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# Hybrid radar emitter recognition based on rough $k$ -means classifier and SVM

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## Abstract

Due to the increasing complexity of electromagnetic signals, there exists a significant challenge for recognizing radar emitter signals. In this article, a hybrid recognition approach is presented that classifies radar emitter signals by exploiting the different separability of samples. The proposed approach comprises two steps, i.e., the primary signal recognition and the advanced signal recognition. In the former step, the rough  $k$ -means classifier is proposed to cluster the samples of radar emitter signals by using the rough set theory. In the latter step, the samples within the rough boundary are used to train the support vector machine (SVM). Then SVM is used to recognize the samples in the uncertain area; therefore, the classification accuracy is improved. Simulation results show that, for recognizing radar emitter signals, the proposed hybrid recognition approach is more accurate, and has a lower time complexity than the traditional approaches.

**Keywords:** Emitter recognition, Rough boundary, Uncertain boundary, Training sample, Time complexity

## Introduction

Radar emitter recognition is a critical function in radar electronic support system, for determining the type of radar emitter [1]. Emitter classification based on a collection of received radar signals is a subject of wide interest in both civil and military applications. For example, in battlefield surveillance applications, radar emitter classification provides an important means to detect targets employing radars, especially those from hostile forces. In civilian applications, the technology can be used to detect and identify navigation radars deployed on ships and cars used for criminal activities [2].

The recent proliferation and complexity of electromagnetic signals encountered in modern environments is greatly complicating the recognition of radar emitter signals [1]. Traditional recognition methods are becoming inefficient against this emerging issue [3]. Many new radar emitter recognition methods were proposed, e.g., intrapulse feature analysis [4], stochastic context-free grammars analysis [1], and artificial intelligence analysis [5-8]. In particular, the artificial intelligence analysis approach attracted much attention. Among the artificial intelligence

approaches, neural network and support vector machine (SVM) are widely used for the radar emitter recognition. In [6], Zhang et al. proposed a method based on rough sets theory and radial basis function (RBF) neural networks. Yin et al. [7] proposed a radar emitter recognition method using the single parameter dynamic search neural network. However, the predication accuracy of the neural network approaches is not high and the application of neural networks requires large training sets, which may be infeasible in practice. Compared to the neural network, the SVM yields higher prediction accuracy while requiring less training samples. Ren et al. [2] proposed a recognition method using fuzzy C-means clustering SVM. Lin et al. proposed to recognize radar emitter signals using the probabilistic SVM [8] and multiple SVM classifiers [9]. These proposed SVM approaches can improve the accuracy of recognition. Unfortunately, the time complexity of SVM increases rapidly with the increasing number of training samples. The classification method with high accuracy and low time complexity is becoming the focus of research.

Classifiers can be categorized into linear classifiers and nonlinear classifiers. A linear classifier can classify linear separable samples, but cannot classify linearly inseparable samples efficiently. A nonlinear classifier can classify

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linearly inseparable samples, nevertheless the time complexity of the nonlinear classifier will be increased when processing linearly separable samples. In practice, the radar emitter signals consist of both linearly separable samples and linearly inseparable samples, which makes classification challenging. In the traditional recognition approach, only one classifier is used; thus, it is difficult to classify all radar emitter signal samples. In this article, a hybrid recognition method based on the rough  $k$ -means theory and the SVM is proposed. To deal with the drawback of the traditional recognition approaches, we apply two classifiers to recognize linearly separable samples and linearly inseparable samples respectively. Samples are firstly recognized by the rough  $k$ -means classifier, while linearly inseparable samples are picked up and further recognized by using RBF-SVM in the advanced recognition. The simulation results show that the proposed approach can recognize radar emitter signals more accurate and has a lower time complexity when compared with the existing approaches.

The rest of the article is organized as follows. In Section 'Basic concepts', some basic concepts are reviewed. In Section 'Radar emitter recognition system', a novel radar emitter recognition model is proposed. The performance of the proposed approach is analyzed in Section 'Simulation results', and conclusions are given in Section 'Conclusions'.

## Basic concepts

### Rough sets

An information system can be expressed by a four-parameters group [10]:  $S = \{U, R, V, f\}$ .  $U$  is a finite and non-empty set of objects called the universe, and  $R = C \cup D$  is a finite set of attributes, where  $C$  denotes the condition attributes and  $D$  denotes the decision attributes.  $V = \cup_{r \in R} v_r$ , ( $r \in R$ ) is the domain of the attributes, where  $v_r$  denotes a set of values that the attribute  $r$  may take.  $f : U \times R \rightarrow V$  is an information function. The equivalence relation  $R$  partitions the universe  $U$  into subsets. Such a partition of the universe is denoted by  $U/R = E_1, E_2, \dots, E_n$ , where  $E_i$  is an equivalence class of  $R$ . If two elements  $u, v \in U$  belong to the same equivalence class  $E \subseteq U/R$ ,  $u$  and  $v$  are indistinguishable, denoted by  $\text{ind}(R)$ . If  $\text{ind}(R) = \text{ind}(R - r)$ ,  $r$  is unnecessary in  $R$ . Otherwise,  $r$  is necessary in  $R$ .

Since it is not possible to differentiate the elements within the same equivalence class, one may not obtain a precise representation for a set  $X \subseteq U$ . The set  $X$ , which can be expressed by combining sets of some  $R$  basis categories, is called set defined, and the others are rough sets. Rough sets can be defined by upper approximation and lower approximation. The elements in the lower bound of  $X$  definitely belong to  $X$ , and elements in the upper bound of  $X$  belong to  $X$  possibly. The upper approximation and

lower approximation of the rough set  $R$  can be defined as follows [11]:

$$\underline{R}(X) = \cup \left\{ Y \in \frac{U}{R} : Y \subseteq X \right\} \quad (1)$$

$$\overline{R}(X) = \cup \left\{ Y \in \frac{U}{R} : Y \cap X \neq \emptyset \right\} \quad (2)$$

where  $\underline{R}(X)$  represents the set that can be merged into  $X$  positively, and  $\overline{R}(X)$  represents the set that is merged into  $X$  possibly.

Suppose  $P$  and  $Q$  are both the equivalent relationship of system  $U$ , and the knowledge systems decided by them are  $U/P = \{[x]_P | x \in U\}$  and  $U/Q = \{[y]_Q | y \in U\}$ . If for any  $[x]_P \in (U/P)$ ,  $\overline{Q}([x]_P) = \underline{Q}([x]_P) = [x]_P$ , then knowledge  $P$  is dependent on knowledge  $Q$  completely, that is to say when disjunctive object is some characteristic of  $Q$ , it must be some characteristic of  $P$ .  $P$  and  $Q$  are of definite relationship. If knowledge  $P$  is dependent on knowledge  $Q$  partly,  $P$  and  $Q$  are of uncertain relationship. So the dependent extent of knowledge  $P$  to knowledge  $Q$  is defined as [10]

$$\gamma_Q = \text{POS}_Q(P) / |U| \quad (3)$$

where  $\text{POS}_Q(P) = \cup \underline{Q}(x)$  and  $0 \leq \gamma_Q \leq 1$ . The value of  $\gamma_Q$  reflects the dependent degree of knowledge  $P$  to knowledge  $Q$ .  $\gamma_Q = 1$  shows knowledge  $P$  is dependent on knowledge  $Q$  completely;  $\gamma_Q$  close to 1 shows knowledge  $P$  is dependent on knowledge  $Q$  highly.  $\gamma_Q = 0$  shows knowledge  $P$  is independent of knowledge  $Q$ .

### Rough $k$ -means algorithm

The  $k$ -means algorithm is one of the most popular iterative descent clustering algorithms [12]. The basic idea is to make the samples have high similarity in a class, and low similarity among classes. The center of a cluster can be given by:

$$t_i = \frac{\sum_{x \in X_i} x}{\text{card}(X_i)}, i = 1, 2, \dots, I \quad (4)$$

where  $x$  denotes the sample to cluster,  $X_i$  denotes the cluster  $i$ ,  $\text{card}(X_i)$  denotes the number of the elements in  $X_i$ , and  $I$  denotes the number of clusters.

The  $k$ -means algorithm is efficient for clustering. But  $k$ -means clustering algorithm has the following problems:

1. The number of clusters in the algorithm must be given before clustering [13].
2. The  $k$ -means algorithm is very sensitive to the initial center selection and can easily end up with a local minimum solution [13,14].
3. The  $k$ -means algorithm is also sensitive to the isolated point [15].

To overcome the problem of isolated points, Pawan and West [15] proposed the rough  $k$ -means algorithm. This method introduces upper approximation and lower approximation into  $k$ -means clustering algorithm. The improved cluster center is given by [15]:

$$C_j = \begin{cases} \omega_{\text{lower}} \times \frac{\sum_{v \in \underline{A}(x)} v_j}{|\underline{A}(x)|} + \omega_{\text{upper}} \\ \quad \times \frac{\sum_{v \in (\overline{A}(x) - \underline{A}(x))} v_j}{|\overline{A}(x) - \underline{A}(x)|} & \text{if } \overline{A}(x) - \underline{A}(x) \neq \emptyset \\ \omega_{\text{lower}} \times \frac{\sum_{v \in \underline{A}(x)} v_j}{|\underline{A}(x)|} & \text{otherwise} \end{cases} \quad (5)$$

where the parameters  $\omega_{\text{lower}}$  and  $\omega_{\text{upper}}$  are lower and upper subject degrees of  $X$  relative to their clustering centers. For each object vector  $v$ ,  $d(x, t_i)$  denotes the distance between the center of cluster  $t_i$  and the sample. The lower and upper subject degrees of  $x$  relative to its cluster is based on the value of  $d(x, t_i) - d_{\min}(x)$  ( $1 \leq i \leq I$ ), where  $d_{\min}(x) = \min_{i \in [1, I]} d(x, t_i)$ . If the value of  $d(x, t_i) - d_{\min}(x) \geq \lambda$ , the sample  $x$  is subject to the lower approximation of its cluster, where  $\lambda$  denotes the threshold for determining upper and lower approximation. Otherwise,  $x$  will be subject to the upper approximation. The comparative degree can be determined by the number of elements in the lower approximation set and the upper approximation set, as follows:

$$\frac{\omega_{\text{lower}}(i)}{\omega_{\text{upper}}(i)} = \frac{|\overline{A}(X_i)|}{|\underline{A}(X_i)|}, (\underline{A}(X_i) \neq \emptyset) \quad (6)$$

$$\omega_{\text{lower}}(i) + \omega_{\text{upper}}(i) = 1. \quad (7)$$

### SVM

In this section, we give a very brief introduction to SVM. Let  $(\mathbf{x}_i, y_i)_{1 \leq i \leq N}$  be a set of training examples, each example  $\mathbf{x}_i \in R^d$ ,  $d$  being the dimension of the input space, belongs to a class labeled by  $y \in \{-1, 1\}$ . It amounts to finding  $\mathbf{w}$  and  $b$ , which satisfy

$$y_i[\mathbf{w} \cdot \mathbf{x}_i + b] \geq 1. \quad (8)$$

The aim of SVM is to find the hyperplane which makes the samples with the same label at the same side of the hyperplane. The quantity  $\frac{\|\mathbf{w}\|}{2}$  is named the margin, and optimal separating hyperplane (OSH) is the separating hyperplane which maximizes the margin. The larger the margin, the better the generalization is expected to be [16].

To search the minimum  $\frac{\|\mathbf{w}\|}{2}$ , Lagrange multiplier is usually used, leading to maximizing

$$w(\alpha) = \sum_{i=1}^N \alpha_i - \frac{1}{2} \sum_{i,j=1}^N \alpha_i \alpha_j y_i y_j (\mathbf{x}_i \cdot \mathbf{x}_j) \quad (9)$$

subject to

$$\sum \alpha_i y_i = 0 \quad (10)$$

where  $\alpha = (\alpha_1, \dots, \alpha_N)$  denotes the non-negative Lagrange multipliers,  $\mathbf{x}_i$  denotes the input of the training data and  $y_i$  denotes the output of the training data [17].

The decision function is

$$f(x) = \text{sign} \left[ \sum_{i=1}^N y_i \cdot a_i(\mathbf{x}_i \cdot \mathbf{x}) + b \right] \quad (11)$$

In the nonlinear case, the approach adapted to noisy data is to make a soft margin. We introduce the slack variables  $(\xi_1, \dots, \xi_i)$  with  $\xi_1 > 0$  so that

$$y_i[\mathbf{w} \cdot \mathbf{x}_i + b] \geq 1 - \xi_i, i = 1, \dots, N. \quad (12)$$

The generalized OSH is the solution of minimizing

$$\frac{1}{2} \mathbf{w} \cdot \mathbf{w} + C \sum_{i=1}^N \xi_i \quad (13)$$

subject to (12) and  $\xi_i > 0$ . The parameter  $\sum \xi_i$  is the upper bound on the number of training errors and  $C$  is the penalty parameter to control errors.

In the nonlinear SVM, a kernel function is introduced to change the initial data into a feature space with high dimension. In the new space the data should be linearly separable. Then the quadratic optimization problem can be converted to maximize

$$w(\alpha) = \sum_{i=1}^N \alpha_i - \frac{1}{2} \sum_{i,j=1}^N \alpha_i \alpha_j y_i y_j K(\mathbf{x}_i \cdot \mathbf{x}_j) \quad (14)$$

subject to (10) and  $0 \leq \alpha_i \leq C$ .  $K(x, x_i)$  is the kernel function. As one of the most popular kernel functions, the RBF kernel function is considered in this article, and it takes the following form [18,19]:

$$K(x, x_i) = \exp\{-\gamma \|\mathbf{x} - \mathbf{x}_i\|^2\}. \quad (15)$$

(14) is converted to maximize

$$w(\alpha) = \sum_{i=1}^n \alpha_i - \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n y_i y_j \alpha_i \alpha_j \exp\{-\gamma \|\mathbf{x}_i - \mathbf{x}_j\|^2\} \quad (16)$$

subject to (10) and  $0 \leq \alpha_i \leq C$ . The new decision function is :

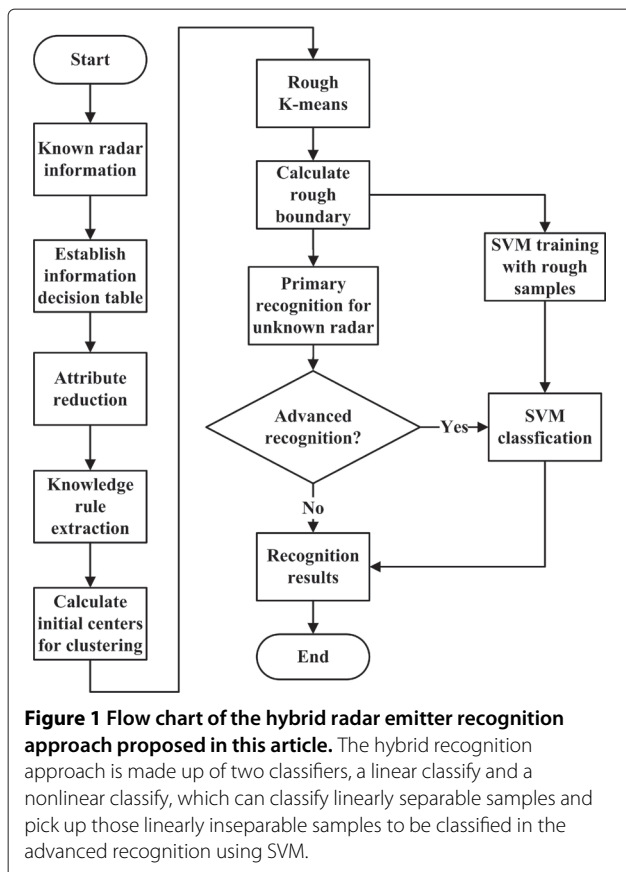
$$f(x) = \text{sign} \left( \sum_{i=1}^{N_s} y_i \cdot a_i \cdot K(\mathbf{x}, \mathbf{x}_i) + b \right) \quad (17)$$

The result of the minimization is determined by the selection of parameters  $C$  and  $\gamma$ . Usually,  $C$  and  $\gamma$  are determined by using cross validation.

### Radar emitter recognition system

In this section, a hybrid radar emitter recognition approach that consists of a rough  $k$ -means classifier in the primary recognition and a SVM classifier in the advanced recognition is proposed. This approach is based on the fact that in the  $k$ -means clustering, the linearly inseparable samples are mostly at the margins of clusters, which makes it difficult to determine which cluster they belong to. To solve this problem, a linear classifier based on the rough  $k$ -means and a nonlinear classifier SVM are adopted. This approach can classify linearly separable samples and pick up those linearly inseparable samples to be classified in the advanced recognition using SVM.

After sorting and feature extraction, radar emitter signals are described by pulses describing words. Radar emitter recognitions are based on these pulses describing words. The process of the hybrid radar emitter recognition approach is shown in Figure 1. Based on the pulses describing words, we can obtain an information sheet of radar emitter signals. By attribute discretization and attribute reduction, the classification rules are extracted. These classification rules are the basis of the initial centers of the rough  $k$ -means classifier, i.e., they determine the initial centers and the number of clusters. After that, the known radar emitter signal samples are clustered by



the rough  $k$ -means while the rough  $k$ -means classifier in the primary recognition is built, as described in the following section. The samples in the margin of a cluster are picked up to be used as the training data for the SVM in the advanced recognition. The unknown samples to be classified are recognized firstly by the rough  $k$ -means classifier. The uncertain sample set, which contains most of the samples with linear inseparability, is classified by the SVM in the advanced recognition.

Based on the process of the recognition approach described above, the accuracy of recognition can be given by:

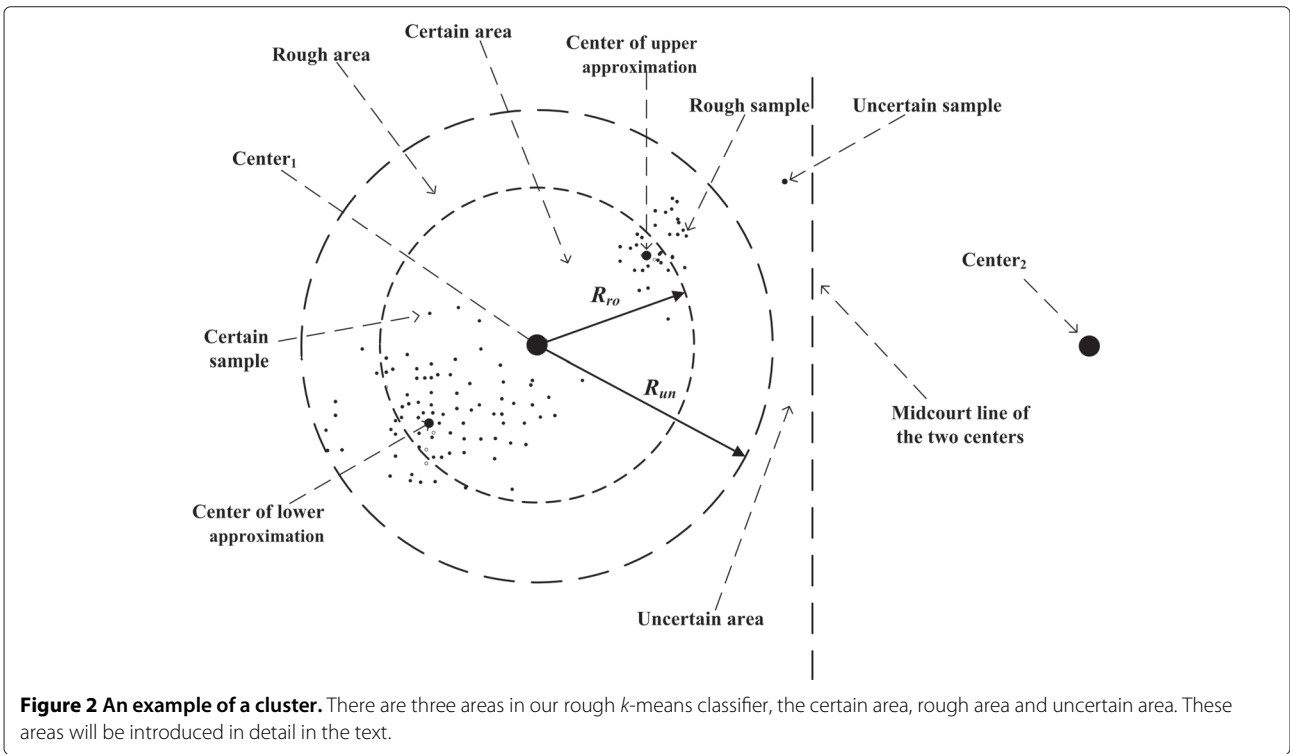
$$A_{\text{total}} = A_{\text{primary}} + (1 - A_{\text{primary}}) \cdot \frac{N_{\text{WIU}}}{N_{\text{W}}} \cdot A_{\text{advanced}} \quad (18)$$

where  $A_{\text{total}}$  is the accuracy of the hybrid recognition,  $A_{\text{primary}}$  is the accuracy of the primary recognition,  $A_{\text{advanced}}$  is the accuracy of the advanced recognition,  $N_{\text{WIU}}$  is the number of samples which are falsely classified in uncertain area, and  $N_{\text{W}}$  is the number of wrong classified samples.

### Primary recognition based on improved rough $k$ -means

As mentioned above, a classifier based on the rough  $k$ -means is proposed as the primary recognition. In the rough  $k$ -means algorithm, there are two areas in a cluster, i.e., certain area and rough area. But in the rough  $k$ -means classifier proposed in this article, there exist three areas. For example, in two dimension, a cluster is depicted in Figure 2. At the edge of the cluster, there is an empty area between the borderline and the midcourt line of the two cluster centers. We name this area as the uncertain area. In clustering, there is no sample in the uncertain area. When the clustering is completed, these clusters will be used as the rough  $k$ -means classifiers. When unknown samples are classified, for each cluster center, samples are nearer than the midcourt line are classified into its class. Linear inseparable samples are usually far from cluster centers and probably out of the cluster, i.e., in the uncertain area. Thus after distributed into their nearest clusters, the unknown samples in uncertain area will be recognized by the advanced recognition. For those unknown samples in the certain area and rough area, the primary recognition outputs final results.

As shown in Figure 2, in the training process of the rough  $k$ -mean classifier, we calculate the cluster center, rough boundary  $R_{\text{ro}}$  and uncertain boundary  $R_{\text{un}}$  in every cluster. After clustering, the center of a cluster and the farthest sample from the center of the cluster are determined. The area between rough boundary and uncertain boundary ( $R_{\text{ro}} < d_x < R_{\text{un}}$ ) is defined as rough area, where  $d_x$  denotes the distance from a sample to the center. In the training, if a training sample is in the rough area, it will be

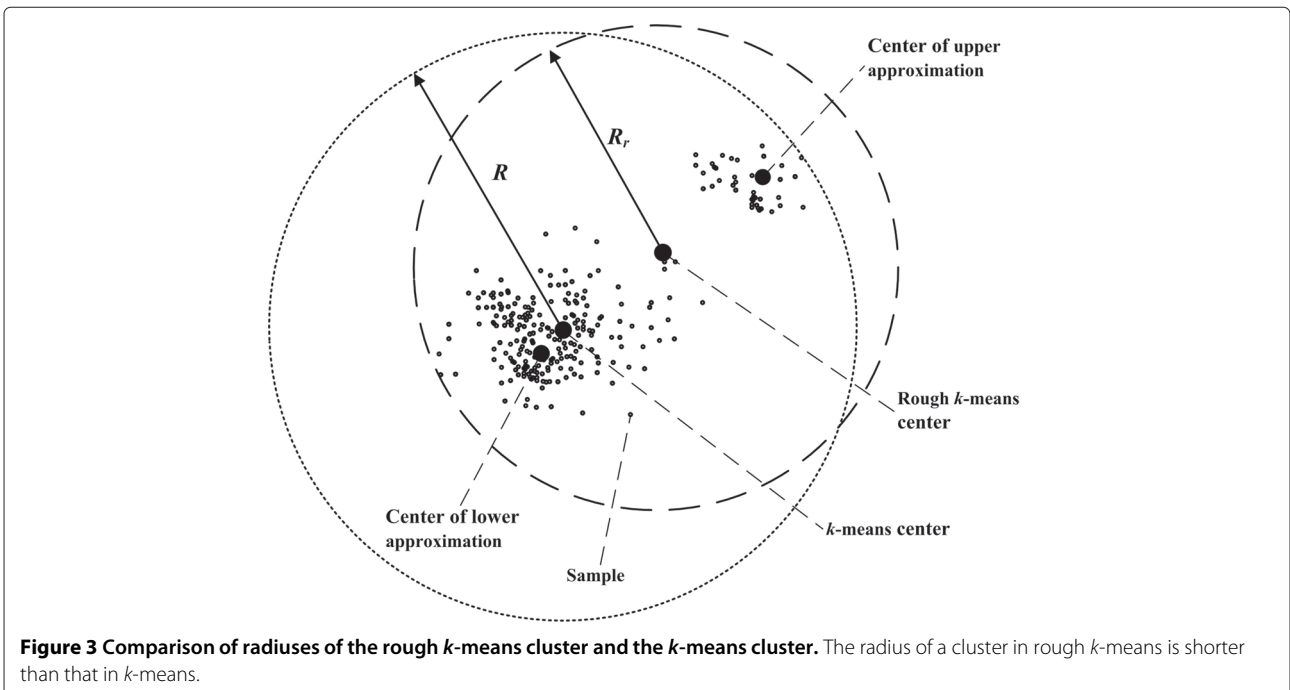


used to train the SVM in the advanced recognition. The uncertain boundary threshold  $R_{un}$  is defined as

$$R_{un} = \max(d_x) \quad (19)$$

where  $\max(d_x)$  is the distance from the farthest sample to the center.

In a cluster, The area beyond uncertain boundary ( $d_x > R_{un}$ ) is the uncertain area. When unknown samples are recognized, they will be distributed into the nearest cluster. If  $d_x > R_{un}$ , these samples will be further recognized by the advanced recognition. For other unknown samples, the result of the primary recognition will be final.



As the discussions in previous section, the  $k$ -means algorithm has some problems. The rough  $k$ -means method can solve the problems of nondeterminacy in clustering and reduce the effect of isolated samples [20]. But it still requires initial centers and the number of centers as priors. In addition, the choice of initial centers is very important for rough  $k$ -means. So the initial centers are usually determined by computing the least means square. In this article, we propose to determine the initial centers based on rough sets theory. Using this approach, the initial centers are computed based on the classification rules of rough sets. The process can be described as follows:

1. Classification rules are obtained based on the rough sets theory.
2. The mean value of every class is obtained.
3. Define the mean values as the initial clustering centers. The clustering number equals to the number of rules:

$$t_p = \frac{\sum_{x \in X_p} x}{\text{card}(X_p)} \quad (20)$$

where  $X_p$  denotes the set of samples in the classification rule  $p$  of the rough sets theory.

In (5), the parameter  $\lambda$  determines the lower and upper subject degree of  $X_k$  relative to some clustering. If the threshold  $\lambda$  is too large, the low approximation set will be empty, while if the threshold  $\lambda$  is too small, the boundary area will be powerless. Usually,  $\lambda$  is set to a value, which makes most samples in the lower approximation and the upper approximation not empty. The threshold  $\lambda$  can be determined by:

1. Compute the Euler distance of every object to  $K$  class clustering centers and distance matrix  $D(i, j)$ .
2. Compute the minimum value  $d_{\min}(i)$  in every row of matrix  $D(i, j)$ .
3. Compute distance between every object and other class center  $d(i)$  and  $d_t(i, j) = d(i) - d_{\min}(i)$ .

**Table 1 Information of known radar emitter signals**

No.	RF (MHz)	PRF (Hz)	ARR (round/s)	PW (us)	Type
1	6558	1319	2	1.61	1
2	5436	2530	1	0.62	1
3	1984	1276	2	0.99	2
4	3787	145	3	0.38	2
5	4406	601	2	0.34	2
6	7745	1698	3	3.81	3
7	3214	2083	2	0.71	3
8	2460	1793	2	1.33	3

**Table 2 Discrete information of known radar emitter signals**

No.	A	B	C	D	Type
1	3	2	2	2	1
2	3	3	1	1	1
3	1	2	2	1	2
4	2	1	3	1	2
5	2	1	2	1	2
6	3	2	3	3	3
7	2	3	2	1	3
8	1	2	2	2	3

4. Obtain the minimum value  $d_s(i)$  (except zero) in every row.
5.  $\lambda$  is chosen from the minimum value  $d_s(i)$ .

After that, known samples are clustered by using (5). The cluster centers  $C$ , the rough boundary  $R_{ro}$  and the uncertain boundary  $R_{un}$  are determined.

In addition, the primary recognition result is effected greatly by radiuses of clusters. Rough  $k$ -means clustering can lessen the radiuses of clusters effectively. As shown in Figure 3, the radius of  $k$ -means cluster is the distance from the cluster center to the farthest isolated sample. In the rough  $k$ -means, the cluster center is the average of the lower approximation center and the upper approximation center. The upper approximation center is near to the farthest sample. So the cluster radius of rough  $k$ -means  $R_r$  is less than the  $k$ -means radius  $R$ , obviously. As the radius is shorten, when unknown samples are recognized, the probability that an uncertain sample is recognized as a certain sample is reduced. Therefore, the accuracy of the primary recognition is increased.

**The time complexity of the hybrid recognition approach**

The time complexity of the approach proposed in this article consists of two parts, namely the time complexity of the primary recognition and the time complexity of the advanced recognition.

**Table 3 Knowledge rules**

No.	A	B	D	Type
1	3	2	2	1
2	3	3	-	1
3	-	2	1	2
4	-	1	-	2
5	-	-	3	3
6	2	3	-	3
7	1	-	2	3

**Table 4 Parameters in primary recognition**

Cluster	Center	$R_{ro}$	$R_{un}$
1	(6567,1324,1.650)	225	662
2	(5643,2569,0.520)	231	578
3	(2196,1534,1.142)	149	356
4	(3987,132,0.430)	130	407
5	(7845,1654,3.940)	465	913
6	(3213,2093,0.695)	200	466
7	(2459,1783,1.331)	128	401

In the training of the primary recognition, samples are clustered by using rough  $k$ -means. The time complexity of the rough  $k$ -means is  $\mathcal{O}(dmt)$ , where  $d$ ,  $m$ , and  $t$  denote the dimensionality of samples, the number of training samples and the iterations, respectively. In this article, the optimal initial centers are determined by analyzing the knowledge rule of the training sample set based on rough set theory, instead of iteration. Thus, the time complexity of the primary recognition is  $\mathcal{O}(dm)$ .

The SVM is used as the advanced recognition in our approach. The time complexity of SVM has nothing with the dimension of samples, but is related with the number of samples. The time complexity of SVM training is discussed with respect to the complexity of the quadratic programming. Standard SVM training has  $\mathcal{O}(m^3)$  time complexity [21].

In conclusion, the time complexity of our hybrid recognition is  $\mathcal{O}(dm) + \mathcal{O}(m'^3)$ , where  $m'$  denotes the number of training samples for SVM in the advanced recognition (After the primary recognition, the training samples for SVM is reduced). In general,  $\mathcal{O}(dm)$  is far less than  $\mathcal{O}(m^3)$ . Therefore, the time complexity of the hybrid recognition training is regard as  $\mathcal{O}(m^3)$ .

## Simulation results

### Data set description and experiment design

The validity and efficiency of the proposed approach is proved by simulations. In the first simulation, radar emitter signals are recognized. The type of radar emitter is the recognition result. The pulse describing words of

the radar emitter signal include a radio frequency (RF), a pulse repeating frequency (PRF), antenna rotate rate (ARR) and a pulse width (PW). 240 groups of data are generated on above original radar information for training, while 200 groups are generated for testing. This simulation is repeated 100 times, and the average recognition is obtained. Another simulation is adopted to test the efficiency of the hybrid recognition with the Iris data set. Iris data set contains 150 patterns belonging to three classes. There are 50 exemplars for each class and each input is a four-dimensional real vector [22]. The recognition accuracy and time complexity are compared between SVM and our approach. There are two parts in this simulation. In the first part, all 150 samples are used in training. And these 150 samples are used to test the training accuracy. In the second part, 60 samples from the Iris data set are used to train classifiers and other 90 samples are used for test. The generalization of the proposed approach is proved.

### Results of experiment 1: classification of the radar emitter signals

An information sheet of radar emitter signals is built, which is shown as Table 1. Data in the information table should be changed into discrete values, because continuous values cannot be processed by the rough sets theory. There are many methods for data discretization and here the equivalent width method [11] is adopted in this article. Based on the equivalent width method, the range is divided into intervals. Intervals of one attribute are of the same size and different attributes can have different numbers of intervals. In our article, attributes are divided into three intervals. The attribute values in the same interval have the same discrete value. The discrete information is shown in Table 2, where  $A$ ,  $B$ ,  $C$ , and  $D$  denote the attribute RF, PRF, ARR, and PW, respectively. After that, the dependent extent of radar type to each attribute is computed used (3).  $\gamma_A = \frac{7}{8}$ ,  $\gamma_B = \frac{7}{8}$ ,  $\gamma_C = 0$ , and  $\gamma_D = \frac{7}{8}$ . As the dependent extent of radar type to the attribute  $C$  (ARR) is 0, the attribute  $C$  is unnecessary for classification and removed. The knowledge rules are obtained. Table 3 shows these rules, where—denotes an any value. Some

**Table 5 Confusion matrices of radar emitter recognition**

	Subc. 1	Subc. 2	Subc. 3	Subc. 4	Subc. 5	Subc. 6	Subc. 7
Subclass 1	32	0	0	0	2	0	0
Subclass 2	0	36	0	0	0	0	0
Subclass 3	0	0	34	0	0	0	3
Subclass 4	0	0	0	33	0	0	0
Subclass 5	0	0	0	0	20	0	0
Subclass 6	1	0	0	0	0	18	0
Subclass 7	0	0	5	0	0	0	16

**Table 6 Results of radar emitter recognition methods**

Recognition method	Average recognition accuracy
RBF neural network	92.0%
RBF-SVM	92.5%
PSVM	94.0%
Method in this article	94.5%

radars have different operating modes and in different operating mode, the emitter signals parameters vary obviously. In the clustering of radar emitter signal samples, if cluster samples of one radar emitter into one cluster, that samples of the same radar may gather in several subregions in the cluster. The aggregation of the cluster would be reduced. Thus, we cluster the samples based on the subregions determined by using rough sets. The samples of three types of radar emitters are distributed into seven clusters.

Based on these knowledge rules, initial clustering centers are obtained using (20). The known radar emitter samples are clustered by using the rough  $k$ -means on these initial cluster centers. As shown in Table 4, 240 training samples are clustered into seven clusters. The cluster centers, rough boundary and uncertain boundary of the primary recognition are computed. The rough  $k$ -means classifier has been built.

The classification accuracy of each radar emitter is as the confusion matrices shown in Table 5. For example, row (1) indicates that on the 34 samples of the subclass 1, 32 have been classified correctly and 2 in subclass 5. The primary recognition accuracy is 86%. The advanced recognition accuracy is 92%. The number of samples that are falsely classified in uncertain areas is 18, while the total number of wrong classified samples is 28. As (18) described, the theoretical accuracy can be computed as:  $A_{total} = 86\% + 14\% \times \frac{18}{28} \times 92\% = 94.28\%$ .

The proposed method is compared with the RBF neural network studied by Zhang et al. [6], the RBF-SVM and the probabilistic SVM radar recognition approach studied by Lin et al. [8]. As shown in Table 6, the accuracy of the hybrid recognition proposed in this article is 94.5%, which is higher than existing methods, i.e., 92, 92.5, and 93%. The accuracy of the hybrid recognition from simulation experiments is close to the theoretical value, i.e., 94.28%.

**Results of experiment 2: classification of the data set Iris**

From Table 7, we can know the proposed approach has not only a higher recognition accuracy than SVM, but also high training accuracy and good generalization. In the first part of this experiment, all the 150 samples are used to train and test these two methods. The hybrid recognition proposed in this article has a high training accuracy, i.e., 99.33%, which is higher than SVM's, i.e., 98.67%. In the second part of this experiment, 60 samples are used as training samples, and other 90 samples are used to test SVM and the hybrid recognition. The recognition accuracy of the proposed approach is 97.78%, which can indicate the hybrid recognition has a good generalization.

In addition, let's compare the time complexities of SVM and the proposed approach. The time complexity of SVM is  $\mathcal{O}(m^3)$ , and that of the proposed approach is  $\mathcal{O}(m'^3)$ , where  $m$  and  $m'$  are the number of training samples for the SVM and the number of training samples for the SVM in the advanced recognition of the hybrid recognition, respectively.

When 150 samples are used as training samples, all of them are used to train the classical SVM.  $m = 150$  and the time complexity of the classical SVM is  $\mathcal{O}(150^3)$ . In our approach, training samples are clustered in the primary recognition, and only the rough samples are used to train the SVM in the advanced recognition. More specifically, there are 70 training samples for the SVM in the advanced recognition, i.e.,  $m' = 70$ , so the time complexity is  $\mathcal{O}(70^3)$ . Similarly, when 60 samples are used as training samples, all of these samples are used to train the classical SVM, while there are 36 training samples for the SVM in the advanced recognition of the hybrid recognition, i.e.,  $m = 60$  and  $m' = 36$ . So in the second part, the time complexity of the classical SVM is  $\mathcal{O}(60^3)$ , while the time complexity of the proposed approach is  $\mathcal{O}(36^3)$ .

From the comparison above, we can know that the time complexity of the hybrid recognition is obviously lower than the classical SVM.

**Conclusions**

In this article, a hybrid recognition method has been proposed to recognize radar emitter signals. The hybrid classifier consists of a rough  $k$ -means classifier (linear classifier) and a SVM (nonlinear classifier). Based on the

**Table 7 Recognition results of Iris**

Method	Recognition accuracy	The number of training samples for SVM	The time complexity
SVM in the first part	98.67%	150	$\mathcal{O}(150^3)$
Our method in the first part	99.33%	70	$\mathcal{O}(70^3)$
SVM in the second part	93.33%	60	$\mathcal{O}(60^3)$
Our method in the second part	97.78%	36	$\mathcal{O}(36^3)$



linear separability of the classifying sample, the sample is classified by the suitable classifier. Thus for the radar emitter sample set containing both linearly separable samples and linearly inseparable samples, the approach can achieve a higher accuracy.

A linear classifier based on the rough set and the rough  $k$ -means has been proposed, i.e., the rough  $k$ -means classifier. The rough  $k$ -means clustering can reduce the radius of the clusters and increase the accuracy of the primary recognition. The initial centers for the rough  $k$ -means are computed based on the rough set, which can reduce the time complexity of the rough  $k$ -means clustering. The rough  $k$ -means classifier can classify linear separable samples efficiently and pick up linearly inseparable samples. These linear inseparable samples are processed by the SVM in the advanced recognition. Therefore, the training samples for the SVM in the advanced recognition are reduced. Simulation results have shown that the proposed approach can achieve a higher accuracy and a lower time complexity, when compared with existing approaches.

The hybrid recognition approach in this article is suitable for the classification of the radar emitter signal sample set containing both linearly separable and linearly inseparable samples. We admit that our hybrid recognition approach is based on the fact that these linearly inseparable samples which reduce the accuracy of clustering are mostly at the edges of clusters. From (18), we know that if the linearly inseparable sample appears frequently in the center region instead of the edge, the accuracy of recognition will be reduced. How to solve this problem is the focus of our future study.

#### Competing interests

The authors declare that they have no competing interests.

#### Authors' contributions

ZW proposed the hybrid recognition model; ZY made the simulation; ZY improved the approach and provide the fund; HS and AN improved the method and revised the manuscript. All authors read and approved the final manuscript.

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