Durham extremely large telescope adaptive optics simulation platform

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Adaptive optics systems are essential on all large telescopes for which image quality is important. These are complex systems with many design parameters requiring optimization before good performance can be achieved. The simulation of adaptive optics systems is therefore necessary to categorize the expected performance. We describe an adaptive optics simulation platform, developed at Durham University, which can be used to simulate adaptive optics systems on the largest proposed future extremely large telescopes as well as on current systems. This platform is modular, object oriented, and has the benefit of hardware application acceleration that can be used to improve the simulation performance, essential for ensuring that the run time of a given simulation is acceptable. The simulation platform described here can be highly parallelized using parallelization techniques suited for adaptive optics simulation, while still offering the user complete control while the simulation is running. The results from the simulation of a ground layer adaptive optics system are provided as an example to demonstrate the flexibility of this simulation platform. © 2007 Optical Society of America

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1. Introduction

Adaptive optics (AO) is a technology widely used in optical and infrared astronomy, and almost all large science telescopes have an AO system. A large number of results have been obtained using AO systems, which would otherwise be impossible for seeing-limited observations. New AO techniques are being studied for novel applications such as wide-field high-resolution imaging and extra-solar planet finding.

The simulation of an AO system is important as it helps to determine how well the AO system will perform. Such simulations are often necessary to determine whether a given AO system will meet its design requirements, thus allowing scientific goals to be met. Additionally, new concepts can be modeled, and the simulated performance of different AO techniques compared, allowing informed decisions to be made when designing or upgrading an AO system and when optimizing the system design parameters.

A full end-to-end AO simulation will typically involve several stages. First, a representation of the atmospheric turbulence is produced, typically by generating simulated atmospheric phase screens, often by using several different screens representing turbulence at different atmospheric heights. The aberrated complex wave amplitude at the telescope aperture is then generated by modeling this atmospheric phase as seen from the telescope pupil. For a stratified atmospheric model this will involve propagating the atmospheric phase screens across the pupil to simulate the effect of the relative velocity of different atmospheric layers. The wavefront at the pupil is then passed to the simulated AO system, which will typically include one or more wavefront sensors and deformable mirrors and a feedback algorithm for closed-loop operation. Additionally, one or more science point-spread functions (PSFs) as corrected by the AO system are calculated. Information about the AO system performance is computed from the PSFs, including quantities such as the Strehl ratio and encircled energy.

The computational requirements for AO simulation scale rapidly with telescope size, and thus simulation of the largest telescopes cannot be done without special techniques, some of which follow:

1. Multiprocessor parallelization allows computations to be spread across multiple processors, though it can suffer from data bandwidth bottlenecks, as often data cannot be transferred between processors at a
rate sufficient to keep them processing for a large proportion of the time.

2. The use of dedicated hardware for algorithm acceleration\(^9\) can produce large performance improvements, though it is somewhat inflexible.

3. Analytical models can also be used,\(^10\) and these can give rapid results, though they are not able to represent noise sources easily.

Here we describe the approaches that we have taken to implement an efficient and scalable simulation framework.

At Durham University we have been developing AO simulation codes for over 10 years.\(^11\) The code has recently been rewritten to take advantage of new hardware, new software techniques, and to allow much greater scalability for advanced simulation of AO systems for extremely large telescopes (ELTs), including multiconjugate AO (MCAO) and extreme AO (XAO) systems.\(^12\)

The Durham AO simulation platform uses the high-level programming language Python (currently, Python 2.4), to select and link together C (American National Standards Institute standard with the Gnu Compiler Collection (GCC) version 3.3), Python, and hardware accelerated algorithms, as well as third-party modules, giving a great deal of flexibility. This allows us to rapidly prototype and develop new and existing AO algorithms, and to prepare new AO system simulations quickly by using the Python code. The use of C and hardware algorithms ensures that processor intensive parts of the simulation platform can be implemented efficiently. The C and Python algorithms make use of optimized libraries including the FFTW (versions 2 and 3), the AMD core math library (version 3.5, for use on AMD platforms, including BLAS and LAPACK routines), the GNU scientific library (currently version 0.7), and the MPICH library (optimized for the Cray XD1). This ensures that high performance can be achieved for computationally intensive algorithms. The hardware accelerated algorithms are implemented within field programmable gate arrays (FPGAs), which can be programmed to provide impressive performance improvements over a standard software implementation. The VHDL hardware description language is used to program the FPGAs, using the Xilinx ISE 7.1 compiler.

The simulation software will run on most Unix-like operating systems, including Linux and Mac OS X. The simulation platform hardware at Durham consists of a Cray XD1 supercomputer,\(^13\) which contains reprogrammable hardware for application acceleration as well as six dual Opteron processor nodes each with 8 Gbits RAM. Additionally, a distributed cluster of conventional Unix workstations is connected by gigabit ethernet. For most simulation tasks, only the XD1 is required, though for large models, or when multiple simulations are run simultaneously, the entire distributed cluster can be used. The simulation is programmed intelligently to make use of optimized libraries and hardware acceleration when these are available, and to use default library replacements when not (for example, the AMD core math library is not available on a Mac OS X platform).

The simulation is object orientated, with high-level objects (for example, a phase screen generation object and a wavefront sensing object) being connected together, allowing data to pass between them in a direction described by the user (for example, atmospheric phase screens may be passed to a deformable mirror object). The high-level simulation objects can contain instances of lower-level objects, which are internal to the simulation objects and used during calculations, for example, a telescope pupil mask object used to define which parts of the atmospheric phase screens are sampled by the wavefront sensor.

2. Extremely Large Telescope Simulation Requirements

When attempting to create a realistic simulation of an AO system on an ELT, a large amount of computing power, memory, and bandwidth will be required. The Durham simulation platform provides these requirements by implementing several key technologies.

A. Multiple Processor Simulation Platform

The Durham simulation platform allows a simulation to comprise multiple processes, meaning that different parts of the simulation can run on different processors and even different computers. However, this means that communication between the processes is essential. To maximize the efficiency of the simulation, we use a combination of shared memory access (where processes have access to the same memory, e.g., within a symmetric multiprocessor (SMP) system) and message passing interface (MPI) communications where appropriate, and a simulation user has control over the type of communication used.

1. Shared Memory Access

Shared memory access allows multiple processes to access the same region of computer memory. All processes can usually have read and write access to this memory. Using shared memory allows a single memory block to be shared between processes, thus reducing the overall memory requirements, and also reducing the processor overhead, since producing an identical copy of the data for each different process is not then essential. Figure 1 is a schematic showing how a typical shared memory system can operate. Shared memory buffers are created by using the Unix shm_open() function call and are mapped into a processor’s virtual address space. Standard synchronization primitives such as semaphores are used to ensure that no processes are reading the shared memory region while it is being written to and to ensure that only one process at a time can write to the shared memory region.

The Durham simulation platform hides the use of synchronization primitives (in this case semaphores) from the user (and simulation objects), such that the parallel processes will read and write to the shared memory region only when it is appropriate to do so.
Fig. 1. Schematic showing how a typical shared memory system operates. Some processes will have read and write access to the memory, while others will have read access only. Synchronization primitives will be used to ensure that data are not read while being written and vice versa.

This removes the possibility of data corruption, while providing a simplified interface for the simulation programmer.

2. Message Passing Interface Communication
Communication between distributed systems that do not share memory requires copies of data sets to be passed between the systems. When the data set is large, or when a large number of small data sets are passed, a bottleneck can occur as processes will then spend a significant amount of time waiting for a data set to arrive or be sent. It is therefore essential that the communication method used to transfer these data sets be as efficient as possible, having both a low latency (so that time is not wasted when sending small data sets) and a high sustained bandwidth (so that large data sets can be sent in a minimum time).

The Durham simulation platform uses the MPI library for this communication as this allows data to be passed efficiently with only a small latency, particularly on the XD1 system. The Cray XD1 has an optimized version of the MPI library, which is targeted to the hardware architecture of this system, making efficient use of the RapidArray Transport interface, the commercial high-bandwidth interconnect found in XD1 systems. Using the Durham system, we measured a MPI communication latency of only 1.6 μs and a maximum sustained bandwidth of 1.4 Gbytes s⁻¹ between the computing nodes.

3. Process Parallelization
Each processor used for a given simulation will be given only one process to run to reduce context switching delays. Each of these processes will contain one or more simulation objects, which are able to access the virtual memory space of other objects within the process, making data transfer between these objects trivial (e.g., the address of a data array can be passed). All simulation objects are executed in a single thread, carrying out their computations for each iteration in turn, which again reduces context switching delays.

Objects in separate processes are able to pass data by using either MPI communications or shared memory as appropriate. When such communication is required, a pair of high-level communication objects are created and are responsible for dealing with a particular communication link (MPI or shared memory). These communication objects are then connected to the simulation objects, which can then behave as if they were connected directly to the object with which they wish to communicate. Each simulation object has a basic set of methods and data objects, which are viewable by other objects. The communication objects then merely have to implement these methods and data objects, transferring data as appropriate. The use of communication objects is transparent to the simulation objects, being handled by the simulation framework.

B. Hardware Acceleration
The Durham AO simulation platform is able to accelerate specific parts of the AO simulation by using reconfigurable logic hardware, FPGAs, and hence reducing the time taken for a given simulation to complete. These FPGAs are an integrated part of the Cray XD1 supercomputer, and, when used correctly, are capable of reducing the execution time of some algorithms by 2 to 3 orders of magnitude while at the same time, freeing the CPU for other operations. This greatly improves the speed at which the simulation can run and is essential for simulation of large AO systems. Implementing algorithms within the FPGAs requires knowledge of a hardware programming language, and so we have developed common libraries that can be plugged into an existing simulation, for example, a wavefront sensor pipeline. The simulation user therefore requires no hardware knowledge, and yet can achieve significant impressive performance improvements using the hardware acceleration.

C. Simulation Creation
A user creates a new simulation by selecting and linking together the various simulation modules as required, either graphically or in a text file. New modules (for example, to investigate a new type of wavefront sensor or deformable mirror) can easily be created and added to the simulation with minimal effort. Once the simulation file has been set up, a parameter file is created, which contains all variables and configuration objects required by the simulation. This parameter file is in XML format and allows an embedded Python code, which can be used to create complicated variables and objects. If suitably defined, a cross-simulation parameter file could be created by using a Python parser for the XML. The parameter file can be created by using a graphic interface, which has the capability to automatically create a skeleton parameter file from the simulation file, and then allow the user to adjust the default values of variables. This allows a new simulation to be set up quickly by an inexperienced user.

D. Simulation Control
Control of a running simulation is achieved by connecting to it by using either the Python command line or graphic tools. This gives the users complete control over a simulation, allowing them to stop, start,
and pause, as well as analyze (allowing them to create plots of parts of the data chain, for example, sub-aperture images) and change the current state of a simulation (for example, changing the value of a variable or the contents of an array). This high degree of flexibility is achieved by allowing the users to send text strings to the simulation, which are treated as Python code, and executed as a separate thread that has access to the global name space. The user can therefore access and alter any part of the simulation, and any requested data can be returned to the user for further analysis. When a simulation comprises more than one process, the user can connect to any or all of these processes.

This control facility is completely detachable from the simulation and can be started and stopped without affecting simulation operation. It is also possible to have several users connected to the same simulation at any given time from anywhere that has internet access to the computers running the simulation. Figure 2 shows a screen shot of the simulation control user interface and demonstrates the powerful functionality that this provides through a simple interface, satisfying both novice and experienced users.

This simulation control capability is unique as it enables a user to implement new capability within a running simulation and to query all objects and variables, even if it was not envisaged that these should be queried before the simulation was created. This high degree of flexibility is essential for ELT AO system simulation as simulation run times can typically be measured in days.

E. Parallelization Approaches

When parallelizing any software, there is usually a trade-off between the amount of processing done and the amount of data that has to be passed between processors. A bottleneck may occur if the CPUs spend a significant amount of time waiting for data, meaning that the parallelization has not been efficient.

It is usually most efficient to create parallelized software that sends as little data as possible between processes so that most time can be spent processing data. At Durham, we typically parallelize our AO system simulations by dividing parallel optical paths into separate processes, as shown in Fig. 3. Each optical path is virtually independent of the others, except that they all require inputs of atmospheric phase screen data and knowledge of any time-varying deformable mirror surface shapes, and may (if part of the wavefront correction path) return new deformable mirror commands, or wavefront sensed values to be passed to other optical paths. By dividing the processes in this way, a minimum amount of time is spent waiting for data, allowing the most efficient use of the CPUs to be made. This will also allow a typical simulation (with several on- and off-axis science targets, and one or more guide stars) to be parallelized into a similar number of processes as there are processors, allowing a single process to run on each processor.

When all the parallel optical paths depend on one algorithm, which generates data for the paths, for example, atmospheric turbulence generation or reconstruction of the deformable mirror commands from the wavefront sensor data, this algorithm can also be parallelized by using a traditional parallelization approach, by splitting the computation over available processors, and passing the data as required. Some optimized libraries, for example, the fastest Fourier transform in the west (FFTW) Fourier transform library, use this technique. However, this parallelization approach is beneficial only for algorithms where the time spent transferring data is small compared with the time spent processing the data.

1. Simulation Scalability

To demonstrate the scalability of the AO simulation, we have simulated a system with three wavefront sensors $32 \times 32$ subapertures each), one science tar-
get, and we assume that atmospheric turbulence is concentrated in two layers. Table 1 provides details of the different simulation objects required for this simulation and gives typical computation times for this example. It should be noted that the computation times do not scale identically with simulation size, and so the ratio of computation times between different algorithms is not constant for larger or smaller simulations.

We demonstrate the strong scalability of the AO simulation platform by keeping the simulation a fixed size, but increasing the number of processors that are used. Table 2 shows the simulations parallelized by placing different simulation objects on different processing nodes. For the small simulation used for this demonstration, this type of parallelization can be suboptimal, because the processing load can be poorly balanced between processors. For example, when placed on two processors, one of these will have two wavefront sensor objects, requiring approximately double the processing time of the other processor (with only one wavefront sensor object).

By parallelizing some of the simulation objects (in this case the wavefront sensing objects), the computational load can be spread more evenly across the processors, thus giving a better performance scaling with computer system size. Table 3 shows the simulations parallelized by using parallelized wavefront sensing objects, allowing a better fit to a greater number of processors to be realized as the processing load can be distributed more evenly. The timing results for these simulations are shown in Fig. 4. This figure shows that the simulation can scale well when it is well suited to the number of processors; for example, using three processors gives a simulation rate three times greater than one processor. However, when the simulation is not well suited to the number of processors (for example, two, four, five, and six processors in the case when the individual simulation objects are unparallelized), the performance is suboptimal. If individual objects are parallelized, the simulation can be better fitted to the number of available processors, as the dotted curve in Fig. 4 shows. However, currently, not all simulation objects can be parallelized.

F. Extremely Large Telescope Simulation Suitability
The Durham AO simulation platform is suited for the simulation of ELT scale AO systems. The XD1 supercomputer has 8 Gbyte memory per computing node, allowing large phase screens, large numbers of wavefront sensing elements (for example, Shack–Hartmann subapertures), and other data to be stored. The tight integration of the FPGAs with memory and CPUs means that parts of the simulation can be accelerated by several orders of magnitude, and the high bandwidth and low latency connections between nodes allows data to be passed rapidly between parallelized processes. This simulation platform provides the capability for rapid simulation of AO systems on all current telescopes and next generation ELTs.

1. Extremely Large Telescope Simulation Details
A simulation of a classical AO system on an ELT has been created to demonstrate the use of the AO sim-

<table>
<thead>
<tr>
<th>Simulation Object</th>
<th>Significant Algorithms</th>
<th>Computation Time</th>
<th>s</th>
</tr>
</thead>
<tbody>
<tr>
<td>Infinite phase screen generation</td>
<td>Matrix operations</td>
<td>$10^{-4}$</td>
<td></td>
</tr>
<tr>
<td>Atmospheric pupil phase simulation</td>
<td>Matrix operations</td>
<td>$7 \times 10^{-4}$</td>
<td></td>
</tr>
<tr>
<td>Deformable mirror simulation</td>
<td>Matrix operations</td>
<td>0.03</td>
<td></td>
</tr>
<tr>
<td>Shack–Hartmann sensor, slope computation</td>
<td>FFT, matrix operations</td>
<td>0.18</td>
<td></td>
</tr>
<tr>
<td>Wavefront reconstruction (SOR)</td>
<td>Matrix operations</td>
<td>0.02</td>
<td></td>
</tr>
<tr>
<td>Science image generation</td>
<td>FFT, matrix operations</td>
<td>0.02</td>
<td></td>
</tr>
</tbody>
</table>

Table 2. How Simulation Objects can be Placed on Different Computing Nodes to Parallelize a Simulation*

<table>
<thead>
<tr>
<th>One CPU Configuration</th>
<th>Two CPUs</th>
<th>Three CPUs</th>
<th>Four CPUs</th>
</tr>
</thead>
<tbody>
<tr>
<td>CPU1</td>
<td>CPU1</td>
<td>CPU2</td>
<td>CPU3</td>
</tr>
<tr>
<td>1. Phase screen (2 km)</td>
<td>1</td>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>2. Phase screen (0 km)</td>
<td>2</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>3. Telescope pupil phase (direction 1)</td>
<td>3</td>
<td>7</td>
<td>6</td>
</tr>
<tr>
<td>4. Telescope pupil phase (direction 2)</td>
<td>6</td>
<td>8</td>
<td>9</td>
</tr>
<tr>
<td>5. Telescope pupil phase (direction 3)</td>
<td>9</td>
<td>10</td>
<td>13</td>
</tr>
<tr>
<td>6. Deformable mirror (direction 1)</td>
<td>13</td>
<td>11</td>
<td></td>
</tr>
<tr>
<td>7. Deformable mirror (direction 2)</td>
<td>12</td>
<td></td>
<td></td>
</tr>
<tr>
<td>8. Deformable mirror (direction 3)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>9. Wavefront sensor (direction 1)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>10. Wavefront sensor (direction 2)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>11. Wavefront sensor (direction 3)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>12. Wavefront reconstructor</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>13. Science calculation (science image)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

*The first column gives a brief description of each object, whose numbers are then referred to in the other columns.
ulation platform. The key parameters of this simulation are detailed in Table 4. This simulation uses an infinite phase screen generator with von Karman statistics. A successive overrelaxation (SOR) wavefront reconstructor is used, which means that it is not necessary to create and invert an interaction matrix of the system. In a system of this size, a full interaction matrix could easily take more memory than available on our Cray XD1 system, also taking a prohibitive length of time (days or weeks) to invert to obtain the control matrix, and so conventional wavefront reconstruction is not an option. We are currently implementing sparse matrix algorithms and Fourier domain wavefront reconstruction algorithms that will greatly reduce the memory and computation requirements. An FPGA hardware accelerator is used for computation of the Shack–Hartmann images and the spot centroid location algorithm. The high number of pixels per subaperture allows elongated Shack–Hartmann spots (e.g., from a laser guide star) to be analyzed. The simulation includes one wavefront sensor and one science target. A more useful simulation may include several wavefront sensors and several science targets, though these are not presented here.

This simulation has been parallelized over five nodes of the Cray XD1, one node for each atmospheric layer, one node for the science target, and one node to combine the atmospheric layers to give the atmospheric phase at the telescope pupil, perform the simulation of the wavefront sensor, and reconstruct the wavefront allowing the deformable mirror surface to be reshaped. Table 5 shows the relative time spent computing each of these algorithms, and it can be seen that by far the most computationally intensive is the simulation of the science target (involving a $8192 \times 8192$ fast Fourier transform for each simulation time step). These timings are pessimistic (worse case), as they include computation of all scientific parameters, including the Strehl ratio and enclosed energy, which would typically only be performed

### Table 3. How the Parallelization of Simulation Objects can be used to Fit a Simulation to a Given Number of CPUs

<table>
<thead>
<tr>
<th>One CPU</th>
<th>Two CPUs</th>
<th>Three CPUs</th>
<th>Four CPUs</th>
<th>Six CPUs</th>
</tr>
</thead>
<tbody>
<tr>
<td>CPU1</td>
<td>CPU1</td>
<td>CPU2</td>
<td>CPU1</td>
<td>CPU1</td>
</tr>
<tr>
<td>1</td>
<td>2</td>
<td>1</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>4</td>
<td>5</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>5</td>
<td>6</td>
<td>7</td>
<td>8</td>
<td>10 a</td>
</tr>
<tr>
<td>7</td>
<td>8</td>
<td>3</td>
<td>10 c</td>
<td>9 a</td>
</tr>
<tr>
<td>9 a</td>
<td>9 b</td>
<td>6</td>
<td>10 d</td>
<td>9 b</td>
</tr>
<tr>
<td>9 c</td>
<td>9 d</td>
<td>9 a</td>
<td>11 a</td>
<td>9 c</td>
</tr>
<tr>
<td>10 a</td>
<td>10 b</td>
<td>9 b</td>
<td>11 b</td>
<td>9 c</td>
</tr>
<tr>
<td>10 c</td>
<td>10 d</td>
<td>9 c</td>
<td>11 c</td>
<td>13</td>
</tr>
<tr>
<td>11 a</td>
<td>11 b</td>
<td>9 d</td>
<td>11 d</td>
<td>9 c</td>
</tr>
<tr>
<td>11 c</td>
<td>11 d</td>
<td>10 a</td>
<td>12</td>
<td>9 c</td>
</tr>
<tr>
<td>12</td>
<td>13</td>
<td>10 b</td>
<td>13</td>
<td>13</td>
</tr>
</tbody>
</table>

The simulation objects are denoted here by a, b, c, and d suffixes for a four-way parallelization of the wavefront sensing algorithm. The numbers represent the simulation objects described in Table 2.

### Table 4. ELT Simulation Model Details

<table>
<thead>
<tr>
<th>Simulation Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Telescope primary</td>
<td>42 m</td>
</tr>
<tr>
<td>Atmospheric layers</td>
<td>3 (0, 2, 10 km)</td>
</tr>
<tr>
<td>Wavefront sensors</td>
<td>1</td>
</tr>
<tr>
<td>Number of subapertures</td>
<td>$256 \times 256$ (16 cm per subaperture)</td>
</tr>
<tr>
<td>CCD pixels per subaperture</td>
<td>$16 \times 16$</td>
</tr>
<tr>
<td>Deformable mirrors</td>
<td>1</td>
</tr>
<tr>
<td>Number of deformable mirror actuators</td>
<td>$256 \times 256$</td>
</tr>
<tr>
<td>Atmospheric resolution</td>
<td>1 cm of sky per phase pixel</td>
</tr>
<tr>
<td>Phase pixels for science image creation</td>
<td>$4096 \times 4096$</td>
</tr>
<tr>
<td>Guide stars</td>
<td>1 (natural guide star)</td>
</tr>
</tbody>
</table>

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Fig. 4. Number of simulation time steps computed per unit time (simulation rate) when the simulation is parallelized over different numbers of processors. The solid curve shows the case when individual objects are not parallelized, while the dotted curve shows the case when the Shack–Hartmann image creation and wavefront sensing algorithm are parallelized, providing a better fit to larger numbers of processors. The simulation rate has been normalized to unity by the rate for an unparallelized simulation (with unparallelized simulation objects).
every 100 or so time steps. Without these calculations, the science object takes less than 50 s to compute and store the instantaneous PSF for this ELT simulation. It should be noted that these timings do not scale in the same way as a function of system size; for example, when simulating a smaller telescope, the computation of the science image takes a significantly smaller fraction of processor time.

For the majority of the time, the other processors are idle, waiting for the science image algorithm to complete. Work is currently under way to place the bulk of this algorithm into hardware, which will result in a significant performance improvement (a factor of 10 times is expected). The computation time of the science target simulation currently scales as \(O(n^2 \log n)\), attributable to the large 2D fast Fourier transform, where \(n\) is the linear size of the phase screen (measured in pixels). This algorithm also uses the most memory as it has to store a zero-padded pupil phase (so that the Fourier transform is sampled at the Nyquist frequency) and both an instantaneous and integrated PSF. The memory requirements for this algorithm scale as \(O(n^3)\) where \(n\) is the linear size of a phase screen, and over 5 Gbyte memory were required for this algorithm in the example here. With the current hardware, it would be possible to create a simulation with one more science object (on the currently spare processing node), and approximately six more wavefront sensing objects, to create (for example) a MCAO simulation, without increasing the simulation iteration time. This has not been implemented at the present time, as the MCAO wavefront reconstructor is not yet complete.

The planet finder instrument for the European Southern Observatory ELT project is currently specified to have 200 \(\times\) 200 subapertures, and this is one of the most demanding proposals. The simulation demonstrated here is therefore of higher order (has a larger number of subapertures) than all present and planned astronomical AO systems.

3. **Simulation Results for Ground Layer Adaptive Optics**

A classical or single guide star AO system can produce only a small corrected field of view, and isoplanatic errors cause the image quality to quickly degrade from the center of this field. When natural guide stars are used, the sky coverage for these AO systems is severely limited, since it is difficult to find stars that are bright enough within each isoplanatic patch of sky. Ground layer AO (GLAO) was proposed as a solution to this problem, by applying a limited AO correction for a large field of view under any atmospheric conditions at optical and infrared wavelengths. A GLAO system is not designed to produce diffraction-limited images, but improves the concentration of the PSF by correcting only the lowest turbulent atmospheric layers. Correction is then virtually identical over the entire field of view since these layers are closer to the ground, while the uncorrected higher layers degrade the spatial resolution isoplanatically.

At Durham, we have implemented a GLAO simulation model by using the AO simulation framework for corrected fields up to 15 arc min in size based on high-resolution turbulence profiles taken at the Gemini observatory, and some of the results are presented here to demonstrate an actual use of the simulation. The Durham simulation model includes detailed wavefront sensor (WFS) noise propagation and produces 2D PSFs and is used to quantify the effects of such noise on the PSF parameters across the GLAO field for various seeing and noise conditions. The capabilities of this model are summarized as follows:

1. The atmosphere can be modeled as any number of independently moving turbulent layers.
2. Multiple laser beacons and guide stars can be modeled.
3. Multiple deformable mirrors of different types can be modeled.
4. Multiple wavefront sensors can be included, encompassing all main detector noise effects, pixelation, and atmospherically induced speckle.
5. The science PSF can be sampled at any number of field points simultaneously.

It is a wholly independent code (not derived from any other simulation platform), but can be used subject to detailed cross-checks with other AO models. This checking has been carried out as part of work for the Gemini telescope consortium. The simulation can also be used for situations where the atmosphere cannot be treated as stratified in layers, but as a 3D entity simply by implementing such a model. However, this is not considered here.

### A. Durham Implementation

A design for the GLAO system is shown in Fig. 5, and this indicates that there are multiple guide stars and multiple science sampling points where the AO system performance is categorized.

We have simulated a system with five laser guide stars, and four discrete atmospheric turbulence layers as shown in Table 6, assuming an 8 m telescope primary mirror. The simulation takes samples of the science field at a wavelength of 1250 nm at ten positions,
on and off axis, as well as the uncorrected image, and uses these samples to categorize the performance of the AO system, with parameters such as the Strehl ratio and encircled energy being computed for each science target location. The simulation uses a Shack–Hartmann wavefront sensor with 10×10 subapertures, and assumes a generic deformable mirror to which combinations of Zernike modes are applied to give the correct mirror shape at each time step (the first 54 Zernike modes were corrected). A typical layout of the science stars and guide stars is shown in Fig. 6, as viewed from the telescope. The guide star angle from the on-axis direction can be varied between 200 and 750 arc sec, and this can be used to investigate the degree of AO correction and the area over which this correction is achieved. The integrated seeing in these models was taken as 0.6 arc sec with a Fried parameter of 0.17. An exposure time of 100 s was used with a WFS integration time of 2 ms. The laser guide stars were assumed to be of 13th magnitude brightness.

B. Parallelization Approaches

There are many ways in which a large simulation such as that presented here can be parallelized. The optimal parallelization approach will reduce the bottlenecks in data transferred between processes and minimize the amount of time in which processors are not actively processing, while, fully utilizing as many processors as possible. As mentioned in Subsection 2.E, when simulating an AO system it is possible to separate the parallel optical paths from different guide stars and science targets onto different processors, reducing the data transfer between processes. This is the approach used here and presented as a flow chart in Fig. 7.

C. Ground Layer Adaptive Optics Simulation Results

When a number of guide stars are evenly spaced about a circle (as viewed from the telescope), there will be some atmospheric correction for starlight passing within this circle, but the degree of correction will fall for starlight outside the circle. If the guide star separation is reduced, better correction will be achieved over a smaller area. Conversely, if the separation is increased, a poorer correction will be achieved over a larger area.

A GLAO system does not aim to achieve a high degree of correction. Rather, a partial degree of correction is achieved over a wide field of view, and the GLAO system is usually designed to be complementary to more conventional AO systems or to be used with integral field spectroscopy units. The correction

<table>
<thead>
<tr>
<th>Table 6. Atmospheric Model Details</th>
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<tbody>
<tr>
<td>Layer height/m</td>
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<tr>
<td>Wind speed/m s⁻¹</td>
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<td>Relative layer strengths</td>
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Fig. 5. Design of a GLAO system.

Fig. 6. Schematic of the relative positions of the laser guide stars and science sampling points used for the GLAO simulation. The science sampling points (larger stars) are spaced uniformly 150 arc sec apart, while the laser guide stars (smaller stars) are positioned equally around a circle with a diameter that can be varied between 200 and 750 arc sec.

Fig. 7. Flow chart showing how the GLAO simulation is carried out using the Durham AO simulation platform. The algorithms in different boxes are implemented on different processors, and arrows show the direction of data flow between the algorithms. Typically, there will be between five and ten science paths (to determine how the AO performance changes at different angles from the vertical axis), and between five and ten AO paths, depending on the number of laser guide stars being used.
achieved from a GLAO system alone typically produces Strehl ratios of only a few percent.

The results of an investigation into the effect of guide star separation are presented here, and Fig. 8 shows that by moving the guide stars out from the on-axis direction, the isoplanatic correction covers a larger area with a smaller degree of correction, hence giving a lower Strehl ratio. This decreases for fields farther from the on-axis direction, but the rate of change is dependent on the guide star separation. The uncorrected Strehl ratio was approximately 0.75%.

The FWHM as a function of angle from the on-axis direction also displays the expected behavior, increasing as the viewing angle is moved away from the axis. When the guide star separation is small, the FWHM is small close to the axis, increasing rapidly away from it, and when guide star separation is large, the FWHM is initially larger, but increases slowly away from the on-axis direction, as shown in Fig. 9. The uncorrected FWHM was 0.35 arc sec.

The GLAO simulation presented here has been compared with other independent AO simulation codes and has been found to be in agreement within the statistical uncertainties.

4. Conclusion

We have developed a new AO simulation capability at Durham for astronomical applications, and this platform is capable of extremely large telescope AO system simulation. This simulation platform is capable of using algorithms implemented within reconfigurable logic to provide hardware acceleration for the most computationally intensive tasks.

A simulation platform includes tools for creating and controlling the simulations, and optimal parallelization techniques specific to AO simulations have been discussed. The flexibility of the simulation platform as well as the ability to query and alter the state of a running simulation make it unique. Additionally, techniques used to parallelize a given simulation reducing the computation time have been described, and these parallelization strategies are specifically aimed at AO system simulation. The simulation platform has been tested against other independent codes and was found to be in agreement with those.

We have demonstrated a use of the AO simulation platform for GLAO simulation and presented some of the results obtained. These results show that the separation of guide stars affects the achievable AO correction and the area over which this correction can be achieved.

References


16. R. M. Myers (r.m.myers@durham.ac.uk), Department of Physics, South Road, Durham DH1 3LE, UK (personal communication, 2006).
