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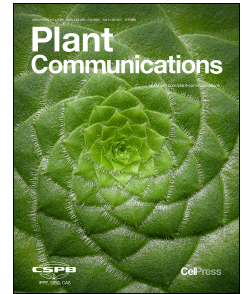
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1 **A predictive model for ethylene-mediated auxin and** 2 **cytokinin patterning in the *Arabidopsis* root**

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12

13 **Running title:** Modelling simultaneous hormone patterns

14

15 **Short summary:**

16 We utilize a wide range of experimental observations to propose a mechanism for
17 simultaneous patterning of auxin and cytokinin concentrations. The mechanism
18 reveals that ethylene signalling is an important factor in achieving simultaneous auxin
19 and cytokinin patterning, while also predicting other experimental observations. This
20 research reveals the importance of hormonal crosstalk in patterning auxin, cytokinin
21 and ethylene in the *Arabidopsis* root.

22

23

24 **ABSTRACT**

25 **The interaction between auxin and cytokinin is important in many aspects of**
26 **plant development. Experimental measurements of both auxin and cytokinin**
27 **concentration and reporter gene expression clearly show the coexistence of**
28 **auxin and cytokinin concentration patterning in *Arabidopsis* root development.**
29 **However, in the context of crosstalk between auxin, cytokinin and ethylene, little**
30 **is known about how auxin and cytokinin concentration patterns simultaneously**
31 **emerge and how they regulate each other in the *Arabidopsis* root. This work**
32 **utilizes a wide range of experimental observations to propose a mechanism for**
33 **simultaneous patterning of auxin and cytokinin concentration. In addition to the**
34 **regulatory relationships between auxin and cytokinin, the mechanism reveals**
35 **that ethylene signalling is an important factor in achieving simultaneous auxin**
36 **and cytokinin patterning, while also predicting other experimental observations.**
37 **Combining the mechanism with a realistic *in silico* root model reproduces**
38 **experimental observations of both auxin and cytokinin patterning. Predictions**
39 **made by the mechanism can be compared with a variety of experimental**
40 **observations, including those conducted by our group and other independent**
41 **experiments reported by other groups. Examples of these predictions include**
42 **patterning of auxin biosynthesis rate, PIN1 and PIN2 pattern changes in *pin3, 4,***
43 **7 mutants, cytokinin patterning change in the *p/s* mutant, PLS patterning, as**
44 **well as various trends in different mutants. This research unravels a plausible**
45 **mechanism for simultaneous patterning of auxin and cytokinin concentrations**
46 **in *Arabidopsis* root development and suggests a key role for ethylene pattern**
47 **integration.**

48 **Key words:** *Arabidopsis* root, auxin patterning, cytokinin patterning, ethylene
49 signalling, *in silico* digital root, spatiotemporal modelling.

50

51 INTRODUCTION

52 A major challenge in plant developmental biology is understanding how development is
53 coordinated by interacting hormones and genes. Plant hormones (Santner and Estelle, 2009)
54 can act antagonistically or synergistically to regulate cell proliferation, elongation and
55 differentiation (Garay-Arroyo et al., 2012; Vanstraelen and Benkova, 2012). The importance
56 of the interaction between auxin and cytokinin in root and shoot development and the
57 maintenance of cell proliferation was shown in very early experiments on cultured tobacco
58 callus (Skoog and Miller, 1957) where the ratio of cytokinin to auxin determined the
59 developmental pathway. While all hormones are involved in the regulation of root
60 development, auxin and cytokinin play central roles in regulating the size of the meristem and
61 root growth (Chandler and Werr 2015; Perilli et al., 2012; Schaller et al., 2015; Friml 2021;
62 Roychoudhry and Kepinski 2022).

63 Auxin and cytokinin cellular concentrations are a function of multiple factors including
64 biosynthesis (Ljung 2013; Jones and Ljung 2011; Zhao 2010; 2014; Casanova-Sáez et al.
65 2021), degradation (Jones and Ljung 2011; Ljung 2013; Casanova-Sáez et al. 2021) and
66 conjugation (Ludwig-Muller 2011). Importantly, both auxin and cytokinin concentrations
67 display distinct patterns in the *Arabidopsis* root. Measuring auxin concentration revealed the
68 presence of IAA concentration gradients within the *Arabidopsis* root tip with a distinct
69 maximum in the organizing quiescent centre (QC) of the root apex (Petersson et al., 2009).
70 Measuring cytokinin concentration revealed an intercellular cytokinin gradient in the primary
71 root tip, with maximum levels in the lateral root cap, columella, columella initials, and QC cells
72 (Antoniadi et al., 2015). Thus, these experimental data directly show that auxin and cytokinin
73 concentration patterns coexist in the *Arabidopsis* root.

74 Many reporter gene expression studies for both auxin and cytokinin are also consistent with
75 the existence of auxin and cytokinin gradients in *Arabidopsis* root (Isoda et al. 2021; Jedlickova
76 et al. 2022). Response patterning, generated by reporter constructs based on various naturally
77 occurring and synthetic promoters, includes imaging of *IAA2::GUS* and *DR5::GFP* (Grieniesen
78 et al., 2007), *DII-VENUS* (Brunoud et al., 2012) and *R2D2* (Liao et al., 2015) for auxin, and
79 *ARR5::GUS* (Werner et al., 2003) and *TCSn::GFP* (Zurcher et al., 2013) for cytokinin. Since
80 the relationship between hormone concentration and the expression of a reporter gene can
81 be non-linear, patterning of reporter gene expression can differ from concentration patterning.
82 Moreover, expression patterning can vary between different response reporters, since, in
83 addition to hormone concentrations, reporter response patterning also depends on other
84 factors such as the sensitivity of the reporter promoter to a hormone. Moreover, reporter

85 expression can also be influenced by multiple signalling pathways as shown in Liu et al.
86 (2017). Nevertheless, patterning of reporter gene expression for both auxin and cytokinin has
87 been widely accepted as a proxy for auxin and cytokinin concentration patterns.

88 Measurements of both auxin and cytokinin concentration and reporter gene expression clearly
89 show the coexistence of auxin and cytokinin concentration patterning in *Arabidopsis* root
90 development (Petersson et al., 2009; Antoniadi et al., 2015; Grieneisen et al., 2007; Liao et
91 al., 2015; Brunoud et al., 2012; Werner et al., 2003; Zurcher et al., 2013). Moreover, a wide
92 range of experimental data show that auxin, cytokinin and ethylene form a complex crosstalk
93 network. Despite progress in experimental studies little is known about how auxin and
94 cytokinin concentration patterns simultaneously emerge and how they regulate each other in
95 the *Arabidopsis* root in the context of crosstalk between auxin, cytokinin and ethylene.
96 Importantly, although various experimental data accumulated over many years have indicated
97 that both auxin and cytokinin patterning play central roles in root development (Chandler and
98 Werr 2015; Perilli et al. 2012; Schaller et al. 2015), an experimentally based mechanism for
99 simultaneous auxin and cytokinin patterning is still elusive. For example: what is the
100 mechanism for the emergence of auxin biosynthesis rate patterning, as experimentally
101 measured in Petersson et al. (2009); what is the mechanism for PIN1 and PIN2 patterning
102 changes in a variety of *pin* mutants, as observed by Blilou et al. (2005) and Omelyanchuk et
103 al. (2016); and what is the mechanism for changes in cytokinin patterning in the *p/ls* mutant
104 reported by Casson et al. (2002)? Therefore, to further elucidate the mechanisms that drive
105 root development, it is essential to better understand the complex multiple relationships
106 between auxin and cytokinin and other developmentally critical hormones, proteins and
107 processes.

108 Auxin fluxes in the *Arabidopsis* root can be described by reverse fountain models (Petrasek
109 and Friml, 2009). Auxin influx and efflux transporters play a key role in auxin patterning
110 (Petrasek and Friml, 2009). Auxin patterning in the *Arabidopsis* root has been subjected to
111 extensive research, in particular, by combining experimental and modelling research
112 (Grieneisen et al. 2007; Band et al. 2014; Moore et al. 2015; 2017; Rutten et al. 2022).
113 Moreover, crosstalk between auxin and cytokinin has also been subjected to combined
114 experimental and modelling studies. For example, Muraro et al. (2011; 2013; 2016) have
115 studied how cytokinin affects auxin-regulated gene expression and how meristem size is
116 regulated by both auxin and cytokinin. Modelling of auxin and cytokinin crosstalk has also
117 been used to elucidate root vascular patterning (Muraro et al. 2014; De Rybel et al. 2014; el-
118 Showk et al. 2015; Mellor et al. 2017; Mellor et al. 2019; Bagdassarian et al. 2023). In addition,

119 how complex auxin and cytokinin hormonal crosstalk regulates cell-fate specification has also
120 been modelled (Garcia-Gomez et al. 2017; 2020). However, in the context of crosstalk
121 between auxin, cytokinin and ethylene, little is known about how auxin and cytokinin
122 concentration patterns regulate each other in the *Arabidopsis* root. We previously showed
123 that, although auxin patterns can be correctly generated by integrating a hormonal crosstalk
124 network with auxin transporters (Moore et al. 2015; 2017), the modelled cytokinin patterns are
125 not in agreement with experimental observations (Moore et al. 2015; Liu et al. 2017). In this
126 work, we propose an integrative mechanism for the simultaneous patterning of both auxin and
127 cytokinin in the *Arabidopsis* root, based on a wide range of experimental data in the literature.
128 The mechanism for simultaneous auxin and cytokinin patterning in *Arabidopsis* root is
129 unravelled by integrating a range of experimental data and is validated by both our
130 experimental data (such as PLS protein patterning and cytokinin response patterning changes
131 in *p/s* mutant), and independent experimental data (such as patterning of the rate of auxin
132 biosynthesis and PIN1 and PIN2 protein patterning changes in *pin3*, *pin4*, *pin7* and *pin3,4,7*
133 mutants).

134

135 RESULTS

136 Interrogating and integrating biological knowledge to form an integrative mechanism 137 for the simultaneous patterning of auxin and cytokinin in the *Arabidopsis* root

138 In developing a model to explain how auxin and cytokinin patterning can be generated, we
139 first looked at relevant evidence from experimental studies. Nordstrom et al. (2004) proposed
140 that auxin inhibits cytokinin biosynthesis and that cytokinin inhibits auxin biosynthesis in the
141 whole seedling. Results indicated that different types of cytokinin (iP and Z type) were
142 predominantly synthesised in either the shoot (Z) or the root (iP) and that while biosynthesis
143 of the Z type cytokinin was inhibited by auxin, the biosynthesis of iP type cytokinin was not
144 inhibited and even potentially promoted by the application of auxin. Therefore, an additional
145 conclusion from this paper could be that while auxin inhibits cytokinin biosynthesis in the whole
146 plant, it might not inhibit cytokinin biosynthesis in the root and could possibly promote it.

147 Additional studies suggest that cytokinin promotes auxin biosynthesis (Jones et al., 2010),
148 auxin upregulates cytokinin biosynthesis through *SHY2* and *IPT5* genes (Dello Iorio et al.,
149 2008), and auxin promotes cytokinin biosynthesis through *TM05* and *LOG4* (De Rybel et al.,
150 2014). Jones et al. (2010) concluded that cytokinin promotes auxin biosynthesis in young

151 developing tissues and that cytokinin inhibits its own biosynthesis through the induction of
152 cytokinin oxidases.

153 Cytokinin concentrations are determined by the balance between biosynthesis, degradation,
154 and transport. Biosynthesis is regulated by rate limiting steps involving the IPT group of
155 enzymes, while irreversible cytokinin degradation occurs through the action of a set of
156 cytokinin oxidases (Werner et al., 2003, 2006). Cytokinin signalling acts through receptors at
157 the plasma membrane and the endoplasmic reticulum (ER) and then through a phospho-relay
158 cascade to activate a set of Type-B ARR transcription factors that target the Type-A ARRs
159 which, while not transcription factors, act as inhibitors of Type-B ARRs (To et al., 2007).
160 Therefore, within this initial pathway cytokinin limits its own responses. Cytokinin is also self-
161 regulated by the activity of cytokinin oxidase (CKX) where increased cytokinin treatment
162 initially increases CKX activity and then reduces it (Figure 4 in Chatfield and Armstrong, 1986).

163 A Type-B ARR of particular interest is ARR2 which appears to have unique properties,
164 whereby phosphorylated ARR2 is rapidly degraded by the proteasome while other Type-B
165 ARRs are not (Kim et al., 2012). Non-degradable ARR2 was found to increase cytokinin
166 sensitivity and to upregulate Type-A ARRs. Multiple ARR2 binding motifs found in the
167 promoter regions of cytokinin-induced genes have led to the suggestion that ARR2 could act
168 as a master regulator of cytokinin signalling responses (Hwang and Sheen, 2001).

169 ARR2 also links the cytokinin pathway with the ethylene pathway (Hass et al., 2004). ARR2
170 binds the *ERF1* promoter and upregulates *ERF1* expression. A stabilized phosphorylated
171 (active) ARR2 showed an ethylene response in the absence of ethylene, even in the presence
172 of AVG, an inhibitor of ethylene biosynthesis. Furthermore, the *arr2* null mutant has a reduced
173 ethylene response, which is rescued by expressing *ARR2* under the control of the *35S*
174 promoter. There are also links in the opposite direction from the ethylene pathway to the
175 cytokinin pathway (Hass et al., 2004) via ARR2. The ethylene receptor ETR1 appears to
176 phosphorylate ARR2 since the ethylene sensitive *etr1-7* (Cancel and Larsen, 2002) loss-of-
177 function mutant (low receptor activity and high downstream ethylene signalling) has reduced
178 levels of phosphorylated ARR2 (Hass et al., 2004). It was concluded that an ETR1-dependent
179 phospho-relay regulates ARR2 phosphorylation and activity (Hass et al., 2004). An additional
180 link between the ethylene and cytokinin pathways is that EIN3 inhibits *ARR5*, a Type-A ARR
181 commonly used in cytokinin reporter constructs (El-Showk et al., 2013; Shi et al., 2012).

182 There are also multiple links between the cytokinin and auxin pathways. Auxin upregulates
183 *IPT* genes through SHY2 (Dello Iorio et al., 2008; Kushwah et al., 2011), and Type-B ARRs

184 ARR1 and ARR12 in turn promote *SHY2* (Dello Iorio et al., 2008; El-Showk et al., 2013), which
185 inhibits *ARF* in the auxin signalling pathway. Auxin also promotes the transcription of *AHP6*,
186 an inhibitor of cytokinin signalling response (Bishopp et al., 2011).

187 ARR2 is suggested to be a central Type-B ARR within the cytokinin signalling pathway, with
188 links to and from the ethylene pathway. Microarray analysis indicates that ARR2 promotes
189 *CKX* expression and activity since *CKX* mRNA is reduced by 2.9 fold in the *arr2* null mutant
190 and increased by 14.1 fold with stabilized activated ARR2, which cannot be degraded and
191 mimics phosphorylation (Hass et al., 2004). Therefore, activity of the ethylene receptor ETR1
192 appears to be able to regulate cytokinin concentrations and response through ARR2 and CKX,
193 by phosphorylating ARR2 and increasing its activity (Hass et al., 2004). As such, it is proposed
194 that active ETR1 receptors (in the absence of ethylene) result in ARR2 phosphorylation and
195 increased ARR2 activity, which in turn results in increased CKX activity and reduced cytokinin.
196 In the presence of ethylene, ETR1 activity is reduced which decreases ARR2 phosphorylation
197 and activity and so reduces CKX activity and increases cytokinin concentrations. This is
198 consistent with experimental results which show an increase in cytokinin concentration in the
199 ethylene hyper-signalling *p/s* mutant compared to wildtype (Liu et al., 2010).

200 These lines of evidence indicate that ethylene responses positively regulate cytokinin
201 concentration by inhibiting CKX activity. In previous studies on auxin, cytokinin and ethylene
202 crosstalk in the *Arabidopsis* root (Liu et al., 2010, 2013; Moore et al., 2015, 2017), the
203 regulation of cytokinin concentration by ethylene signalling was not studied. In previous work
204 (Moore et al., 2015), even after cytokinin biosynthesis was restricted to the vascular cylinder,
205 the modelled cytokinin patterning was still significantly different from experimental
206 observations (Werner et al., 2003). Previous studies were only able to reproduce auxin
207 patterning, and an experimentally based mechanism for the simultaneous emergence of auxin
208 and cytokinin patterning in the *Arabidopsis* root remained elusive. Here we show that the
209 biological evidence discussed above is vital to explain the simultaneous patterning of auxin
210 and cytokinin, while also allowing model predictions to match other experimental observations.
211 Figure 1A summarises the mechanism in detail, and Figure 1B shows a simplified form, in
212 which the red lines highlight the biological evidence discussed above. Specifically, this
213 indicates that cytokinin promotes auxin biosynthesis, auxin promotes cytokinin biosynthesis,
214 and ethylene signalling inhibits cytokinin degradation, so promoting cytokinin accumulation.
215 As demonstrated below, combining such a mechanism with cell-to-cell communications
216 simultaneously generates auxin and cytokinin patterning and also makes predictions that
217 match independent experimental observations.

218 **Relationship of auxin, cytokinin and ethylene in a homogenous cell following the**
219 **mechanism**

220 The mechanism shown in Figures 1A and 1B describes how auxin, cytokinin and ethylene
221 mutually promote each other. For a cell without communications with other cells, Figure 2
222 shows that increasing any of auxin, cytokinin or ethylene biosynthesis rate always
223 simultaneously enhances the concentration of all three hormones. For example, increasing or
224 decreasing the key parameter for auxin biosynthesis by 1% from its value for wild type (Figure
225 2A) results in a similar increase or decrease of both auxin and cytokinin concentration by ca.
226 0.6%, while ethylene concentration increases or decreases by ca. 0.2%. Figure S1 shows an
227 example of simultaneously enhancing the concentration of auxin, cytokinin and ethylene by
228 increasing auxin biosynthesis rate in homogenous cells of the root.

229 **The mechanism reproduces experimental observations of both auxin and cytokinin**
230 **patterning in a realistic *in silico* root**

231 The mechanism described in Figure 1 is a hormonal crosstalk network for auxin, ethylene and
232 cytokinin extracted from a more complex auxin, ethylene and cytokinin network in Arabidopsis
233 root development (Liu et al., 2017). Investigating patterning requires the combination of a
234 crosstalk network with a realistic digital root structure. A method to generate a 2-dimensional
235 (2D) digital realistic root was previously developed and described in detail (Moore et al., 2017).
236 The digital *in silico* root, as summarised in Figure 1 in Moore et al. (2017), is derived from
237 experimental imaging and contains actual cell geometry and multicellular root organisation
238 that allows the study of cell-cell communication (Band et al., 2014). In the *in silico* root, each
239 cell contains two spatial identities: the cytosol, and the plasma membrane and cell wall,
240 specific to each cell. For simplicity, adjacent plasma membrane and cell wall entities for the
241 same cell are represented by a single identity containing both cell wall and plasma membrane
242 properties. The *in silico* root also includes extracellular space but does not include any
243 subcellular structures.

244 The regulation and placement of the auxin influx and efflux carriers (PIN1,2,3,4,7 and AUX1,
245 LAX2,3 and ABCB) within the *in silico* root is based on experimental data as described
246 previously (Moore et al., 2015, 2017). PIN1 and PIN2 carrier levels are regulated by the three
247 hormones (Figure 1A). The rate that cytosolic PIN1 or PIN2 protein is placed at, and removed
248 from, the plasma membrane was selected so that their polarity in the *in silico* root is similar to
249 experimentally observed polarity (Moore et al., 2015, 2017). Other auxin carriers are
250 prescribed based on experimental data because there is insufficient experimental data to
251 establish how their levels and polarity are regulated by the three hormones (Moore et al.,

252 2017). PIN3, PIN4 and PIN7 efflux carrier concentration levels and polar localisation have
253 prescribed concentrations at selected cell faces based on experimental imaging described in
254 the literature (Blilou et al., 2005). The non-polar auxin influx carriers AUX1, LAX2 and LAX3
255 also have prescribed localizations and levels based on experimental imaging (Band et al.,
256 2014). The relative concentrations of PIN3, PIN4, PIN7, AUX1, LAX2 and LAX3 carriers are
257 adjusted to generate wildtype auxin patterning. Since the ABCB family of auxin carriers can
258 reversibly redirect auxin flux, the role of ABCB carriers in transporting auxin has been implicitly
259 incorporated into the non-polar base level of PIN and AUX1/LAX activity, to simplify modelling
260 analysis.

261
262 Where available, we have used parameter values from the literature (Moore et al., 2015,
263 2017). Since it is unknown if the biological knowledge accumulated in the literature is capable
264 of simultaneously generating auxin and cytokinin patterning in the *Arabidopsis* root, we have
265 adjusted the unknown parameters and examined the patterning of both auxin and cytokinin,
266 to test the relationship between the known signalling interactions described above and the
267 simultaneous patterning of auxin and cytokinin. Figures 3 and 4 show that the mechanism
268 described in Figure 1, coupled with the realistic *in silico* root, can simultaneously generate
269 auxin and cytokinin patterning that is in general agreement with experimental results. This
270 indicates that the biological knowledge accumulated in the literature is sufficient to describe a
271 mechanism to simultaneously generate auxin and cytokinin patterning in the *Arabidopsis* root.

272 Figures 3A and 3B show that the auxin concentration patterning generated by this mechanism
273 is similar to auxin response patterning observed using DR5-GFP fluorescence. Figures 3A,
274 3C-3F display the auxin concentration patterning generated by this mechanism, showing
275 patterning in the root tip (Figure 3A), and progressive enlargements in the elongation zone
276 (Figures 3C, 3D) and QC region (Figures 3E, 3F). A pronounced auxin maximum occurs in
277 the QC region (Figures 3A, 3E, 3F), with relatively high auxin levels in the columella and the
278 root cap (Figures 3A, 3E). Auxin concentration declines, from the QC maximum, in the cell
279 files above the initials and proximally up the vascular cylinder (Figures 3A, 3E). Interestingly,
280 there is a clear increase in auxin concentration in the epidermis starting in the TZ and moving
281 into the elongation zone (Figure 3A, 3C) and a similar but less obvious increase in the cortex
282 (Figure 3A). Figures 3C and 3D show the existence of predicted auxin gradients within
283 individual cells, with auxin declining at the proximal boundary of the epidermal cells in the
284 elongation zone where the PIN efflux carriers remove auxin from the cell, and then increasing
285 at the distal boundary of the neighbouring shootward cell due to the action of the auxin influx

286 carriers. Auxin gradients may also emerge in extracellular space due to diffusion of auxin
287 (Figures 3D, 3F).

288 Modelled auxin concentration patterning (Figures 3A, 3C to 3F) is in agreement with various
289 experimental observations, including IAA distribution (Figure S2A; Figure 3 in Petersson et al.,
290 2009), auxin response patterning *DR5::GFP* and *IAA2::GUS* (Figure S2B; S2C; Figures 3 and
291 4 in Grieneisen et al., 2007), and relative auxin levels based on the DII-VENUS inverse auxin
292 response reporter (Figure S2D; Figure 2 in Brunoud et al., 2012). The different experimental
293 observations give somewhat differing results for auxin patterning. The relative IAA distribution,
294 based on cell sorting and mass spectrometry of various *Arabidopsis* lines, shows a distinct
295 auxin maximum in the QC region, and higher auxin levels in the lateral root cap, cortex,
296 endodermis and vascular cylinder compared to the columella and epidermis (Figure S2A;
297 Figure 3 in Petersson et al., 2009). However, apart from the distinct differences between these
298 regions the relative IAA distribution does not provide much additional information on auxin
299 gradients. The *DR5::GFP* auxin response reporter (Figure S2B; Figure 3 in Grieneisen et al.,
300 2007) identifies a high auxin response in the QC region and the proximal region of the
301 columella, with the signal quickly declining in a shootward direction along the centre line of the
302 vascular cylinder. There is no indication of relatively high auxin response in the lateral root
303 cap or of an increase in the epidermis in the elongation zone (EZ). *In silico* results are in better
304 agreement with the *IAA2::GUS* auxin reporter (Figure S2C; Figure 4 in Grieneisen et al.,
305 2007), with a high auxin response in the QC region, columella and lateral root cap, and a
306 proximally declining signal in the vascular cylinder. However, a noticeable difference between
307 *in silico* results and experimental data using the *IAA2::GUS* reporter is that the reporter does
308 not indicate a signal increase in the epidermis in the EZ. The auxin response image derived
309 from the DII-VENUS auxin reporter (Figure S2D; Figure 2 in Brunoud et al., 2012) which gives
310 an inverse auxin response signal, shows a maximum auxin response in the QC, high auxin
311 response in the columella and lateral root cap, and a reduced response moving shootward
312 along the vascular cylinder. In the epidermis, the response declines proximal to the initials and
313 then starts to increase again at the beginning of the transition zone (TZ) , which is ca.
314 longitudinal position 650 in Figure 3. *In silico* patterning is in good agreement with results
315 generated by the DII-VENUS reporter (Figure S2D; Figure 2 in Brunoud et al., 2012). However,
316 this epidermal patterning trend is not observable using *DR5::GFP* (Figure 3B; S2B). Following
317 Brunoud et al. (2012), a possible explanation is that responses of these reporters can differ
318 since *DR5* auxin response is also influenced by multiple signalling pathways.

319

320 Many features of *in silico* cytokinin concentration patterning (Figures 4A, 4C to 4F) are similar
321 to those of *in silico* auxin patterning (Figures 3A, 3C to 3F). Cytokinin displays a maximum
322 relative concentration in the QC region (but not to the same degree as auxin), with high
323 concentrations in the columella and lateral root cap and with gradients similar to auxin in the
324 vascular cylinder and epidermis.

325 Key features of the modelled cytokinin concentration patterning agree with experimental
326 observations using ARR5-GFP fluorescence (Figure 4B) and other experimental observations
327 as described below. The relative cytokinin concentration measured using cell sorting and mass
328 spectrometry (Figure S3A; Figure 5 in Antoniadi et al., 2015) indicate high cytokinin
329 concentrations in the QC region, columella and lateral root cap, medium concentrations in the
330 vascular cylinder and in the epidermis and cortex in the TZ and EZ, and lower concentrations
331 in the endodermis. The *in silico* concentration patterning (Figures 4A, 4C to 4F) is very similar
332 to these experimental observations. Cytokinin response was also measured using the
333 *ARR5::GUS* reporter (Figure S3B; Figure 3 in Werner et al., 2003) or using the *TCSn::GFP*
334 reporter (Figure S3C; Figure 4 in Zurcher et al., 2013).

335 One marked difference between the experimental results for relative cytokinin concentration
336 measurements (Figure S3A; Figure 5 in Antoniadi et al., 2015) and cytokinin response
337 observations (Figure 4B; Figure S3B; Figure 3 in Werner et al., 2003; Figure S3C; Figure 4 in
338 Zurcher et al., 2013) occurs in the QC region. While a high cytokinin concentration is measured
339 in the QC by Antoniadi et al. (2015), a high cytokinin response is observed in the initials just
340 proximal to the QC (Figure 4B; Figure S3B; Figure 3 in Werner et al., 2003; Figure S3C; Figure
341 4 in Zurcher et al., 2013). The modelled concentration patterning (Figure 4A) more closely
342 matches the measured cytokinin concentration patterning in the QC (Figure S3A; Figure 5 in
343 Antoniadi et al., 2015). A possible explanation for the difference between these experimental
344 results is that cytokinin response is suppressed by the very high auxin concentration in the
345 QC, via AHP6 signalling (Bishopp et al., 2011; Liu et al., 2017). On the other hand, Figures
346 4A and 4E also show that cytokinin concentration in a row of the cells below QC is noticeably
347 lower. This is inconsistent with the measured cytokinin concentration patterning in those cells
348 (Figure S3A; Figure 5 in Antoniadi et al., 2015). Thus, how AHP6 signalling regulates cytokinin
349 response in those cells remains to be elucidated since modelled auxin concentration in those
350 cells is relatively low (Figure 3).

351 **Modelling predictions match a variety of experimental observations**

352 The above results demonstrate that simultaneous patterning of both auxin and cytokinin in the
353 *Arabidopsis* root (Figures 3 and 4) can emerge from a model based on a wide range of
354 biological data. A further question is whether the mechanism can predict independent
355 experimental observations. To predict different experimental outputs, we integrated the
356 mechanism with the realistic digital root and parameters for reproducing simultaneous
357 patterning of both auxin and cytokinin. This allows *in silico* predictions to be compared with a
358 variety of experimental observations, generated both by our group and independently by other
359 groups, as follows.

360 **a) Auxin response trends in cell files above the initials**

361 Relative auxin concentration trends in the epidermis, cortex, endodermis cells files above the
362 initials were experimentally established using the R2D2 reporter (Figure S4A; Supplementary
363 Figure 7 in Liao et al. 2015). Using the *in silico* wildtype, the auxin concentration was calculated
364 at all grid points in the digital root. The average auxin concentration in each cell was then
365 calculated by averaging all grid points within the cell. The computed auxin trends for the
366 epidermis, cortex, and endodermis cells files above the initials (Figure 5A) closely match
367 experimental results as shown by superimposing the *in silico* results onto the experimental
368 graph (Figure S4B, C, D, E). Specifically, in all four cell layers, a significant decrease in auxin
369 concentration is observed immediately in the cells above the initials, then the reduction in
370 auxin concentration becomes much slower. In the epidermis, following the initial decrease,
371 auxin concentration then increases slightly for the cells further above its initial. In the cortex
372 and the pericycle the overall decrease in relative auxin concentration, in both experimental
373 results and modelling results, is somewhat greater than observed in other cell layers. This
374 demonstrates that the model is able to predict the pattern of auxin concentration for different
375 tissues. However, when the four cell files are compared to each other, Figure S4F shows that
376 for the cells near the initials, the level of the average auxin concentration does not follow a
377 clear order. This is in contrast to experimental observations (Figure S4A), in which the average
378 auxin concentration follows a clear order and sequentially decreases from epidermis,
379 endodermis, cortex, to pericycle. For the cells further above the initials, the average auxin
380 concentration follows the clear order that agrees with experimental observations. This
381 indicates a limitation of the model to quantitatively predict the order of the average auxin
382 concentration among some cells of the four cell files.

383 **b) Auxin response minimum in the transition zone**

384 Experimental results indicate that a minimum in the auxin response along the root axis (Figure
385 S5A; Figure 3 in Di Mambro et al. 2017) occurs at the boundary of the proximal meristem and

386 distal transition zone, and that this minimum triggers a key developmental switch between cell
387 division and cell differentiation (Di Mambro et al., 2017). Using the *in silico* wildtype, a
388 longitudinal auxin concentration profile was calculated (Figure 5B) by progressively averaging
389 auxin concentrations along the axis of the root (Figure 2A). The *in silico* results (Figure 5B)
390 display an auxin concentration minimum in the distal TZ, similar to experimental observations
391 (Figure S5A; Figure 3 in Di Mambro et al. 2017). Specifically, the longitudinal auxin
392 concentration profile (Figure 5B) shows that auxin concentration decreases quickly from QC,
393 approximately remains unchanged until above transition zone, then increases in the
394 elongation zone. This demonstrates that, after both auxin and cytokinin patterning is fitted to
395 experimental observations, an auxin concentration minimum intrinsically emerges in the distal
396 TZ (Figure S5B).

397 **c) Average auxin concentration trends in WT, *pls* mutant, *pls etr1* double mutant, and** 398 **PLSox**

399 Experimental data have demonstrated that up- or down-regulation of the *PLS* gene or the
400 ethylene receptor protein ETR1 alters ethylene signalling responses (Casson et al. 2002;
401 Chilley et al., 2006; Liu et al., 2010b). In *etr1* mutant, ethylene signalling response is up-
402 regulated. Figure 5C shows that *in silico* predictions of the trend in average auxin
403 concentration for the *pls* mutant, *pls etr1* double mutant, and the *PLS* overexpressing
404 transgenic (*PLSox*), are in general agreement with experimental observations (Figure S6A;
405 Figure 4C in Chilley et al. 2006). In the *pls* mutant, the experimentally measured auxin
406 concentration is lower than in the wildtype; in the *pls etr1* double mutant auxin concentration
407 is higher than the *pls* mutant, but still slightly lower than in the wildtype; and in *PLS*
408 overexpressing seedlings, auxin concentration is higher than wildtype (Figure S6A; Figure 4C
409 in Chilley et al. 2006). Modelled auxin concentration trends were superimposed over the
410 experimental results (Figure S6B) and the modelled trends are in general agreement with
411 experimental observations although, in the *pls etr1* double mutant, modelled auxin
412 concentration is markedly lower than its experimental counterpart. *PLS* is a protein interacting
413 with ethylene receptors (Casson et al. 2002; Chilley et al., 2006; Liu et al., 2010b; Mudge et
414 al. 2023), and manipulating *PLS* activity affects ethylene signalling (Chilley et al., 2006; Liu et
415 al., 2010b). Therefore, when both auxin and cytokinin patterning are fitted to experimental
416 observations following the mechanism (Figure 1), the effects of genetic manipulation of
417 ethylene signalling on average auxin concentration in the root can also be predicted.

418 **d) Patterning the rate of auxin biosynthesis**

419 The rate of auxin biosynthesis also demonstrates patterning in the root tip (Figure S7; Figure
420 5 in Petersson et al. 2009). Using the *in silico* wildtype simulation, the computed patterning of
421 the rate of auxin biosynthesis shows high levels of biosynthesis in the columella and the QC
422 region, lower levels in the TZ, and an increase in biosynthesis rates in the epidermis, cortex
423 and central vascular cylinder in the EZ. There is a close match between experimental (Figure
424 S7; Figure 5 in Petersson et al. 2009) and predicted auxin biosynthesis rate patterning (Figure
425 5D). Thus, the proposed mechanism is not only able to predict important features of auxin
426 concentration patterning, but also to predict patterning of the rate of auxin biosynthesis.
427 Therefore, auxin patterning, transport and metabolism are elucidated as an integrated system
428 in this work.

429 **e) The average concentration trend of PIN1 and PIN2 proteins in WT, PLSox transgenic,**
430 ***pls* and *etr1* mutants, and *pls etr1* double mutant.**

431 Immunolocalization experiments (Figure S8; Figure 1B in Liu et al. 2013) showed that both
432 PIN1 and PIN2 protein levels increase in the *pls* mutant and decrease in PLSox compared to
433 wildtype; in the ethylene-insensitive *etr1* mutant PIN1 and PIN2 levels are lower than in
434 wildtype; and the *pls etr1* double mutant exhibits reduced PIN1 and PIN2 levels compared to
435 *pls* and is marginally lower than wildtype. The *in silico* trends for these mutants (Figure 6A)
436 are similar to experimental observations, demonstrating that the proposed mechanism is able
437 to predict changes in PIN1 and PIN2 levels, and therefore predict how genetic manipulations
438 can alter the average auxin transporter concentration in the root.

439 **f) Predicted changes in PIN1 and PIN2 concentrations in *pin3*, *pin4*, *pin7* mutants**

440 So far, we have demonstrated that the *in silico* wildtype simulation is able to predict many
441 features of auxin patterning and trends in auxin, and PIN1 and PIN2 levels in various mutants.
442 A further question is whether PIN1 and PIN2 patterning changes can also be predicted.

443 Production and degradation of both PIN1 and PIN2 in a cell is assumed to follow the same
444 mechanism based on experimental observations as analysed previously (Moore et al. 2015;
445 2017; Liu et al. 2013). However, PIN1 and PIN2 are distinguished by their polarity and location
446 settings in different parts of the root tip.

447 Figure 6B shows *in silico* predictions for the percentage change in PIN1 or PIN2
448 concentrations relative to WT for the *pin3*, *pin4* and *pin7* single mutants and the *pin3pin4pin7*
449 triple mutant. Figure 6C is an enlargement of the proximal vasculature for the *pin4* single
450 mutant image in Figure 6B. Modelled change in PIN1 patterning for the *pin3*, *pin4* and *pin7*
451 single mutants (Figures 6B and 6C) is similar to experimental observations (Figure S9A;

452 Figure 6 in Omelyanchuk et al. 2016). In particular, the region of PIN1 expression extends
453 shootward up the vasculature in these mutants (Figure S9A; Figure 6 in Omelyanchuk et al.
454 2016).

455 The modelled PIN1 concentration changes in the *pin3* mutant versus wildtype (Figure 6B)
456 shows a significant increase in the proximal vasculature and in the columella. This is
457 consistent with experimentally observed PIN1 expression in the same mutant (Figure S9A;
458 Figure 6 in Omelyanchuk et al. 2016).

459 Moreover, the modelled PIN1 concentrations in the *pin4* mutant show slight increases at the
460 plasma membrane in the proximal vasculature (Figure 6B). This is consistent with
461 experimental *pin4* mutant observations (Figure S9A; Figure 6 in Omelyanchuk et al. 2016).

462 In addition, the modelled PIN1 patterning change in the *pin7* mutant (Figure 6B) is similar to
463 experimental observations (Figure S9A; Figure 6 in Omelyanchuk et al. 2016), in which an
464 increase in *PIN1* concentration can be seen in the proximal vasculature of the *pin7* mutant.

465 Thus, the integrative mechanism for the simultaneous auxin and cytokinin patterning is able
466 to make correct predictions on the change of PIN1 patterning in *pin3*, *pin4* and *pin7* mutant.

467 In addition, experimental observations show changes in PIN2 patterning in the *pin3pin4pin7*
468 triple mutant. A clear increase in PIN2 level in the vasculature emerges (Figure S9B; Figure 1
469 in Blilou et al. 2005). Modelled change in PIN2 patterning for the *pin3pin4pin7* triple mutant
470 predicts a significant increase in PIN2 concentrations in the vasculature (Figure 6B), which is
471 consistent with experimental observation (Figure S9B; Figure 1 in Blilou et al. 2005).

472 These results indicate that the integrative mechanism proposed in this research predicts the
473 main features of patterning change in PIN1 and PIN2 concentration in *pin3*, *pin4*, *pin7* mutants
474 and as such elucidates how PIN1 and PIN2 patterning changes in single and triple *pin*
475 mutants.

476 **g) Cytokinin patterning and concentration change in *pls* mutant.**

477 Figures 5 and 6 demonstrate that the mechanism described in Figure 1 is able to predict
478 patterning and/or trends in auxin concentration, auxin biosynthesis rate, and PIN1,2. The
479 mechanism can also predict patterning and concentration change for cytokinin in *pls* mutant.

480 First, auxin, cytokinin, and ethylene all regulate gene expression (Binder 2020; Kieber and
481 Schaller 2018; Weijers and Wagner 2016). *PLS* gene expression is regulated by both auxin
482 and ethylene (Chilley et al., 2006; Liu et al. 2010). Modelled patterning of *PLS* expression

483 predicts measured proPLS::PLS:GFP fluorescence (Figure 7A). Modelled PLS levels are high
484 in the columella, lateral root cap and QC region, which is consistent with experimental
485 observations (Figure 7A). This demonstrates that the mechanism proposed in this research is
486 also able to predict gene expression patterning.

487 PLS protein has a role in regulating ethylene signalling (Chilley et al., 2006; Liu et al. 2010)
488 that in turn regulates auxin and cytokinin concentration and signalling (Figure 1). Thus, an
489 important question is how PLS patterning regulates concentration and patterning of other
490 components in Figure 1.

491

492 Figure 7B predicts that, in the *pls* mutant, modelled cytokinin concentration has a 1.48 -fold
493 increase relative to wildtype. This compares favourably to experimental results (Table 1 in Liu
494 et al., 2010) that show a 1.42 median fold increase. In addition, modelling reveals that cytokinin
495 concentration in *pls* shows a significant increase in the columella, lateral root cap and QC
496 region (Figure 7C), which is similar to experimental observations using TCSn:GFP
497 fluorescence (Figure 7D). Thus, effects of *pls* mutant on the concentration and patterning of
498 cytokinin are correctly predicted by the mechanism proposed in this research (Figure 1).

499

500 In addition, Figure S10 predicts that ethylene concentration in *pls* mutant is the same as that
501 in wildtype. This is consistent with experimental observations (Chilley et al., 2006).

502

503 **Modelling reveals the role of regulatory relationships in auxin and cytokinin** 504 **concentration and patterning**

505 So far, we have demonstrated that the model based on the mechanism, Figure 1, is able to
506 not only generate simultaneous patterning of both auxin and cytokinin, but also predict a
507 variety of experimental observations. Here we further show that the model is able to develop
508 insights into the role of regulation in auxin and cytokinin patterning.

509 **a) Auxin influx and efflux transporters are the key driver for auxin patterning**

510 Figure S11 shows that auxin patterning still emerges when auxin biosynthesis is not regulated
511 by cytokinin or ethylene with all auxin transporters being fixed as those in the wildtype. This
512 indicates auxin influx and efflux transporters are the key players for generating auxin
513 patterning. Moreover, both cytokinin and ethylene patterning still emerges. However, Figure
514 S11 also reveals that the percentage change in the concentration of auxin, cytokinin and
515 ethylene is different in different cells, and therefore the regulation of auxin biosynthesis plays

516 a fine-tuning role in patterning. In the absence of auxin biosynthesis regulation, Figures S12,
 517 S13 and S14 show that predictions about the trends in different mutants (Figure S12C, S12D,
 518 S13A, S14B) are affected. In particular, the patterning of auxin biosynthesis rate cannot be
 519 predicted anymore (Figure S12D). In addition, Figure S11 shows that the concentration of
 520 auxin, cytokinin and ethylene in the epidermis is higher than that in the cortex. This is
 521 consistent with the mutual positive regulation of auxin, cytokinin and ethylene (Figure 1, 2,
 522 S1). This high concentration in epidermis still exists when the regulation of auxin biosynthesis
 523 by ethylene and cytokinin is removed, but it is generally less obvious since the percentage
 524 reduction relative to wildtype is relatively large (Figure S11). High concentration in epidermis
 525 was also previously modelled (Band et al. 2014) in the absence of regulation in auxin
 526 biosynthesis. Therefore, regulation of auxin biosynthesis plays a fine-tuning role in the high
 527 auxin concentration in the epidermis. Figure 2, 3, S11 also show that the intracellular gradient
 528 of auxin, cytokinin and ethylene in epidermis is large. To the best of our knowledge, no
 529 experimental observations about this gradient have been observed.

530 **b) Regulation of cytokinin degradation by ethylene signalling is important for predicting**
 531 **auxin and cytokinin concentration trend in mutants**

532 Figure S15, S16, S17 show that, in the absence of the regulation of cytokinin degradation by
 533 ethylene signalling, auxin concentration trend in mutants and patterning in auxin biosynthesis
 534 rate are incorrectly predicted (Figure 15C; 15D). Moreover, Figure S17B predicts a lower
 535 average cytokinin concentration in *pIs* mutant than that in wildtype, which is opposite to
 536 experimental observations (Figure 5).

537 **c) Regulation of cytokinin biosynthesis by auxin signalling is important for predicting**
 538 **auxin concentration trend in mutants and patterning of auxin biosynthesis rate**

539 Figures S18, S19, S20 show that, in the absence of the regulation of cytokinin biosynthesis
 540 by auxin signalling, auxin concentration trend in mutants and patterning in auxin biosynthesis
 541 rate are incorrectly predicted (Figure 18C; 18D). Moreover, Figure 20C shows that cytokinin
 542 patterning does not emerge anymore.

543 **d) Role of changes in PIN1 and PIN2 concentration and patterning in various mutants**

544 Figures S21, S22, S23 and S24 show that changes in PIN1 and PIN2 concentration and
 545 patterning in *pin3*, *pin4*, *pin7* or *pin3,4,7* mutants play a fine-tuning role in the concentration
 546 and patterning of auxin, cytokinin and ethylene. Interestingly, they differentially affect different
 547 cells. For example, in *pin3,4,7* triple mutant, if PIN1 and PIN2 are fixed at wildtype levels,
 548 auxin concentration in some stele and columella cells increases with a larger percentage.

549

550 e) Role of various mutants related to ethylene signalling

551 In addition to the analysis of the role of regulatory relationships in auxin and cytokinin
552 concentration and patterning, modelling can also predict the role of various mutants for future
553 experimental validations. For example, Figures S25, S26, S27 and S28 reveal that various
554 mutants related to ethylene signalling can simultaneously change the concentration and
555 patterning of auxin, cytokinin and ethylene.

556 DISCUSSION

557 By interrogating and integrating biological knowledge, this research has revealed a
558 mechanism for the simultaneous patterning of auxin and cytokinin in the *Arabidopsis* root.
559 Based on modelling of the mechanism and experimental investigations, this research reveals
560 that simultaneous auxin and cytokinin concentration patterning emerges from multi-level
561 regulation of auxin, cytokinin and ethylene in the root, as summarised in Figure S29.

562 The mechanism not only simultaneously generates auxin and cytokinin patterning that agrees
563 with experimental observations in the *Arabidopsis* root (Figures 2, 3), but also makes a wide
564 range of predictions that are validated by experimental measurements generated by our group
565 and by independent experimental observations generated by other groups (Figures 5,6,7).
566 Therefore, we consider that the mechanism is plausible, based on current knowledge.

567 This mechanism suggests some important aspects about simultaneous patterning of auxin
568 and cytokinin, with a novel key role played by ethylene. The following regulatory relationships
569 are important for simultaneously generating auxin and cytokinin patterning. First, cytokinin
570 promotes auxin biosynthesis (Jones et al., 2010), auxin upregulates cytokinin biosynthesis
571 through SHY2 and IPT5 (Dello loio et al., 2008), and auxin promotes cytokinin biosynthesis
572 through TM05 and LOG4 (De Rybel et al., 2014). This compares to previously proposed
573 regulatory relationships (Moore et al., 2015), where auxin inhibited cytokinin biosynthesis and
574 cytokinin inhibited auxin biosynthesis (based on Nordstrom et al., 2004) which, while
575 generating auxin patterning similar to experimental observation, could not generate
576 representative cytokinin patterning. Second, a novel ethylene regulatory link is also important
577 for the simultaneous patterning of auxin and cytokinin, and for the simulation to predict a range
578 of experimental results. This new regulatory link is based on experimental evidence discussed
579 in this manuscript and in Liu et al. (2017). Briefly, an ETR1-dependent phospho-relay
580 promotes ARR2 phosphorylation and activity, ARR2 promotes *CKX* expression and activity,
581 and cytokinin degradation occurs through the action of a set of CKX (Werner et al., 2003,

582 2006). These and other experimental observations (Kim et al., 2012; Werner et al., 2003;
583 Werner et al., 2006; To et al., 2007, Hass et al., 2004) establish the regulation of cytokinin
584 concentration by ethylene signalling through components of the cytokinin pathway. Inclusion
585 of these regulatory links generates simultaneous patterning of both auxin and cytokinin similar
586 to experimental observations and in addition enables the mechanism to predict a variety of
587 experimental observations (Figures 3 to 7).

588 This research therefore demonstrates that, although the regulation of auxin, cytokinin and
589 ethylene concentration in *Arabidopsis* root is very complex (Liu et al., 2017), and the
590 experimental data available in the literature are diverse, the integration of the available
591 experimental data is able to derive a plausible mechanism to both study the patterning of auxin
592 and cytokinin as an integrative system and also predict various experimental observations. As
593 a result, this work proposes a mechanism which enables the rational study of the complex and
594 important simultaneous regulation of auxin and cytokinin patterning.

595 Since auxin and cytokinin responses are induced by their concentrations, it is reasonable to
596 consider that auxin and cytokinin response patterning is closely related to auxin and cytokinin
597 concentration patterning. In principle, the mechanism proposed in this work can be extended
598 to analyse auxin and cytokinin responses by establishing links between concentration and
599 response. However, the relationship between concentration and response is generally
600 nonlinear. For example, it was shown that modelling the response of DII-VENUS reporter to
601 auxin requires a model to describe the nonlinear relationship between DII-VENUS and auxin
602 concentration (Band et al. 2012). Moreover, given the complexity of the pathways and multiple
603 links between pathways (Liu et al., 2017), all hormone responses will, to varying degrees, be
604 regulated by multiple hormone activity. Two good examples of this are the regulation of the
605 cytokinin response regulator ARR5 by both ethylene and cytokinin, and the regulation of
606 cytokinin response by both cytokinin and auxin through AHP6 (Liu et al., 2017). Thus,
607 response modelling may require analysis of how interactions between multiple hormones
608 determine response levels. For example, it was shown that elucidating cytokinin response also
609 needs to consider response regulation by auxin (De Rybel et al., 2014). A gene regulatory
610 network involving both auxin and cytokinin establishes and maintains vascular patterning
611 (Muraro et al. 2014). Moreover, the link from transverse auxin fluxes to lateral root initiation is
612 regulated by both auxin and cytokinin (el-Showk et al., 2015). Importantly, all of these studies
613 demonstrate that relationships between auxin and cytokinin concentration and response are
614 nonlinear (Mellor et al., 2017). Thus, establishing the link between hormone concentration and

615 response needs to carefully establish the various concentration-to-response relationships
616 based on relevant experimental data.

617 Cytokinin movement in the root can be passive via diffusion but can also be regulated by
618 cytokinin transporters. This work considers that cytokinin movement is via diffusion due to lack
619 of knowledge about distribution of cytokinin transporters in the root and the kinetics of such
620 transporters (Kang et al., 2017). Once the kinetics of cytokinin transporters have been
621 established, interesting future research can include the study of how the cytokinin transporters
622 and cytokinin diffusion work together to transport cytokinin and influence patterning and
623 development.

624 Extracting a mechanism for simultaneously patterning of auxin and cytokinin necessitates the
625 simplification of complex interactions between multiple hormones. The mechanism (Figure 1)
626 is a simplified version of the more complex network of interactions between auxin, cytokinin
627 and ethylene summarised in Liu et al. (2017). In the mechanism, auxin, cytokinin and ethylene
628 are assumed to regulate PIN1 and PIN2 in the same way. This assumption was based on the
629 analysis of a variety of experimental data (Liu et al. 2013; Moore et al., 2015, 2017). Although
630 the main features of patterning changes in PIN1 and PIN2 concentration in *pin3*, *pin4*, *pin7*
631 mutants (Figure 6) can be predicted using the proposed mechanism, a feature in which
632 enhanced PIN1 protein was detected in lateral-basal membranes of the endodermis in *pin3*,
633 *pin4*, *pin7* triple mutant (Blilou et al. 2005) cannot be predicted using the mechanism. This
634 could imply that, while the regulation of both PIN1 and PIN2 by auxin, cytokinin and ethylene
635 can be largely described by the same relationships as described by Figure 1, some subtle
636 differences in the regulatory relationships may exist. Thus, the regulation of PIN1 and PIN2
637 may need to be further refined experimentally and computationally in the future. Therefore,
638 formulating a mechanism such as Figure 1 in this work, while making a variety of predictions,
639 can also identify knowledge gaps by highlighting differences between predictions and
640 experimental observations.

641 With various experimental data being accumulated and new data becoming available, it is
642 evident that elucidating the role of the complex regulatory relationships of multiple hormones
643 in plant development is becoming a major challenge (Schaller et al., 2015; Liu et al., 2017).
644 This work demonstrates that integrating such data can unravel a mechanism for simultaneous
645 patterning of auxin and cytokinin in the *Arabidopsis* root. Various predictions indicate that a
646 variety of experimental observations can also be elucidated by the same mechanism. By
647 integrating additional hormones in the future, the regulation of multiple hormone concentration
648 and response patterning in the *Arabidopsis* root can be quantitatively and rationally explored.

649

650 **METHODS**

651 **Plant materials**

652 *Arabidopsis* seed were obtained from lab stocks or from the Nottingham *Arabidopsis* Stock
653 Centre (NASC). All mutant and reporter lines are in Col-0 background except *pls* (C24).
654 Seedlings were grown on 10 cm square plates of 1/2 Murashige and Skoog agar media
655 sealed with micropore tape as described (Chilley *et al.* 2006). Seedlings were grown in
656 SANYO growth cabinets (22C°, 18hr photoperiod).

657

658 **Microscopy and image analysis**

659 Prior to confocal imaging, TCSn:GFP, *pls-3*/TCSn:GFP, R2D2, proPIN3:PIN3:GFP and
660 proPIN7:PIN7:GFP seedlings were fixed using the ClearSee method previously described by
661 Kurihara *et al.* (2015). The ClearSee protocol enables rapid fixing and clearing of plant
662 tissues whilst retaining the activity of fluorescent proteins and is compatible with various
663 fluorescent dyes (Ursache *et al.* 2018)

664 To prepare 4% paraformaldehyde (PFA) solution for the fixing procedure, 4 g of PFA powder
665 was added to 1L of 1x phosphate-buffered saline (PBS) solution on a magnetic stirrer and
666 heated to around 60 °C. To ensure the PFA powder is dissolved, the pH was raised using
667 1M KOH until the solution is clear. The pH was then adjusted to 6.9 with 1M HCL solution.
668 The solution was cooled and filtered before use. The PFA solution was used fresh or kept a
669 4C° and used within a week.

670 Seedlings were transferred with forceps to the 4% PFA solution where they were fixed under
671 vacuum for 30 minutes. Following fixation, seedlings were washed in 1X PBS solution twice
672 before the addition of ClearSee solution, where they were again placed under vacuum for 30
673 minutes.

674 ClearSee solution is prepared via mixing together xylitol (10% w/v), sodium deoxycholate
675 (15% w/v) and urea (25% w/v) and H₂O in a solution for 30 minutes. Fixed seedlings were
676 left in ClearSee solution at room temperature for at least a week with the ClearSee replaced
677 every few days. Following clearing, seedlings were stained and imaged.

678 Seedlings were examined using a Zeiss LCSM 800 or LCSM 880 (<https://www.zeiss.com/microscopy/int/home.html>). Roots were imaged using either a x10 or x20 air objective lens. Z-stacks were taken of each seedling to gain the maximum information possible. Settings such as gain, line, Z-step, averaging etc. were altered between each fluorescent reporter to optimise image quality and consistency.

683 To visualise cell structure and organisation under LCSM, cleared seedlings were submerged in 0.1% Calcofluor White in ClearSee solution for 30 minutes. Following staining, Calcofluor White solution was replaced by ClearSee and seedlings were washed for another 30 minutes. For LCSM, fixed seedlings were mounted on slides in ClearSee solution under a coverslip.

688

689 **Digital root construction and spatiotemporal modelling**

690 The details for construction of a digital root, numerical methods, averaging hormone concentration for a cell, and averaging hormone concentration in the digital root were previously reported (Moore et al. 2015; 2017; Liu et al. 2017) and remain the same for this research. In particular, digital root structure with actual cell geometries, polar localisation of efflux carriers and nonpolar localisation of influx carriers were described in detail (Moore et al. 2017; Liu et al. 2017). The images of PIN1,2,3,4,7 and AUX1 and LAX2,3 were shown in Moore et al. 2017. The parameter values for modelling equations in this research are included in Table S1, S2 and S3.

698 **Comparison of modelling and experimental results**

699 Comparison of modelling and experimental results in this research focuses on longitudinal trends along the root and does not attempt to make quantitative comparison at cell or pixel level for the following reasons. i) Although the modelled digital root was constructed based on the typical anatomy of an *Arabidopsis* root and although it includes important root features such as type, geometry, size and wall of each cell, and extracellular matrix (Moore et al. 2015; Liu et al. 2017), the cell size, geometry or wall location in the digital root is not exactly the same as its counterpart in experimental images of any individual root. Therefore, it is impossible to make direct quantitative comparison with experimental images at a cellular or pixel level. ii) Experimental images in our experiments and those in the literature generally show the trends and patterning of measured components and generally do not quantify actual concentrations of any components. Thus, direct concentration comparison is not as

710 important as trend and pattern comparison. iii) Biologically, patterning generally refers to
711 trend or gradient change, and is considered to play a crucial role in root development. Thus,
712 comparisons between modelled and experimental results in this research concentrates
713 on the similarity or differences in trends and patterning.

714

715 **SUPPLEMENTAL INFORMATION**

716 Supplemental information is available at *Plant Communications Online*.

717

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724

725 **AUTHOR CONTRIBUTIONS**

726 J.L. and K.L. initiated the project; S.M., J.L. and K.L. designed modelling and experimental
727 study and drafted the manuscript; J.L., K.L. J.F.T and C.C. supervised the study; S.M., J.L.
728 and G.J. carried out modelling and experimental work; all authors edited the final draft of the
729 manuscript.

730

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732 The authors declare no conflicts of interest.

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- 947

948 **Figure Legends**949 **Figure 1. An integrative mechanism for simultaneous auxin and cytokinin patterning**
950 **in the *Arabidopsis* root development.**

951 Auxin metabolism in each cell is regulated by ethylene and cytokinin signalling. Auxin
 952 transport within a cell is due to diffusion and its transport between cells is predominantly
 953 facilitated by the functions of PIN and AUX1 transporters. Cytokinin metabolism is regulated
 954 by auxin and ethylene, and it transports via diffusion. Ethylene metabolism is regulated by
 955 auxin and cytokinin, and it transports via diffusion. The POLARIS protein regulates ethylene
 956 signalling by interacting with its receptors. The mechanism integrates metabolism and
 957 transport of auxin, cytokinin and ethylene into an integrative system, and the patterning of
 958 the three hormones is regulated mutually. A. Detailed network for mutual regulation of auxin,
 959 cytokinin and ethylene, and the network is extracted from the more comprehensive network
 960 in Liu et al. (2017). B. Schematic description about mutual regulation between auxin,
 961 cytokinin and ethylene. This is a simplified summary of the detailed network (Figure 1A) with
 962 the red lines highlighting links based on additional biological evidence that is analysed in
 963 detail in this research. → indicates activation; -I indicates inhibition. Connections marked
 964 using red-coloured lines in B highlight the novel regulatory relationships explored in this
 965 research. Connections marked using black-coloured lines in B are the regulatory
 966 relationships previously examined (Moore et al. 2015; 2017, Liu et al. 2017). All connections
 967 are based on either experimental data in our lab or established biological evidence in the
 968 literature. Auxin, auxin hormone; ET, ethylene; CK, cytokinin; PINm, PIN mRNA; PINp, PIN
 969 protein; PLSm, POLARIS mRNA; PLSp, POLARIS protein; X, downstream ethylene
 970 signalling; Ra*, active form of auxin receptor; Ra, inactive form of auxin receptor; Re*, active
 971 form of ethylene receptor, ETR1. Re, inactive form of ethylene receptor, ETR1; CTR1*,
 972 active form of CTR1; CTR1, inactive form of CTR1.

973

974 **Figure 2. Relationship of auxin, cytokinin and ethylene in a homogenous cell.**

975 A. Effects of changing auxin biosynthesis rate on auxin, cytokinin and ethylene
 976 concentration. B. Effects of changing cytokinin biosynthesis rate on auxin, cytokinin and
 977 ethylene concentration. C. Effects of changing ethylene biosynthesis rate on auxin, cytokinin
 978 and ethylene concentration.

979

980 **Figure 3. Modelled auxin concentration patterning.**

981 Modelled auxin patterning (A, C-F) is in good agreement with both IAA concentration
 982 distribution measured experimentally (Figure S2A; Figure 3 in Petersson et al. 2009) and
 983 auxin response patterning shown as DR5::GFP fluorescence (B). Approximately, along
 984 longitudinal direction, meristem is at the position of 200 μm to 650 μm ; transition zone (TZ)
 985 is at the position of 650 μm to 750 μm and elongation zone is at the position of 750 μm to
 986 1200 μm . Equations and parameter values are included in Table S1, S2 and S3.

987

988 **Figure 4. Modelled cytokinin concentration patterning.**

989 Modelled cytokinin concentration patterning (A, C-F) is in good agreement with both cytokinin
 990 concentration distribution measured experimentally (Figure S3A; Figure 5 in Antoniadi et al.
 991 2015) and cytokinin response patterning shown as ARR5::GFP fluorescence (B). Equations
 992 and parameter values are included in Table S1.

993 **Figure 5. Spatiotemporal modelling predicts auxin concentration, patterning and
 994 biosynthesis rate of various experimental observations as reported in the literature.**

995 A. Auxin response distribution along cell position from the initials in different cell types (Similar
 996 to Figure S4; Supplementary Figure 6 in Liao et al. 2015). B. Minimum auxin response
 997 distribution in transition zone (similar to Figure S5; Figure 3 in Di Mambro et al. 2017). C.
 998 Average auxin concentration in different mutants (similar to Figure S6; Figure 4C in Chilley et
 999 al. 2006). D. Auxin biosynthesis rate distribution (similar to Figure S7; Figure 5 in Petersson
 1000 et al. 2009). Meristem is at the position of ca. 200 μm to 650 μm ; transition zone (TZ) is at the
 1001 position of 650 μm to 750 μm ; and elongation zone is at the position of 750 μm to 1200 μm ,
 1002 in the longitudinal axis.

1003 **Figure 6. Spatiotemporal modelling predicts changes in PIN1 and PIN2 level and
 1004 patterning in various mutants.**

1005 A. Modelled PIN1 and PIN2 level change in various mutants (Similar to Figure S8; Figure 1B
 1006 in Liu et al. 2013); B. Modelled PIN1 and PIN2 patterning change in *pin3*, *pin4* and *pin7* single
 1007 mutants (similar to Figure S9A; PIN1 patterning change in Figure 6 in Omelyanchuk et al.
 1008 2016) and modelled PIN1 and PIN2 patterning change in *pin3,4,7* triple mutants (similar to
 1009 Figure S9B; PIN2 patterning change in Figure 1 in Blilou et al. 2005). C. Enlargement of *pin4*
 1010 mutant in Figure 6B.

1011 **Figure 7. Modelled change in cytokinin concentration and patterning in *pls* mutant
 1012 predicts experimental observation.**

1013 A. Modelled PLS protein distribution (right panel in A) and measured PLS GFP fluorescence
 1014 (left pane in A). The actual concentration of PLS protein has not been experimentally

1015 quantified, and therefore the colour of the experimental image indicates the relative change in
1016 the level of PLS protein. B. Modelled change in cytokinin concentration in the *pls* mutant
1017 relative to wildtype (similar to Table 1 in Liu et al. 2010). C. Modelled change in cytokinin
1018 concentration in *pls* mutant; D. TCSn:GFP fluorescence in wild type and *pls* mutant.

1019

1020 **Supplementary Information**

1021 **Figure S1.** An example of simultaneously enhancing the concentration of auxin, cytokinin
1022 and ethylene by increasing auxin biosynthesis rate in homogenous cells of the root.

1023 **Figure S2.** Experimental observations about auxin.

1024 **Figure S3.** Experimental observations about cytokinin.

1025 **Figure S4.** Experimental observations about auxin response trends in cell files above the
1026 initials and comparison between experimental observations and modelled results.

1027 **Figure S5.** Experimental observations about auxin response minimum in the transition zone
1028 and comparison between experimental observations and modelled results.

1029 **Figure S6.** Experimental observations about average auxin concentration trends in WT, *pls*
1030 mutant, *pls etr1* double mutant, and PLSox and comparison between experimental
1031 observations and modelled results.

1032 **Figure S7.** Experimental observations about patterning the rate of auxin biosynthesis.

1033 **Figure S8.** Experimental observations about the average concentration trend of PIN1 and
1034 PIN2 proteins in WT, PLSox transgenic, *pls* and *etr1* mutants, and *pls etr1* double mutant.

1035 **Figure S9.** Experimental observations about changes in PIN1 and PIN2 concentrations in
1036 *pin3*, *pin4*, *pin7* mutants.

1037 **Figure S10.** Modelled ethylene concentration in wild type and the *pls* mutant.

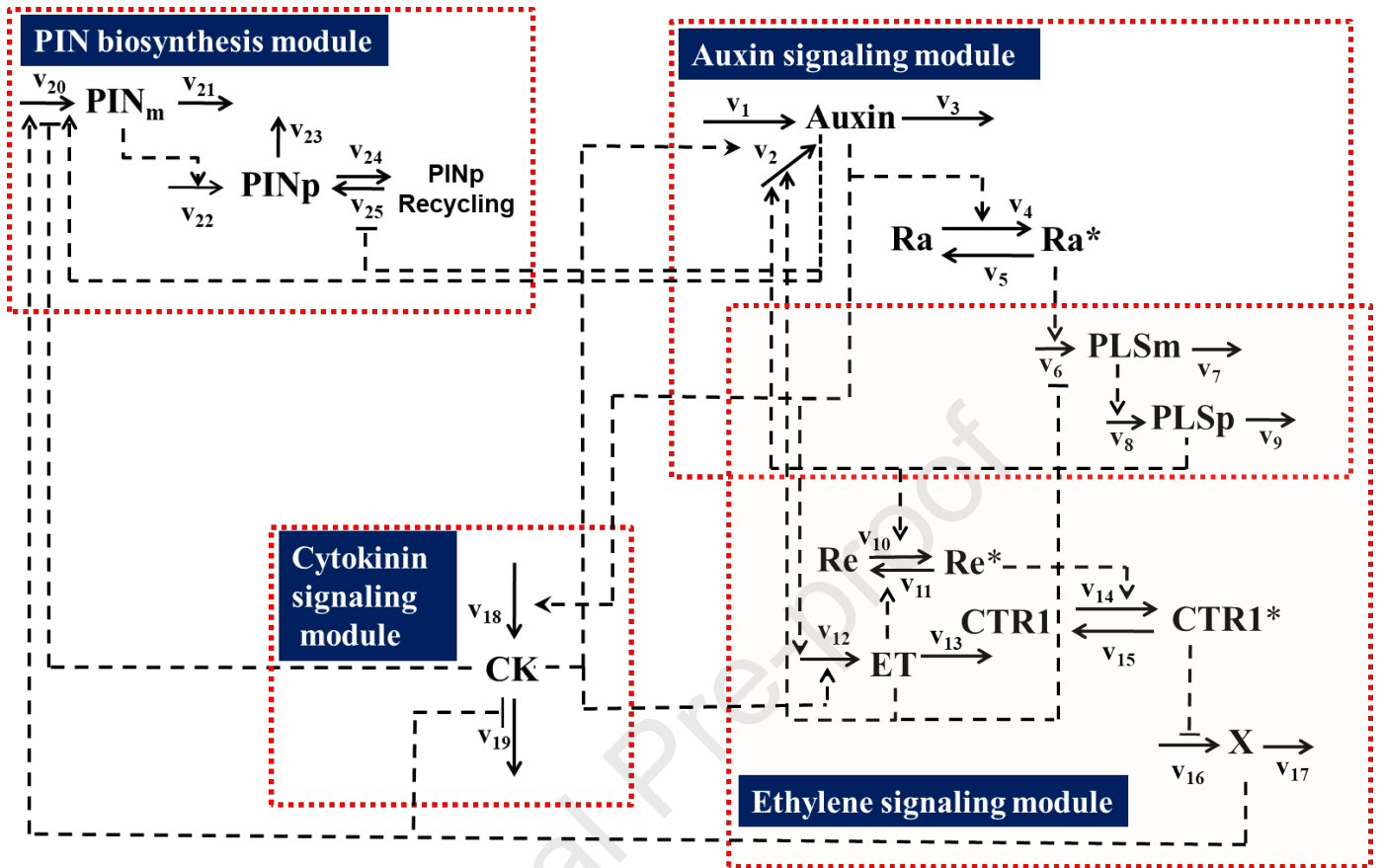
1038 **Figure S11.** Modelling reveals that auxin patterning still emerges when auxin biosynthesis is
1039 not regulated by cytokinin or ethylene ($k_{2a}=0$) with all auxin transporters being fixed as
1040 those in the wildtype.

1041 **Figure S12.** Same as Figure 5 in the main text, but in the absence of auxin biosynthesis
1042 regulation ($k_{2a}=0$).

- 1043 **Figure S13.** Same as Figure 6 in the main text, but in the absence of auxin biosynthesis
1044 regulation ($k_{2a}=0$).
- 1045 **Figure S14.** Same as Figure 7 in the main text, but in the absence of auxin biosynthesis
1046 regulation ($k_{2a}=0$).
- 1047 **Figure S15.** Same as Figure 5 in the main text, but in the absence of the regulation of
1048 cytokinin degradation by ethylene signalling ($k_{19a}=0$).
- 1049 **Figure S16.** Same as Figure 6 in the main text, but in the absence of the regulation of
1050 cytokinin degradation by ethylene signalling ($k_{19a}=0$).
- 1051 **Figure S17.** Same as Figure 7 in the main text, but in the absence of the regulation of
1052 cytokinin degradation by ethylene signalling ($k_{19a}=0$).
- 1053 **Figure S18.** Same as Figure 5 in the main text, but in the absence of the regulation of
1054 cytokinin biosynthesis by auxin signalling ($k_{18a}=0$).
- 1055 **Figure S19.** Same as Figure 6 in the main text, but in the absence of the regulation of
1056 cytokinin biosynthesis by auxin signalling ($k_{18a}=0$).
- 1057 **Figure S20.** Same as Figure 7 in the main text, but in the absence of the regulation of
1058 cytokinin biosynthesis by auxin signalling ($k_{18a}=0$).
- 1059 **Figure S21.** Role of changes in PIN1 and PIN2 concentration and patterning in *pin3* mutant.
- 1060 **Figure S22.** Role of changes in PIN1 and PIN2 concentration and patterning in *pin4* mutant.
- 1061 **Figure S23.** Role of changes in PIN1 and PIN2 concentration and patterning in *pin7* mutant.
- 1062 **Figure S24.** Role of changes in PIN1 and PIN2 concentration and patterning in *pin3,4,7*
1063 triple mutant.
- 1064 **Figure S25.** Role of PLS over expressor in the concentration and patterning of auxin,
1065 cytokinin and ethylene.
- 1066 **Figure S26.** Role of *ctr1* mutant in the concentration and patterning of auxin, cytokinin and
1067 ethylene.
- 1068 **Figure S27.** Role of decreasing CTR1 downstream response in the concentration and
1069 patterning of auxin, cytokinin and ethylene.

- 1070 **Figure S28.** Role of increasing CTR1 downstream response in the concentration and
1071 patterning of auxin, cytokinin and ethylene.
- 1072 **Figure S29.** Schematic summary of the complex multi-level regulatory relationships for
1073 simultaneous auxin and cytokinin concentration patterning in the root.
- 1074 **Table S1.** Hormonal crosstalk rate equations and parameter values for species biosynthesis,
1075 decay, activation and inactivation at each grid point.
- 1076 **Table S2.** PIN1 and PIN2 rate equations for localisation to and from the plasma membrane.
- 1077 **Table S3.** Species flux between nearest neighbour.

A



B

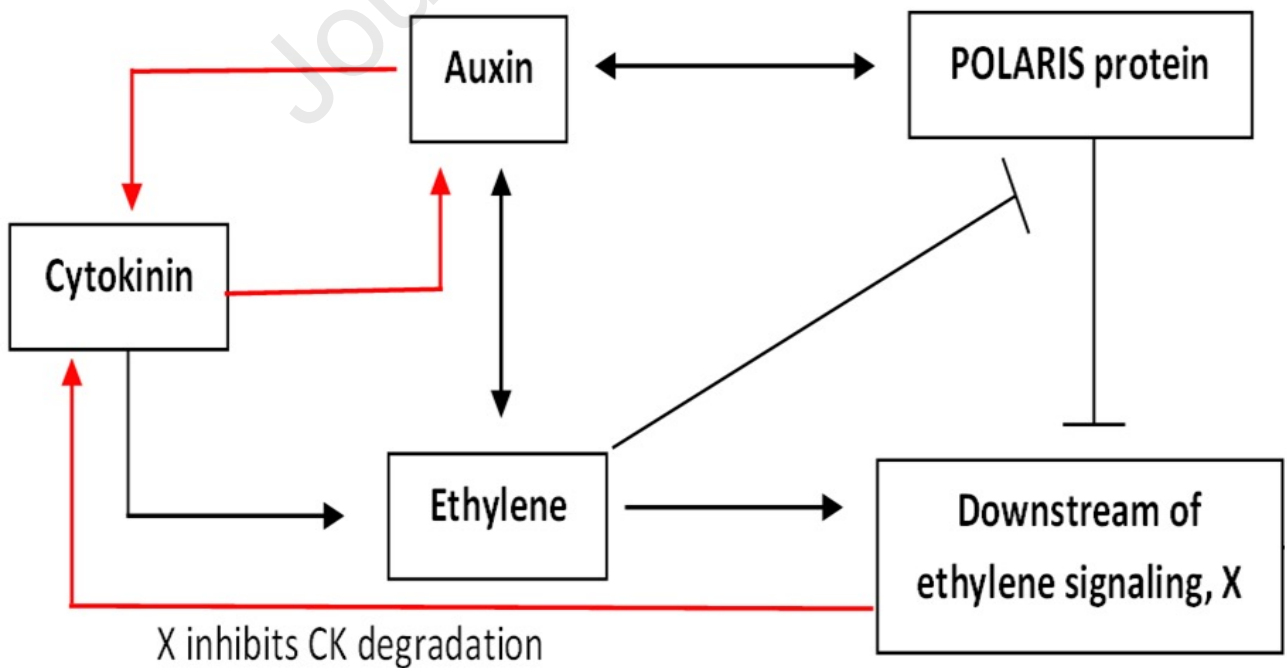


Figure 1. An integrative mechanism for simultaneous auxin and cytokinin patterning in the *Arabidopsis* root development.

Auxin metabolism in each cell is regulated by ethylene and cytokinin signalling. Auxin transport within a cell is due to diffusion and its transport between cells is predominantly facilitated by the functions of PIN and AUX1 transporters. Cytokinin metabolism is regulated by auxin and ethylene, and it transports via diffusion. Ethylene metabolism is regulated by auxin and cytokinin, and it transports via diffusion. The POLARIS protein regulates ethylene signalling by interacting with its receptors. The mechanism integrates metabolism and transport of auxin, cytokinin and ethylene into an integrative system, and the patterning of the three hormones is regulated mutually. A. Detailed network for mutual regulation of auxin, cytokinin and ethylene, and the network is extracted from the more comprehensive network in Liu et al. (2017). B. Schematic description about mutual regulation between auxin, cytokinin and ethylene. This is a simplified summary of the detailed network (Figure 1A) with the red lines highlighting links based on additional biological evidence that is analysed in detail in this research. → indicates activation; -| indicates inhibition. Connections marked using red-coloured lines in B highlight the novel regulatory relationships explored in this research. Connections marked using black-coloured lines in B are the regulatory relationships previously examined (Moore et al. 2015; 2017, Liu et al. 2017). All connections are based on either experimental data in our lab or established biological evidence in the literature. Auxin, auxin hormone; ET, ethylene; CK, cytokinin; PINm, PIN mRNA; PINp, PIN protein; PLSm, POLARIS mRNA; PLSp, POLARIS protein; X, downstream ethylene signalling; Ra*, active form of auxin receptor; Ra, inactive form of auxin receptor; Re*, active form of ethylene receptor, ETR1. Re, inactive form of ethylene receptor, ETR1; CTR1*, active form of CTR1; CTR1, inactive form of CTR1.

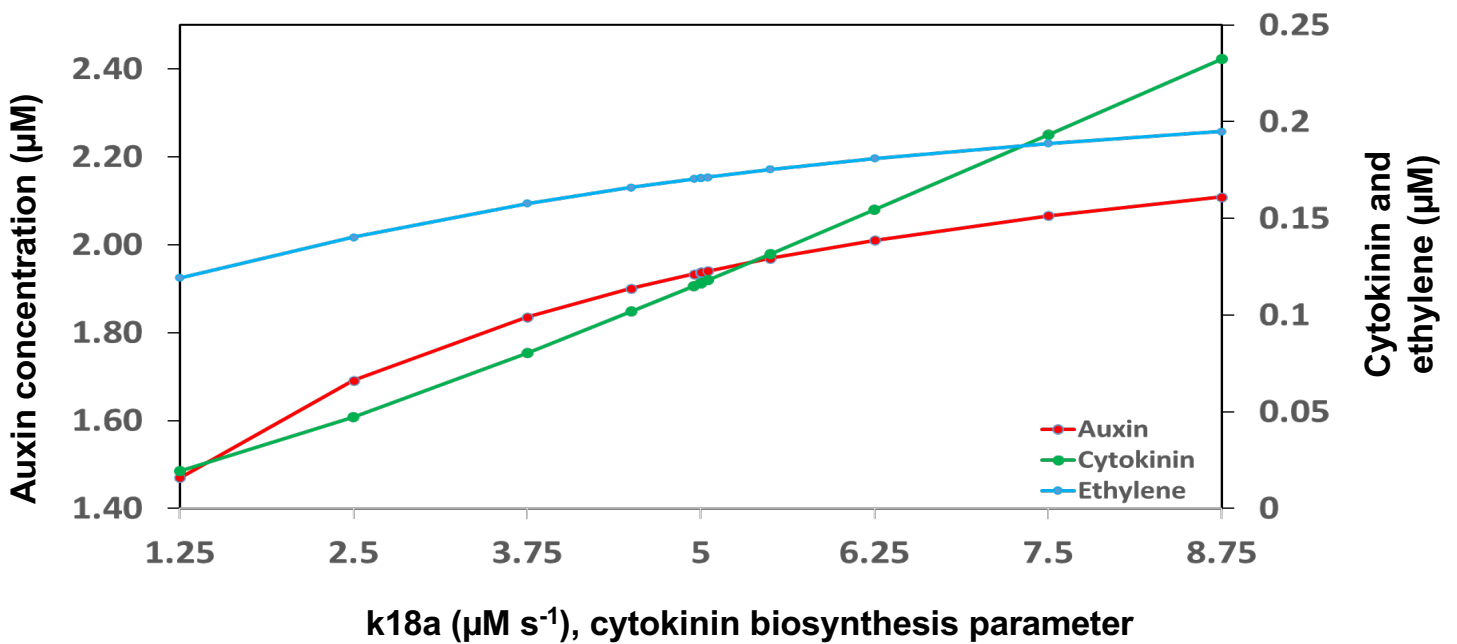
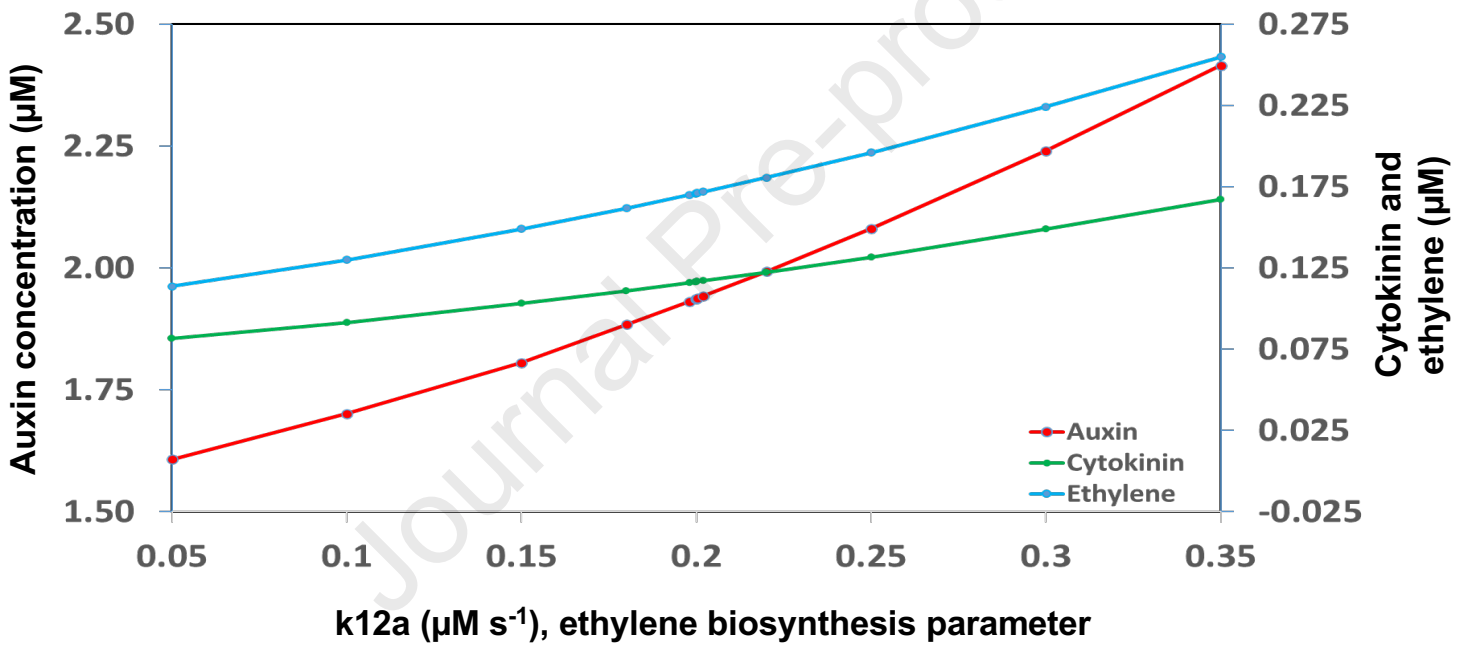
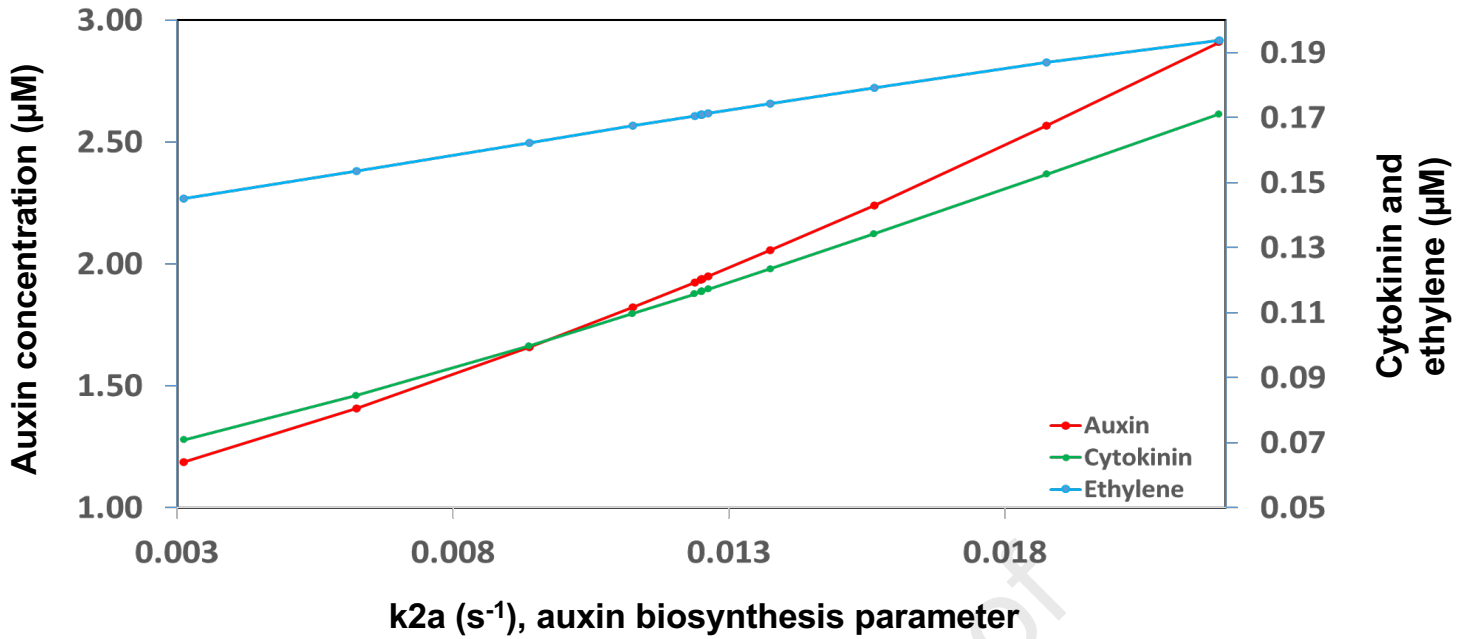


Figure 2. Relationship of auxin, cytokinin and ethylene in a homogenous cell.

A. Effects of changing auxin biosynthesis rate on auxin, cytokinin and ethylene concentration. B. Effects of changing cytokinin biosynthesis rate on auxin, cytokinin and ethylene concentration. C. Effects of changing ethylene biosynthesis rate on auxin, cytokinin and ethylene concentration.

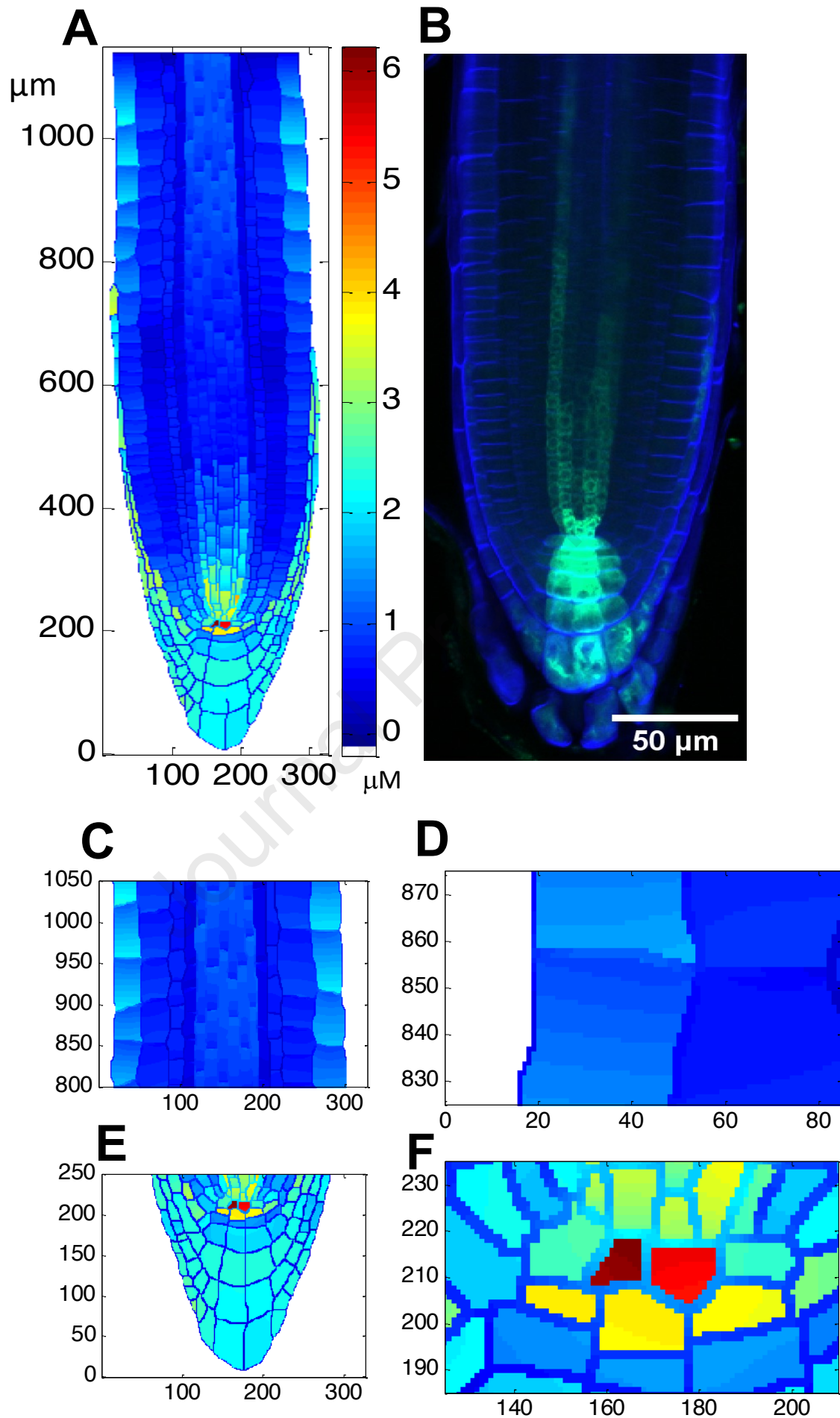


Figure 3. Modelled auxin concentration patterning.

Modelled auxin patterning (A, C-F) is in good agreement with both IAA concentration distribution measured experimentally (Figure S2A; Figure 3 in Petersson et al. 2009) and auxin response patterning shown as DR5::GFP fluorescence (B). Approximately, along longitudinal direction, meristem is at the position of 200 μm to 650 μm ; transition zone (TZ) is at the position of 650 μm to 750 μm and elongation zone is at the position of 750 μm to 1200 μm . Equations and parameter values are included in Table S1, S2 and S3.

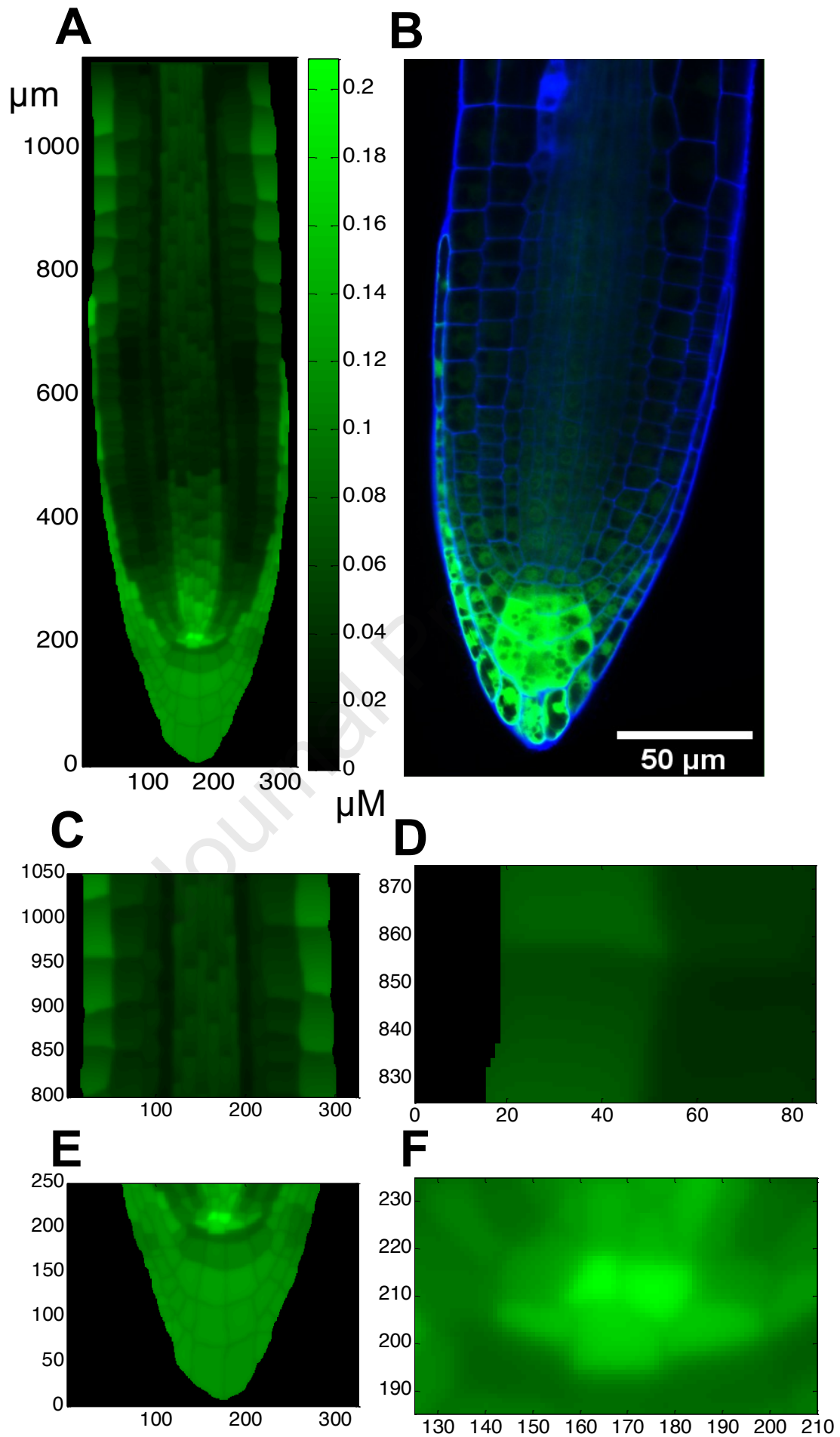


Figure 4. Modelled cytokinin concentration patterning.

Modelled cytokinin concentration patterning (A, C-F) is in good agreement with both cytokinin concentration distribution measured experimentally (Figure S3A; Figure 5 in Antoniadis et al. 2015) and cytokinin response patterning shown as ARR5::GFP fluorescence (B). Equations and parameter values are included in Table S1.

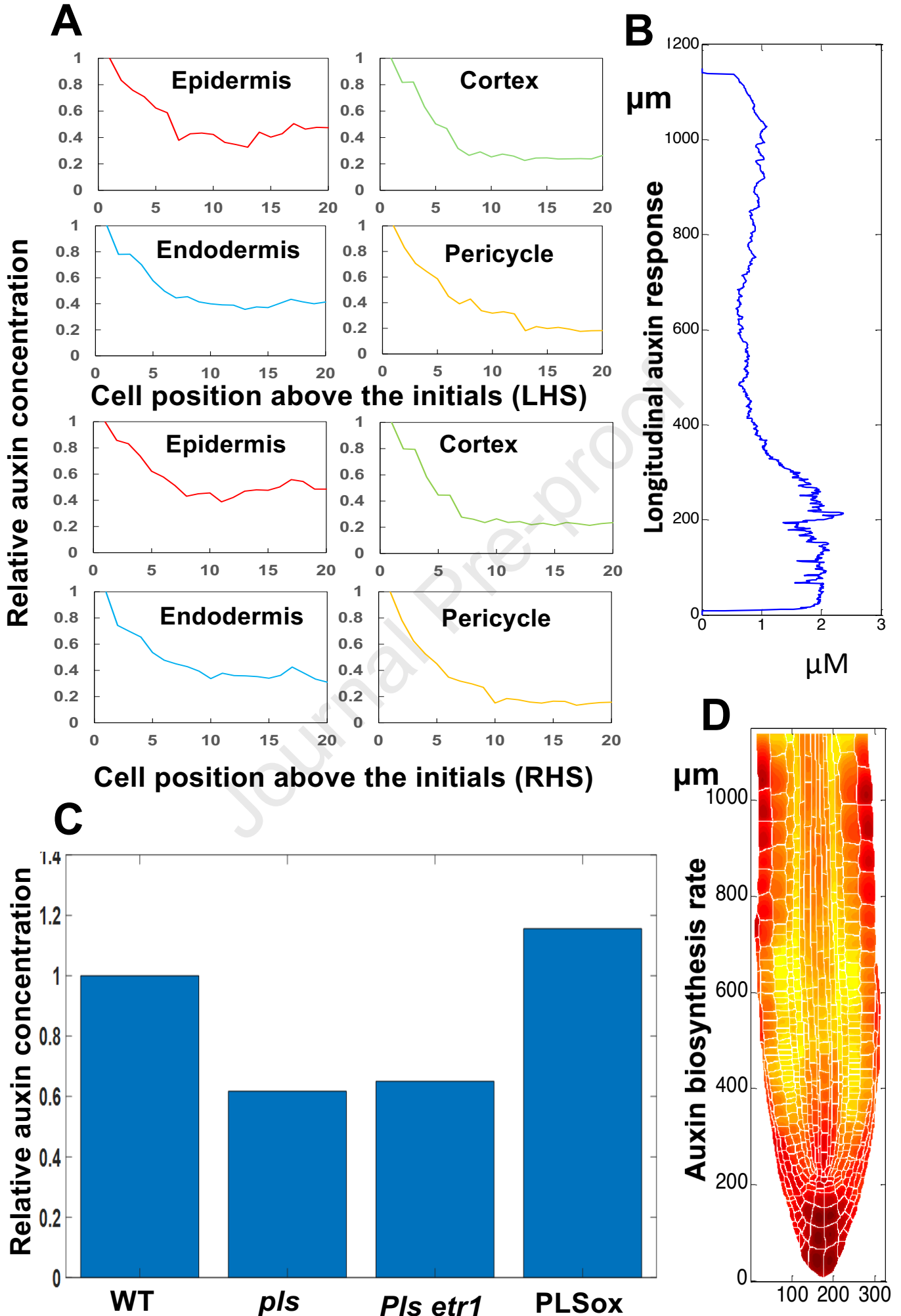


Figure 5. Spatiotemporal modelling predicts auxin concentration, patterning and biosynthesis rate of various experimental observations as reported in the literature.

A. Auxin response distribution along cell position from the initials in different cell types (Similar to Figure S4; Supplementary Figure 6 in Liao et al. 2015). B. Minimum auxin response distribution in transition zone (similar to Figure S5; Figure 3 in Di Mambro et al. 2017). C. Average auxin concentration in different mutants (similar to Figure S6; Figure 4C in Chilley et al. 2006). D. Auxin biosynthesis rate distribution (similar to Figure S7; Figure 5 in Petersson et al. 2009). Meristem is at the position of ca. 200 μm to 650 μm ; transition zone (TZ) is at the position of 650 μm to 750 μm ; and elongation zone is at the position of 750 μm to 1200 μm , in the longitudinal axis.

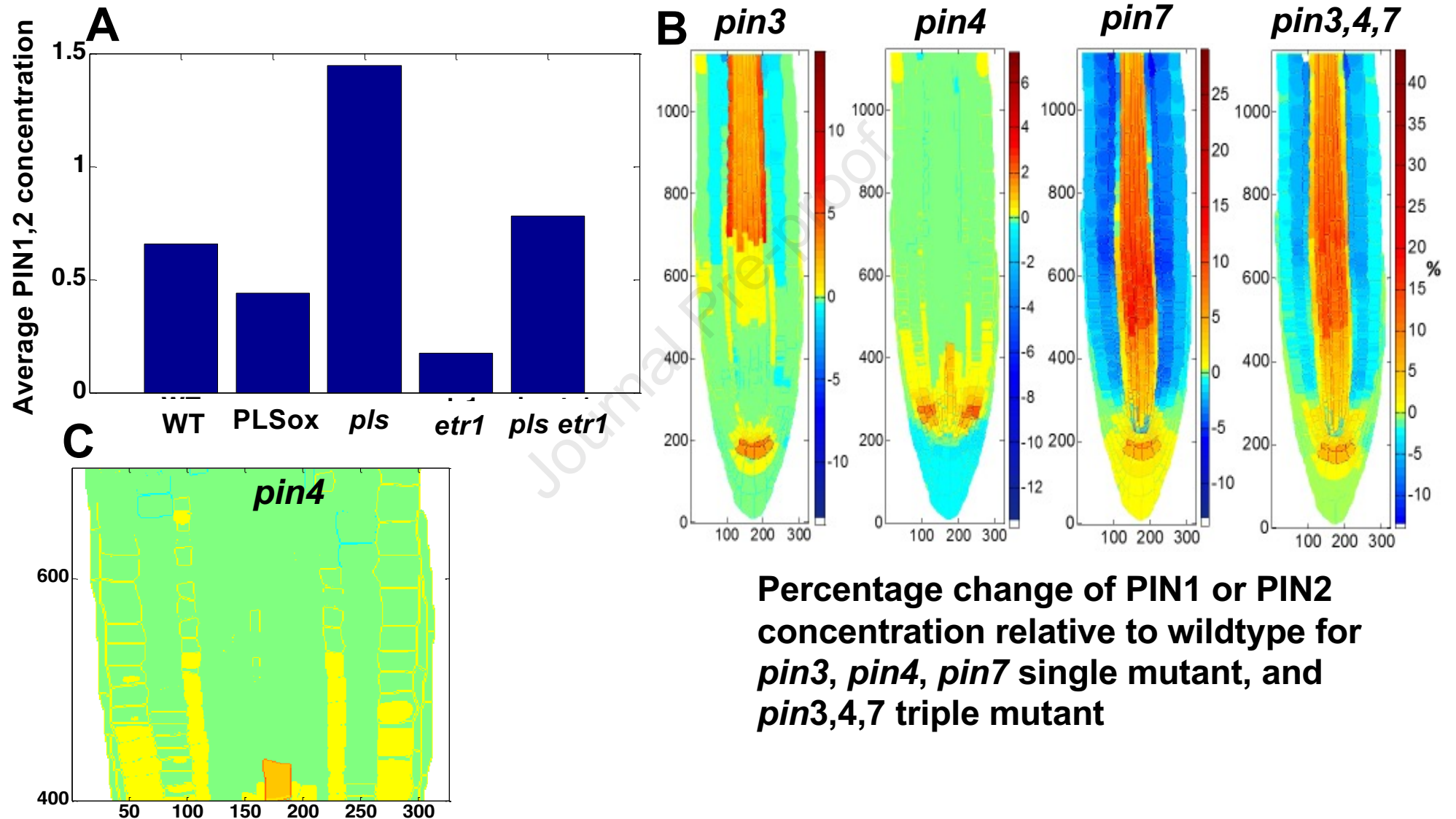


Figure 6. Spatiotemporal modelling predicts changes in PIN1 and PIN2 level and patterning in various mutants.

A. Modelled PIN1 and PIN2 level change in various mutants (Similar to Figure S8; Figure 1B in Liu et al. 2013); B. Modelled PIN1 and PIN2 patterning change in *pin3*, *pin4* and *pin7* single mutants (similar to Figure S9A; PIN1 patterning change in Figure 6 in Omelyanchuk et al. 2016) and modelled PIN1 and PIN2 patterning change in *pin3,4,7* triple mutants (similar to Figure S9B; PIN2 patterning change in Figure 1 in Blilou et al. 2005). C. Enlargement of *pin4* mutant in Figure 6B.

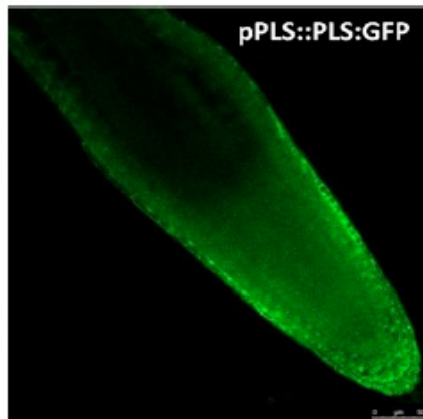
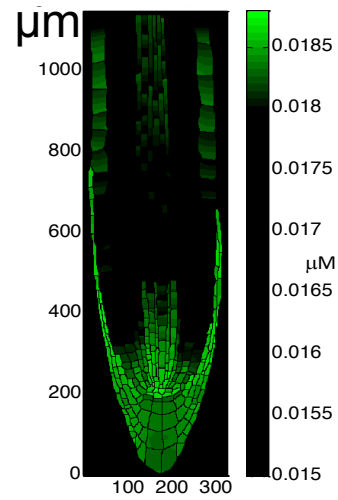
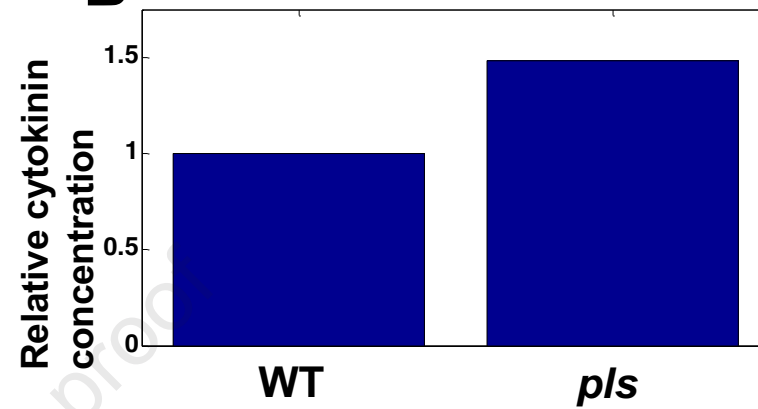
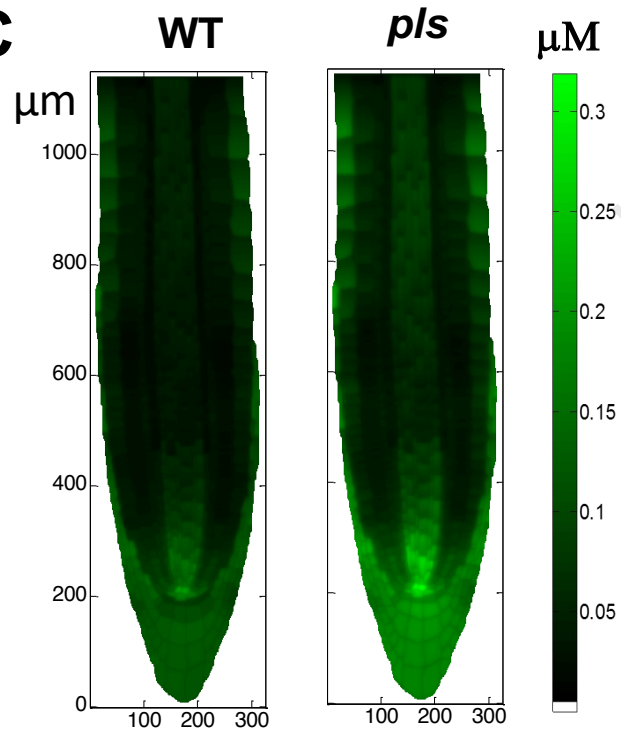
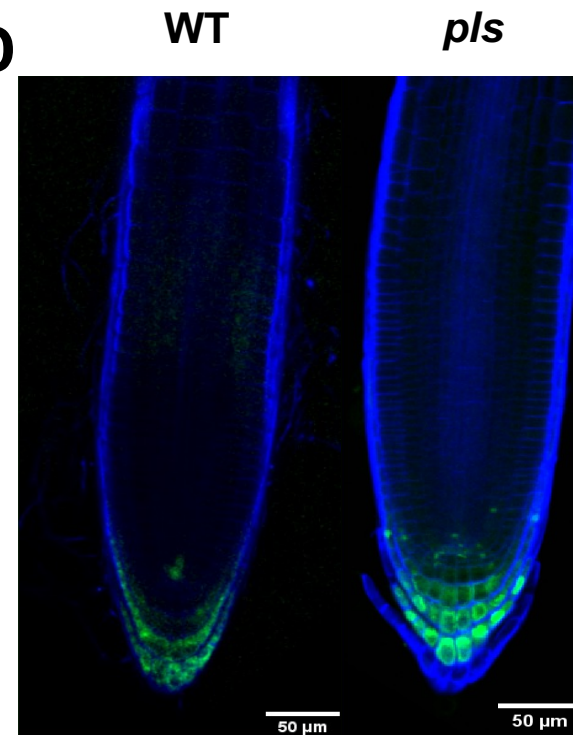
A Experiment**Model****B****C****D**

Figure 7. Modelled change in cytokinin concentration and patterning in *p/s* mutant predicts experimental observation.

A. Modelled PLS protein distribution (right panel in A) and measured PLS GFP fluorescence (left pane in A). The actual concentration of PLS protein has not been experimentally quantified, and therefore the colour of the experimental image indicates the relative change in the level of PLS protein. B. Modelled change in cytokinin concentration in the *p/s* mutant relative to wildtype (similar to Table 1 in Liu et al. 2010). C. Modelled change in cytokinin concentration in *p/s* mutant; D. TCSn:GFP fluorescence in wild type and *p/s* mutant.