

Galaxy formation using halo merger histories taken from N -body simulations

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ABSTRACT

We develop a hybrid galaxy formation model that uses outputs from an N -body simulation to follow the merger histories (or ‘merger trees’) of dark matter haloes and treats baryonic processes, such as the cooling of gas within haloes and subsequent star formation, using the semi-analytic model of Cole et al. We compare this hybrid model with an otherwise identical model that utilizes merger-tree realizations generated using a Monte Carlo algorithm and find that, apart from the limited mass resolution imposed by the N -body particle mass, the only significant differences between the models are caused by the known discrepancy between the distribution of halo progenitor masses predicted by the extended Press–Schechter theory and that found in N -body simulations. We investigate the effect of limited mass resolution on the hybrid model by comparing with a purely semi-analytic model that has greatly improved mass resolution. We find that the mass resolution of the simulation we use, which has a particle mass of $1.4 \times 10^{10} h^{-1} M_{\odot}$, is insufficient to produce a reasonable luminosity function for galaxies with magnitudes in the b_J band fainter than -17 .

Key words: methods: numerical – galaxies: formation.

1 INTRODUCTION

Hierarchical models of galaxy formation must describe both the growth and collapse of density perturbations to form dark matter haloes and the baryonic processes that lead to the formation of stars. Despite uncertainty as to the exact nature of the dark matter itself, the formation and evolution of dark matter haloes appears to be reasonably well understood. The two main approaches to this problem are direct numerical simulations and analytic techniques such as the Press–Schechter theory (Press & Schechter 1974). Encouragingly, the mass functions of dark matter haloes predicted using these very different approaches are found to agree to within 50 per cent (Gross et al. 1998; Governato et al. 1999; Jenkins et al. 2001). The analytic model described by Sheth & Tormen (2002) based on the assumption that objects collapse ellipsoidally rather than spherically achieves even better agreement with N -body simulations. Mo & White (2002) present halo abundances from this and several other models.

This understanding of the hierarchical build up of structure provides the starting point for semi-analytic models of galaxy formation, which attempt to follow the development of galaxies from primordial density fluctuations. In semi-analytic models, merger

histories for dark matter haloes may be taken directly from dark matter simulations (e.g. Kauffmann et al. 1999; van Kampen, Jimenez & Peacock 1999). Alternatively, extensions to the Press–Schechter theory that predict the conditional halo mass function (Bond et al. 1991; Bower 1991) and halo survival times, formation times and merger rates (Lacey & Cole 1993) may be used to construct realizations of merger histories for individual haloes. Simple analytic modelling is then used to follow the evolution of the baryonic component, including prescriptions for processes such as star formation and its possible effects on the remaining gas. Semi-analytic models (e.g. Cole 1991; Lacey & Silk 1991; White & Frenk 1991; Cole et al. 1994, 2000; Somerville & Primack 1999) have successfully reproduced many observable properties of galaxies, such as the local field galaxy luminosity function and distributions of colour and morphology. When combined with N -body simulations, semi-analytic models have also successfully reproduced galaxy clustering properties (e.g. Governato et al. 1998; Kauffmann et al. 1999; Benson et al. 2000; Wechsler et al. 2001).

Semi-analytic models utilizing merger trees generated using algorithms based on the extended Press–Schechter (EPS) formalism have two closely related advantages over models that take merger histories from N -body simulations. Creating Monte Carlo realizations of merger trees for a set of haloes generally requires fewer computing resources than carrying out an N -body simulation of a

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similar number of haloes. In both cases, improving the mass resolution increases the computational load, but since the load is much less in the Monte Carlo case, significantly better mass resolution may be achieved. Methods based on the Press–Schechter theory, however, are only applicable to initially Gaussian fluctuation fields. N -body simulations, on the other hand, have the advantage that the non-linear evolution of density fluctuations is followed in complete generality, without the need for any of the assumptions involved in creating EPS merger trees.

There are advantages to both of these methods, and which is more appropriate depends on the problem being addressed. In this paper we investigate the effects of the choice of merger trees on the predictions of one particular semi-analytic model. We describe a new method of extracting merger trees from an N -body simulation and incorporate these merger trees into a semi-analytic galaxy formation model based on that of Cole et al. (2000). We compare the predictions of this model with those of a similar model utilizing Monte Carlo realizations of halo merging histories. In order to identify the reasons for the discrepancies that we find, we determine the changes that must be made to the Monte Carlo model to reproduce the N -body results.

The use of N -body merger trees in semi-analytic models allows a halo-by-halo comparison between the semi-analytic treatment of baryonic processes, such as gas cooling, and direct numerical simulations of galaxy formation. In a companion paper (Helly et al. 2003) we carry out such a comparison between a ‘stripped down’ version of the semi-analytic model described in this paper and a smoothed particle hydrodynamics simulation of a cosmological volume.

This paper is laid out as follows. In Section 2 we explain how we obtain merger trees from an N -body simulation. In Section 3 we investigate the effect on our semi-analytic model of utilizing merger trees derived from N -body simulations rather than Monte Carlo realizations. In Section 4 we present our conclusions.

2 EXTRACTING MERGER TREES

We now present the method we used to calculate the merger histories of dark matter haloes identified in an N -body simulation. The simulation, which will be referred to as the GIF simulation, was carried out by the Virgo Consortium using a parallel adaptive particle–particle/particle–mesh (AP^3M) code known as HYDRA (Couchman, Thomas & Pearce 1995; Pearce & Couchman 1997) as part of the GIF project. The simulation assumes the Λ -cold dark matter (Λ CDM) cosmology with mean mass density parameter $\Omega_0 = 0.3$, cosmological constant $\Lambda_0 = 0.7$ in units of $3H_0^2/c^2$, power spectrum shape parameter $\Gamma = 0.21$, present-day rms linear fluctuation amplitude in $8h^{-1}$ Mpc spheres $\sigma_8 = 0.90$, and Hubble constant $h = 0.7$ in units of $100 \text{ km s}^{-1} \text{ Mpc}^{-1}$. It contains 256^3 dark matter particles each of mass $1.4 \times 10^{10} h^{-1} M_\odot$ in a box of side $141.3h^{-1}$ Mpc. The gravitational softening length in the simulation is $30h^{-1}$ kpc at $z = 0$. This simulation is described in more detail by Jenkins et al. (1998), where it is referred to as Λ CDM2, and by Kauffmann et al. (1999). While halo catalogues and merger trees based on this simulation are publically available, here we make use of only the simulation outputs themselves and construct merger trees using a somewhat different algorithm from that of Kauffmann et al. We use 44 output times from the simulation that are spaced equally in $\log_{10}(1+z)$ between $z = 0$ and ~ 20 .

2.1 Identifying haloes

In order to construct merger histories for dark matter haloes in an N -body simulation, a catalogue of haloes must be produced for each

simulation output using a group-finding algorithm. The algorithm used here is the ‘friends of friends’ (FOF) method of Davis et al. (1985), which simply links together any particles with separations less than the linking length b , usually expressed in terms of the mean interparticle separation. Given sufficiently large numbers of particles in each object, the FOF algorithm finds regions bounded by a surface of constant density. The density threshold is proportional to $1/b^3$.

The FOF approach has the advantage that it imposes no constraints on the geometry of the haloes identified, but it may occasionally artificially join two nearby haloes if a transient ‘bridge’ of a few particles forms between them. It will be seen in Section 2.2 that this can cause problems when attempting to generate merger trees using FOF group catalogues, and a method of identifying and splitting artificially joined haloes is described in Section 2.2.

The usual choice for the linking length in cosmologies with $\Omega = 1$ is $b = 0.2$ (e.g. Lacey & Cole 1994), which identifies haloes with a mean density similar to that predicted by the top hat spherical collapse model (Cole & Lacey 1996). However, in cosmologies with $\Omega < 1$ there is no rigorous justification for any particular choice. Here, we choose to set $b = 0.2$ at all redshifts as in the $\Omega = 1$ case [see Eke, Cole & Frenk (1996) and Jenkins et al. (2001) for further discussion].

The other parameter needed by the FOF algorithm is the minimum number of particles, N_{\min} , required to constitute a group. It is important that N_{\min} be as small as possible, since detailed merger trees can only be obtained for haloes much larger than the smallest resolvable group. Kauffmann et al. (1999) found that in their simulations groups as small as 10 particles are dynamically stable systems and that for 95 per cent of these groups, 80 per cent of the particles remain in the same group at subsequent times.

We therefore identify haloes using a linking length $b = 0.2$ at all redshifts, with a minimum group size of 10 particles. The resulting catalogues may still contain some groups that consist of unbound particles that happen to be close together at this particular time-step. To remove these, we follow Benson et al. (2001b) and calculate the total energy of each group. Unbound groups are not immediately discarded, because they may only be unbound as a result of the presence of a small number of fast moving particles. The binding energy of each particle is calculated, and the least bound particle is removed from the group. This is repeated until the group becomes bound. If half of the particles are removed or the group is reduced to less than N_{\min} particles we discard it. Up to 5 per cent of all groups are discarded, with a similar number of groups being reduced in mass by this procedure. The affected groups generally consist of around 10–20 particles.

We use the procedure described above to generate halo catalogues for 44 simulation outputs between redshifts $z = 20$ and 0, spaced approximately evenly in $\log_{10}(1+z)$.

2.2 Constructing N -body merger trees

In an idealized picture of the process of hierarchical structure formation (e.g. Press–Schechter theory), dark matter haloes may increase in mass by mergers, but cannot lose mass. Consequently, any halo identified in a simulation prior to the final output time should still exist at subsequent output times, although it may have become subsumed within a larger halo through a merger. In any case, the constituent particles of the original halo should still all be members of a single group. It should therefore be possible to identify each halo in the simulation as a progenitor of a single halo at the next output time.

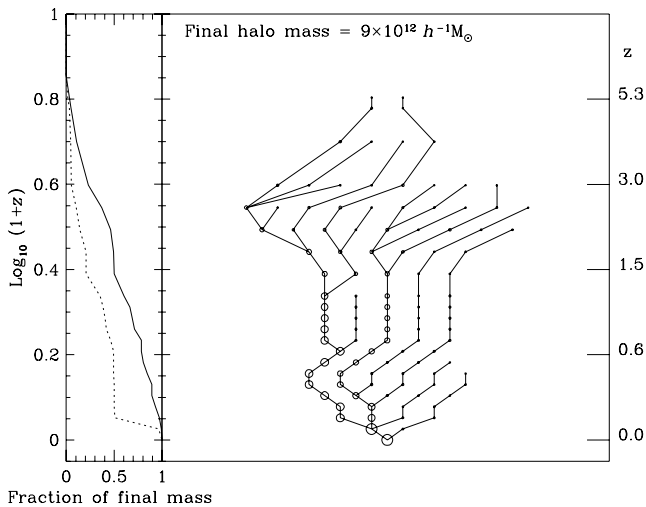


Figure 1. An example of a merger tree obtained from the GIF simulation for a halo of mass $9 \times 10^{12} h^{-1} M_{\odot}$ at redshift $z = 0$. Each circle represents a dark matter halo identified in the simulation, with the area of the circle being proportional to the halo mass. The vertical position of each halo on the plot is determined by $\log_{10}(1+z)$ at the redshift at which it exists, the horizontal positioning is arbitrary. The solid lines connect haloes to their progenitors. The solid line in the panel on the left-hand side shows the fraction of the final mass contained in resolved progenitors as a function of redshift. The dotted line shows the fraction of the final mass contained in the largest progenitor as a function of redshift.

In practice there are several ways in which a halo can lose particles. Haloes may be disrupted by tidal forces caused by other nearby haloes. The masses of simulated haloes can also fluctuate because the FOF algorithm imposes a somewhat arbitrary boundary on the halo and outlying particles that are considered group members at one time-step may lie just beyond the boundary at the next time-step.

The technique we use to determine merger histories is intended to take into account this uncertainty in the definition of a halo and a possible loss of particles. First, we consider two adjacent output times from the simulation, t_1 and t_2 , where $t_1 < t_2$. Each halo at time t_1 is labelled as a progenitor of whichever halo at time t_2 contains the largest fraction of its particles. This process is repeated for all pairs of adjacent output times. It is then straightforward to trace the merger history of each halo that exists at the final output time. Fig. 1 shows an example of a merger tree created in this way for a halo with a final mass of approximately $9 \times 10^{12} h^{-1} M_{\odot}$, or around 700 particles.

In the semi-analytic model used here, galaxies are assumed to form at the centres of dark matter haloes, so the centre of each halo in the merger tree must be defined. We choose to follow Kauffmann et al. (1999), who identified the most bound dark matter particle as the position of any galaxy that forms in the halo. We define the binding energy of a particle as the sum of its kinetic energy and the gravitational potential energy owing to the other particles in the halo. This approach differs from that of Benson et al. (2001a), who associated the central galaxy in a halo with the centre of mass. Once a galaxy forms it is assumed to follow this particle until the parent halo merges with another halo and dynamical friction, calculated as described in Cole et al. (2000), causes the galaxy to merge with the central galaxy of the new halo. We therefore check that the most bound particle of a halo remains a member of the same halo as the majority of the constituent particles of the halo at the next output time. If this is not so, we choose the most bound particle from those

that *are* in the correct halo at the later output time. This problem generally only occurs in smaller haloes that may be easily disrupted.

During the construction of the merger trees, we also attempt to deal with the problem mentioned in Section 2.1 – the possibility that nearby haloes may be artificially linked by the FOF algorithm. The problem occurs if two haloes become temporarily linked by a transient ‘bridge’ of particles that causes the FOF group finder to consider them as a single, large group. When the bridge is later broken, the group splits, leaving the two original haloes. Our tree building method would identify the large, joined group as a progenitor of the larger of the two final groups.

These situations are identified by looking for groups at the earlier time t_1 , the particles of which are shared between two or more groups at the subsequent output time t_2 . This indicates that between times t_1 and t_2 the group has split into smaller groups, which we refer to here as ‘fragments’.

We split such spuriously joined groups into one new group for each fragment that contains more than N_{\min} of its constituent particles. Particles belonging to one of these fragments at time t_2 are assigned to the corresponding new group at the earlier time t_1 . Particles belonging to no fragment, or to a fragment with fewer than N_{\min} particles from the joined group, are assigned to the new group corresponding to the fragment ‘closest’ to their position at time t_1 . The separations used are weighted by a factor of $M^{-1/3}$ to account for the spatial extent of the groups, where M is the mass of the fragment.

The splitting procedure is first carried out for haloes at the penultimate time-step and then repeated for each earlier output time in order of increasing redshift. For each time-step a modified group catalogue is produced, which is then used to determine whether any haloes at the previous time-step need to be split. This ensures that if any bridge between a pair of haloes persists for more than one time-step the haloes are split at each time-step where the bridge exists.

2.3 Mass conservation

In the GALFORM semi-analytic model of Cole et al. (2000), haloes may gain mass through mergers with other haloes. The mass of a halo always increases with time, and the difference between the mass of a halo and the sum of the masses of its progenitors is caused by the accretion of small, unresolved dark matter haloes.

The *N*-body merger trees may contain haloes that decrease in mass from one time-step to the next for the reasons described in Section 2.2 – the nature of the definition of a halo imposed by the FOF group finder and the possibility of disruption by tidal forces. Consequently, a halo in an *N*-body merger tree may be somewhat *less* massive than its progenitors. In the GALFORM model this corresponds to the unphysical situation where a negative amount of mass is accreted in the form of subresolution haloes.

The solid lines in Fig. 2 show the distribution of the ratio $\sum M_{\text{prog}}/M_{\text{halo}}$, where M_{halo} is the mass of a halo and $\sum M_{\text{prog}}$ is the total mass of the immediate progenitors of the halo, which exist at the previous time-step. Haloes at all time-steps (other than the first) are included. If these merger trees had been created using the technique of Cole et al. (2000), then this ratio would always be less than unity. It can be seen from Fig. 2 that for haloes less massive than approximately $10^{12} h^{-1} M_{\odot}$ the total mass in the progenitors can occasionally exceed the mass of the halo they form at the next time-step by up to 50 per cent. More massive haloes are less affected, but there are still rare instances where the largest haloes have progenitors with masses 5–10 per cent greater than the mass of the halo.

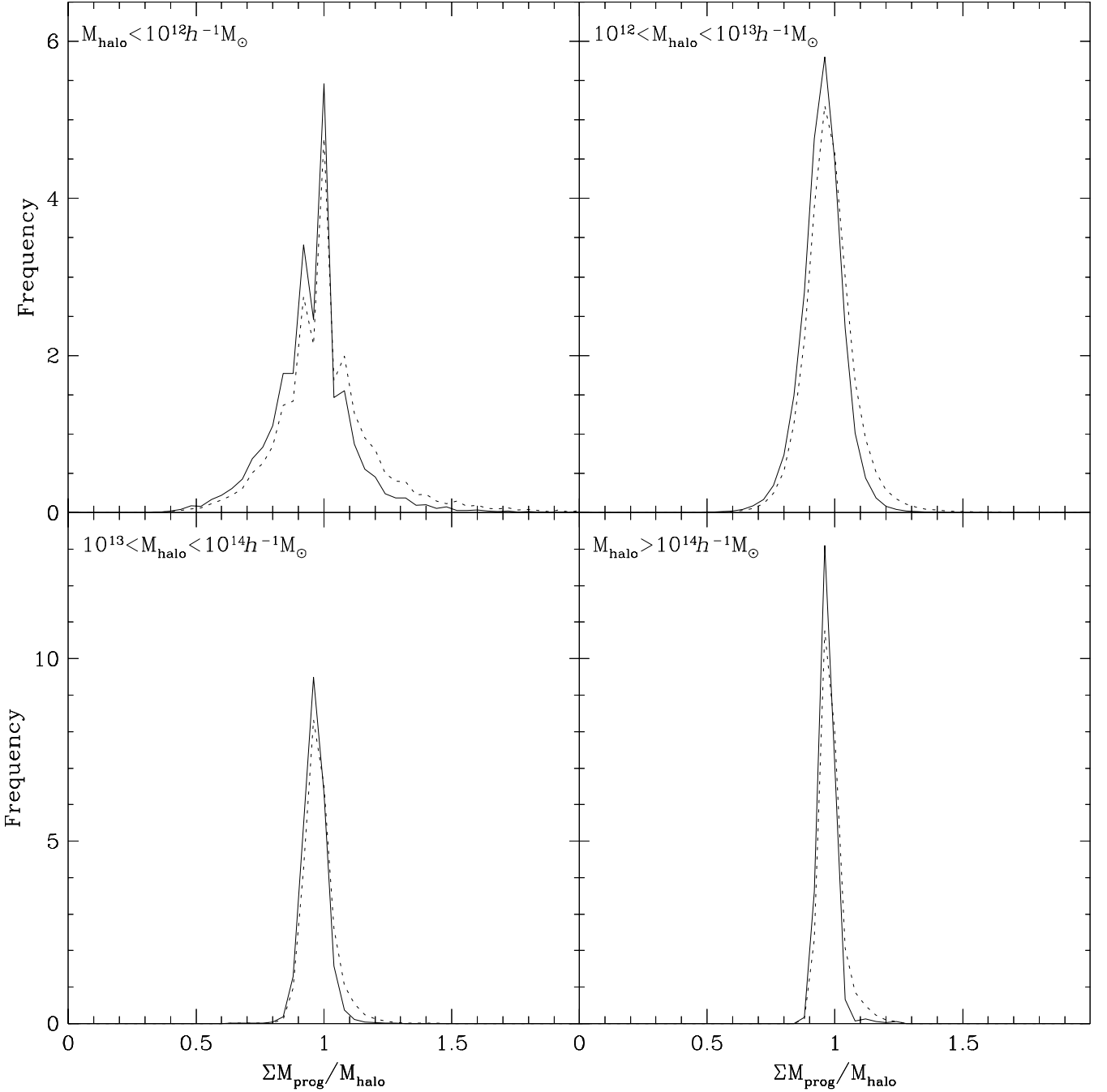


Figure 2. The solid lines show the distribution of the ratio of the total mass of the immediate progenitors of a halo, $\sum M_{\text{prog}}$, to the mass of the halo at the next time-step, M_{halo} . Each panel shows the distribution of $\sum M_{\text{prog}}/M_{\text{halo}}$ for haloes in the mass range shown at the top of the panel. The dotted lines show the distribution of $\sum M_{\text{prog}}/M_{\text{halo}}$ if $\sum M_{\text{prog}}$ is evaluated after the progenitors have been increased in mass to at least the total mass of *their* progenitors. Where this ratio is greater than 1, it is the factor by which M_{halo} must be changed to ensure mass conservation if we choose to add mass.

Mass conservation can be forced on the N -body merger trees by simply adjusting the masses of some of the haloes. Two opposite approaches to the problem are possible. Mass can be added to those haloes that are less massive than their progenitors, or mass can be removed from the progenitors themselves. In order to show that the changes made to the halo masses have little effect on the semi-analytic model, we create merger trees using both methods.

Enforcing the conservation of mass in merger trees by adding mass is relatively straightforward. If a halo is less massive than its

progenitors, its mass is increased to match that of the progenitors. The halo may, in turn, be a progenitor of a later halo that may now become less massive than its own progenitors. This later mass of the halo will then also be increased. Changes made to halo masses at early times may therefore propagate to later times.

Similarly, if mass is removed from a halo to force conservation of mass, it may become less massive than its progenitors and reductions in mass could then propagate to earlier times. We attempt to remove mass in such a way as to minimize the effects on earlier haloes.

Each halo has a certain amount of ‘excess’ mass beyond that of its progenitors, which was accreted over the previous time-step in the form of subresolution objects. This mass, if it exists, may be removed without the change propagating to earlier haloes. When a halo that is less massive than its progenitors is found, mass is first removed from the excess mass of the largest progenitor. If still more mass must be removed, it is taken from the excess mass of the other progenitors in decreasing order of mass. If all of the excess mass of the progenitors is removed and yet more mass needs to be taken away, the masses of all of the progenitor haloes are simply scaled down by a constant factor.

The dotted lines in Fig. 2 show the sizes of the changes we are forced to make when we enforce mass conservation by adding mass to haloes. These lines show the distribution of the ratio $\sum M_{\text{prog}}/M_{\text{halo}}$ if $\sum M_{\text{prog}}$ is evaluated after the progenitors of the halo at all previous time-steps have been made at least as massive as their own progenitors. M_{halo} is still the original halo mass. Where this ratio exceeds unity, it is the factor by which M_{halo} must be scaled to ensure that the halo is at least as massive as its progenitors. It can be seen that the required changes to individual haloes are generally small, and adjustments are required much less frequently in well-resolved haloes. However, the masses of a minority of haloes are affected quite significantly and it is necessary to show that these changes do not affect the galaxy population predicted by the semi-analytic model. The algorithms described above are two opposite ways of dealing with the problem of mass conservation in the merger trees. While artificially altering the halo masses is clearly not ideal, if, as is the case, both methods produce very similar results when the merger trees are fed into the semi-analytic model we can then conclude that the changes we have made are insignificant. This comparison is carried out in Section 3.3.

3 COMPARISON BETWEEN GALFORM AND *N*-BODY GALFORM

In this section we describe our semi-analytic model, indicating how it differs from the model of Cole et al. (2000) on which it is based. We also explain how merger trees obtained from a simulation may be incorporated into the model.

3.1 The *N*-body GALFORM model

We use the GALFORM semi-analytic model to treat the process of galaxy formation within the dark matter haloes in the GIF simulation. The model is described in detail by Cole et al. (2000) so here we present only a brief description of features that are important to this work. The original model of Cole et al. will be referred to as ‘standard GALFORM’, and the version using merger trees taken from a simulation will be referred to as ‘*N*-body GALFORM’.

The starting point for the standard GALFORM model is a set of merger trees created using a Monte Carlo technique. The history of each halo is divided into a number of discrete time-steps. Extended Press–Schechter theory is used to estimate the probability that a halo ‘fragments’ into two progenitors when a step back in time of size δt is taken. The masses of the fragments are chosen at random from a distribution consistent with extended Press–Schechter theory. Haloes are repeatedly split in this way to create merger trees. A mass resolution limit is imposed on the merger trees, below which progenitors are considered to be material acquired through continuous accretion. The mass resolution is normally set sufficiently high that the results of interest are not sensitive to its value. In the *N*-body GALFORM model, we replace these merger trees with those calculated

directly from the GIF simulation as described in Section 2.2. The mass resolution limit is then determined by the mass of the smallest halo that can be resolved in the simulation.

The dark matter haloes in the merger tree are assumed to be spherically symmetric with the radial density profile of Navarro, Frenk & White (1996, 1997):

$$\rho(r) \propto \frac{1}{r/r_{\text{NFW}}(r/r_{\text{NFW}} + 1)^2}, \quad (1)$$

where r_{NFW} is the scale radius of the halo and is related to the concentration parameter, c , defined by Navarro et al. (1997) through $r_{\text{NFW}} = r_{\text{virial}}/c$, where r_{virial} is the virial radius of the halo. The concentration parameter is set using the method described in the appendix of the same paper. We do not allow for any scatter in the concentration parameter as a function of halo mass.

Our treatment of the cooling of gas within haloes is identical to that of Cole et al. (2000). Initially, the amount of gas in each halo is taken to be equal to the mass of the halo times the universal baryon fraction. The gas is assumed to be shock-heated to the virial temperature of the halo when it forms. We assume that the radial density profile of the gas is given by

$$\rho_{\text{gas}}(r) \propto 1/(r^2 + r_{\text{core}}^2), \quad (2)$$

where the core radius is given by $r_{\text{core}}/r_{\text{NFW}} \approx \frac{1}{3}$ in accordance with the simulations of Navarro, Frenk & White (1995). This core radius is allowed to grow with time from an initial value, r_{core}^0 , as gas is removed by cooling in order to maintain the same gas density at the virial radius. This ensures that the pressure at the virial radius, which would be maintained by shocks from infalling material, remains unchanged.

To determine the rate at which gas can cool and form a disc at the centre of the halo, the cooling time of the gas is calculated as a function of radius using the cooling function of Sutherland & Dopita (1993). Gas that has had time to cool and fall to the centre of the halo is added to the disc where it is available to form stars.

When haloes merge, the most massive galaxy becomes the central galaxy in the new halo. The resolution of the simulations used here is insufficient to follow the evolution of substructure within the dark matter haloes. Instead, the dynamical friction time-scale, as defined by Lacey & Cole (1993), is used to determine when each satellite will merge on to the central galaxy. It should be noted at this point that the orbital parameters used to determine the dynamical friction time for each galaxy are assigned at random from a distribution consistent with the numerical results of Tormen (1997), even when using merger trees obtained from the simulation.

3.2 Parameters in the *N*-body GALFORM model

The GALFORM semi-analytic model requires a number of parameters to be specified, which can be divided into three categories. There are numerical parameters, parameters describing the background cosmology and parameters that describe the physical model of galaxy formation.

The numerical parameters are the mass resolution, M_{res} , the number of time-steps in the merger tree and the starting redshift. In the *N*-body GALFORM model these are all constrained by the properties of the simulation used to obtain the merger trees. The mass resolution is the mass of the smallest halo that our group-finding algorithm can resolve, there is one time-step for each simulation output and the starting redshift is the redshift of the first output. The cosmological parameters Ω_0 , Λ_0 , h , σ_8 , Γ and, in the case of a simulation with a baryonic component, Ω_b , are also fixed by the simulation.

The remaining parameters allow us to vary the treatment of the processes involved in galaxy formation. The parameters we are interested in are as follows.

- (i) r_{core}^0 , the initial size of the core in the radial gas density profile, specified in terms of r_{NFW} (see equation 2).
- (ii) The evolution of r_{core} with time. The radius r_{core} may be a fixed fraction of r_{NFW} or it may be allowed to increase with time as described in Section 3.1.
- (iii) f_{df} , a factor by which the dynamical friction time-scale for a satellite galaxy, which is used to determine when the galaxy merges with the central galaxy of the halo, may be scaled. Increasing f_{df} reduces the rate at which galaxy mergers occur within haloes.

The other parameters in the model are the same as those in the reference model of Cole et al. (2000), with the following minor changes: $v_{\text{hot}} = 250 \text{ km s}^{-1}$ and $f_{\text{ellip}} = 0.5$. The parameter v_{hot} determines the efficiency with which energy injection from supernovae and young stars reheats and ejects cold gas from galactic discs. The parameter f_{ellip} is used to decide the outcome of mergers between central and satellite galaxies. If the ratio of the mass of the satellite to the mass of the central galaxy is greater than f_{ellip} , any gas in the discs of the two galaxies is converted into stars and an elliptical galaxy is produced. If the ratio is smaller than f_{ellip} , any stars present in the satellite are added to the bulge of the central galaxy and any gas is added to the disc. These changes to the Cole et al. model are required to obtain a realistic luminosity function at $z = 0$ with the higher baryon density, $\Omega_b = 0.038$, which we use here.

Our prescription for star formation differs slightly from that of Cole et al. In our model, the time-scale for star formation is given by

$$\tau_* = \tau_*^0 \left(V_{\text{disc}} / 200 \text{ km s}^{-1} \right)^{\alpha_*}, \quad (3)$$

where V_{disc} is the circular velocity of the galaxy disc and the time-scale, τ_*^0 , is set to 3 Gyr. We set $\alpha_* = -2.5$. The way τ_* scales with redshift in this model results in reduced star formation and more gas-rich mergers at high redshift and has been shown (Lacey et al. 2001) to better reproduce the properties of SCUBA and Lyman break galaxies. Kauffmann & Haehnelt (2000) also find that a star formation scheme with an increased star formation time-scale at high redshift is required to reproduce observations of damped Ly α absorption systems and the increase in number density of bright quasars from $z = 0$ to 2. It should also be noted that, for the purposes of this comparison, the details of our star formation prescription are not critical, since the same scheme is used in both the standard and N -body GALFORM models.

3.3 Effects of mass conservation

The upper panels of Fig. 3 show the galaxy luminosity functions in the b_J and K bands predicted by the N -body GALFORM model with the parameters of Section 3.2, using the two different methods described in Section 2.3 to enforce mass conservation in the merger trees. Over most of the luminosity range plotted, the two curves are essentially identical but there appear to be more galaxies at very faint b_J magnitudes when mass is removed from the merger trees. The majority of these galaxies formed in haloes near the 10-particle ($\simeq 1.4 \times 10^{11} h^{-1} M_\odot$) mass resolution limit imposed by the FOF group finder and their haloes subsequently merged with other, larger dark matter haloes. When mass conservation is enforced by removing mass from the merger trees (the dotted lines in Fig. 3)

it is possible to end up with some haloes with mass lower than the resolution limit that can harbour galaxies with b_J -band magnitudes around -14 or fainter. If, instead, mass is added to haloes less massive than their progenitors, then the merger trees contain no haloes with masses below the FOF resolution threshold and hence fewer faint galaxies.

These subresolution haloes often exist in the merger trees of larger haloes and could affect the evolution of larger, brighter galaxies. However, the agreement of the luminosity functions suggests that any effect is insignificant. The global star formation history and Tully–Fisher relation shown in the lower panels of Fig. 3 are similarly unaffected.

Overall, the choice of mass conservation method appears to make very little difference to the quantities plotted in Fig. 3, which suggests that the small amounts of mass being added to or removed from the merger trees do not significantly affect the properties of the resulting galaxies. The only region of the luminosity function that is affected is largely populated by galaxies that formed in haloes with little or no resolved merger history, where the model cannot be expected to give reliable results. For the remainder of this paper we choose to enforce mass conservation by adding mass to the merger trees since this does not introduce haloes with masses below the resolution limit.

3.4 Comparison with standard GALFORM

The mass resolution of the merger trees taken from the GIF simulation is equal to 10 particle masses or $1.4 \times 10^{11} h^{-1} M_\odot$, i.e. $N_{\text{min}} = 10$. This is much larger than the mass resolution, $M_{\text{res}} = 5.0 \times 10^9 h^{-1} M_\odot$, used by Cole et al. (2000). This will clearly affect the properties of the galaxies predicted by the N -body GALFORM model, since gas will be unable to cool and start forming stars until lower redshifts when haloes with masses greater than M_{res} have formed. In order to investigate the effect of limited mass resolution on the N -body GALFORM model, we identify the properties of the merger trees that differ between standard and N -body GALFORM and use this knowledge to produce a modified version of the standard GALFORM model that reproduces the behaviour of the N -body GALFORM model. We can then increase the mass resolution of the merger trees in the modified model and observe the effects on the predicted galaxy properties.

There are four main reasons why the merger trees in the two models may differ. First, there is the difference in mass resolution described above. Therefore, we initially degrade the mass resolution of the standard GALFORM model to match that of the GIF simulation by setting the minimum halo mass, M_{res} , equal to the mass of $(N_{\text{min}} - 1)$ dark matter particles – any halo of this mass or less in the N -body simulation would not be identified by the FOF group finder and would not be included in the N -body merger trees.

Secondly, Jenkins et al. (2001) have shown that the Press & Schechter (1974) halo mass function (used in the standard GALFORM model) differs somewhat from the mass function determined from N -body simulations. We replace the Press–Schechter mass function in the standard GALFORM model with the mass function determined by Jenkins et al. This ensures that the distribution of halo masses at $z = 0$ in the standard GALFORM model matches the distribution in the simulation.

The number of time-steps also differs between the two models. In the standard GALFORM model we use 150 time-steps evenly spaced in $\log_{10}(1+z)$, whereas in the N -body case we have only 44 simulation outputs. However, we find that if we degrade the time resolution

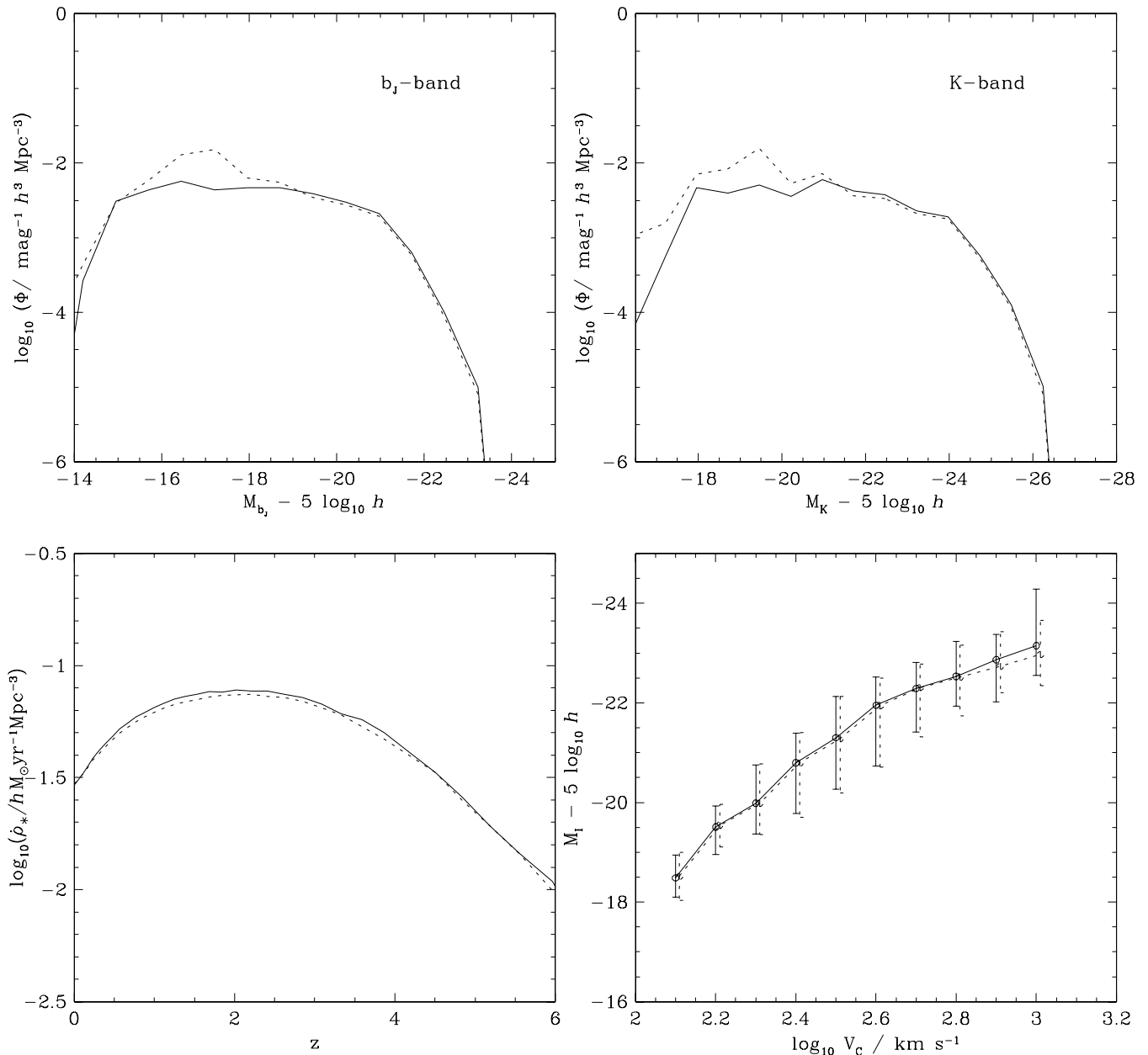


Figure 3. Luminosity functions, star formation histories and Tully–Fisher relations for galaxies predicted by the *N*-body GALFORM model using merger trees obtained from the GIF simulation with two different methods of enforcing mass conservation. The solid lines show results obtained when mass conservation in the merger trees is enforced by increasing the masses of haloes less massive than their progenitors. The dotted lines show the results obtained if, instead, the masses of the progenitors of such haloes are reduced.

of the standard GALFORM model to match that of the *N*-body model the properties of the galaxy populations predicted change very little.

Finally, the distribution of progenitor masses for haloes of a given mass predicted by the standard GALFORM model does not reproduce the distribution found in *N*-body simulations with complete accuracy. Benson et al. (2001a) show that an empirical correction can be used to bring the progenitor mass distributions in the semi-analytic and *N*-body merger trees into closer agreement. The threshold linear overdensity for collapse from the spherical collapse model, δ_c , is replaced with an effective threshold $\delta_c^{\text{eff}} = f_{\delta_c} \delta_c$. In the Λ CDM cosmology employed in the GIF simulation, the following form for f_{δ_c} was found by Benson et al. to give reasonable agreement between

the progenitor mass functions between redshifts 0 and 3:

$$f_{\delta_c} = 1 + 0.14 \left[\log_{10} \left(M_{\text{halo}} / h^{-1} M_{\odot} \right) - 15.64 \right], \quad (4)$$

where M_{halo} is the mass of the final halo at redshift $z = 0$. This form of modification was suggested by Tormen (1998).

These modifications are intended to produce semi-analytic merger trees with statistical properties closely matched to those of the *N*-body merger trees. Fig. 4 shows the galaxy luminosity functions in the b_j and K bands, Tully–Fisher relations and global star formation histories for both the modified GALFORM model described above (dotted lines) and the *N*-body GALFORM model (dashed lines). It can be seen from the figure that these two models predict populations of galaxies with very similar statistical properties. The

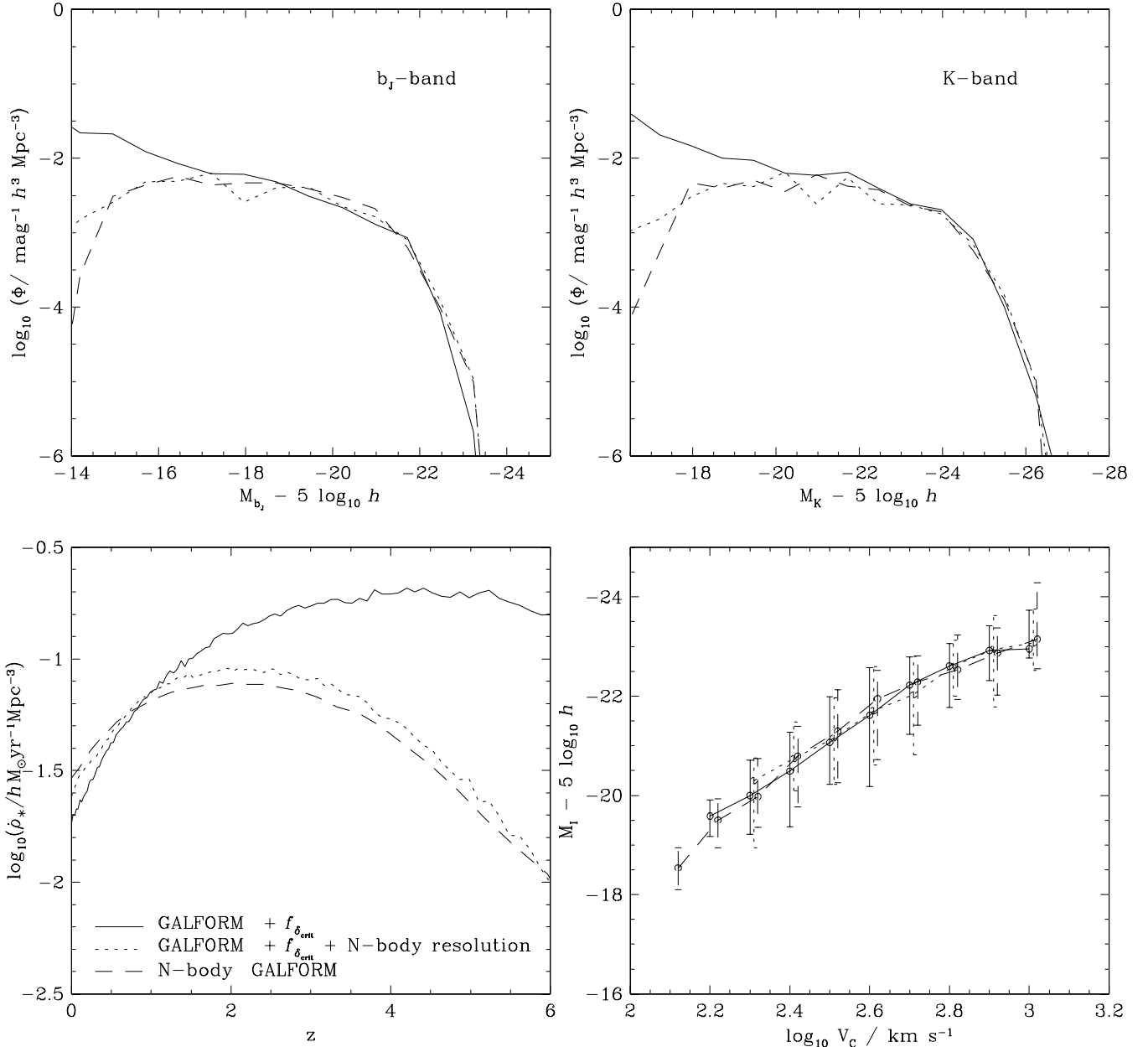


Figure 4. Luminosity functions, star formation histories and Tully–Fisher relations for three different models. The solid lines correspond to the GALFORM model using Monte Carlo generated merger trees as described by Cole et al. (2000), with the modifications explained in Section 3 and a mass resolution of $5 \times 10^9 h^{-1} M_{\odot}$. The dotted lines show results from the same model with a mass resolution of $1.4 \times 10^{11} h^{-1} M_{\odot}$, equivalent to that of the GIF simulation. The dashed lines show results obtained from the N -body GALFORM model that uses merger trees derived from the simulation.

luminosity functions are in reasonable agreement for K brighter than approximately -18 and b_j brighter than approximately -15 . The Tully–Fisher relations and star formation histories are also in close agreement.

As pointed out previously, the fainter galaxies in these models occupy haloes with very poorly resolved merger histories and their properties may be largely determined by the effects of limited mass resolution. The solid lines in Fig. 4 show the properties of the galaxies in the modified GALFORM model when the minimum halo mass M_{res} is reduced to $5.0 \times 10^9 h^{-1} M_{\odot}$. This is much less massive than the smallest halo Benson et al. were able to resolve in their simulations and consequently, in this regime, equation (4) has not been tested and cannot be relied upon to produce a realistic distribution

of progenitor masses. We do not expect this model to reproduce the results of Cole et al. but we show it only to provide some indication of the magnitude of the effect of introducing low-mass haloes into the merger trees.

This ‘improvement’ in mass resolution increases the number of faint galaxies, which form in small, previously unresolved haloes. With a higher minimum halo mass the gas in these small haloes is unable to cool until it becomes incorporated into objects more massive than M_{res} . This is reflected in the luminosity functions, which show that there are slightly more bright galaxies and far fewer faint galaxies at $z = 0$ in the model with poor mass resolution. The star formation history is consistent with this, showing that poor mass resolution results in reduced star formation at $z > 1$ and increased

star formation at $z \approx 0$. However, calculating the global star formation rate involves a sum over all haloes. At high redshifts this includes a large number of haloes of low mass, the abundances of which may be unrealistic owing to our extrapolation of equation (4). Reducing M_{res} appears to have little or no effect on the Tully–Fisher plot.

Overall, the predictions of the *N*-body GALFORM model closely match those of the standard GALFORM model when we take into account the differences in the halo mass function, the progenitor mass distribution and the mass resolution. The differences between the modified GALFORM models with high and low mass resolution indicate that, at low luminosities, the properties of the galaxies in the *N*-body model are seriously affected by the resolution of the simulation. In order to attempt to reproduce the properties of observed galaxy populations accurately with b_j -band magnitudes fainter than approximately -17 , an *N*-body simulation with significantly improved mass resolution would be required.

4 CONCLUSIONS

In this paper we have examined how the statistical properties of the galaxies predicted by a semi-analytic model depend on the way in which the dark matter halo merger histories are created. We have developed a method for calculating merger histories from *N*-body simulations and used the resulting merger trees in a semi-analytic model of galaxy formation based on that of Cole et al. (2000). We refer to this model as *N*-body GALFORM and compare it with an otherwise identical ‘standard GALFORM’ model, which uses halo merger histories generated using the Monte Carlo algorithm of Cole et al. This algorithm is based on the extended Press–Schechter theory.

We find that in a significant number of cases, haloes in the *N*-body merger trees are less massive than their progenitors at the previous time-step. When this happens we are forced artificially to adjust the masses of the halo or its progenitors, since in our semi-analytic galaxy formation model haloes may not lose mass. However, the luminosity function, Tully–Fisher relation and global star formation history of the galaxies predicted by the semi-analytic model remain almost exactly the same whether we add mass to the halo or remove mass from the progenitors when we encounter this problem. We conclude that the changes we are forced to make to the halo masses have very little effect on the semi-analytic model.

If the mass resolution in the standard GALFORM model is degraded to that of the *N*-body simulation and the empirical fit of Benson et al. (2001a) is used to correct the distribution of halo progenitor masses, we obtain luminosity functions and Tully–Fisher relations in very good agreement with the *N*-body GALFORM model. This shows that, apart from the issue of mass resolution, the only significant statistical differences between the *N*-body merger trees and those of Cole et al. are caused by the known discrepancy between EPS theory and the results of *N*-body simulations.

By improving the mass resolution in the standard GALFORM model to that used by Cole et al. we were able to obtain an indication of the effects of limited mass resolution on the *N*-body model. The mass resolution in the *N*-body merger trees is imposed by the particle mass in the GIF simulation, since haloes with fewer than 10 particles ($1.4 \times 10^{11} h^{-1} M_{\odot}$) are not resolved. This limitation has a noticeable effect on the galaxy luminosity function and we find slightly more very bright galaxies, since gas may only cool in resolved haloes. If only massive haloes are resolved, cooling is delayed, resulting in brighter galaxies at $z = 0$. However, the most

obvious effect of poor mass resolution is a drastic reduction in the number of galaxies with b_j magnitudes fainter than approximately -17 . This demonstrates that the mass resolution of the GIF simulation is insufficient to make reliable predictions at these magnitudes. At brighter magnitudes the luminosity functions remain in good agreement.

In conclusion, when used as the starting point for semi-analytic modelling of galaxy formation, merger trees taken from an *N*-body simulation using the technique described in this paper result in similar galaxy populations to those obtained using the (slightly modified) Monte Carlo algorithm of Cole et al. This supports the reliability of our method and provides a means to populate large cosmological *N*-body simulations with semi-analytic galaxies at a fraction of the computational cost of a hydrodynamic simulation of the same volume. When applied to the dark matter component of a smooth particle hydrodynamics (SPH) simulation, our model will also allow us to compare SPH and semi-analytic treatments of galaxy formation, and, in particular, the cooling of gas within haloes, on a halo-by-halo basis. This comparison is reported in a companion paper (Helly et al. 2003).

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