

# **The LABOCA survey of the Extended** *Chandra Deep Field***-South: clustering of submillimetre galaxies**

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## **ABSTRACT**

We present a measurement of the spatial clustering of submillimetre galaxies (SMGs) at  $z = 1-3$ . Using data from the 870  $\mu$ m Large APEX Bolometer Camera (LABOCA) submillimetre survey of the Extended*Chandra Deep Field*-South, we employ a novel technique to measure the cross-correlation between SMGs and galaxies, accounting for the full probability distributions for photometric redshifts of the galaxies. From the observed projected two-point crosscorrelation function we derive the linear bias and characteristic dark matter halo masses for the SMGs. We detect clustering in the cross-correlation between SMGs and galaxies at the  $>4\sigma$ level. Accounting for the clustering of galaxies from their autocorrelation function, we estimate an autocorrelation length for SMGs of  $r_0 = 7.7^{+1.8}_{-2.3} h^{-1}$  Mpc assuming a power-law slope  $\gamma = 1.8$ , and derive a corresponding dark matter halo mass of log( $M_{halo}[h^{-1}M_{\odot}]) = 12.8^{+0.3}_{-0.5}$ Based on the evolution of dark matter haloes derived from simulations, we show that that the *z* = 0 descendants of SMGs are typically massive (∼2–3*L*∗) elliptical galaxies residing in moderate- to high-mass groups  $(\log(M_{\text{halo}}[h^{-1} M_{\odot}]) = 13.3^{+0.3}_{-0.5})$ . From the observed clustering we estimate an SMG lifetime of ∼100 Myr, consistent with lifetimes derived from gas consumption times and star formation time-scales, although with considerable uncertainties. The clustering of SMGs at *z* ∼ 2 is consistent with measurements for optically selected quasistellar objects (QSOs), supporting evolutionary scenarios in which powerful starbursts and QSOs occur in the same systems. Given that SMGs reside in haloes of characteristic mass  $\sim$ 6 × 10<sup>12</sup> *h*<sup>−1</sup> M<sub>O</sub>, we demonstrate that the redshift distribution of SMGs can be described remarkably well by the combination of two effects: the cosmological growth of structure and the evolution of the molecular gas fraction in galaxies. We conclude that the powerful starbursts in SMGs likely represent a short-lived but universal phase in massive galaxy evolution, associated with the transition between cold gas-rich, star-forming galaxies and passively evolving systems.

**Key words:** galaxies: evolution – galaxies: high-redshift – galaxies: starburst – large-scale structure of Universe – submillimetre: galaxies.

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# **1 INTRODUCTION**

Submillimetre galaxies (SMGs) are a population of high-redshift ultraluminous infrared galaxies (ULIRGs) selected through their redshifted far-infrared emission in the submillimetre waveband (e.g. Smail, Ivison & Blain 1997; Barger et al. 1998; Hughes et al. 1998; Blain et al. 2002). The redshift distribution of this population appears to peak at *z* ∼ 2.5 (e.g. Chapman et al. 2003, 2005; Wardlow et al. 2011), so that SMGs are at their commonest around the same epoch as the peak in powerful active galactic nuclei (AGN) and specifically quasi-stellar objects (QSOs; e.g. Richards et al. 2006; Assef et al. 2011). This correspondence may indicate an evolutionary link between SMGs and QSOs, similar to that suggested at low redshift between ULIRGs and QSOs by Sanders et al. (1988). However there is little direct overlap (∼a few per cent) between the high-redshift SMG and QSO populations (e.g. Page et al. 2004; Chapman et al. 2005; Stevens et al. 2005; Alexander et al. 2008; Wardlow et al. 2011). The immense far-infrared luminosities of SMGs are widely believed to arise from intense, but highly obscured, gas-rich starbursts (e.g. Alexander et al. 2005; Greve et al. 2005; Tacconi et al. 2006, 2008; Pope et al. 2008; Ivison et al. 2011), suggesting that they may represent the formation phase of the most massive local galaxies: giant ellipticals (e.g. Eales et al. 1999; Swinbank et al. 2006).

SMGs and QSOs may thus represent phases in an evolutionary sequence that eventually results in the population of local massive elliptical galaxies. This is a compelling picture, but testing the evolutionary links is challenging due to the lack of an easily measured and conserved observable to tie the various populations together. For example, the stellar masses of both QSOs and SMGs are difficult to measure reliably due to either the brightness of the nuclear emission in the QSOs (e.g. Croom et al. 2004; Kotilainen et al. 2009) or strong dust obscuration and potentially complex star formation histories for the SMGs (e.g. Hainline et al. 2011; Wardlow et al. 2011; but see also Dunlop 2011; Michałowski et al. 2011), while the details of the high-redshift star formation that produced local massive elliptical galaxies are likewise poorly constrained (e.g. Allanson et al. 2009). Deriving dynamical masses for QSO hosts from rest-frame optical spectroscopy is difficult due to the very broad emission lines from the AGN, while dynamical mass measurements using CO emission in gas-rich QSOs are also challenging, due to the potential nonisotropic orientation of the QSO hosts on the sky and the lack of high-resolution velocity fields necessary to solve for this (Coppin et al. 2008), as well as the general difficulties in modelling CO kinematics (e.g. Tacconi et al. 2006; Bothwell et al. 2010; Engel et al. 2010).

Another possibility is to compare source populations via the masses of their central black holes. For QSOs and the population of SMGs that contain broad-line AGN, the black hole mass can be estimated using virial techniques based on the broad emission lines (e.g. Vestergaard 2002; Peterson et al. 2004; Kollmeier et al. 2006; Vestergaard & Peterson 2006; Shen et al. 2008). Such studies generally find that SMGs have small black holes relative to the local black hole–galaxy mass relations (e.g. Alexander et al. 2008; Carrera et al. 2011), while the black holes in *z* ∼ 2 QSOs tend to lie above the local relation, with masses similar to those in local massive ellipticals (e.g. Bennert et al. 2010; Decarli et al. 2010; Merloni et al. 2010). These results suggest that SMGs represent an earlier evolutionary stage, prior to the QSO phase in which the black hole reaches its final mass. However, high-redshift virial black hole mass estimates are highly uncertain (e.g. Marconi et al. 2008; Fine et al. 2010; Netzer & Marziani 2010) and may suffer from significant selection effects (e.g. Lauer et al. 2007; Kelly et al. 2010; Shen & Kelly 2010), and so conclusions about connections between populations are necessarily limited.

The difficulties discussed above lead us to take another route to compare SMGs to high-redshift QSOs and low-redshift ellipticals: through their clustering. Spatial correlation measurements provide information about the characteristic bias and hence mass of the haloes in which galaxies reside (e.g. Kaiser 1984; Bardeen et al. 1986), and so provide a robust mass estimate that is free of many of the systematics in measuring stellar or black hole masses. The observed clustering of SMGs and QSOs can thus allow us to test whether these populations are found in similar haloes and so may evolve into each other over short time-scales. With knowledge of how haloes evolve over cosmic time (e.g. Lacey & Cole 1993; Fakhouri, Ma & Boylan-Kolchin 2010), we can also explore the links to modern elliptical galaxies (e.g. Overzier et al. 2003), as well as the higher redshift progenitors of SMGs. Clustering measurements can also provide constraints on theoretical studies that explore the nature of SMGs in a cosmological context. Recent models for SMGs as relatively long-lived  $(>0.5 \text{ Gyr})$  star formation episodes in the most massive galaxies, driven by the early collapse of the dark matter (DM) halo (Xia et al. 2011), or powered by steady accretion of intergalactic gas (Davé et al. 2010), yield strong clustering for bright sources (850  $\mu$ m fluxes  $>$ a few mJy) with correlation lengths  $r_0 \gtrsim 10 \, h^{-1}$  Mpc. In contrast, models in which SMGs are short-lived bursts in less massive galaxies, with large luminosities produced by a top-heavy initial mass function, predict significantly weaker clustering with  $r_0 \sim 6 h^{-1}$  Mpc (Almeida, Baugh & Lacey 2011).

Attempts to measure the clustering of SMGs from their projected two-dimensional distribution on the sky have for the most part been ambiguous (Scott et al. 2002; Borys et al. 2003; Webb et al. 2003; Weiß et al. 2009; Lindner et al. 2011; Williams et al. 2011). Weiß et al. (2009) used the largest, contiguous extragalactic 870-µm survey [of the Extended *Chandra Deep Field*-South (ECDFS)], to derive the clustering of  $\gtrsim$  5-mJy SMGs from their projected distribution on the sky. They estimated a correlation length of <sup>13</sup> <sup>±</sup> <sup>6</sup> *<sup>h</sup>*−<sup>1</sup> Mpc. Most recently, Williams et al. (2011) analysed an 1100-µm survey of a region of the COSMOS field and placed  $1\sigma$  upper limits on the clustering of bright SMGs (with apparent 870-μm fluxes  $\gtrsim$ 8–10 mJy) of  $\gtrsim$ 6–12 *h*<sup>-1</sup> Mpc.

Other work has attempted to improve on angular correlation measurements by including redshift information. Using the spectroscopic redshift survey of 73 SMGs with 870-µm fluxes of  $\gtrsim$ 5 mJy spread across seven fields from Chapman et al. (2005), Blain et al. (2004) estimated a clustering amplitude from the numbers of pairs of SMGs within a  $1000 \text{ km s}^{-1}$  wide velocity window. They derived an effective correlation length of 6.9  $\pm$ 2.1 *h*<sup>−1</sup> Mpc, suggesting that SMGs are strongly clustered. However their methodology was subsequently criticized by Adelberger (2005), who suggested that accounting for angular clustering of sources and the redshift selection function significantly increases the uncertainties. Using data from the *Chandra Deep Field*-North, Blake et al. (2006) computed the angular cross-correlation between SMGs and galaxies in slices of spectroscopic and photometric redshift. They obtained a significant SMG–galaxy cross-correlation signal, with hints that SMGs are more strongly clustered than the optically selected galaxies, although with only marginal ( $\sim$ 2 $\sigma$ ) significance. Previous work has therefore pointed toward SMGs being a strongly clustered population, but their precise clustering amplitude, along with their relationship to QSOs and ellipticals, remains uncertain.

To make improved measurements of the clustering of SMGs, we need either much larger survey areas (see Cooray et al. 2010 for a wide-field clustering measurement for far-IR detected sources) or the inclusion of redshift information (to allow us to reduce the effects of projection on our clustering measurements). To this end, we have re-analysed the Weiß et al. (2009) survey of ECDFS using new spectroscopic and photometric redshift constraints on the counterparts to SMGs (Wardlow et al. 2011) as well as a large catalogue of 'normal' (less-active) galaxies in the same field. We employ a new clustering analysis methodology (Myers, White & Ball 2009, hereafter M09) to calculate the projected spatial cross-correlation between SMGs and galaxies, to obtain the tightest constraint to date on the clustering amplitude of SMGs.

This paper is organized as follows. In Section 2 we introduce the SMG and galaxy samples, and in Section 3 we give an overview of the methodology used to measure correlation functions and estimate DM halo masses. In Section 4 we present the results, explore the effects of photometric redshift errors, compare with previous measurements, and discuss our results in the context of the physical drivers, lifetimes and evolutionary paths of SMGs. In Section 5 we summarize our conclusions. Throughout this paper we assume a cosmology with  $\Omega_m = 0.3$  and  $\Omega_{\Lambda} = 0.7$ . For direct comparison with other works, we assume  $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (except for comoving distances and DM halo masses, which are explicitly given in terms of  $h = H_0/(100 \text{ km s}^{-1} \text{ Mpc}^{-1})$ ). In order to easily compare to estimated halo masses in other recent works on QSO clustering (e.g. Croom et al. 2005; Myers et al. 2006; da  $\hat{A}$ ngela et al. 2008; Ross et al. 2009), we assume a normalization for the matter power spectrum of  $\sigma_8 = 0.84$ . All quoted uncertainties are  $1\sigma$  (68 per cent confidence).

# **2 SMG AND GALAXY SAMPLES**

Our SMG sample comes from the survey of the ECDFS using the Large APEX Bolometer Camera (LABOCA; Siringo et al. 2009) on the Atacama Pathfinder Experiment (APEX; Güsten et al. 2006) 12-m telescope [the LABOCA ECDFS Submillimetre Survey (LESS); Weiß et al. 2009]. LESS mapped the full  $0.35 \text{ deg}^2$ ECDFS to an 870-µm noise level of  $\sim$ 1.2 mJy beam<sup>-1</sup> and detected 126 SMGs at  $>3.7\sigma$  significance (Weiß et al. 2009, equivalent to a false-detection rate of ∼4 per cent). Radio and mid-infrared counterparts to LESS SMGs were identified by Biggs et al. (2011) using a maximum likelihood technique. Spectroscopic and photometric redshifts were obtained for a significant fraction of these counterparts by Wardlow et al. (2011) and we refer the reader to that work for more details. For this study, we restrict our analysis to the 50 SMGs that have secure counterparts at  $z = 1-3$  and do not lie close to bright stars (as discussed below). The upper limit of  $z = 3$  on the sample is included to maximize overlap in redshift space with the galaxy sample, in order to obtain a significant cross-correlation signal, while the lower bound of  $z = 1$  is included to prevent the SMG sample from being biased toward low redshifts. Of the SMGs in the sample, 22 SMGs (44 per cent) have spectroscopic redshifts (Danielson et al., in preparation) and the remainder have photometric redshifts with a typical precision of  $\sigma$ <sub>z</sub>/(1 + *z*) ~ 0.1 (Wardlow et al. 2011). The  $870$ - $\mu$ m flux distribution for the SMGs having secure counterparts (Biggs et al. 2011) is consistent with that for all LESS SMGs (Weiß et al. 2009), indicating that the requirement that SMGs have secure counterparts does not strongly bias the fluxes of our SMG sample.

For the cross-correlation analysis, we also require a comparison population in the same field. For this we adopt the ∼50 000

galaxies detected in the *Spitzer* IRAC/MUSYC Public Legacy Survey in the ECDFS (Damen et al. 2011). Fig. 1 shows the sky positions of the SMGs and galaxies (outside the regions masked for the correlation analysis, as discussed below). We use an IRAC selected sample to ensure that each galaxy has photometry in a sufficient number of bands, and over a wide enough wavelength range, to allow robust estimates of photometric redshift. Photo-*z*s are calculated using template fits to the optical and IRAC photometry in an identical method to that used for the SMGs (see Wardlow et al. 2011). The fits are performed with  $HYPER-Z$  (Bolzonella, Miralles  $&$ Pelló 2000) and the resulting redshift distribution, compared to that for the SMGs, is shown in Fig. 2. The photometric analysis uses chisquared minimization, which allows the calculation of confidence intervals for the best-fitting redshift. These can be presented as a probability distribution function (PDF) for the redshift, or equivalently, the comoving line-of-sight distance  $\chi$  (calculated for our assumed cosmology). We define the PDF for each galaxy as  $f(\chi)$ , where  $\int f(\chi) d\chi = 1$ . Examples of the PDFs for the galaxies are shown in Fig. 3.

Finally, in order to calculate the correlation functions, we first create random catalogues of 'galaxies' at random positions within the actual spatial coverage of our survey. Like many fields, the ECDFS contains several bright stars with large haloes, around which few galaxies are detected. Therefore, we use the background map produced by SEXTRACTOR (Bertin & Arnouts 1996) from the combined IRAC image during the source extraction procedure to create a mask. This mask is applied to the random catalogues, the SMGs and the IRAC galaxies, so that the positions of the random galaxies are unbiased with respect to the SMG and IRAC galaxy samples, and thus the mask does not affect the cross-correlation measurement.



**Figure 1.** Two-dimensional distribution of the 50 LESS SMGs and ∼50 000 IRAC galaxies in the ECDFS that are used in our analysis. The SMGs shown represent the subset of the 126 SMGs in the full LESS sample (Weiß et al. 2009) that are in the redshift range  $1 < z < 3$  and are in regions of good photometry, and so are used in this analysis. The IRAC galaxies are chosen to reside at  $0.5 < z < 3.5$ . The SMGs are shown here individually, while the density of galaxies is given by the grey-scale. The blank areas represent regions which are excluded from the analysis, including areas of poor photometry (e.g. around bright stars) or additional sources identified by eye in the vicinity of SMG, as discussed in Section 2. The high density of IRAC galaxies in the field enables an accurate measurement of the SMG– galaxy cross-correlation function.



**Figure 2.** Redshift distributions for the IRAC galaxy sample in the redshift range  $0.5 < z < 3.5$  (dotted line), and the SMG sample in the range  $1 <$ *z* < 3 (solid line). The histogram for galaxies has been scaled so that the distribution can be directly compared to that of the SMGs. Also shown is the redshift distribution for 11 241 galaxies (dashed line) selected to match the overlap in the redshift distributions of the SMGs and galaxies, as used in the galaxy autocorrelation measurement (Section 3.2). For the SMGs, 44 per cent have spectroscopic redshifts, while the remainder of the SMGs and all the IRAC galaxies have redshift estimates from photometric redshift calculations (Wardlow et al. 2011).



**Figure 3.** Example probability distribution functions for three IRAC galaxies and an SMG. We mark the 'best' (peak) comoving distance for each galaxy. Note that for each galaxy in this example, the line-of-sight distance between the 'peak' redshift of the galaxy and the SMG redshift is far too large for them to be physically associated. However, because of the uncertainty in the galaxy redshifts (shown by the PDFs), there is a non-negligible probability that the galaxies lie close to the line-of-sight distance of the SMG.

As discussed in Biggs et al. (2011) and Wardlow et al. (2011), some of the SMG identifications were performed manually by examining the regions around the SMGs. These additional sources are excluded from the clustering analysis so as not to bias the results.

# **3 CORRELATION ANALYSIS**

To measure the spatial clustering of SMGs, we can in principle derive the autocorrelation of the SMGs themselves. However, as we have discussed, current SMG samples are too limited in size and available redshift information to make this feasible. Alternatively, we can measure the cross-correlation of a population with a sample of other sources (for example, less-active galaxies) which populate the same volume (e.g. Gawiser et al. 2001; Adelberger & Steidel 2005; Blake et al. 2006; Coil et al. 2007; Hickox et al. 2009). The much larger number of galaxies in the ECDFS (∼1000× more than the SMGs in a comparable redshift range) allows far greater statistical accuracy in the measurement of clustering.

To calculate the real-space projected cross-correlation function  $w_p(R)$  between SMGs and galaxies we employ a method derived by M09. This method enables us to take advantage of the full photo-*z* PDF for each galaxy, by weighting pairs of SMGs and galaxies based on the probability of their overlap in redshift space. This method allows us to calculate the SMG–galaxy cross-correlation using the full sample of  $z \approx 50000$  IRAC galaxies, while the derive the clustering of the galaxies themselves using a smaller sample that is selected to match the overlap in the redshift distributions of the galaxies and SMGs. Our clustering analysis is identical in most respects to the QSO–galaxy cross-correlation study presented in Hickox et al. (2011, hereafter H11). Because the method is somewhat involved, we present only the key details here and refer the reader to H11 for a full discussion.

#### **3.1 Cross-correlation method**

The two-point correlation function  $\xi(r)$  is defined as the probability above Poisson of finding a galaxy in a volume element d*V* at a physical separation *r* from another randomly chosen galaxy, such that

$$
dP = n[1 + \xi(r)]dV, \tag{1}
$$

where  $n$  is the mean space density of the galaxies in the sample. The projected correlation function  $w_p(R)$  is defined as the integral of  $\xi(r)$  along the line of sight,

$$
w_{\rm p}(R) = 2 \int_0^{\pi_{\rm max}} \xi(R, \pi) \, \mathrm{d}\pi,\tag{2}
$$

where *R* and  $\pi$  are the projected comoving separations between galaxies in the directions perpendicular and parallel, respectively, to the mean line of sight from the observer to the two galaxies. By integrating along the line of sight, we eliminate redshift-space distortions owing to the peculiar motions of galaxies, which distort the line-of-sight distances measured from redshifts.  $w_p(R)$  has been used to measure correlations in a number of surveys (e.g. Zehavi et al. 2005; Li et al. 2006; Coil et al. 2007, 2008, 2009; Gilli et al. 2007, 2009; Wake et al. 2008b; Hickox et al. 2009, 2011; M09; Donoso et al. 2010; Krumpe, Miyaji & Coil 2010; Allevato et al. 2011; Starikova et al. 2011).

In the range of separations  $0.3 \le r \le 50$  *h*<sup>−1</sup> Mpc,  $\xi(r)$  for galaxies and QSOs is roughly observed to be a power law,

$$
\xi(r) = (r/r_0)^{-\gamma},
$$
\n(3)

with  $\gamma$  typically  $\approx$ 1.8 (e.g. Zehavi et al. 2005; Coil et al. 2007, 2008; Ross et al. 2009). For sufficiently large  $\pi_{\text{max}}$  such that we average over all line-of-sight peculiar velocities,  $w_p(R)$  can be directly related to  $\xi(r)$  (for a power law parametrization) by

$$
w_{\mathbf{p}}(R) = R\left(\frac{r_0}{R}\right)^{\gamma} \frac{\Gamma(1/2)\Gamma[(\gamma - 1)/2]}{\Gamma(\gamma/2)}.
$$
 (4)

To calculate  $w_p(R)$  for the cross-correlation between SMGs and galaxies, we use the method of M09, which accounts for the photometric redshift probability distribution for each galaxy individually.

Following M09, the projected cross-correlation function can be calculated using

$$
w_{\rm p}(R) = N_{\rm R} N_{\rm S} \sum_{i,j} c_{i,j} \frac{D_{\rm S} D_{\rm G}(R)}{D_{\rm S} R_{\rm G}(R)} - \sum_{i,j} c_{i,j}, \qquad (5)
$$

where

$$
c_{i,j} = f_{i,j} / \sum_{i,j} f_{i,j}^2.
$$
 (6)

Here *R* is the projected comoving distance from each SMG, for a given angular separation  $\theta$  and radial comoving distance to the SMG of  $\chi$ <sub>\*</sub>, such that  $R = \chi$ <sup>\*</sup> $\theta$ .  $D_S D_G$  and  $D_S R_G$  are the number of SMG–galaxy and SMG–random pairs in each bin of *R*, and  $N<sub>S</sub>$  and  $N<sub>R</sub>$  are the total numbers of SMGs and random galaxies, respectively.  $f_{i,j}$  is defined as the average value of the radial PDF  $f(\chi)$  for each galaxy *i*, in a window of size  $\Delta \chi$  around the comoving distance to each spectroscopic source *j*. We use  $\Delta \chi$  = 100 *h*−<sup>1</sup> Mpc to effectively eliminate redshift-space distortions, although the results are insensitive to the details of this choice. We refer the reader to M09 and H11 for a detailed derivation and discussion of these equations. In this calculation as well as in the galaxy autocorrelation, we account for the integral constraint as described in H11. This correction increases the observed clustering amplitude by  $≈15$  per cent.

#### **3.2 Galaxy autocorrelation**

To estimate DM halo masses for the SMGs, we calculate the relative bias between SMGs and galaxies, from which we derive the absolute bias of the SMGs relative to DM. As discussed below, calculation of absolute bias (and thus halo mass) requires a measurement of the autocorrelation function of the IRAC galaxies. The large size of the galaxy sample enables us to derive the clustering of the galaxies accurately from the angular autocorrelation function  $\omega(\theta)$  alone. Although we expect the photometric redshifts for the IRAC galaxies to be reasonably well constrained (as discussed in Section 2), by using the angular correlation function we minimize any uncertainties relating to individual galaxy photo-*z*s for this part of the analysis. The resulting clustering measured for the galaxies has significantly smaller uncertainties than that for the SMG–galaxy cross-correlation.

We calculate the angular autocorrelation function  $\omega(\theta)$  using the Landy & Szalay (1993) estimator:

$$
\omega(\theta) = \frac{1}{RR}(DD - 2DR + RR),\tag{7}
$$

where *DD*, *DR* and *RR* are the number of data–data, data–random and random–random galaxy pairs, respectively, at a separation  $\theta$ , where each term is scaled according to the total numbers of SMGs, galaxies and randoms.

The galaxy autocorrelation varies with redshift, owing to the evolution of large-scale structure, and because the use of a fluxlimited sample means we select more luminous galaxies at higher *z*. This will affect the measurements of relative bias between SMGs and galaxies, since the redshift distribution of the SMGs peaks at higher *z* than that for the galaxies and so relatively higher *z* galaxies dominate the cross-correlation signal. To account for this in our measurement of galaxy autocorrelation, we randomly select galaxies based on the overlap of the PDFs with the SMGs in comoving distance (in the formalism of Section 3.1 this is  $f_{i,j}$  for each galaxy, averaged all SMGs). We select the galaxies so their distribution in redshift is equivalent to the *weighted* distribution for all galaxies

(weighted by  $\langle f_{i,j} \rangle$ ). The redshift distribution of this galaxy sample is shown in Fig. 2. We use this smaller galaxy sample to calculate the angular autocorrelation of IRAC galaxies.

### **3.3 Uncertainties and model fits**

We estimate uncertainties on the clustering directly from the data using bootstrap resampling. Following H11, we divide the field into a small number of sub-areas (we choose  $N_{sub} = 8$ ), and for each bootstrap sample we randomly draw a total of  $3N<sub>sub</sub>$  subareas (with replacement), which has been shown to best approximate the intrinsic uncertainties in the clustering amplitude (Norberg et al. 2009). To account for shot noise owing to the relatively small size of the SMG sample, we take the sets of  $3N<sub>sub</sub>$  bootstrap subareas and randomly draw from them (with replacement) a sample of sources (SMGs or galaxies) equal in size to the parent sample; only pairs including these sources are used in the resulting cross-correlation calculation. We use the bootstrap results to derive the covariance between different bins of *R*, calculating the covariance matrix using equation (12) of H11.

We fit the observed  $w_p(R)$  with two models: a power law and a simple bias model (described in Section 3.4). We compute model parameters by minimizing  $\chi^2$  (taking into account the covariance matrix as in equation 13 of H11) and derive  $1\sigma$  errors in each parameter by the range for which  $\Delta \chi^2 = 1$ . We use the same formalism for computing fits to the angular correlation functions, where  $\omega(\theta) = A\theta^{-\delta}$ . We convert *A* and *δ* to real-space clustering parameters  $r_0$  and  $\gamma$  following the procedure described in section 4.6 of H11.

### **3.4 Absolute bias and dark matter halo mass**

The masses of the DM haloes in which galaxies and SMGs reside are reflected in their absolute clustering bias  $b_{\text{abs}}$  relative to the DM distribution. The linear bias  $b_{\text{abs}}^2$  is given by the ratio of the autocorrelation function of the galaxies (or SMGs) to that of the DM. We determine  $b_{\text{abs}}$  following the method outlined in section 4.7 of H11, similar to the approach used previously by a number of studies (e.g. Myers et al. 2006, 2007; Coil et al. 2007, 2008, 2009; Hickox et al. 2009); in what follows we briefly describe this procedure.

We first calculate the two-point autocorrelation of DM as a function of redshift. We use the HALOFIT code of Smith et al. (2003) assuming our standard cosmology, and the slope of the initial fluctuation power spectrum,  $\Gamma = \Omega_{\rm m} h = 0.21$ , to derive the DM power spectrum, and thus its projected correlation function  $w_{\rm p}^{\rm DM}(R)$ , averaged over the redshift distribution for which the SMGs and galaxies overlap. We then fit the observed  $w_p(R)$  of the SMG–galaxy cross-correlation, on scales 0.3–15 *h*−<sup>1</sup> Mpc, with a model comprising a simple linear scaling of  $w_p^{DM}(R)$ . The best-fitting linear scaling of the DM correlation function corresponds to  $b_S b_G$ , the product of the linear biases for the SMGs and galaxies, respectively. This simple model produces a goodness-of-fit comparable to that of the power-law model in which the slope  $\gamma$  is allowed to float.

To determine  $b_S$  we therefore need to estimate  $b_G$ . We obtain  $b_G$ for the galaxies from their angular autocorrelation in a similar manner to that applied to the SMG–galaxy cross-correlation. Again we calculate the autocorrelation for the DM  $\omega_{DM}(\theta)$ , by integrating the power spectrum from HALOFIT using equation (A6) of Myers et al. (2007). We fit the observed  $\omega(\theta)$  with a linear scaling of  $\omega_{DM}(\theta)$  on scales 0.3–10 arcmin (corresponding to 0.3–10  $h^{-1}$  Mpc at  $z = 2$ ).

This linear scaling corresponds to  $b<sub>G</sub><sup>2</sup>$  and thus (combined with the cross-correlation measurement) yields the SMG bias  $b_S$ . Finally, we convert  $b_G$  and  $b_S$  to  $M_{halo}$  using the prescription of Sheth, Mo & Tormen (2001), as described in H11. This characteristic *M*halo corresponds to the top-hat virial mass (see e.g. Peebles 1993, and references therein), in the simplified case in which all objects in a given sample reside in haloes of the same mass. This assumption is justified by the fact (as discussed Section 4.4) that SMGs have a very small number density compared to the population of similarly clustered DM haloes, such that it is reasonable that SMGs may occupy haloes in a relatively narrow range in mass. We note that this method differs from some prescriptions in the literature which assume that sources occupy all haloes above some minimum mass; this is particularly relevant for populations with high number densities that could exceed the numbers of available DM haloes over a limited mass range. Given the halo mass function at *z* ∼ 2 (e.g. Tinker et al. 2008) the derived minimum mass is typically a factor of ∼2 lower, for the same clustering amplitude, than the 'average' mass quoted here.

# **4 RESULTS AND DISCUSSION**

The projected cross-correlation function of the SMG sample with the IRAC galaxies is shown in Fig. 4. We plot the best-fitting powerlaw model, and show the correlation function of the DM calculated as in Section 3.4, which we fit to the data through a linear scaling. The power-law and linear bias fit parameters are presented in Table 1. For SMGs the observed real-space projected crosscorrelation is well detected on all scales from 0.1–15 *h*−<sup>1</sup> Mpc, and the power-law fits return  $\gamma \sim 1.8$ , similar to many previous correlation function measurements for galaxies (e.g. Zehavi et al. 2005; Coil et al. 2008) and QSOs (e.g. Coil et al. 2007; Ross et al. 2009). The best-fitting parameters for the SMG–galaxy cross-correlation are  $r_{0,SG} = 5.3 \pm 0.8 h^{-1}$  Mpc,  $\gamma = 1.7 \pm 0.2$ . If we fix the value of  $\gamma$  to 1.8, we obtain  $r_{0,SG} = 5.1 \pm 0.6 h^{-1}$  Mpc, corresponding



**Figure 4.** The projected SMG–galaxy cross-correlation function (derived using equation 5). Uncertainties are estimated from bootstrap resampling. A power-law fit to  $w_p(R)$  is shown by the solid line, and the projected correlation function for DM is shown by the dotted line. Fits are performed over the range in separation of  $R = 0.3-15 h^{-1}$  Mpc. Both the power-law model with  $\gamma = 1.8$  and a linear scaling of the DM correlation function provide satisfactory fits to the observed  $w_p(R)$ . Together with the observed galaxy autocorrelation, this measurement yields the clustering amplitude and DM halo mass for the SMGs, as described in Section 4.

to a clustering signal that is significant at the  $> 4\sigma$  level, the most significant measurement of SMG clustering to date. From the fit of the DM model, we obtain  $b_S b_G = 5.83 \pm 1.36$ .

We next compute the autocorrelation of IRAC galaxies for the sample described in Section 3.2. The observed  $\omega(\theta)$  is shown in Fig. 5, along with the corresponding power-law fit and scaled correlation function for DM, calculated as discussed in Section 3.4. Fit parameters are given in Table 1. The power-law model fits well on the chosen scales of 0.3–10 arcmin. The best-fitting power-law parameters are  $r_{0,\text{GG}} = 3.3 \pm 0.3$  and  $\gamma = 1.8 \pm 0.2$ , and the bestfitting scaled DM model yields  $b_{\text{G}}^2 = 2.99 \pm 0.40$  or  $b_{\text{G}} = 1.73 \pm 0.00$ 0.12.

This accurate value for  $b<sub>G</sub>$  yields  $b<sub>S</sub> = 3.37 \pm 0.82$  for the SMGs. Converting this to DM halo mass using the prescription of Sheth et al. (2001) as described in Section 3.4, we arrive at  $\log (M_{\text{halo}}[h^{-1} M_{\odot}]) = 12.8^{+0.3}_{-0.5}$ . The corresponding halo mass for the galaxies is  $\log (M_{\text{halo}}[h^{-1} M_{\odot}]) = 11.5 \pm 0.2.$ 

For comparison with other studies that attempted to directly measure the autocorrelation function of SMG, it is useful to present the SMG clustering in terms of effective power-law parameters for their autocorrelation. Assuming linear bias, the SMG autocorrelation can be inferred from the cross-correlation by  $\xi_{SS} = \xi_{SG}^2/\xi_{GG}$ (e.g. Coil et al. 2009). Adopting a fixed  $\gamma = 1.8$  for the SMG– galaxy cross-correlation, we thus obtain  $r_{0,SS} = 7.7^{+1.8}_{-2.3} h^{-1}$  Mpc for the autocorrelation of the SMGs.

### **4.1 Effects of SMG photo-***z* **errors**

One uncertainty in our estimate of  $w_p(R)$  for the SMG–galaxy crosscorrelation is due to the lack of accurate (i.e. spectroscopic) redshifts for roughly half of the SMG population. As described in Section 3, in calculating  $w_p(R)$  for the cross-correlation, we simply assume that the SMGs lie exactly at the best redshifts from the photo-*z* analysis of Wardlow et al. (2011). Any uncertainties in the SMGs photo-*z*s could therefore affect the resulting clustering measurement. (Note that photo-*z* uncertainties in the galaxies are accounted for implicitly in the correlation analysis, as we utilize the full galaxy photo-*z* PDFs.) To examine the effects of SMG photo-*z* errors, we follow the procedure outlined in section 6.3 of H11. We take advantage of the 44 per cent of SMGs that do have spectroscopic redshifts, and determine how errors in those redshifts affect the observed correlation amplitude.

Specifically, we shift the redshifts of the spectroscopic SMGs by offsets  $\Delta z/(1+z)$  selected from a Gaussian random distribution with dispersion  $\sigma$ <sub>*z*</sub>/(1 + *z*). To ensure that this step does not artificially smear out the redshift distribution beyond the range probed by the galaxies, we require that the random redshifts lie in the range 1 < *z* < 3; any random redshift that lies outside this range is discarded and a new redshift is selected from the random distribution. Using these new redshifts we recalculate  $w_p(R)$ , using the full formalism described in Section 3. We perform the calculation 10 times for each of several values of  $\sigma$ <sub>*z*</sub>/(1 + *z*) from 0.05 up to 0.3 (corresponding to the range of photo-*z* uncertainties). For each trial we obtain the relative bias by calculating the mean ratio of  $w_p(R)$ , on scales  $1-10 h^{-1}$  Mpc, relative to the  $w_p(R)$  for the best estimates of redshift. We then average the 10 trials at each  $\sigma_z$ , and find that at most the photo-*z* errors cause the clustering amplitude to decrease by ∼10 per cent. The precise magnitude of this effect is unclear given the range of uncertainties in the SMG photo-*z* estimates, but it is significantly smaller than the statistical uncertainties. We therefore neglect this effect in our final error estimates.





<sup>*a*</sup>Number of objects in the SMG sample and in the galaxy sample used for the galaxy autocorrelation.

<sup>*b*</sup>Median redshift for the SMG sample and for the galaxy sample used for the galaxy autocorrelation.

*<sup>c</sup>*Power-law model parameters are for the autocorrelation of SMGs (derived from SMG–galaxy projected spatial crosscorrelation, along with the galaxy angular autocorrelation) and galaxies (derived from their angular autocorrelation). *d*Parameters derived from the observed linear fit of the DM model to the observed correlation function, in order to obtain the absolute bias for the SMGs and galaxies (denoted *b*<sub>S</sub> and *b*<sub>G</sub>, respectively). The linear scaling from the fit corresponds to  $b_Sb_G$  for the SMG–galaxy cross-correlation, and  $b_G^2$  for the galaxy autocorrelation, which in turn yield  $b_G$  and  $b_S$ .<br>
"DM halo mass derived from the absolute bias, using the method described in Section 3.4.



**Figure 5.** The angular autocorrelation function of IRAC galaxies, selected to match the overlap of the SMGs and galaxies in redshift space. Uncertainties are estimated from bootstrap resampling. The angular correlation function for DM, evaluated for the redshift distributions of the galaxies, is shown by the dotted grey line. The power-law fit was performed on scales 0.3–10 arcmin and is shown as the solid line. Both the power-law model with  $\delta = 0.8$  and a linear scaling of the DM correlation function provide satisfactory fits to the observed  $\omega(\theta)$ . The observed amplitude of the galaxy autocorrelation yields the absolute bias of the galaxies, which we use to obtain the absolute bias and DM halo mass of the SMGs.

## **4.2 Comparison with previous results**

Here we compare our results to other measurements of SMG clustering in the literature. The observed clustering may depend on the flux limit of the submm sample, as discussed by Williams et al. (2011); measurements of  $r_0$  that use SMG samples with similar submm flux limits are shown in Fig. 6(a). Our measurement is significantly more accurate than previous measurements, owing to the inclusion of redshift information and the improved statistics in the cross-correlation. The uncertainties are comparable to those quoted by Blain et al. (2004) who estimated  $r_0$  using counts of close pairs in redshift space from spectroscopic surveys. However, these authors did not account for significant additional sources of error, as discussed by Adelberger (2005). Uncertainties in the redshift selection function for spectroscopic objects, along with the presence of redshift spikes and angular clustering of sources, can strongly impact the number of expected pair counts for an unclustered distribution, and therefore significantly affect the results for the clustering amplitude (Adelberger 2005). In Fig. 6(a) the large error bars for the Blain et al. (2004) point represent the increase in the uncertainty

by 60 per cent due to angular clustering of sources and redshift spikes (as estimated by Adelberger 2005), but does not include the additional uncertainty on the redshift selection function. None the less, our measurement of  $r_0$  is consistent with most previous angular clustering estimates as well as the Blain et al. (2004) result, and represents a significant improvement in precision.

As discussed in Section 3.4, we convert the observed clustering amplitude to  $M_{halo}$  by assuming that SMGs obey simple linear bias relative to the DM and reside in haloes of similar mass. Motivated by the presence of a large overdensity of SMGs and powerful starforming galaxies in one redshift survey field, Chapman et al. (2009) proposed that SMGs obey 'complex bias' that depends on largescale environment and merger history, and that they may reside in somewhat smaller haloes than would be inferred from a linear bias model. Future studies using significantly larger SMG samples may be able to confirm the existence of more complex clustering, but for the present analysis we adopt the simplest scenario and derive *M*halo assuming linear bias.

The characteristic halo mass we measure for SMGs is similar to that measured for bright far-IR sources (with fluxes >30 mJy at 250 µm) detected by the *Herschel Space Observatory* using an angular clustering analysis (Cooray et al. 2010). While it remains uncertain to what extent bright 250 µm sources and 850-µm-selected SMGs represent a common population, both samples comprise the luminous end of the star-forming galaxy population detected at those wavelengths and so may represent physically similar systems. In contrast, our observed SMG clustering is significantly stronger than that reported by Amblard et al. (2011) for 'submillimetre galaxies' based on a power spectrum analysis of *Herschel* 350-µm maps, which yields a minimum  $M_{\text{halo}}$  of ~3 × 10<sup>11</sup> M<sub>○</sub> (see Viero et al. 2009 for similar results from BLAST). The differences in clustering amplitude compared to SMGs result from the fact that the power spectrum analysis includes unresolved faint sources corresponding to far fainter far-IR luminosities, characteristic of typical *z* ∼ 2 starforming galaxies rather than the powerful, luminous starbursts that are conventionally referred to as SMGs in the literature.

## **4.3 Progenitors and descendants of SMGs**

Our improved clustering measurement allows us to place SMGs in the context of the cosmological history of star formation and growth of DM structures. Because the clustering amplitude of DM haloes and their evolution with redshift are directly predicted by simulations and analytic theory, we can use the observed clustering to connect the SMG populations to their descendants and progenitors, estimate lifetimes and constrain starburst triggering mechanisms.



**Figure 6.** (a) Our new measurement of the autocorrelation length  $r_0$  for SMGs, compared to previous results using samples with similar ∼850 µm flux limits. The two sets of error bars on the Webb et al. (2003) measurement indicate statistical ( $\pm 3 h^{-1}$  Mpc) and systematic ( $\pm 3 h^{-1}$  Mpc) uncertainties separately. On the Blain et al. (2004) measurement, the smaller errors represent the uncertainties quoted by the authors, while the larger errors account for angular clustering and redshift spikes as estimated by Adelberger (2005). Our results are consistent with previous measurements and represent a significant improvement in precision. (b) Our measurement of the autocorrelation length  $r_0$  of SMGs, compared to the approximate  $r_0$  (with associated measurement uncertainties) for a variety of galaxy and AGN populations: optically selected Sloan Digital Sky Survey (SDSS) QSOs at 0 < *z* < 3 (Myers et al. 2006; Ross et al. 2009), LBGs at  $1.5 \lesssim z \lesssim$  3.5 (Adelberger et al. 2005), Multiband Imaging Photometer for *Spitzer* (MIPS) 24-µm-selected star-forming galaxies at  $0 < z < 1.4$  (Gilli et al. 2007), typical red and blue galaxies at  $0.25 \lesssim z \lesssim 1$  from the AGN and Galaxy Evolution Survey (Hickox et al. 2009) and Deep Extragalactic Evolutionary Probe 2 (DEEP2; Coil et al. 2008) spectroscopic surveys, luminous red galaxies (LRGs) at  $0 < z < 0.7$  (Wake et al. 2008a) and optically selected galaxy clusters at  $0.1 < z < 0.3$  (Estrada, Sefusatti & Frieman 2009). In addition, we show the full range of  $r_0$  for low-redshift galaxies with  $r$ -band luminosities in the range 1.5–3.5*L*∗, derived from the luminosity dependence of clustering presented by Zehavi et al. (2011); these luminous galaxies are primarily ellipticals, as discussed in Section 4.3. Dotted lines show  $r_0$  versus redshift for DM haloes of different masses. The thick solid line shows the expected evolution in  $r_0$ , accounting for the increase in mass of the halo, for a halo with mass corresponding to the best-fitting estimate for SMGs at  $z = 2$ . The results indicate that SMGs are clustered similarly to QSOs at *z* ∼ 2 and can be expected to evolve into luminous elliptical galaxies in the local Universe.

We first compare the clustering amplitude of SMGs with other galaxy populations over a range of redshifts.<sup>1</sup> Fig.  $6(b)$  shows the approximate ranges of measurements of  $r_0$  for a variety of galaxy and AGN populations. We also show the evolution of  $r_0$  with redshift for DM haloes of different masses, determined by fitting a power law with  $\gamma = 1.8$  to the DM correlation function output by HALOFIT. Finally, we show the observed  $r_0$  for the current SMG sample, along with the expected evolution in  $r_0$  for haloes that have the observed  $M_{halo}$  for SMGs at  $z = 2$ , calculated using the median growth rate of haloes as a function of *M*halo and *z* (Fakhouri et al.  $2010$ ).<sup>2</sup>

Fig. 6(b) shows that while the DM halo mass for the SMGs will increase with time from  $z \sim 2$  to  $z = 0$ , the observed  $r_0$  stays essentially constant, meaning that the progenitors and descendants of SMGs will be populations with similar clustering amplitudes. Our measurement of  $r_0$  shows that the clustering of SMGs is consistent with optically selected QSOs (e.g. Croom et al. 2005; Myers et al.  $2006$ ; da  $\hat{A}$ ngela et al.  $2008$ ; Ross et al.  $2009$ ). SMGs are more strongly clustered than the typical star-forming galaxy populations at all redshifts (e.g. Adelberger et al. 2005; Gilli et al. 2007; Hickox et al. 2009; Zehavi et al. 2011), and are clustered similarly or weaker than massive, passive systems (e.g. Quadri et al. 2007, 2008; Blanc et al. 2008; Wake et al. 2008a; Kim et al. 2011; Zehavi et al. 2011). The clustering results indicate that SMGs will likely evolve into the most massive, luminous early-type galaxies at low redshift. We note that the descendants of typical SMGs are not likely to reside in massive clusters at  $z = 0$ , but into moderate- to high-mass groups of ∼a few × 10<sup>13</sup> *h*<sup>−1</sup> M<sub>○</sub>. Although *some* SMGs could evolve into<br>measing abotto aclarize the abounced electric apparent that weat massive cluster galaxies, the observed clustering suggests that most will end up in less massive systems.

A schematic picture of the evolution of SMGs is shown in Fig. 7, which shows evolution in the mass of haloes with redshift as traced by their median growth rate (Fakhouri et al. 2010). The typical progenitors of SMGs would have  $M_{halo} \sim 10^{12} h^{-1} M_{\odot}$  at  $z \sim 5$ , which corresponds to the host haloes of bright Lyman-break galaxies (LBGs) at those redshifts (e.g. Hamana et al. 2004; Lee et al. 2006). At low redshift, the SMG descendants will have  $M_{halo}$  =  $(0.6–5) \times 10^{13} h^{-1}$  M<sub>O</sub>. Halo occupation distribution fits to galaxy clustering suggest that these haloes host galaxies with luminosities *L*∼2–3*L*<sup>∗</sup> (Zehavi et al. 2011), a population dominated by ellipticals with predominantly slow-rotating kinematics (e.g. Cappellari et al. 2011; Tempel et al. 2011). Assuming typical mass-to-light ratios for massive galaxies (e.g. Baldry, Glazebrook & Driver 2008), these luminosities correspond to stellar masses  $∼(1.5-2.5) × 10^{11} M_{\odot}$ , in close agreement with direct measurements of the relationship between halo mass and central galaxy stellar mass for X-ray selected groups and clusters, for which  $\log M_{\star} \approx 0.27 \log M_{\text{halo}} + 7.6$  (Stott et al. 2012).

#### **4.4 SMG lifetime and star formation history**

We next estimate the SMG lifetime, making the simple assumption that every DM halo of similar mass passes through an

<sup>&</sup>lt;sup>1</sup> Myers et al. (2006) and Ross et al. (2009) determine  $r_0$  from QSOs assuming a power-law correlation function with  $\gamma = 2$ . To estimate  $r_0$  for  $\gamma = 1.8$ , we multiply the quoted values by 0.8, appropriate for fits over the range  $1 \lesssim R \lesssim 100 \, h^{-1} \, \text{Mpc}.$ 

<sup>2</sup> Note that here we use the median growth rate of haloes, which for haloes of ∼10<sup>13</sup> *h*<sup>−1</sup> M<sub>○</sub> is ≈35 per cent lower than the *mean* growth rate, owing to the long high-mass tail in the halo mass distribution.



**Figure 7.** Broad schematic for the evolution of halo mass versus redshift for SMGs, showing the approximate halo masses corresponding to likely progenitors and descendants of SMGs. Lines indicate the median growth rates of haloes with redshift (Fakhouri et al. 2010). SMG host haloes are similar to those of QSOs at *z* ∼ 2, and correspond to bright LBGs at *z* ∼ 5 (Hamana et al. 2004; Lee et al. 2006) and ∼2–3*L*<sup>∗</sup> ellipticals at *z* = 0 (Zehavi et al. 2011; Stott et al. 2012).

SMG phase, $3$  so that

$$
t_{\rm SMG} = \Delta t \frac{n_{\rm SMG}}{n_{\rm halo}},\tag{8}
$$

where  $\Delta t$  is the time interval over the redshift range covered by the SMG sample, and  $n_{SMG}$  and  $n_{halo}$  are the space densities of SMGs and DM haloes, respectively.

Using the halo mass function of Tinker et al. (2008), the space density of haloes with  $\log (M_{\text{halo}}[h^{-1} M_{\odot}]) = 12.8^{+0.3}_{-0.5}$  is  $dn_{\text{halo}}/d \ln M = (2.1^{+7.3}_{-1.5}) \times 10^{-4} \text{ Mpc}^{-3}$ . We adopt a space density of SMGs at  $z \sim 2$  of  $\sim$ 2 × 10<sup>-5</sup> Mpc<sup>-3</sup>, corresponding to results from previous surveys (e.g. Chapman et al. 2005; Coppin et al. 2006; Schael et al., in preparation). This density is ∼50 per cent higher than that observed in the LESS field (Wardlow et al. 2011), which has been shown to contain a somewhat smaller density of SMGs compared to other surveys (Weiß et al. 2009).

The ratio of these space densities yields a duty cycle (the fraction of haloes that host an SMG at any given time) of ∼10 per cent. We assume the SMGs occupy the redshift range  $1.5 < z < 2.5$ , which includes roughly half of the SMGs in the Wardlow et al. (2011) sample and corresponds to  $\Delta t = 1.6$  Gyr. We thus obtain a lifetime for SMGs of  $t_{\text{SMG}} = 110^{+280}_{-80}$  Myr. Clearly, even our improved measurement of SMG clustering yields only a weak constraint on the lifetime, but this is consistent with lifetimes estimated from gas consumption times and star formation time-scales (e.g. Greve et al. 2005; Tacconi et al. 2006; Hainline et al. 2011) and theoretical models of SMG fuelling through mergers (e.g. Mihos & Hernquist 1994; Springel, Di Matteo & Hernquist 2005; Narayanan et al. 2010).

Constraints on SMG descendants from clustering can also yield insights into their formation histories. Measurements of the stellar plus molecular gas masses of SMGs from SED fitting and dynamical studies are in the range  $∼(1-5) \times 10^{11}$  M<sub>O</sub> (Swinbank et al. 2006; Hainline et al. 2011; Ivison et al. 2011; Michałowski et al. 2011;

Wardlow et al. 2011). While these estimates can be uncertain by factors of a few, they are in a similar range to the stellar masses of SMG descendants as indicated by their clustering, as discussed above. This correspondence suggests that if a significant fraction of the molecular gas is converted to stars during the SMG phase, then these galaxies will subsequently experience relatively little growth in mass from  $z \sim 2$  to the present. This in turn puts limits on the star formation history. Star-forming galaxies at *z* ∼ 2 typically exhibit specific star formation rates of  $M_{\star}/M_{\star} \sim 2 \,\text{Gyr}^{-1}$  (Elbaz et al. 2011), at which the SMGs would only need to form stars for 500 Myr in order to double in mass. We may therefore conclude, from the clustering and stellar masses alone, that the SMGs evolve from star-forming to passive states relatively quickly (within a Gyr or so) after the starburst phase, and that the descendants spend most of their remaining time as relatively passive systems. This scenario is consistent with measurements of the stellar populations in ∼2–3*L*<sup>∗</sup> ellipticals, which have typical ages of ∼10 Gyr and show little evidence for younger components (e.g. Nelan et al. 2005; Allanson et al. 2009), implying that the vast majority of stars were formed above  $z \sim 2$  with little additional star formation at lower redshifts.

The halo masses of SMGs may also provide insight into the processes that prevent their descendants from forming new stars. Star formation can be shut off rapidly at the end of the SMG phase, either by exhaustion of the gas supply, or by energy input from a QSO (e.g. Di Matteo, Springel & Hernquist 2005; Springel et al. 2005). Powerful winds are observed in luminous AGN (e.g. Feruglio et al. 2010; Fischer et al. 2010; Greene et al. 2011; Sturm et al. 2011) and have also been seen in some SMGs (e.g. Alexander et al. 2010; Harrison et al., in preparation), although for the SMGs it is unclear whether the winds are driven by the starburst or AGN. Even if the formation of stars is rapidly quenched, over longer time-scales the galaxy would be expected to accrete further gas from the surrounding halo, resulting in significant additional star formation (e.g. Bower et al. 2006; Croton et al. 2006). Recent work suggests that energy from accreting supermassive black holes, primarily in the form of radio-bright relativistic jets, can couple to the hot gas in the surrounding halo, producing a feedback cycle that prevents rapid cooling (e.g. Rafferty, McNamara & Nulsen 2008). This mechanical black hole feedback is a key ingredient of successful models for the passive galaxy population (e.g. Bower et al. 2006; Croton et al. 2006; Bower, McCarthy & Benson 2008; Somerville et al. 2008). Interestingly, the clustering of radio galaxies at  $z \lesssim$ 0.8 indicates that they reside in haloes of mass  $\gtrsim 10^{13} h^{-1} M_{\odot}$  (e.g. Wake et al. 2008b; Hickox et al. 2009; Mandelbaum et al. 2009; Donoso et al. 2010; Fine et al. 2011), precisely the environments that will host the descendants of SMGs. Thus the strong observed clustering for SMGs can relate them directly to the radio-bright active galactic nucleus population that may regulate their subsequent star formation.

## **4.5 Evolutionary links with QSOs and the SMG redshift distribution**

Finally, the observed clustering of SMGs provides insights into the processes that trigger and (possibly) shut off their rapid star formation activity. As discussed in Section 1, powerful local starbursts (i.e. ULIRGs) are predominantly associated with major mergers and appear to be associated with the fuelling of luminous QSOs as part of an evolutionary sequence (e.g. Sanders et al. 1988). However it is unclear if a similar connection exists between SMGs and high-*z* QSOs. One robust prediction of any evolutionary picture is

<sup>&</sup>lt;sup>3</sup> If the average halo experiences more or fewer SMG phases in the given time interval, the lifetime of each episode will be correspondingly shorter or longer, respectively.

that SMGs and QSOs *must* display comparable large-scale clustering, since the evolutionary time-scales are significantly smaller than those for the growth of DM haloes. At all redshifts, QSOs are found in haloes of similar mass  $\sim$ a few × 10<sup>12</sup> *h*<sup>−1</sup> M<sub>O</sub> (e.g.) Croom et al. 2005; Myers et al. 2006; da Ângela et al. 2008; Ross et al. 2009; Fig. 6). The characteristic *M*halo provides a strong constraint on models of QSO fuelling by the major mergers of gas-rich galaxies (e.g. Kauffmann & Haehnelt 2000; Springel et al. 2005; Hopkins et al. 2006), secular instabilities (e.g. Mo, Mao & White 1998; Bower et al. 2006; Genzel et al. 2008) or accretion of recycled cold gas from evolved stars (Ciotti & Ostriker 2007; Ciotti, Ostriker & Proga 2010), and is similar to the mass at which galaxy populations transition from star forming to passive (e.g. Brown et al. 2008; Coil et al. 2008; Conroy & Wechsler 2009; Tinker & Wetzel 2010). The observed clustering of SMGs at *z* ∼ 2 from the present work is consistent with that for QSOs, as well as highly active obscured objects including powerful obscured AGN (Allevato et al. 2011, H11) and dust-obscured galaxies (Brodwin et al. 2008), which also have small volume densities and thus similarly short lifetimes. Thus these may indeed represent different phases in the same evolutionary sequence, and energy input from the QSO may be responsible for the rapid quenching of star formation at the end of the SMG phase (e.g. Di Matteo et al. 2005; Springel et al. 2005) as discussed in Section 4.4.

A connection with QSOs may imply that triggering of SMGs is also related (at least indirectly) to the mass of the parent DM halo. In this case, the evolution of large-scale structure may broadly explain why the SMG population peaks at *z* ∼ 2.5 and falls at higher and lower redshifts. In the simplest possible such scenario, SMG activity is triggered when the halo reaches a certain mass  $M_{halo}$  = *M*thresh (see fig. 16 of Hickox et al. 2009 for a schematic illustration of this picture). In a given volume, the number of haloes crossing this mass threshold as a function of redshift is

$$
\frac{dN_{\text{thresh}}}{dz} \propto n_{\text{halo}}(M_{\text{thresh}}, z) \dot{M}_{\text{halo}}(M_{\text{thresh}}, z) t_{\text{SMG}} \frac{dV}{dz},\tag{9}
$$

where  $n_{\text{halo}}$  and  $\dot{M}_{\text{halo}}$  are the number density (e.g. Tinker et al. 2008) and typical growth rate (Fakhouri et al. 2010), respectively, of haloes of mass  $M_{\text{thresh}}$  at redshift *z*,  $t_{\text{SMG}}$  is the SMG lifetime and d*V*/d*z* is the differential comoving volume over the survey area. If an SMG is triggered every time a halo reaches  $M<sub>thresh</sub>$ , then the observed number density of SMGs will be proportional to d*N*thresh/d*z*. However, the huge star formation rates of SMGs require a large reservoir of molecular gas (e.g. Greve et al. 2005; Tacconi et al. 2006, 2008), and the molecular gas fraction increases strongly with redshift (e.g. Tacconi et al. 2010; Geach et al. 2011; Lagos et al. 2011). This evolution may explain why the most powerful starbursts at low redshift (ULIRGs) have lower typical SFRs than *z* ∼ 2 SMGs (e.g. Le Floc'h et al. 2005; Rodighiero et al. 2010). Therefore it may be reasonable to assume that the number counts of SMGs also depend on  $f_{\text{mol}}$ , with the simplest possible prescription being

$$
\frac{dN_{\text{SMG}}}{dz} \propto \frac{dN_{\text{thresh}}}{dz} f_{\text{mol}}(z). \tag{10}
$$

In Fig. 8 we show the observed redshift distribution of LESS SMGs (Wardlow et al. 2011), compared to the distributions predicted by equations (9) and (10), assuming  $M_{\text{thresh}} = 6 \times$  $10^{12} h^{-1}$  M<sub> $\odot$ </sub>. For simplicity, the evolution in  $f_{\text{mol}}$  is taken from predictions of the GALFORM model of Lagos et al. (2011), which agrees broadly with observations (see fig. 2 of Geach et al. 2011) and so provides a simple parametrization of the current empirical limits on the molecular gas fraction in galaxies. It is clear from



**Figure 8.** Redshift distribution of LESS SMGs (Wardlow et al. 2011), compared to the simple models for SMG triggering based on the rate at which haloes cross a threshold mass  $M_{\text{thresh}} = 6 \times 10^{12} h^{-1} M_{\odot}$  (see Section 4.5). The uncertainties in the number counts are an approximation of Poisson counting statistics (Gehrels 1986). The black dotted line shows the (arbitrarily normalized) number of haloes crossing this threshold in each redshift interval (equation 9) while the dashed red line shows this distribution multiplied by the evolution in the molecular gas fraction (equation 10), where  $f_{\text{mol}}$  is taken from the model predictions of Lagos et al. (2011) and is shown by the grey dot–dashed line. The remarkable agreement between the second model and the observed number counts suggests that the evolution of the SMG population can be described simply in terms of two quantities: the growth of DM structures and the variation with redshift of the molecular gas fraction in galaxies.

Fig. 8 that there is remarkable correspondence between our extremely simple prescription and the observed redshifts of SMGs. Of course this 'model' does not account for a wide range of possible complications and the normalizations of the distributions are arbitrary. However, this exercise clearly demonstrates that if SMGs, like QSOs, are found in haloes of a characteristic mass, then their observed redshift distribution may be explained simply by two effects: the cosmological growth of structure combined with the evolution of the molecular gas fraction. Thus SMGs likely represent a shortlived but universal phase in massive galaxy evolution, associated with the transition between cold gas-rich, star-forming galaxies and passively evolving systems.

## **5 CONCLUSIONS**

In this paper we measure the cross-correlation between SMGs and galaxies in the LESS survey of ECDFS, and observe significant clustering at the  $>4\sigma$  level. We obtain an autocorrelation length for the SMGs of  $r_0 = 7.7^{+1.8}_{-2.3} h^{-1}$  Mpc, assuming  $\gamma = 1.8$ . This clustering amplitude corresponds to a characteristic DM halo mass of  $\log (M_{\text{halo}}[h^{-1}M_{\odot}]) = 12.8^{+0.3}_{-0.5}$ . Using this estimate of  $M_{\text{halo}}$ and the space density of SMGs, we obtain a typical SMG lifetime of  $t_{\text{SMG}} = 110^{+280}_{-80}$  Myr.

The observed clustering indicates that the low-redshift descendants of typical SMGs are massive (∼2–3*L*∗) elliptical galaxies at the centres of moderate- to high-mass groups. This prediction is consistent with previous suggestions based on the dynamical (Swinbank et al. 2006) and stellar masses (e.g. Hainline et al. 2011) of SMGs, and is also consistent with observations of local massive ellipticals, which indicate that they formed the bulk of their stars at *z* > 2 and have been largely passive since. The clustering of SMGs is very similar to that observed for QSOs at the same redshifts, consistent with evolutionary scenarios in which SMGs and QSOs are triggered by a common mechanism. Assuming that SMGs, like QSOs, are transient phenomena that are observed in haloes of similar mass at all redshifts, the redshift distribution of SMGs can be explained remarkably well by the combination of the cosmological growth of structure and the evolution of the molecular gas fraction in galaxies.

This accurate clustering measurement thus provides a valuable observational constraint on the role of SMGs in the cosmic evolution of galaxies and large-scale structures. We conclude that SMGs likely represent a short-lived but universal phase in massive galaxy evolution that is associated with the rapid growth of black holes as luminous QSOs, and corresponds to the transition between cold gas-rich, star-forming galaxies and passively evolving systems.

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