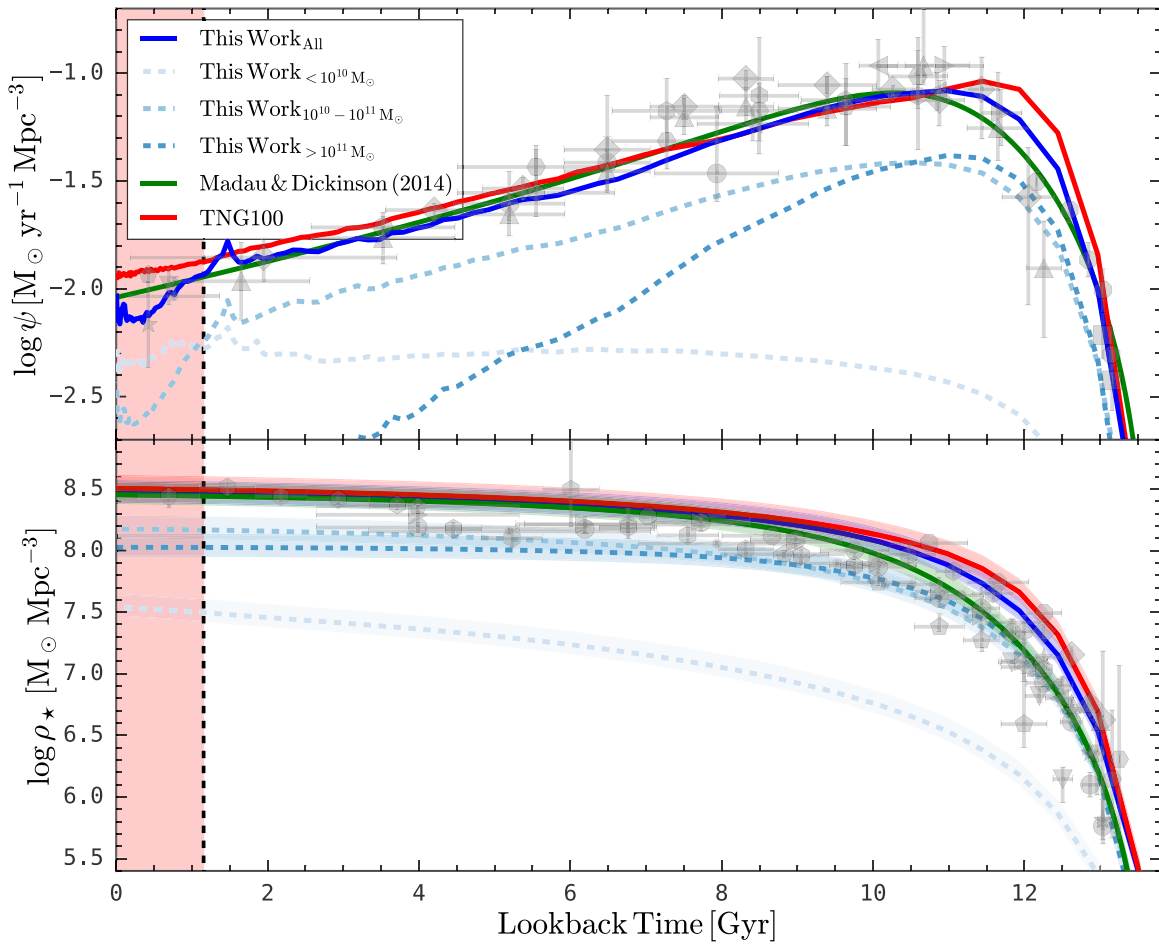


Figure 8. The upper panel depicts the comparison of the cosmic SFR density, defined as the comoving SFR density as a function of look-back time. The gray symbols are the observational results from direct SFR density estimates at different redshifts (D. B. Sanders et al. 2003; T. T. Takeuchi et al. 2003; D. Schiminovich et al. 2005; T. K. Wyder et al. 2005; T. Dahlen et al. 2007; N. A. Reddy & C. C. Steidel 2009; A. S. G. Robotham & S. P. Driver 2011; B. Magnelli et al. 2011; O. Cucciati et al. 2012; R. J. Bouwens et al. 2012a, 2012b; M. A. Schenker et al. 2013; B. Magnelli et al. 2013; C. Gruppioni et al. 2013; P. Madau & M. Dickinson 2014), and the fitting line of these observational results is shown as the green solid line (P. Madau & M. Dickinson 2014). The result of the TNG100 simulation is shown in the red solid line, and the result obtained with our method is shown in the blue solid line. The three blue dashed lines are the cosmic SFR density that end up in descendant galaxies with different stellar masses at $z \sim 0$. The lower panel shows the comparison of the cosmic stellar mass density, defined as the comoving stellar mass density as a function of look-back time. Solid lines are integrated from cosmic SFR density with a return factor of 0.41 (based on the Chabrier initial mass function). The error bands are based on return factors of 0.25 and 0.5. The gray symbols are the observational results integrated from stellar mass functions between $10^8 M_{\odot}$ and $10^{13} M_{\odot}$ (K. I. Caputi et al. 2011; V. González et al. 2011; P. Santini et al. 2012; O. Ilbert et al. 2013; A. Muzzin et al. 2013; K. Duncan et al. 2014; K. I. Caputi et al. 2015; A. Grazian et al. 2015; A. H. Wright et al. 2018; S. Kikuchi et al. 2020; D. J. McLeod et al. 2021; J. E. Thorne et al. 2021; J. R. Weaver et al. 2023). Our method effectively captures both the cosmic SFR density and cosmic stellar mass density, aligning closely with direct measurements and revealing detailed insights into galaxy evolution.

broadband photometry using our method (see Section 3) with TNG100 as a physical prior. Second, we synthesize the full spectrum of each galaxy from its SFH and metal enrichment history using the FSPS package adopting the MILES stellar library, Padova isochrones, and Chabrier initial mass function. Finally, we measure the spectral indices following the procedure done for the observed spectrum.

Figure 9 shows the comparison between the reconstructed and the observed spectral indices. It should be noted that we exclude galaxies with unreliable spectral index measurements, which includes galaxies whose measurement error in $D_n(4000)$ is above 0.07 or whose measurement error in $H\delta_A$ is above 2.5 \AA . This excludes 5% and 4% of SDSS galaxies, respectively. Here, one can see that Spearman's correlation coefficients for both indices are around 0.85, which means that about 85% of the variation for these two spectral indices can be captured by the optical broadband photometry. Besides, the reconstructed spectral indices closely follow the observed

values on the one-to-one line except for galaxies with high $D_n(4000)$ and negative $H\delta_A$, which are quenched galaxies and dominated by old stellar populations. We have inspected the result for star-forming galaxies (not shown here) and found that the systematic deviation becomes negligible.

Many previous studies have conducted similar tests on different SED-fitting procedures. For instance, Y.-M. Chen et al. (2012) developed a method based on principal component analysis (PCA) and applied it to BOSS spectra. They were able to retrieve the $D_n(4000)$ and $H\delta_A$ indices for high-redshift galaxies ($0.4 < z < 0.7$) with a precision comparable to our model, benefiting from the rich information available in the full spectra. In a related study, A. Nersesian et al. (2024) utilized the Prospector procedure on galaxies around $z \sim 1$ with COSMOS2020 photometry. Their results, which involved comparisons with direct observations from the Large Early Galaxy Astrophysics Census (LEGA-C) survey (A. van der Wel et al. 2016, 2021), demonstrated that the recovered $H\delta_A$

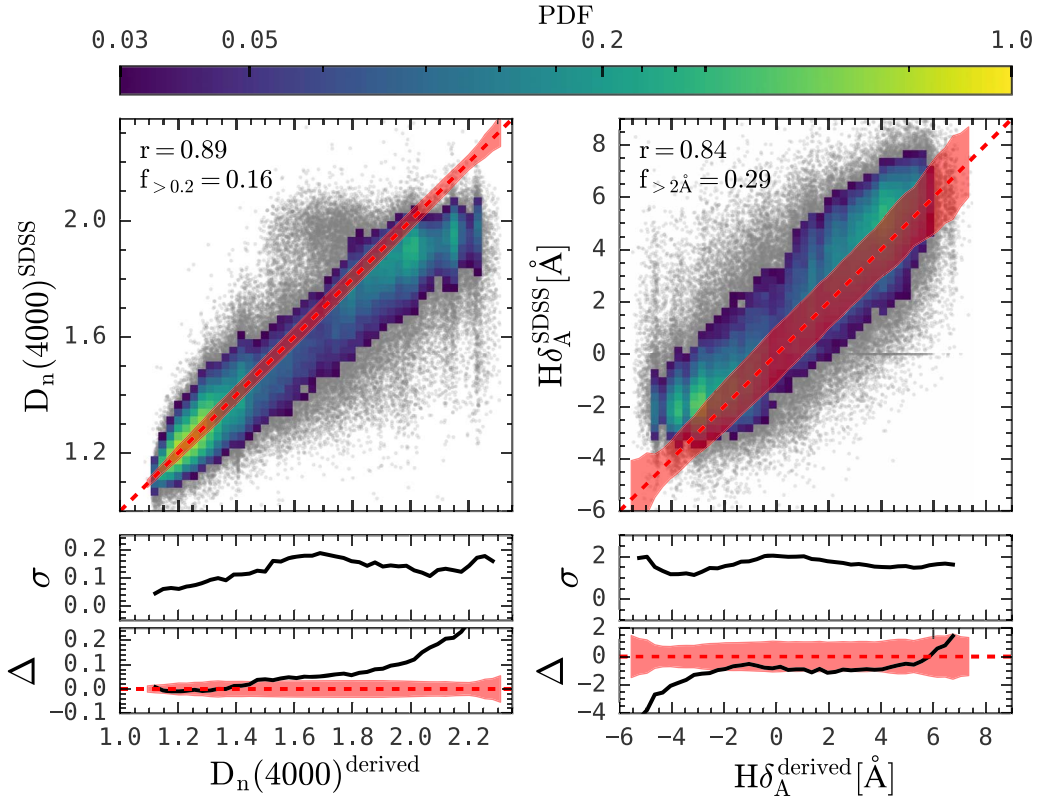


Figure 9. The top panels show the comparison between measured and reconstructed spectral indices, $D_n(4000)$ (left) and $H\delta_A$ (right) for the SDSS main galaxy sample. Individual galaxies are represented by gray dots, and the heat map illustrates the normalized probability distribution. The bottom panels highlight the standard deviation and systematic bias relative to directly measured values. The red-shaded regions show the median observational errors. This figure shows that our reconstructed spectral indices resemble the directly measured values with strong correlations (Spearman's coefficient ≈ 0.85)

indices generally aligned with actual measurements, showing no significant systematic offsets. These findings are consistent with our results.

The success in reconstructing spectral indices has three implications. First, our method can deliver physical SFHs and metal enrichment histories, so that the synthesized spectral indices resemble the results obtained from direct observation, even though we only use broadband photometry. Second, much information provided by these two spectral indices is contained in broadband photometry. Third, the remaining $\approx 15\%$ variation contains additional information about the underlying interesting physical properties (A. Nersesian et al. 2024), whose extraction requires an extension of the current method to the full-spectrum situation. This could be explored in future work.

6. Summary

The SEDs of galaxies contain rich information about their evolutionary histories and have been routinely used to derive fundamental galaxy properties such as stellar mass, SFR, stellar age, and star formation history (SFH) through SED-fitting techniques. However, SED fitting, especially when limited to broadband photometry, may not be sufficient to tightly constrain the SFH and metal enrichment history. Consequently, conventional methods, both parametric and nonparametric, often fail to accurately recover the observed cosmic SFR density, due to strong degeneracy, and oversimplified and nonphysical assumptions about SFHs that are unable to account for complex SFH variations across different galaxy populations.

To address this issue, this study introduces a novel method for estimating the physical properties of galaxies from their observed broadband SEDs, utilizing hydrodynamical galaxy formation simulations as priors. We validated this method on simulated galaxies and subsequently applied it to observations. Our main findings are summarized as follows:

1. Testing on the TNG100 SDSS-mock with five-band photometry (u, g, r, i, z) including dust effects, our method accurately recovers the stellar mass, current SFR, and typical galaxy formation times from optical broadband photometry. The standard deviations are around 0.05, 0.3, and 0.2 dex, respectively, and the systematic bias is negligible (see Figure 1, 2, and 4).
2. When applied to observed SDSS galaxies using optical photometry (u, g, r, i, z) with spectroscopic redshift, our method consistently estimates stellar mass and SFRs that align with those in the MPA-JHU and GSWLC catalogs, showing a standard deviation of ~ 0.1 dex for stellar mass and ~ 0.4 dex for SFR (see Figure 5 and 6).
3. Using the derived stellar mass and SFR from our method on a mass-completed sample in SDSS, the bimodal distribution of galaxies on the $\log M_* - \log \text{SFR}$ plane (i.e., main sequence and passive sequence) and the quenched fraction for centrals and satellites all closely match those obtained from MPA-JHU results. Interestingly, despite employing SFHs from TNG100 as priors, the statistical properties of derived galaxy properties (such as the main sequence, quenched fraction, and environmental effects) are more aligned with MPA-JHU than TNG itself (see Figure 7). For instance, the sharp

quenching threshold around $\log M_* \sim 10.5$ in TNG100 (as shown in Figure 7) is due to its implemented AGN feedback model. The quenched fractions derived from our method evidently have not been influenced by these specific quenching mechanisms in TNG.

4. Using the SFHs of individual SDSS galaxies derived from our method, we estimate the cosmic SFR density, and also the cosmic stellar mass density by integrating these SFHs. Both results show remarkable consistency with direct observational measurements up to $z \sim 6$. This is the first time that SFHs derived from SEDs accurately match direct observational measurements. We also find that the stellar populations of massive galaxies are already largely formed about 10 Gyr ago, while recent star formation predominantly occurs in low-mass galaxies (see Figure 8), consistent with the downsizing trend established in the literature.
5. From the estimated SFHs and metal enrichment histories of individual galaxies in SDSS, we synthesize two spectral indices, $D_n(4000)$ and $H\delta_A$. Our synthesized spectral indices closely match direct observational results. This validation supports the reliability of our derived star formation and metal enrichment histories, despite solely relying on broadband photometry (see Figure 9).

It is important to note that our method does not depend on simulations being considered “the truth” (e.g., TNG100). Unlike conventional parametric methods, simulations offer a large set of physically realistic SFH templates. As a result, our approach effectively excludes many physically unrealistic SFHs that are often included in conventional SED-fitting methods, which might otherwise yield better fits due to strong degeneracies within the SED. This exclusion of physically unrealistic templates represents a significant advantage of our methodology.

Meanwhile, we must also emphasize that galaxies in the real Universe may or may not follow every SFH provided by the simulations. And the relative fraction of certain galaxy populations that evolve according to a specific SFH may differ significantly from those predicted by the simulations. In fact, when applying our method to SDSS galaxies, as illustrated in Figure 7, we successfully recovered the observed quench fraction and the detailed distribution of galaxies on the $\log M_* - \log \text{SFR}$ plane, whereas TNG100 produced noticeably different results. The derived star formation rate density and stellar mass density from our method also show a better match with direct observations compared to TNG100. Again, we emphasize that it is not necessary for the TNG simulations to be an accurate representation of reality. They just offer an extremely broad set of plausible SFHs, much wider than any prior parametric or nonparametric approach.

Our method not only provides robust and accurate estimates of stellar population evolution, particularly galaxy SFHs, using only broadband photometry, but also demonstrates high efficiency. Our tests show that it can process the star formation and metal enrichment histories for one million galaxies in less than 10 minutes using a single Intel-i5 core. These features make it an exceptionally promising tool for ongoing facilities

like Euclid (R. Laureijs et al. 2011) and upcoming ones such as the Chinese Space Station Telescope (H. Zhan 2011) and the Large Synoptic Survey Telescope (Z. Ivezić et al 2019), which will deliver vast quantities of high-quality multiband photometric data. Moreover, its outstanding computational efficiency allows for the application of pixel-to-pixel SED fittings to derive resolved galaxy properties. In the future, we will use this method also for galaxy samples at high redshifts, using TNG templates at the corresponding cosmic times.

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This research made use of NASA's Astrophysics Data System for bibliographic information. The computation in this work is supported by the HPC toolkit HIP (Y. Chen & K. Wang 2023).²⁰

Software: IPYTHON (F. Perez & B. E. Granger 2007), NUMPY (C. R. Harris et al. 2020), PANDAS (The Pandas Development Team 2024), SCIPY (P. Virtanen et al. 2020), ASTROPY (Astropy Collaboration et al. 2022), H5PY (A. Collette et al. 2023), MATPLOTLIB (J. D. Hunter 2007), NUMBA (S. K. Lam et al. 2015), SEABORN (M. Waskom 2021), EXTINCTION (K. Barbary 2016), TQDM (C. da Costa-Luis et al. 2024),

Data Availability

The derived properties in this paper are publicly available on Zenodo under an open-source Creative Commons Attribution license at doi:[10.5281/zenodo.14209295](https://doi.org/10.5281/zenodo.14209295) and are described in Table 1. The detailed star formation history and halo properties, including halo mass and halo assembly history, will be fully publicly available in our following data release paper, together with various other derived properties of the halos and galaxies.

²⁰ <https://github.com/ChenYangao/hipp>

Table 1
Catalog Columns

Column name	Description
plate	SDSS spectroscopic plate number
fiberid	SDSS spectroscopic fiber number
mjd	SDSS spectroscopic observation date
ra	SDSS R.A. in J2000
dec	SDSS decl. in J2000
z	SDSS spectroscopic redshift
log_mstar	Stellar Mass [M_{\odot}]
log_mstar_err	Error of the stellar mass [M_{\odot}]
sfr_10myr/100myr/1gyr	Star formation rate averaged over the recent 10 Myr/100 Myr/1 Gyr [$M_{\odot} \text{ yr}^{-1}$]
sfr_10myr/100myr/1gyr_err	Error of star formation rate averaged over the recent 10 Myr/100 Myr/1 Gyr timescale [$M_{\odot} \text{ yr}^{-1}$]
t50/70/90	Cosmic time that 50%/70%/90% of the mass have formed [Gyr]
t50/70/90_err	Error of cosmic time that 50%/70%/90% of the mass have formed [Gyr]
weighted_dist	Weighted distance \mathcal{D}_i mentioned in Section 3; galaxy with $\mathcal{D}_i \geq 0.19$ should not be used in principle

Appendix A Parameterization of SFH

This Appendix discusses our method for parameterizing SFHs of galaxies within the IllustrisTNG framework. Instead of relying solely on discrete snapshots, our approach integrates the formation times and initial masses of stellar particles over continuous periods to accurately reflect the galaxy's current spectral energy distribution. This method accounts for the dynamic changes in stellar particle locations due to processes such as mergers and interactions.

We adopt a refined SFH binning algorithm adapted from S. Shamshiri et al. (2015), where we set the nearest bin to the present epoch ($z = 0$) at $t_0 = 0.01$ Gyr. The bins increase exponentially back in time:

$$b^0 t_0, b^0 t_0, b^1 t_0, b^1 t_0, \dots, b^n t_0, b^n t_0 \quad (\text{A1})$$

where b is the scaling factor and $2(n + 1)$ the total number of bins. The age of the universe, T , is thus:

$$T = \sum_{i=0}^n 2b^i t_0 = 2 \frac{b^{n+1} - 1}{b - 1} t_0 \quad (\text{A2})$$

Determining the values for t_0 , $2(n + 1)$, and b allows us to define the time intervals for each bin accurately. We conduct a test to evaluate the efficacy of this algorithm in recovering the actual spectra of galaxies and to determine the optimal number of bins required for reconstruction. For this test, we perform a stellar population analysis on galaxies in the TNG100 simulation using FSPS and compare the spectra generated with different binning algorithms and bin numbers. Since our

objective is to test the SFH, we only consider the continuum from the stellar component.

As shown in Figure 10, we evaluate the SFH binning algorithms by comparing their ability to reconstruct the real spectra of a star-forming galaxy (Subhalo ID = 545413) and a quenched galaxy (Subhalo ID = 403629). The effectiveness of each method is measured by the accuracy with which it captures the spectral details

We first treat each stellar particle in the galaxy as a single stellar population and combine them to obtain the most accurate real spectra. We then evaluate different SFH binning methods in the upper panels of Figures 10(a1) and (b1) with 100 bins, including methods used in this study, bins with uniform scale factor a , and uniform time intervals. We also utilize TNG snapshots as bin edges (and add another bin edge at scale factor $a = 0$). Galaxies are then expressed as 100 single stellar populations formed in the middle of the bin.

For most galaxies, our SFH binning algorithm can recover the real spectra within 0.1 dex, while other binning methods can lead to significant bias to the real spectra in the short wavelength range. This is because our method can provide a much smaller bin size near $z = 0$, where recent star formation can contribute significantly to UV spectra. We also investigate the influence of bin numbers for our method in Figures 10 (a2) and (b2), with bin numbers ranging from 10 to 1000. Our analysis confirms that using 100 bins optimally balances computational efficiency and the fidelity of spectral recovery within 0.1 dex. The results validate our algorithm's capability to reconstruct detailed and accurate SFHs for galaxies, supporting its application in broader astrophysical studies.

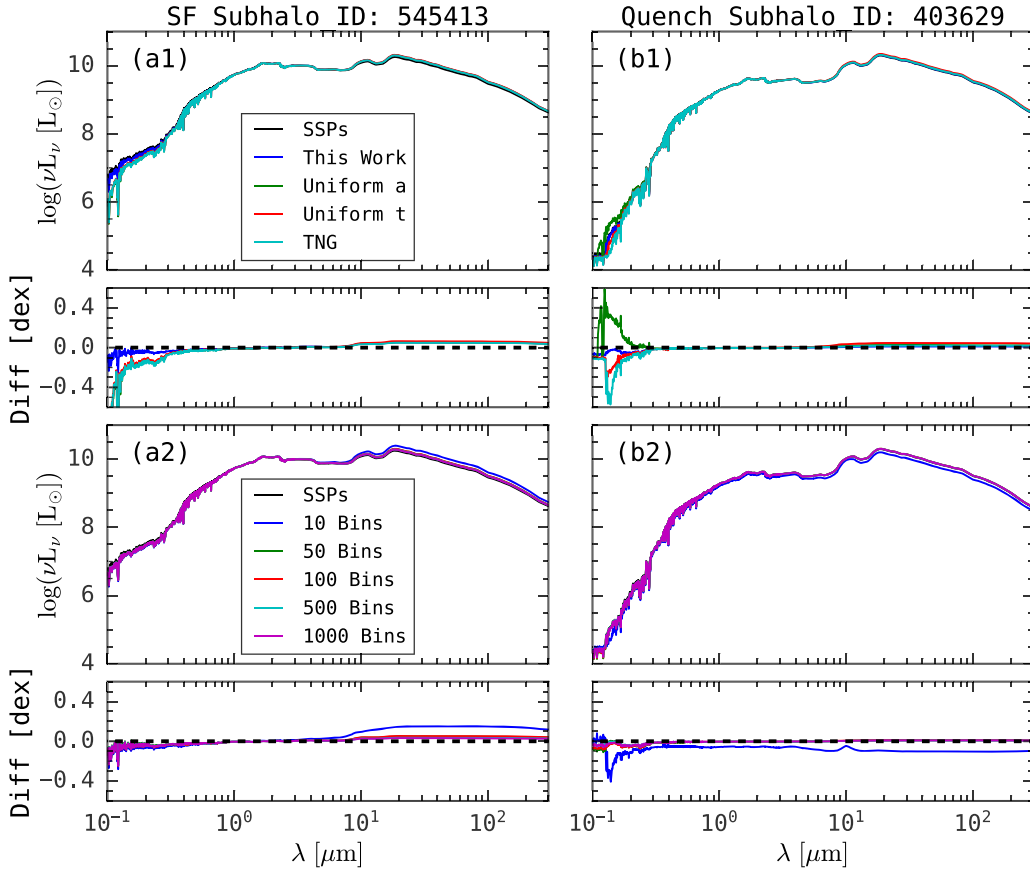


Figure 10. Spectra generated with FSPS using various SFH binning algorithms and bin numbers are compared. Both star-forming and quenched galaxies are included, with Subhalo IDs 545413 and 403629, from left to right, respectively. The spectra discrepancies between different methods and real spectra generated by combining stellar particles as single stellar populations are quantified in dex in the lower panels. The top two figures (a1, b1) present the comparison between different SFH binning algorithms with a fixed number of 100 bins. The blue lines correspond to spectra with the SFH binning algorithm employed in this study. The green and red lines represent spectra generated using uniform scale factors and a uniform time SFH binning algorithm, respectively. The cyan lines demonstrate the binning method that utilizes TNG snapshots as bin edges. The bottom figures (a2, b2) display the spectra with varying bin numbers using our method, ranging from 10 bins to 1000 bins. This figure illustrates that our method, utilizing 100 bins, effectively recovers UV-to-IR spectra with minimal bias (less than 0.1 dex).

Appendix B Validation of SFH-based Cosmic SFR Density

This Appendix assesses the accuracy of deriving cosmic SFR density using the SFHs of galaxies (the fossil record method) from the IllustrisTNG simulation compared to direct snapshot-based methods.

Cosmic SFR density is traditionally estimated from IR and UV luminosity functions representing direct observations across various epochs. The SFH-based approach applied in this work, aggregating historical star formation data from simulations, provides an alternative estimation method. The latter approach gives a smaller value than the former because of

the contribution of intracluster light and small galaxies. Here, we quantify the difference between these two approaches using TNG100 in Figure 11.

The upper panel shows the SFH-based SFR density (red line) against the directly measured ones from TNG100 snapshots (blue dots). The lower panel illustrates their differences, predominantly less than 0.05 dex, suggesting that our SFH-based method captures the cosmic SFR density with minimal bias, despite minor deviations in early epochs due to coarse temporal resolution in SFH sampling. This supports the robustness of using integrated SFH for cosmic SFR density estimation in cosmological studies.

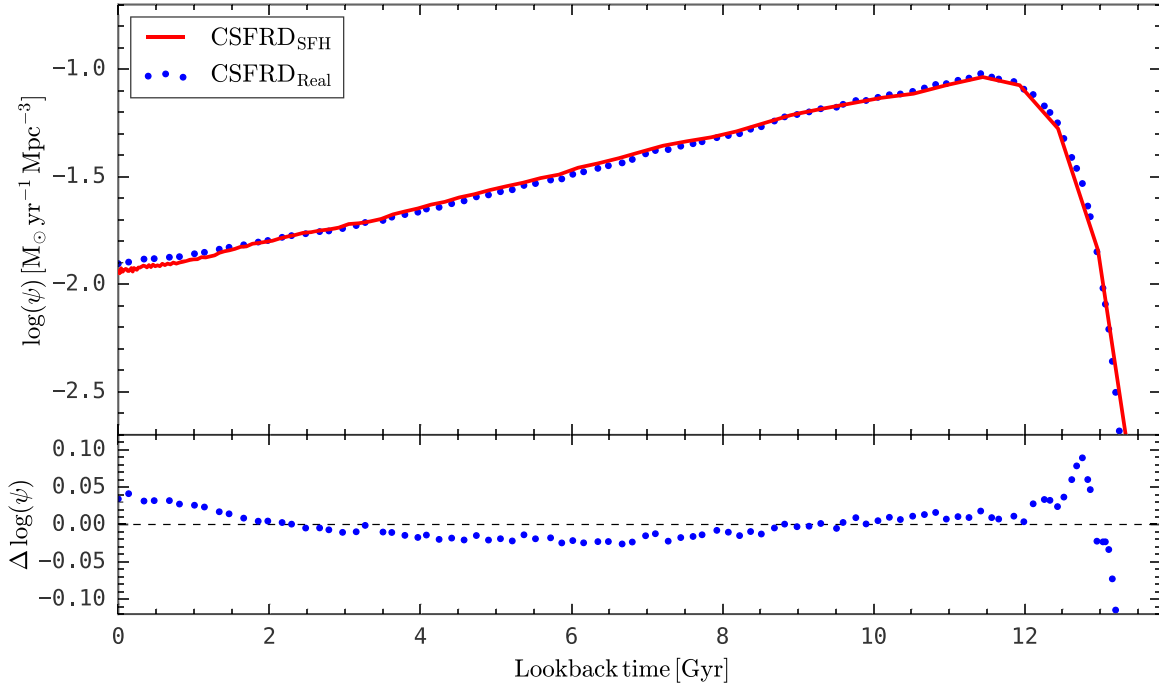


Figure 11. Comparison between SFH-based and direct measurement of cosmic SFR density in TNG100. In the upper panel, the red line shows the cosmic SFR density calculated as the sum of the SFHs of all TNG100 galaxies with a stellar mass more than $10^9 h^{-1} M_{\odot}$ at $z = 0$, while the blue dots depict the direct measurements of SFRs from galaxies in each TNG100 snapshot. Differences are highlighted in the lower panel, showing minor discrepancies (less than 0.05 dex).

Appendix C

Evaluating Dust Attenuation on Spectral Indices

In this Appendix, we investigate the effects of dust attenuation on spectral indices, which were not considered in our initial stellar population synthesis. We assess how dust impacts the indices $D_n(4000)$ and $H\delta_A$, which are critical for interpreting the age and activity of stellar populations.

Using FSPS, we generate mock spectra for a representative sample of TNG100 galaxies and apply the extinction law from D. Calzetti et al. (2000) to simulate dust effects. This process involves varying levels of attenuation ($A_V = 0.4, 0.8, 1.2$ mag)

to cover a broad range of realistic conditions (see Figure 8(b) in S. Salim & D. Narayanan 2020). Our findings in Figure 12 confirm that both $D_n(4000)$ and $H\delta_A$ are relatively robust against dust, with only minor deviations observed even under a significant dust presence. For $D_n(4000)$, attenuation raises the value, and this effect becomes stronger for higher intrinsic $D_n(4000)$ galaxies. For $H\delta_A$, there seems to be no clear trend. This reinforces the utility of these indices in dusty environments and aligns with findings from prior studies, such as those by G. Kauffmann et al. (2003), highlighting their reliability in diverse galactic conditions.

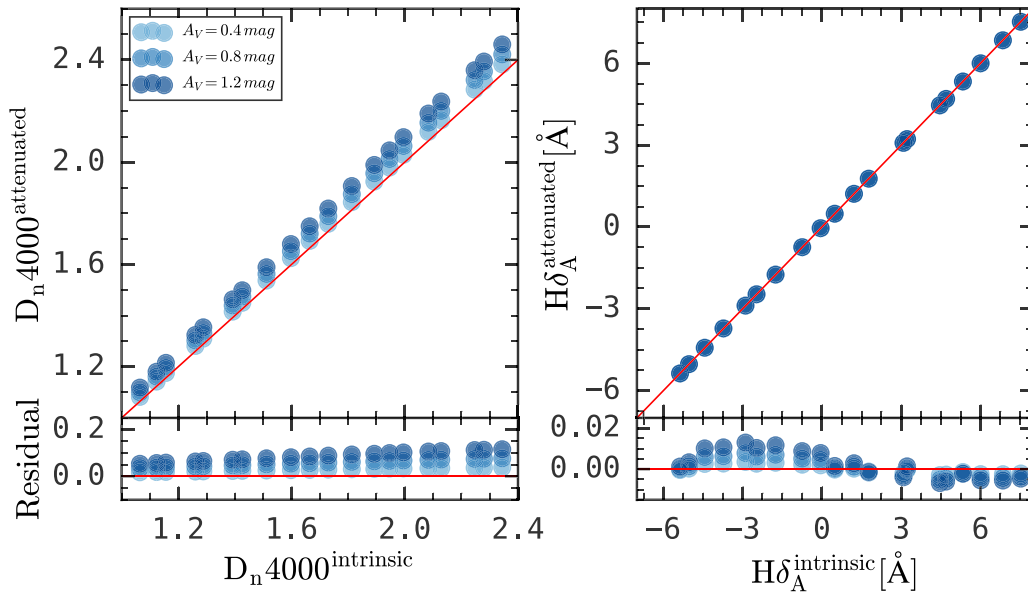



Figure 12. Impact of dust attenuation on spectral indices $D_n(4000)$ and $H\delta_A$. The upper panels compare intrinsic and dust-affected indices across 20 randomly selected TNG100 galaxies. Galaxies with different A_V are indicated by different colors. The red solid lines are the one-to-one reference lines. The lower panels quantify the differences. These two spectral indices are insensitive to dust attenuation, with the largest changes being $\lesssim 0.15$ for $D_n(4000)$ and $\lesssim 0.02$ Å for $H\delta_A$.

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References

- Abazajian, K. N., Adelman-McCarthy, J. K., Agüeros, M. A., et al. 2009, *ApJS*, **182**, 543
- Abramson, L. E., Gladders, M. D., Dressler, A., et al. 2016, *ApJ*, **832**, 7
- Astropy Collaboration, Price-Whelan, A. M., Lim, P. L., et al. 2022, *ApJ*, **935**, 167
- Baldry, I. K., Balogh, M. L., Bower, R. G., et al. 2006, *MNRAS*, **373**, 469
- Baldry, I. K., Glazebrook, K., Brinkmann, J., et al. 2004, *ApJ*, **600**, 681
- Balogh, M. L., Morris, S. L., Yee, H. K. C., Carlberg, R. G., & Ellingson, E. 1999, *ApJ*, **527**, 54
- Barbary, K. 2016, extinction v0.3.0, Zenodo, doi:10.5281/zenodo.804967
- Behroozi, P., Wechsler, R. H., Hearin, A. P., & Conroy, C. 2019, *MNRAS*, **488**, 3143
- Blanton, M. R., & Roweis, S. 2007, *AJ*, **133**, 734
- Blanton, M. R., Schlegel, D. J., Strauss, M. A., et al. 2005, *AJ*, **129**, 2562
- Boquien, M., Burgarella, D., Roehlly, Y., et al. 2019, *A&A*, **622**, A103
- Bouché, N., Dekel, A., Genzel, R., et al. 2010, *ApJ*, **718**, 1001
- Bouwens, R. J., Illingworth, G. D., Oesch, P. A., et al. 2012a, *ApJ*, **754**, 83
- Bouwens, R. J., Illingworth, G. D., Oesch, P. A., et al. 2012b, *ApJL*, **752**, L5
- Brinchmann, J., Charlot, S., White, S. D. M., et al. 2004, *MNRAS*, **351**, 1151
- Bruzual, G., & Charlot, S. 2003, *MNRAS*, **344**, 1000
- Calzetti, D., Armus, L., Bohlin, R. C., et al. 2000, *ApJ*, **533**, 682
- Cappellari, M. 2012, pPXF: Penalized Pixel-Fitting stellar kinematics extraction, Astrophysics Source Code Library, ascl:1210.002
- Caputi, K. I., Cirasuolo, M., Dunlop, J. S., et al. 2011, *MNRAS*, **413**, 162
- Caputi, K. I., Ilbert, O., Laigle, C., et al. 2015, *ApJ*, **810**, 73
- Carnall, A. C., McLure, R. J., Dunlop, J. S., & Davé, R. 2018, *MNRAS*, **480**, 4379
- Carnall, A. C., McLure, R. J., Dunlop, J. S., et al. 2019, *MNRAS*, **490**, 417
- Chabrier, G. 2003, *PASP*, **115**, 763
- Chauke, P., van der Wel, A., Pacifici, C., et al. 2018, *ApJ*, **861**, 13
- Chen, Y., Mo, H. J., Li, C., et al. 2021, *MNRAS*, **507**, 2510
- Chen, Y., & Wang, K. 2023, HIPP: High-Performance Package for Scientific Computation, Astrophysics Source Code Library, ascl:2301.030
- Chen, Y.-M., Kauffmann, G., Tremonti, C. A., et al. 2012, *MNRAS*, **421**, 314
- Chiosi, C. 1980, *A&A*, **83**, 206
- Cid Fernandes, R., Mateus, A., Sodré, L., Stasińska, G., & Gomes, J. M. 2005, *MNRAS*, **358**, 363
- Collette, A., Kluyver, T., Caswell, T. A., et al. 2023, h5py/h5py: v3.8.0-aarch64-wheels, Zenodo, doi:10.5281/zenodo.7568214
- Conroy, C. 2013, *ARA&A*, **51**, 393
- Conroy, C., & Gunn, J. E. 2010, *ApJ*, **712**, 833
- Conroy, C., Gunn, J. E., & White, M. 2009, *ApJ*, **699**, 486
- Conroy, C., & Wechsler, R. H. 2009, *ApJ*, **696**, 620
- Crain, R. A., & van de Voort, F. 2023, *ARA&A*, **61**, 473
- Crain, R. A., Theuns, T., Dalla Vecchia, C., et al. 2009, *MNRAS*, **399**, 1773
- Cucciati, O., Tresse, L., Ilbert, O., et al. 2012, *A&A*, **539**, A31
- Cui, J., Gu, Q., & Shi, Y. 2024, *MNRAS*, **528**, 2391
- da Costa-Luis, C., Larroque, S. K., Altendorf, K., et al. 2024, tqdm: A Fast Extensible Progress Bar for Python and CLI v4.66.5, Zenodo, doi:10.5281/zenodo.595120
- Dahlen, T., Mobasher, B., Dickinson, M., et al. 2007, *ApJ*, **654**, 172
- Davis, M., Efstathiou, G., Frenk, C. S., & White, S. D. M. 1985, *ApJ*, **292**, 371
- De Lucia, G., & Blaizot, J. 2007, *MNRAS*, **375**, 2
- Dekel, A., & Mandelker, N. 2014, *MNRAS*, **444**, 2071
- Dekel, A., Zolotov, A., Tweed, D., et al. 2013, *MNRAS*, **435**, 999
- Diemer, B., Sparre, M., Abramson, L. E., & Torrey, P. 2017, *ApJ*, **839**, 26
- Dolag, K., Borgani, S., Murante, G., & Springel, V. 2009, *MNRAS*, **399**, 497
- Donnari, M., Pillepich, A., Nelson, D., et al. 2021, *MNRAS*, **506**, 4760
- Donnari, M., Pillepich, A., Nelson, D., et al. 2019, *MNRAS*, **485**, 4817
- Dou, J., Peng, Y., Renzini, A., et al. 2021, *ApJ*, **915**, 94
- Duncan, K., Conselice, C. J., Mortlock, A., et al. 2014, *MNRAS*, **444**, 2960
- Eales, S., de Vis, P., Smith, M. W. L., et al. 2017, *MNRAS*, **465**, 3125
- Faber, S. M. 1972, *A&A*, **20**, 361
- Feldmann, R. 2017, *MNRAS*, **470**, L59
- Finlator, K., Davé, R., & Oppenheimer, B. D. 2007, *MNRAS*, **376**, 1861
- Gallazzi, A., Brinchmann, J., Charlot, S., & White, S. D. M. 2008, *MNRAS*, **383**, 1439
- Gallazzi, A., Charlot, S., Brinchmann, J., White, S. D. M., & Tremonti, C. A. 2005, *MNRAS*, **362**, 41
- Gallazzi, A. R., Pasquali, A., Zibetti, S., & Barbera, F. L. 2021, *MNRAS*, **502**, A457
- Gladders, M. D., Oemler, A., Dressler, A., et al. 2013, *ApJ*, **770**, 64
- González, V., Labbé, I., Bouwens, R. J., et al. 2011, *ApJL*, **735**, L34
- Grazian, A., Fontana, A., Santini, P., et al. 2015, *A&A*, **575**, A96
- Gruppioni, C., Pozzi, F., Rodighiero, G., et al. 2013, *MNRAS*, **432**, 23
- Guo, Q., White, S., Boylan-Kolchin, M., et al. 2011, *MNRAS*, **413**, 101
- Han, Y., Fan, L., Zheng, X. Z., Bai, J.-M., & Han, Z. 2023, *ApJS*, **269**, 39
- Harris, C. R., Millman, K. J., van der Walt, S. J., et al. 2020, *Natur*, **585**, 357
- Heavens, A., Panter, B., Jimenez, R., & Dunlop, J. 2004, *Natur*, **428**, 625
- Hunter, J. D. 2007, *CSE*, **9**, 90
- Ilbert, O., McCracken, H. J., Le Fèvre, O., et al. 2013, *A&A*, **556**, A55
- Ivezić, Ž., Kahn, S. M., Tyson, J. A., et al. 2019, *ApJ*, **873**, 111
- Iyer, K., & Gawiser, E. 2017, *ApJ*, **838**, 127
- Iyer, K. G., Gawiser, E., Faber, S. M., et al. 2019, *ApJ*, **879**, 116
- Jimenez, R., Panter, B., Heavens, A. F., & Verde, L. 2005, *MNRAS*, **356**, 495
- Johnson, B., Foreman-Mackey, D., Sick, J., et al. 2022, dfm/python-fsps: python-fsps v0.4.2rc1, Zenodo, doi:10.5281/zenodo.7113363
- Johnson, B. D., Leja, J., Conroy, C., & Speagle, J. S. 2021, *ApJS*, **254**, 22
- Katz, N., Hernquist, L., & Weinberg, D. H. 1992, *ApJL*, **399**, L109
- Kauffmann, G., White, S. D. M., & Guiderdoni, B. 1993, *MNRAS*, **264**, 201
- Kauffmann, G., White, S. D. M., Heckman, T. M., et al. 2004, *MNRAS*, **353**, 713
- Kauffmann, G., Heckman, T. M., White, S. D. M., et al. 2003, *MNRAS*, **341**, 33
- Kikuchihara, S., Ouchi, M., Ono, Y., et al. 2020, *ApJ*, **893**, 60
- Kroupa, P. 2001, *MNRAS*, **322**, 231
- Lacey, C. G., & Fall, S. M. 1985, *ApJ*, **290**, 154
- Lam, S. K., Pitrou, A., & Seibert, S. 2015, in Proc. Second Workshop on the LLVM Compiler Infrastructure in HPC (New York: ACM), 1
- Laureijs, R., Amiaux, J., Arduini, S., et al. 2011, arXiv:1110.3193
- Lee, S.-K., Ferguson, H. C., Somerville, R. S., Wiklund, T., & Giallisco, M. 2010, *ApJ*, **725**, 1644
- Lee, S.-K., Idzi, R., Ferguson, H. C., et al. 2009, *ApJS*, **184**, 100
- Leja, J., Carnall, A. C., Johnson, B. D., Conroy, C., & Speagle, J. S. 2019a, *ApJ*, **876**, 3
- Leja, J., Johnson, B. D., Conroy, C., van Dokkum, P. G., & Byler, N. 2017, *ApJ*, **837**, 170
- Leja, J., Johnson, B. D., Conroy, C., et al. 2019b, *ApJ*, **877**, 140
- Li, Y. A., Ho, L. C., Shangguan, J., Zhuang, M.-Y., & Li, R. 2023, *ApJS*, **267**, 17
- Lilly, S. J., Carollo, C. M., Pipino, A., Renzini, A., & Peng, Y. 2013, *ApJ*, **772**, 119
- Lilly, S. J., Le Fèvre, O., Hammer, F., & Crampton, D. 1996, *ApJL*, **460**, L1
- Lu, Z., Mo, H. J., Lu, Y., et al. 2015, *MNRAS*, **450**, 1604
- MacArthur, L. A. 2005, *ApJ*, **623**, 795
- Madau, P., & Dickinson, M. 2014, *ARA&A*, **52**, 415
- Madau, P., Ferguson, H. C., Dickinson, M. E., et al. 1996, *MNRAS*, **283**, 1388
- Magnelli, B., Elbaz, D., Chary, R. R., et al. 2011, *A&A*, **528**, A35
- Magnelli, B., Popesso, P., Berta, S., et al. 2013, *A&A*, **553**, A132
- Maraston, C., Pforr, J., Renzini, A., et al. 2010, *MNRAS*, **407**, 830
- Marigo, P., & Girardi, L. 2007, *A&A*, **469**, 239
- Marigo, P., Girardi, L., Bressan, A., et al. 2008, *A&A*, **482**, 883
- Marinacci, F., Vogelsberger, M., Pakmor, R., et al. 2018, *MNRAS*, **480**, 5113

- McLeod, D. J., McLure, R. J., Dunlop, J. S., et al. 2021, *MNRAS*, 503, 4413
- Moster, B. P., Somerville, R. S., Maulbetsch, C., et al. 2010, *ApJ*, 710, 903
- Muzzin, A., Marchesini, D., Stefanon, M., et al. 2013, *ApJ*, 777, 18
- Naiman, J. P., Pillepich, A., Springel, V., et al. 2018, *MNRAS*, 477, 1206
- Neistein, E., van den Bosch, F. C., & Dekel, A. 2006, *MNRAS*, 372, 933
- Nelan, J. E., Smith, R. J., Hudson, M. J., et al. 2005, *ApJ*, 632, 137
- Nelson, D., Pillepich, A., Springel, V., et al. 2018, *MNRAS*, 475, 624
- Nelson, D., Springel, V., Pillepich, A., et al. 2019, *ComAC*, 6, 2
- Nersesian, A., van der Wel, A., Gallazzi, A., et al. 2024, *A&A*, 681, A94
- Noll, S., Burgarella, D., Giovannoli, E., et al. 2009, *A&A*, 507, 1793
- O'Connell, R. W. 1976, *ApJ*, 206, 370
- Ocvirk, P., Pichon, C., Lançon, A., & Thiébaud, E. 2006, *MNRAS*, 365, 46
- Pacifici, C., Charlot, S., Blaizot, J., & Brinchmann, J. 2012, *MNRAS*, 421, 2002
- Pacifici, C., Kassin, S. A., Weiner, B. J., et al. 2016, *ApJ*, 832, 79
- Papovich, C., Dickinson, M., & Ferguson, H. C. 2001, *ApJ*, 559, 620
- Peng, Y.-j., Lilly, S. J., Kovač, S. J., et al. 2010, *ApJ*, 721, 193
- Peng, Y.-j., Lilly, S. J., Renzini, A., & Carollo, M. 2012, *ApJ*, 757, 4
- Peng, Y.-j., & Maiolino, R. 2014, *MNRAS*, 443, 3643
- Perez, F., & Granger, B. E. 2007, *CSE*, 9, 21
- Pillepich, A., Nelson, D., Hernquist, L., et al. 2018a, *MNRAS*, 475, 648
- Pillepich, A., Springel, V., Nelson, D., et al. 2018b, *MNRAS*, 473, 4077
- Pilyugin, L. S., Grebel, E. K., & Mattsson, L. 2012, *MNRAS*, 424, 2316
- Planck Collaboration, Ade, P. A. R., Aghanim, N., et al. 2016, *A&A*, 594, A13
- Reddy, N. A., & Steidel, C. C. 2009, *ApJ*, 692, 778
- Renzini, A. 2006, *ARA&A*, 44, 141
- Renzini, A., & Peng, Y.-j. *ApJL* 2015, 801, L29
- Robotham, A. S. G., & Driver, S. P. 2011, *MNRAS*, 413, 2570
- Rodríguez-Gomez, V., Genel, S., Vogelsberger, M., et al. 2015, *MNRAS*, 449, 49
- Salim, S., Boquien, M., & Lee, J. C. 2018, *ApJ*, 859, 11
- Salim, S., & Narayanan, D. 2020, *ARA&A*, 58, 529
- Salim, S., Rich, R. M., Charlot, S., et al. 2007, *ApJS*, 173, 267
- Salim, S., Lee, J. C., Janowiecki, S., et al. 2016, *ApJS*, 227, 2
- Sánchez, S. F., Avila-Reese, V., Rodríguez-Puebla, A., et al. 2019, *MNRAS*, 482, 1557
- Sánchez, S. F., Kennicutt, R. C., Gil de Paz, A., et al. 2012, *A&A*, 538, A8
- Sánchez-Blázquez, P., Peletier, R. F., Jiménez-Vicente, J., et al. 2006, *MNRAS*, 371, 703
- Sanders, D. B., Mazzarella, J. M., Kim, D. C., Surace, J. A., & Soifer, B. T. 2003, *AJ*, 126, 1607
- Santini, P., Fontana, A., Grazian, A., et al. 2012, *A&A*, 538, A33
- Schaye, J., Crain, R. A., Bower, R. G., et al. 2015, *MNRAS*, 446, 521
- Schaye, J., Kugel, R., Schaller, M., et al. 2023, *MNRAS*, 526, 4978
- Schenker, M. A., Robertson, B. E., Ellis, R. S., et al. 2013, *ApJ*, 768, 196
- Schiminovich, D., Ilbert, O., Arnouts, S., et al. 2005, *ApJL*, 619, L47
- Schmidt, M. 1959, *ApJ*, 129, 243
- Schmidt, M. 1968, *ApJ*, 151, 393
- Shamshiri, S., Thomas, P. A., Henriques, B. M., et al. 2015, *MNRAS*, 451, 2681
- Simha, V., Weinberg, D. H., Conroy, C., et al. 2014, arXiv:1404.0402
- Somerville, R. S., & Primack, J. R. 1999, *MNRAS*, 310, 1087
- Springel, V. 2010, *MNRAS*, 401, 791
- Springel, V., White, S. D. M., Tormen, G., & Kauffmann, G. 2001, *MNRAS*, 328, 726
- Springel, V., Pakmor, R., Pillepich, A., et al. 2018, *MNRAS*, 475, 676
- Takeuchi, T. T., Yoshikawa, K., & Ishii, T. T. 2003, *ApJL*, 587, L89
- Talbot, R. J. J., & Arnett, W. D. 1971, *ApJ*, 170, 409
- Terrazas, B. A., Bell, E. F., Pillepich, A., et al. 2020, *MNRAS*, 493, 1888
- The pandas development Team 2024, pandas-dev/pandas: Pandas, v2.2.2, Zenodo, doi:10.5281/zenodo.3509134
- Thomas, D., Maraston, C., Bender, R., & Mendes de Oliveira, C. 2005, *ApJ*, 621, 673
- Thorne, J. E., Robotham, A. S. G., Davies, L. J. M., et al. 2021, *MNRAS*, 505, 540
- Tinsley, B. M. 1974, *ApJ*, 192, 629
- Tinsley, B. M. 1980, *FCPh*, 5, 287
- Trussler, J., Maiolino, R., Maraston, C., et al. 2020, *MNRAS*, 491, 5406
- van der Wel, A., Noeske, K., Bezanson, R., et al. 2016, *ApJS*, 223, 29
- van der Wel, A., Bezanson, R., D'Eugenio, F., et al. 2021, *ApJS*, 256, 44
- Virtanen, P., Gommers, R., Oliphant, T. E., et al. 2020, *NatMe*, 17, 261
- Walcher, C. J., Coelho, P. R. T., Gallazzi, A., et al. 2015, *A&A*, 582, A46
- Wang, E., & Lilly, S. J. 2021, *ApJ*, 910, 137
- Wang, E., & Lilly, S. J. 2022, *ApJ*, 929, 95
- Wang, K., Peng, Y., & Chen, Y. 2023, *MNRAS*, 523, 1268
- Waskom, M. 2021, *JOSS*, 6, 3021
- Weaver, J. R., Davidzon, I., Toft, S., et al. 2023, *A&A*, 677, A184
- Wetzell, A. R., Tinker, J. L., Conroy, C., & van den Bosch, F. C. 2013, *MNRAS*, 432, 336
- White, S. D. M., & Frenk, C. S. 1991, *ApJ*, 379, 52
- Worthey, G., Faber, S. M., Gonzalez, J. J., & Burstein, D. 1994, *ApJS*, 94, 687
- Worthey, G., & Ottaviani, D. L. 1997, *ApJS*, 111, 377
- Wright, A. H., Driver, S. P., & Robotham, A. S. G. 2018, *MNRAS*, 480, 3491
- Wu, P.-F., van der Wel, A., Gallazzi, A., et al. 2018, *ApJ*, 855, 85
- Wu, P.-F., Nelson, D., van der Wel, A., et al. 2021, *AJ*, 162, 201
- Wyder, T. K., Treyer, M. A., Milliard, B., et al. 2005, *ApJL*, 619, L15
- Yang, X., Mo, H. J., van den Bosch, F. C., et al. 2007, *ApJ*, 671, 153
- Yang, X., Mo, H. J., van den Bosch, F. C., Zhang, Y., & Han, J. 2012, *ApJ*, 752, 41
- York, D. G., Adelman, J., Anderson, J. E. J., et al. 2000, *AJ*, 120, 1579
- Zhan, H. 2011, *SSPMA*, 41, 1441
- Zhou, S., Merrifield, M., & Aragón-Salamanca, A. 2022, *MNRAS*, 513, 5446
- Zhou, S., Mo, H. J., Li, C., Boquien, M., & Rossi, G. 2020, *MNRAS*, 497, 4753
- Zibetti, S., Gallazzi, A. R., Ascasibar, Y., et al. 2017, *MNRAS*, 468, 1902
- Zibetti, S., Gallazzi, A. R., Hirschmann, M., et al. 2020, *MNRAS*, 491, 3562