

# Effective theory approach to unstable particle production

M. Beneke<sup>1</sup>, A.P. Chapovsky<sup>1</sup>, A. Signer<sup>2</sup> and G. Zanderighi<sup>3</sup>

<sup>1</sup>*Institut für Theoretische Physik E, RWTH Aachen, D-52056 Aachen, Germany*

<sup>2</sup>*IPPP, Department of Physics, University of Durham, Durham DH1 3LE, England*

<sup>3</sup>*Fermi National Accelerator Laboratory, Batavia, IL 60510*

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Using the hierarchy of scales between the mass,  $M$ , and the width,  $\Gamma$ , of a heavy, unstable particle we construct an effective theory that allows calculations for resonant processes to be systematically expanded in powers of the coupling  $\alpha$  and  $\Gamma/M$ . We illustrate the method by computing the next-to-leading order line shape of a scalar resonance in an abelian gauge-Yukawa model.

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Higher-order calculations for processes involving massive, unstable particles close to resonance suffer from the breakdown of ordinary perturbation theory, since the intermediate propagator becomes singular. This singularity is avoided if the finite width,  $\Gamma$ , of the unstable particle is taken into account in the construction of the propagator via resummation of self-energy insertions. There are a number of approaches along this line to avoid the problem [1]. However, so far there is no method that allows to systematically improve the accuracy of calculations order by order in perturbation theory. The purpose of this letter is to present such a method.

We are concerned with processes involving an unstable particle close to resonance. The main idea is to exploit the hierarchy of scales  $\Gamma \ll M$ , where  $M$  is the pole mass, in order to systematically organize the calculations in a series in the coupling,  $\alpha$ , and  $\Gamma/M$ . While the expansion in  $\alpha$  is standard, we construct an effective theory to perform the expansion in  $\Gamma/M$ . A first step in this direction has been presented in [2]. The main idea of our approach is similar to non-relativistic QCD, where an expansion in  $\alpha$  and the velocity of the heavy quarks is made. We will identify all relevant modes and use them to write the operators of the Lagrangian of the effective theory. This Lagrangian is then matched to the underlying theory, using the method of regions [3]. In this letter we will outline the basic idea and we refer to [4] for more details.

We consider a toy model that involves a massive scalar field,  $\phi$ , and two fermion fields. The scalar as well as one of the fermion fields,  $\psi$ , (the “electron”) are charged under an abelian gauge symmetry, whereas the other fermion,  $\chi$ , (the “neutrino”) is neutral. The model allows for the scalar to decay into an electron-neutrino pair through a Yukawa interaction. The Lagrangian is

$$\begin{aligned} \mathcal{L} = & (D_\mu \phi)^\dagger D^\mu \phi - \hat{M}^2 \phi^\dagger \phi + \bar{\psi} i \not{D} \psi + \bar{\chi} i \not{\partial} \chi \\ & - \frac{1}{4} F^{\mu\nu} F_{\mu\nu} - \frac{1}{2\xi} (\partial_\mu A^\mu)^2 \\ & + y \phi \bar{\psi} \chi + y^* \phi^\dagger \bar{\chi} \psi - \frac{\lambda}{4} (\phi^\dagger \phi)^2 + \mathcal{L}_{\text{ct}}, \end{aligned} \quad (1)$$

where  $\hat{M}$  and  $\mathcal{L}_{\text{ct}}$  denote the renormalized mass and the

counterterm Lagrangian and  $D = \partial - igA$ . We define  $\alpha_g \equiv g^2/(4\pi)$ ,  $\alpha_y \equiv (yy^*)/(4\pi)$  (at the scale  $\mu$ ) and assume  $\alpha_g \sim \alpha_y \sim \alpha$ , and  $\alpha_\lambda \equiv \lambda/(4\pi) \sim \alpha^2/(4\pi)$ .

We would like to obtain the totally inclusive cross section for the process

$$\bar{\nu}(q) + e^-(p) \rightarrow X \quad (2)$$

as a function of  $s \equiv (p+q)^2$  by calculating the forward scattering amplitude  $\mathcal{T}(s)$  and taking its imaginary part. (The total cross section of process (2) has an initial state collinear singularity which has to be absorbed into the electron distribution function. In what follows it is understood that this singularity is subtracted minimally.) In particular, we are interested in the region  $s \approx M^2$ , or more precisely  $s - M^2 \sim M\Gamma \sim \alpha M^2 \ll M^2$ . In this kinematic region the cross section is enhanced due to the propagator of the scalar. Furthermore, at each order in  $\alpha$  we get additional contributions proportional to  $\alpha \hat{M}^2/(s - M^2) \sim 1$  due to self-energy insertions.

We now turn to the main part of this letter and discuss how to construct the effective theory. Our approach is based on the hierarchy of scales  $\Gamma \ll M$ . Thus, we systematically expand the cross section in powers of  $\alpha$  and

$$\delta \equiv \frac{s - \hat{M}^2}{\hat{M}^2} \sim \frac{\Gamma}{M}. \quad (3)$$

In a theory that formulates this expansion correctly, other issues like resummation of self-energy insertions and gauge invariance are taken care of automatically. In a first step we integrate out hard momenta  $k \sim M$ . The effective theory will then not contain any longer dynamical hard modes since their effect is included in the coefficients of the operators. The hard effects are associated with what is usually called factorizable corrections, whereas the effects of the dynamical modes correspond to the non-factorizable corrections [2]. On the level of Feynman diagrams, this amounts to using the method of regions to separate loop integrals into various contributions [3]. The hard part is obtained by expanding the integrand in  $\delta$ . The difference between the full integral

and its hard part has to be reproduced by modes corresponding to momentum configurations that are near mass-shell. The main task is to identify these modes, and to write the operators of the effective Lagrangian in terms of the corresponding field operators and then to compute the coefficients of the operators by matching (up to a certain order in  $\alpha$  and  $\delta$ ).

Our goal is to carry out this programme for our model to an order in  $\alpha$  and  $\delta$  that is sufficient to compute  $\mathcal{T}^{(0)} + \mathcal{T}^{(1)}$ , the forward scattering amplitude at next-to-leading order (NLO), where  $\mathcal{T}^{(0)}$  sums up all terms that scale as  $(\alpha/\delta)^n \sim 1$  and  $\mathcal{T}^{(1)}$  contains all terms that are suppressed by an additional power of  $\alpha$  or  $\delta$ .

The basic process under consideration is the following: we start with highly energetic fermions, produce a near mass-shell scalar which then decays again into highly energetic fermions. Accordingly we split the effective Lagrangian into three parts. Roughly speaking, the first,  $\mathcal{L}_{\text{HSET}}$ , describes the heavy scalar field near mass-shell and its interaction with the gauge field. The second part,  $\mathcal{L}_{\text{SCET}}$ , describes energetic (charged) fermions and their interactions with the gauge field. Finally, the third part,  $\mathcal{L}_{\text{int}}$ , describes the external fermions and how they interact to produce the final state. We will discuss these three parts in turn.

The construction of  $\mathcal{L}_{\text{HSET}}$  follows closely the construction of the effective Lagrangian for heavy quark effective theory (HQET) [5]. We write the momentum of the scalar particle near resonance as  $P = \hat{M}v + k$ , where the velocity vector  $v$  satisfies  $v^2 = 1$  and the residual momentum  $k$  scales as  $M\delta$ . We will call such a scalar field a “soft” field (in [2] the term “resonant” has been used). Thus, for a soft scalar field we have  $P^2 - \hat{M}^2 \sim M\delta$  and this remains true if the scalar particle interacts with a soft gauge boson with momentum  $M\delta$ . In analogy to HQET we remove the rapid spatial variation  $e^{-i\hat{M}v \cdot x}$  from the  $\phi$ -field and define

$$\phi_v(x) \equiv e^{i\hat{M}v \cdot x} \mathcal{P}_+ \phi(x), \quad (4)$$

where  $\mathcal{P}_+$  projects onto the positive frequency part to ensure that  $\phi_v$  is a pure destruction field. We now write the effective Lagrangian in terms of  $\phi_v$  and construct the bilinear terms so as to reproduce the two-point function close to resonance. Denoting the complex pole of the propagator by  $\bar{s}$  and the residue at the pole by  $R_\phi$  the propagator can be written as

$$\frac{i R_\phi}{P^2 - \bar{s}} = \frac{i R_\phi}{2\hat{M}vk + k^2 - (\bar{s} - \hat{M}^2)}. \quad (5)$$

We define the matching coefficient

$$\Delta \equiv \frac{\bar{s} - \hat{M}^2}{\hat{M}} \quad (6)$$

and  $a_\top^\mu \equiv a^\mu - (va)v^\mu$  for any vector. There are two solutions to  $P^2 = \bar{s}$ , one of which is irrelevant since it

scales as  $vk \sim \hat{M}$ . For the other we find

$$\begin{aligned} vk &= -\hat{M} + \sqrt{\hat{M}^2 + \hat{M}\Delta - k_\top^2} \\ &= \frac{\Delta}{2} - \frac{\Delta^2 + 4k_\top^2}{8\hat{M}} + \mathcal{O}(\delta^3), \end{aligned} \quad (7)$$

where we expanded in  $\delta$  in the second line. Therefore, the bilinear terms are given by

$$\begin{aligned} \mathcal{L}_{\phi\phi} &= 2\hat{M}\phi_v^\dagger \left( iv \cdot D_s - \frac{\Delta}{2} \right) \phi_v \\ &+ 2\hat{M}\phi_v^\dagger \left( \frac{(iD_{s\top})^2}{2\hat{M}} + \frac{\Delta^2}{8\hat{M}} \right) \phi_v + \dots, \end{aligned} \quad (8)$$

where  $D_s \equiv \partial - igA_s$  denotes the soft covariant derivative. In obtaining  $\mathcal{L}_{\phi\phi}$  we exploited the fact that the gauge invariance of the full Lagrangian is not broken by the separation into hard and soft parts. Therefore, the effective Lagrangian must be gauge invariant as well and we can obtain the interaction of the scalar with the soft photon simply by replacing  $\partial \rightarrow D_s$ . The gauge invariance of  $\Delta$  follows from the gauge invariance of  $\bar{s}$  and  $\hat{M}$ . Furthermore,  $\Delta$  is given entirely by hard contributions, which justifies its interpretation as matching coefficient. Using (6) we can express it in terms of the hard part of the self-energy  $\Pi_h(s)$ . Writing  $\Pi_h(s) = \hat{M}^2 \sum_{k,l} \delta^l \Pi^{(k,l)}$ , where it is understood that  $\Pi^{(k,l)} \sim \alpha^k$ , we obtain

$$\begin{aligned} \Delta &\equiv \sum_i \Delta^{(i)} = \\ &\hat{M} \Pi^{(1,0)} + \hat{M} \left( \Pi^{(2,0)} + \Pi^{(1,1)} \Pi^{(1,0)} \right) + \dots \end{aligned} \quad (9)$$

Explicit results for  $\Delta^{(1)}$  and  $\Delta^{(2)}$  in the  $\overline{\text{MS}}$  and pole renormalization scheme can be found in [4]. Here we only note that in the pole scheme  $\bar{s} \equiv M^2 - iM\Gamma$ , so  $\Delta = -i\Gamma$  when  $\hat{M} = M$ . Inserting the expansion (9) into (8) and supplementing  $\mathcal{L}_{\phi\phi}$  with the kinetic terms for soft photons and fermions we obtain

$$\begin{aligned} \mathcal{L}_{\text{HSET}} &= 2\hat{M}\phi_v^\dagger \left( iv \cdot D_s - \frac{\Delta^{(1)}}{2} \right) \phi_v \\ &+ 2\hat{M}\phi_v^\dagger \left( \frac{(iD_{s\top})^2}{2\hat{M}} + \frac{[\Delta^{(1)}]^2}{8\hat{M}} - \frac{\Delta^{(2)}}{2} \right) \phi_v \\ &- \frac{1}{4} F_{s\mu\nu} F_s^{\mu\nu} + \bar{\psi}_s i \not{D}_s \psi_s + \bar{\chi}_s i \not{\partial} \chi_s. \end{aligned} \quad (10)$$

Each term in  $\mathcal{L}_{\text{HSET}}$  can be assigned a scaling power in  $\delta$ . In momentum space the propagator of the  $\phi_v$  field scales as  $1/\delta$ . Hence, because  $\int d^4k$  counts as  $\delta^4$ , the soft scalar field  $\phi_v(x)$  scales as  $\delta^{3/2}$ . Since  $\Delta^{(1)} \sim D_s \sim M\delta$ , both terms in the first line of (8) scale as  $\delta^4$  and are leading terms. The terms in the second line are suppressed by one power in  $\delta$  or  $\alpha$ . Finally, since  $A_s^\mu$  scales as  $\delta$  and the soft fermion fields scale as  $\delta^{3/2}$  (see [7]) the terms in the last line of (8) scale as  $\delta^4$ . In (8) we have left out terms

further suppressed in  $\delta$  or  $\alpha$ . As we will see, they are not needed for the calculation of the line shape at NLO. However, we stress that the expansion can be performed to whatever accuracy is needed.

We note that computing the scalar propagator to all orders in  $\delta$  using  $\mathcal{L}_{\text{HSET}}$  does not reproduce (5). Instead near resonance we obtain  $i\varpi^{-1}R_{\text{eff}\phi}/(P^2 - \bar{s})$ , where  $\varpi^{-1} \equiv (\hat{M}^2 + \hat{M}\Delta - k_+^2)^{1/2}/\hat{M} = 1 + \mathcal{O}(\delta, \alpha)$ . The difference in the normalization is taken into account in matching calculations by an additional wave-function normalization factor  $\varpi^{-1/2}$  for each external  $\phi_v$ -line in the effective theory.

Next, we turn to the construction of the effective Lagrangian,  $\mathcal{L}_{\text{SCET}}$ , associated with the energetic fermions. We need a “collinear” mode to describe a fermion with large momentum in the say  $\vec{n}_-$  direction. Such modes have been discussed previously within the context of soft-collinear effective theory (SCET) [6]. The Lagrangian has been worked out to order  $\delta$  in [7] and we can take the parts relevant to us from there. (What we call “soft” here what is usually called “ultrasoft” in the context of SCET and in the power counting our  $\delta$  corresponds to  $\lambda^2$  in [7].) For each direction defined by an energetic particle we introduce two reference light-like vectors,  $n_\pm$ , with  $n_+^2 = n_-^2 = 0$  and  $n_+n_- = 2$  and we write the corresponding momentum as

$$p^\mu = (n_+p) \frac{n_-^\mu}{2} + p_\perp^\mu + (n_-p) \frac{n_+^\mu}{2}, \quad (11)$$

where  $n_+p \sim M$ ,  $n_-p \sim M\delta$  and  $p_\perp \sim M\delta^{1/2}$ . Given a certain direction  $n_-$  we introduce the collinear field  $\psi_c$  which satisfies  $\not{n}_-\psi_c = 0$ . The terms relevant for the calculation of  $\mathcal{T}^{(0)} + \mathcal{T}^{(1)}$  are then given by

$$\mathcal{L}_{\text{SCET}} = \bar{\psi}_c \left( in_-D + i\not{D}_\perp \frac{1}{in_+D_c + i\epsilon} i\not{D}_\perp c \right) \frac{\not{n}_+}{2} \psi_c. \quad (12)$$

Since we are concerned with the forward scattering amplitude, the only directions defined by energetic particles are given by the incoming electron and (anti)neutrino. Thus, we have two sets of collinear modes, one for the incoming electron,  $\psi_{c1}$ , and one for the incoming (anti)neutrino,  $\chi_{c2}$ . Of course, in the case of the neutrino, the covariant derivatives in (12) have to be replaced by ordinary derivatives. All terms in (12) scale as  $\delta^2$ . Terms of order  $\delta^{5/2}$  and  $\delta^3$  exist, but they are not needed for our application, since they would result in contributions suppressed by an additional power of  $\alpha$  and, therefore, contribute only at NNLO. Again there is no difficulty in going to higher orders in the expansion if needed.

The last part to consider is  $\mathcal{L}_{\text{int}}$ . It has to include operators that allow the production and decay of the unstable particle. Without introducing additional modes it is not possible to include such vertices as ordinary interaction terms in the effective Lagrangian [4]. The reason is that the momenta associated with generic collinear fields

$\psi_{c1}$  and  $\bar{\chi}_{c2}$  do not add up to a momentum of the form  $P = Mv + k$ . Either we have to implement this kinematic constraint on our external states by hand [4] or we have to introduce a new “external-collinear” mode. Adopting the second option, we define an external-collinear mode with large momentum in the  $\vec{n}_-$  direction by assigning it a momentum  $\hat{M}n_-/2 + k$ , where  $k \sim \delta$ . This mode has the same virtuality  $\hat{M}\delta^{1/2}$  as a generic collinear mode but the momentum is not given by (11), because it has a fixed large component such that the two incoming fermions produce a scalar near mass shell. For such a mode it is useful to extract the fixed large momentum and to define

$$\psi_{n_-}(x) \equiv e^{i\hat{M}/2(n_-x)} \mathcal{P}_+ \psi_{c1}(x), \quad (13)$$

and similarly for  $\chi_{n_+}$ . For the purpose of computing  $\mathcal{T}^{(0)} + \mathcal{T}^{(1)}$  it is sufficient to take the first term of  $\mathcal{L}_{\text{SCET}}$ , (12), with a soft photon only to describe the interaction of the external-collinear fermions with the photons

$$\mathcal{L}_\pm = \bar{\psi}_{n_-} in_-D_s \frac{\not{n}_+}{2} \psi_{n_-} + \bar{\chi}_{n_+} in_+ \partial \frac{\not{n}_-}{2} \chi_{n_+}. \quad (14)$$

With the external-collinear modes we can implement the production and decay vertices as interaction terms in  $\mathcal{L}_{\text{int}}$ . It is also convenient to integrate out generic collinear fields and keep only the external-collinear modes in the effective theory. Because adding soft fields results in a further suppression in  $\delta$  we then find that we can restrict ourselves to

$$\begin{aligned} \mathcal{L}_{\text{int}} &= C y \phi_v \bar{\psi}_{n_-} \chi_{n_+} + C y^* \phi_v^\dagger \bar{\chi}_{n_+} \psi_{n_-} \\ &+ F \frac{yy^*}{\hat{M}^2} (\bar{\psi}_{n_-} \chi_{n_+}) (\bar{\chi}_{n_+} \psi_{n_-}), \end{aligned} \quad (15)$$

where  $C = 1 + \mathcal{O}(\alpha)$  and  $F$  are the matching coefficients. The external fields scale as  $\delta^{3/2}$ . Thus, an insertion of a  $\phi\psi\chi$  operator results in  $\int d^4x \phi_v \bar{\psi}_{n_-} \chi_{n_+} \sim \delta^{1/2}$ . The forward scattering amplitude can be obtained by two insertions of this operator. Taking into account the scaling of the external state  $\langle \bar{\nu} e^- | \sim \delta^{-1}$  we see that  $\mathcal{T}^{(0)} \sim \alpha/\delta$ . The four-fermion operator is suppressed in  $\delta$  and results in a contribution of order  $\alpha$  to  $\mathcal{T}$ . Thus, to compute  $\mathcal{T}^{(1)}$  we need  $C^{(1)}$ , the  $\mathcal{O}(\alpha)$  contribution to the matching coefficient  $C$ , while  $F$  is only needed at tree level.

The coefficient  $C^{(1)}$  is obtained by matching the on-shell three-point function of a scalar field, an electron and a neutrino at order  $y\alpha$  and at leading order in  $\delta$ . In particular, this involves the computation of (the hard part) of the vertex diagram, and the additional wave-function normalization factor  $\varpi^{-1/2}$  mentioned above has to be taken into account. For the precise matching equation as well as the explicit result for  $C^{(1)}$  we refer to [4]. Here it suffices to say that these are standard loop calculations. To obtain  $F^{(0)}$  (the LO contribution to  $F$ ) we have to match the four-point function at tree level, but include subleading terms in  $\delta$ . The explicit result is  $F^{(0)} = 1/4$ .

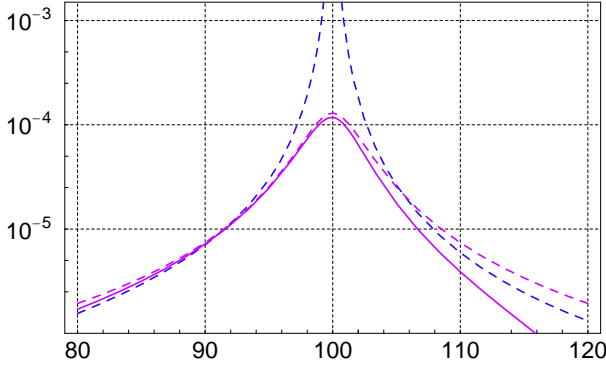


FIG. 1: The line shape (in  $\text{GeV}^{-2}$ ) in the effective theory at LO (light grey/magenta dashed) and NLO (light grey/magenta) and the LO cross section off resonance in the full theory (dark grey/blue dashed) as a function of the center-of-mass energy (in GeV).

We have now completed the construction of the effective Lagrangian  $\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{HSET}} + \mathcal{L}_{\pm} + \mathcal{L}_{\text{int}}$  to an accuracy sufficient to compute  $\mathcal{T}$  at NLO. At leading order there is only one diagram, involving two three-point vertices and one resonant scalar propagator. We get

$$i\mathcal{T}^{(0)} = \frac{-iyy^*}{2\hat{M}\mathcal{D}} [\bar{u}(p)v(q)] [\bar{v}(q)u(p)], \quad (16)$$

where we defined  $\mathcal{D} \equiv \sqrt{s} - \hat{M} - \Delta^{(1)}/2$ . In the effective theory there are three classes of diagrams that contribute to  $\mathcal{T}^{(1)}$ . Firstly, there are hard corrections consisting of a propagator insertion  $[\Delta^{(1)}]^2/4 - \hat{M}\Delta^{(2)}$  as well as a vertex insertion  $C^{(1)}$ . Secondly, there is a four-point vertex diagram due to the  $(\bar{\psi}\chi)(\bar{\chi}\psi)$  operator in  $\mathcal{L}_{\text{int}}$ . The third class are soft-photon loop diagrams, corresponding to the non-factorizable corrections. Adding up all these contributions and using the explicit result for  $C^{(1)}$  (in the  $\overline{\text{MS}}$  scheme) [4] we obtain

$$i\mathcal{T}^{(1)} = i\mathcal{T}^{(0)} \times \quad (17)$$

$$\left[ a_g \left( 3 \ln \frac{-2\hat{M}\mathcal{D}}{\nu^2} + 4 \ln \frac{-2\hat{M}\mathcal{D}}{\hat{M}^2} \ln \frac{-2\hat{M}\mathcal{D}}{\nu^2} - 7 \ln \frac{-2\hat{M}\mathcal{D}}{\hat{M}^2} - \frac{3}{2} \ln \frac{\hat{M}^2}{\mu^2} - \frac{7}{2} + \frac{2\pi^2}{3} \right) + a_y \left( 2 \ln \frac{\hat{M}^2}{\mu^2} - \frac{1}{2} - i\pi \right) - \frac{[\Delta^{(1)}]^2}{8\hat{M}\mathcal{D}} + \frac{\Delta^{(2)}}{2\mathcal{D}} - \frac{\mathcal{D}}{2\hat{M}} \right],$$

where  $a_i \equiv \alpha_i/(4\pi)$ . The initial state collinear singularities have been subtracted minimally and we denote the corresponding factorization scale by  $\nu$  to distinguish it from the renormalization scale  $\mu$ .

We can now perform the polarization average and take the imaginary part of  $(\mathcal{T}^{(0)} + \mathcal{T}^{(1)})/s$ . This result describes the line shape near resonance with a relative error of  $\alpha^2$ . Moving away from the resonance, the relative

error becomes of order unity, since  $\delta$  is not small any longer. To obtain a good description for all values of  $\sqrt{s}$ , the result of the effective theory has to be matched to the off-resonance result of the full theory.

In Figure 1 we show the leading order line shape in the effective theory and the tree-level (order  $\alpha^2$ ) cross section off resonance in the full theory. The two results agree in an intermediate region where both calculations are valid. This allows to obtain a consistent LO result for all values of  $\sqrt{s}$ . We also show the NLO line shape. For the numerical results we have chosen to use the  $\overline{\text{MS}}$  scheme with  $\alpha_y = \alpha_g = 0.1$  and  $\alpha_\lambda = (0.1)^2/(4\pi)$ . The pole mass is assumed to be  $M = 100$  GeV which results in the  $\overline{\text{MS}}$  value  $\hat{M} = 98.8$  GeV for the LO result and  $\hat{M} = 99.1$  GeV for the NLO result. Furthermore, we have chosen a variable factorization scale such that there are no large logarithms involving  $\nu$ . We remark that in order to obtain an improved NLO result for the whole region of  $\sqrt{s}$ , the NLO line shape would have to be matched to the NLO off-resonance cross section in the full theory.

The example considered here is based on a rather simple toy model. Nevertheless, it allows to address the conceptual issues related to unstable particles. The main result is that, using an effective theory approach, calculations can be performed in a systematic way in expanding in the small quantities  $\alpha$  and  $\Gamma/M$ . Applying our method to the Standard Model might require more tedious calculations, but the main result remains valid. In particular, as discussed in [4], NNLO line-shape calculations now appear feasible.

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