

MASSIVE GRAVITY WRAPPED IN THE COSMIC WEB

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ABSTRACT

We study how the filamentary pattern of the cosmic web changes if the true gravity deviates from general relativity (GR) on a large scale. The $f(R)$ gravity, whose strength is controlled to satisfy the current observational constraints on the cluster scale, is adopted as our fiducial model and a large, high-resolution N -body simulation is utilized for this study. By applying the minimal spanning tree algorithm to the halo catalogs from the simulation at various epochs, we identify the main stems of the rich superclusters located in the most prominent filamentary section of the cosmic web and determine their spatial extents per member cluster to be the degree of their straightness. It is found that the $f(R)$ gravity has the effect of significantly bending the superclusters and that the effect becomes stronger as the universe evolves. Even in the case where the deviation from GR is too small to be detectable by any other observables, the degree of the supercluster straightness exhibits a conspicuous difference between the $f(R)$ and the GR models. Our results also imply that the supercluster straightness could be a useful discriminator of $f(R)$ gravity from the coupled dark energy since it is shown to evolve differently between the two models. As a final conclusion, the degree of the straightness of the rich superclusters should provide a powerful cosmological test of large scale gravity.

Key word: large-scale structure of universe

1. INTRODUCTION

The deepest and most profound question in modern cosmology is what caused the universe to accelerate at the present epoch. Although the Planck mission team recently confirmed the stunning agreement between the predictions of the standard Λ CDM (cosmological constant Λ + cold dark matter) model and the cosmic microwave background temperature power spectrum measured with unprecedentedly high precision (Planck Collaboration et al. 2013a, 2013b), the notorious fine tuning problem of Λ still haunts cosmologists to vigorously look for alternative models. There have been two main directions in developing viable alternatives. One direction is to replace Λ with some dynamic dark energy with negative pressure that could induce the current acceleration of the universe without requiring fine tuned conditions (see Amendola & Tsujikawa 2010 for a comprehensive review). Among various dynamic dark energy scenarios, the coupled dark energy (cDE) model where a scalar field dark energy interacts with dark matter has been found to be quite promising because of its capacity to alleviate several reported tensions between the Λ CDM model and the observations (e.g., Baldi et al. 2011; Baldi 2012; Lee & Baldi 2012; Salvatelli et al. 2013).

The other main direction is to modify general relativity (GR) on a large scale which makes the concept of anti-gravitational dark energy unnecessary to explain the observed distance–luminosity relation of Type Ia supernovae (see Clifton et al. 2012 for a comprehensive review). The tremendous success of GR on the local scale, however, leaves only very little room for possible deviation of true gravity from GR. The $f(R)$ gravity (e.g., Hu & Sawicki 2007; Li & Barrow 2007 and references therein) is one of the few modified gravity models which has so far survived severe cosmological tests (Reyes et al. 2010; Wojtak et al. 2011). In this model, $f(R)$ represents an arbitrary function of the Ricci scalar R that is substituted for R in the Einstein–Hilbert action, and its derivative called the scalaron, df/dR , induces a fifth force on the large scale, the strength of

which is quantified by its absolute magnitude at the present epoch, $f_{R0} \equiv |df/dR|_0$ (Sotiriou & Faraoni 2010; de Felice & Tsujikawa 2010). An essential feature of $f(R)$ gravity is the presence of the chameleon mechanism that blocks the deviation of gravity from GR in a dense environment; the denser the environment is, the weaker the fifth force is (e.g., Khoury & Weltman 2004; Mota & Shaw 2007).

Although the abundance of galaxy clusters and the strength of their gravitational clusterings have been widely used as one of the most powerful probes of background cosmology (for a review, see Allen et al. 2011), these probes are unlikely to be efficient at discriminating modified gravity, since the galaxy clusters are usually located in highly dense supercluster environments where the chameleon effect should be very strong. A recent trend in the cosmological study of $f(R)$ gravity is to explore its effect on low-density regions and to figure out which observable among the low-density phenomena is the best indicator of $f(R)$ gravity. For instance, the dynamic mass of field galaxies, the spin parameters of dwarf void galaxies, the abundance of cosmic voids, etc., have been suggested as useful indicators of large-scale gravity (Zhao et al. 2011a; Lee et al. 2013; Clampitt et al. 2013).

Very recently, by analyzing the halo catalogs from N -body simulations, Shim & Lee (2013) showed that the degree of the straightness of rich superclusters changes significantly with the presence of cDE. Their results are summarized as follows. (1) The superclusters tend to be less straight in cDE models with stronger coupling. (2) The difference in the degree of supercluster straightness is much larger than that in the abundance of clusters (or superclusters) among different cDE models. (3) The difference is larger at higher redshifts. Shim & Lee (2013) provided the following explanation for their result: the fifth force generated by the coupling between dark matter and dark energy in cDE models plays a role in making the gravitational clustering of galaxy clusters less isotropic, which is best manifested by the straightness of the superclusters that correspond to the most prominent filamentary structures of the cosmic web.

It is intriguing to ask if the long-range fifth force generated by the scalaron in the $f(R)$ gravity model also affects on the supercluster straightness. In fact, given the results of Shim & Lee (2013), it is reasonable to expect that the superclusters should be less straight in $f(R)$ gravity models than in the GR model. The essential work to undertake here is to investigate quantitatively how sensitively the degree of the supercluster straightness is changed by the presence of $f(R)$ gravity, and to examine whether or not it would be powerful enough to distinguish $f(R)$ not only from GR but also from cDE.

The contents of the upcoming sections are outlined as follows. In Section 2, the data from N -body simulations for $f(R)$ gravity and the algorithms employed to determine the superclusters and their degree of straightness are briefly described. In Section 3, the main results concerning the dependence of the degree of supercluster straightness on the strength of $f(R)$ gravity are presented. In Section 4, we draw our final conclusion.

2. DATA AND ALGORITHM

To run an N -body simulation for a $f(R)$ gravity model, it is first necessary to specify the function $f(R)$. We adopt the following Hu–Sawicki model characterized by the two parameters n and c_1/c_2 (Hu & Sawicki 2007):

$$f(R) = -m^2 \frac{c_1(-R/m^2)^n}{c_2(-R/m^2)^n + 1}. \quad (1)$$

Here, $m \equiv 8\pi G \bar{\rho}_m/3$, where $\bar{\rho}_m$ represents the mean mass density of the universe at the present epoch. Following previous works (Oyaizu 2008; Zhao et al. 2011b), the two parameter values are set at $c_1/c_2 = 6\Omega_\Lambda/\Omega_m$ and $n = 1$. The comparison between the observed abundance evolution of galaxy clusters and the analytic mass function has yielded a tight constraint of $|f_{R0}| \lesssim 10^{-4}$ for the Hu–Sawicki $f(R)$ model (Schmidt et al. 2009; Lombriser et al. 2010). Given this cluster-scale constraint, we consider three models: GR and two $f(R)$ gravity models, F5 and F6, for which the value of $|f_{R0}|$ is set at 10^{-5} and 10^{-6} , respectively. Throughout this paper, GR represents the standard Λ CDM cosmology where the gravity is described by GR.

For each model, we run a large N -body simulation by employing the ECOSMOG code (Li et al. 2012b). The simulation contains a total of 1024^3 dark matter particles in its periodic box of linear size $1 h^{-1}$ Gpc. The initial conditions for each model are all tuned by setting the key cosmological parameters at $\Omega_m = 0.24$, $\Omega_\Lambda = 0.76$, $\Omega_b = 0.045$, $h = 0.73$, $\sigma_8 = 0.8$, and $n_s = 0.96$. The Amiga’s Halo Finder (AHF) code (Knollmann & Knebe 2009) is utilized to identify the bound halos from the spatial distributions of the dark matter particles. For a detailed description of the simulations and the halo-identification procedures, see Knollmann & Knebe (2009) and Li et al. (2012a, 2012b).

Two additional algorithms are employed for our analysis: the friends-of-friends (FoF) group finder and the minimal spanning tree (MST) algorithm. The former is used for the identification of the superclusters and the latter detects the interconnection among the member clusters of each supercluster. Both of the codes treat the cluster-size halos as particles without weighting them by their mass. In other words, no information on the masses of cluster-size halos is required to apply the two algorithms. Only the lower cut-off mass has to be specified when the cluster-size halos are selected (see Section 3). It is worth mentioning here that the AHF that is used to identify the bound halos is not appropriate to find the superclusters since the AHF is

basically a refined spherical overdensity algorithm (Knollmann & Knebe 2009), while the superclusters are well known to have filamentary shapes (e.g., Dekel et al. 1984; West 1989; Plionis et al. 1992; Jaaniste et al. 1998; Basilakos et al. 2001; Basilakos 2003; Einasto et al. 2007; Wray et al. 2006; Einasto et al. 2011).

The MST technique has been widely used to understand the interconnected structures of the cosmic web (e.g., Barrow et al. 1985; Krzewina & Saslaw 1996; Doroshkevich et al. 2001; Colberg 2007; Park & Lee 2009a, 2009b; Shim & Lee 2013). As mentioned in Shim & Lee (2013), its usefulness lies in the fact that it does not require that the underlying distribution of dark matter particles be known, and thus it can be directly applied to the observed spatial distributions of galaxies or clusters. In the following section, we describe in detail how the degree of supercluster straightness is measured from the data with the help of the above algorithms, and how it is different among the three models GR, F6, and F5. Five different epochs will be considered: $a = 1.0, 0.9, 0.8, 0.7, 0.6$, where a is the scale factor.

3. EFFECT OF $f(R)$ GRAVITY ON THE SUPERCLUSTER STRAIGHTNESS

We use the same procedures that Shim & Lee (2013) followed to determine the degree of supercluster straightness at each epoch for each model.

1. Select those halos with mass $M_c \geq 10^{13} h^{-1} M_\odot$ as the clusters and identify the FoF groups of clusters as the superclusters. As is conventionally done when marginally bound superclusters are identified as the FoF groups (e.g., Wray et al. 2006; Kasun & Evrard 2005; Lee & Park 2006; Lee & Evrard 2007; Shim & Lee 2013), the linking length is set at one third of the mean separation distance among the selected clusters.
2. Find the MSTs of those rich superclusters with $N_c \geq 3$, where N_c is the number of the member clusters (nodes), and prune each supercluster MST to determine its main stem, called a “spine” by Shim & Lee (2013).
3. Select only those rich superclusters with $N_{\text{node}} \geq 3$ after the pruning, where N_{node} denotes the number of the nodes that make up the spine of each supercluster.
4. Measure the size of each supercluster spine as $S = (\sum_{i=1}^3 (x_{i,\text{max}} - x_{i,\text{min}})^2)^{1/2}$ when the comoving Cartesian coordinates of a node, $\{x_i\}_{i=1}^3$, are in the range of $x_{i,\text{min}} \leq x_i \leq x_{i,\text{max}}$.
5. Determine the degree of straightness for each supercluster spine as its specific size, defined as $\tilde{S} = S/N_{\text{node}}$ by Shim & Lee (2013), and then take the average of \tilde{S} over all the selected supercluster spines.

Figure 1 plots the mass functions of the clusters (top panel) and the superclusters (bottom panel) at the present epoch ($a = 1.0$) for three different models. As can be seen, the mass functions have the highest amplitudes in the F5 model; meanwhile, there is almost no difference between the GR and the F6 cases. Table 1 lists the number of supercluster spines which consist of three or more nodes and the average values of their specific masses, defined as $M_{\text{spine}}/N_{\text{node}}$, where M_{spine} is the sum of the masses of all the nodes of a supercluster spine.

In Figure 2, the pruning process of a supercluster MST is depicted at $z = 0$ for the GR case in the two-dimensional plane projected onto the x_1 – x_2 plane. In the left panel, the solid line represents a supercluster MST before pruning and the dots

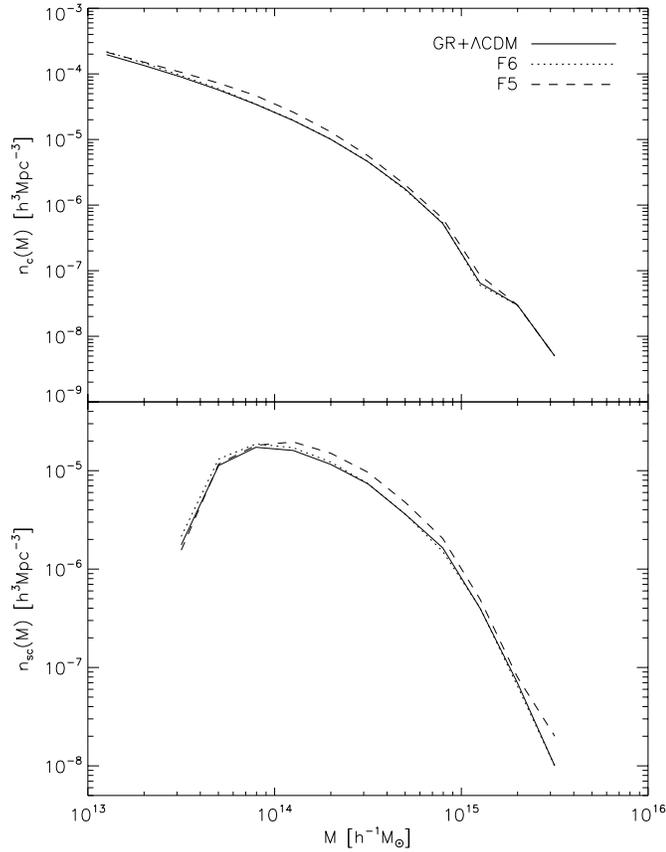


Figure 1. Mass functions of the cluster and supercluster halos at $z = 0$ for three different gravity models in the top and bottom panels, respectively.

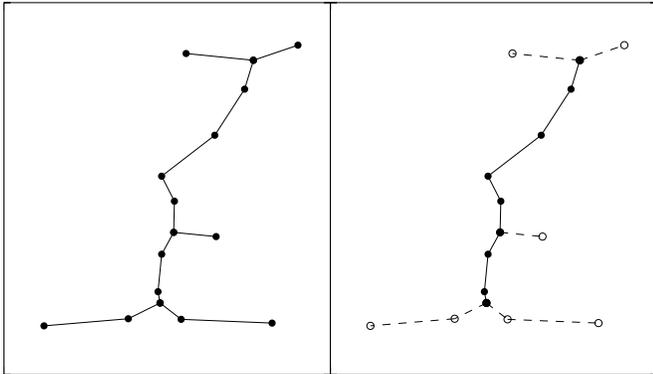


Figure 2. Pruning of a supercluster to determine its main stems (spine).

Table 1

Numbers of Those Supercluster Spines with Three or More Nodes and Their Mean Specific Mass for the Three Models

Model	N_{spine}	$\langle \tilde{M}_{\text{spine}} \rangle$ ($10^{13} h^{-1} M_{\odot}$)
GR	14204	3.92
F6	15260	3.80
F5	16592	4.18

connected by the solid line correspond to their nodes. In the right panel, the solid line corresponds to a supercluster spine (i.e., MST after pruning) while the dashed lines represent the minor branches pruned away from the MST. For a detailed explanation of the pruning process, please see Colberg (2007). Figure 3 plots the number distribution of the supercluster spines,

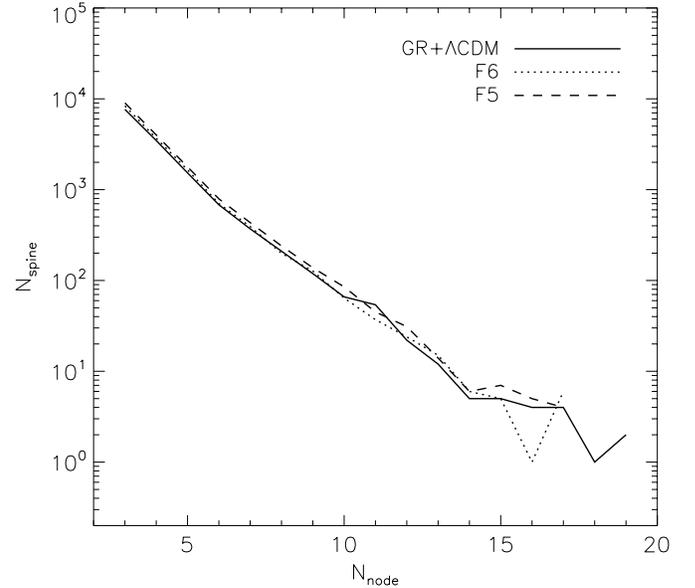


Figure 3. Number distribution of the superclusters as a function of node at $z = 0$ for three different models.

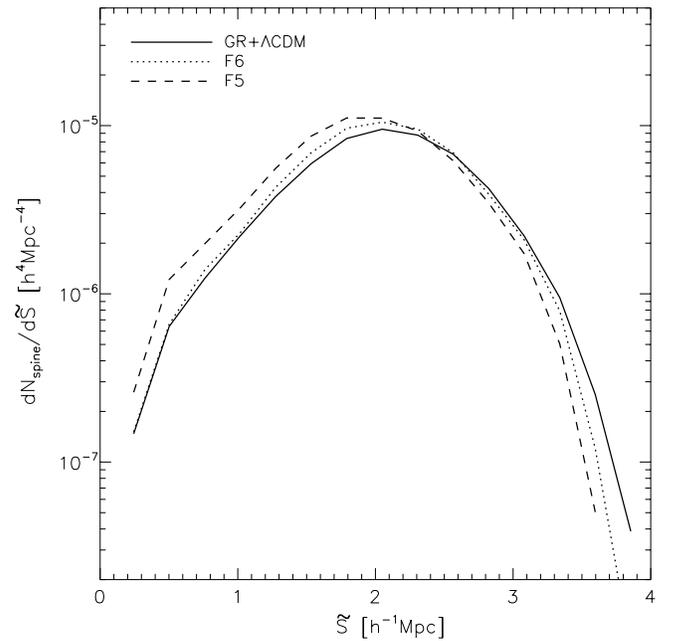


Figure 4. Specific size distributions of the superclusters at $z = 0$ for three different models.

N_{spine} , versus the number of nodes, N_{node} , at the present epoch for three models. The result shows that other than the numerical fluctuations, there is almost no difference in the node number distribution of the supercluster spines between the GR and F6 models, while the F5 model has a noticeably higher amplitude.

Figure 4 plots the specific size function, defined as $dN_{\text{spine}}/d\tilde{S}$ per unit volume, at the present epoch for the three models. As can be seen, there is a noticeable difference in the specific size function among the three models. The specific size function has the highest (lowest) amplitude in the GR (F5) case. Note that there is an appreciable difference in the specific size function even between GR and F6. The comparison with the results shown in Figure 1 reveals that the difference in the specific size functions among the three models is much bigger than that in the mass function of the superclusters. In other words, the specific

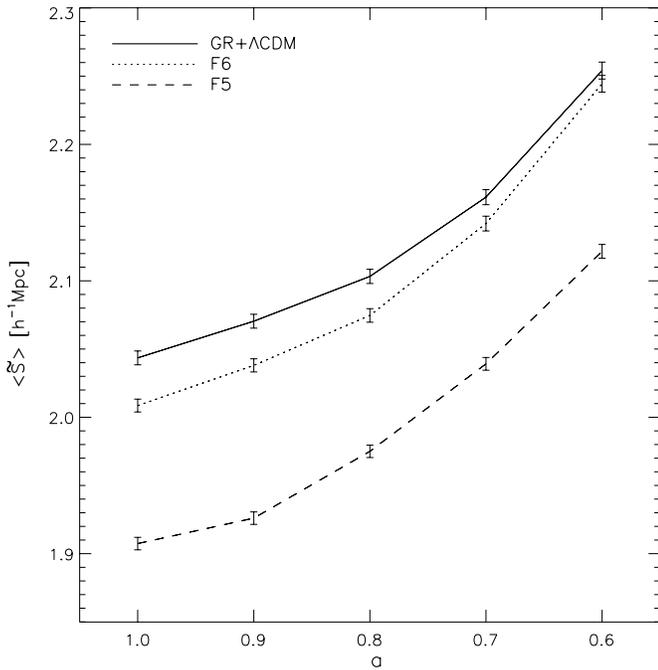


Figure 5. Evolution of the mean specific sizes of the superclusters with the scale factor a for three different models.

size function of the supercluster spine should be a much better indicator of large-scale gravity.

Figure 5 shows the average specific sizes of the supercluster spines versus the scale factor for the three models, demonstrating how $\langle \tilde{S} \rangle$ evolves in each model. The errors are calculated as one standard deviation in the measurements of the averages. As can be seen, the mean specific sizes of the superclusters in the GR (F5) model have the highest (lowest) values at all epochs. Note that there is a significant difference between the F6 and the GR models in the average specific size of the supercluster spines, although it looks small compared with the difference between the F5 and the GR models. This result implies that the degree of straightness of the superclusters should be useful as a new cosmological test of gravity.

Note also that the difference in $\langle \tilde{S} \rangle$ between the F6 and GR models increases as the universe evolves. In other words, the effect of $f(R)$ gravity on the degree of supercluster straightness becomes stronger as the universe evolves. It is interesting to compare this result with that of Shim & Lee (2013), according to which the effect of cDE on the degree of the supercluster straightness is stronger at earlier epochs (see Figure 8 in Shim & Lee 2013). Both the cDE and the $f(R)$ gravity have the same effect of lowering the degree of supercluster straightness but their evolution is directly opposite, which implies that the degree of supercluster straightness can be useful in distinguishing between the two models.

4. DISCUSSION AND CONCLUSION

A cosmological test of gravity has become a touchy topic. If an observable is to be regarded as powerful in testing gravity, then it should be sensitive enough not only to detect any little deviation of true gravity from GR, but also to discriminate the effect of modified gravity from that of other energy contents such as cDE, warm dark matter (WDM), etc. Since it has been shown by many authors that the linear growth factor $D(z)$ and the Hubble expansion rate $H(z)$ in modified gravity models

evolve differently from those in the standard Λ CDM or the dynamic dark energy models, much effort has been made to find observables which depend strongly on $D(z)$ and $H(z)$ (e.g., Linder 2005; Zhang et al. 2007; Huterer & Linder 2007; Wang 2008; Zhao et al. 2009; Song & Koyama 2009; Shapiro et al. 2010, and references therein).

Very recently, however, Wei et al. (2013) theoretically proved that it is practically impossible to distinguish among the scenarios of modified gravity, cDE, and WDM just by measuring $D(z)$ and $H(z)$, because the predictions of the three scenarios for the evolution of those two quantities are effectively identical (see also Wei & Zhang 2008). They called this degeneracy among the three scenarios the “cosmological trinity.” Given their claim, there is an urgent need for work to figure out which cosmological test has the power to break this inherent “trinity.”

Here, we have shown that the degree of supercluster straightness has the capacity to complete such a delicate mission. We have found that the superclusters are significantly less straight in $f(R)$ gravity models than in GR+ Λ CDM. This effect is shown to become stronger in models with larger values of f_{R0} . However, even the F6 model, which is almost indistinguishable from the standard GR+ Λ CDM model, exhibits an appreciable difference in the degree of supercluster straightness. The crucial implication of our result is that although the densities in the clusters are high enough to screen modified gravity inside the clusters, the intra-cluster force can still be unscreened.

A comparison of our results with those obtained by Shim & Lee (2013), that is, that the effect of cDE on the degree of supercluster straightness becomes stronger at higher redshifts, indicates that the degree of supercluster straightness can be useful for discriminating the effect of modified gravity from that of cDE. Although we have not investigated how the degree of the superclusters is affected in the WDM models, it is very likely that the presence of WDM would make the superclusters more straight. As discussed in Shim & Lee (2013), the high peculiar velocities of dark matter particles play a role in making the clustering of galaxy clusters more anisotropic. That is, the WDM would make the superclusters more straight than the CDM.

To use the degree of the supercluster straightness as a cosmological test of gravity, however, it would be much more desirable to have a theoretical framework within which the specific sizes of the supercluster spines could be evaluated for any cosmological models. Since we have obtained our results numerically from an N -body simulation which ran for a fixed model with specified values of the cosmological parameters, we do not know how much change it would cause to the degree of supercluster straightness if different initial conditions were used as the simulation inputs. Given that the size of the main stem of a supercluster may correspond to the free streaming scale of the member clusters which can be treated as particles, it might be possible to model how sensitive the free streaming scales of the clusters are to the initial conditions of the universe with the help of the Lagrangian perturbation theory.

We also mention that there is a good practical advantage of using supercluster straightness as a probe of gravity. Unlike the other cosmological probes based on galaxy clusters, such as the cluster mass function, two-point correlations of the galaxy clusters, etc., it does not require accurate measurements of the masses of the galaxy clusters, which are hard to achieve in practice. Once a sample of the galaxy clusters with masses larger than a certain threshold value is constructed, the only

information required to identify the superclusters and measure their straightness is the spatial positions of the sample clusters. Recently, a large sample of the galaxy clusters identified by the FoF algorithm from the Sloan Digital Sky Survey have been made available (e.g., Tempel et al. 2012). As mentioned in Shim & Lee (2013), once the redshift distortion effects are properly accounted for, our methodology can be readily applied to the observational data sets to determine the distribution of the supercluster straightness from the real universe. Our future work is in the direction of establishing a theoretical model for the distribution of the supercluster straightness and applying our technique to real observations.

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REFERENCES

- Allen, S. W., Evrard, A. E., & Mantz, A. B. 2011, *ARA&A*, 49, 409
- Amendola, L., & Tsujikawa, S. 2010, *Dark Energy* (Cambridge: Cambridge Univ. Press)
- Baldi, M. 2012, *MNRAS*, 420, 430
- Baldi, M., Lee, J., & Macciò, A. V. 2011, *ApJ*, 732, 112
- Barrow, J. D., Bhavsar, S. P., & Sonoda, D. H. 1985, *MNRAS*, 216, 17
- Basilakos, S. 2003, *MNRAS*, 344, 602
- Basilakos, S., Plionis, M., & Rowan-Robinson, M. 2001, *MNRAS*, 323, 47
- Clampitt, J., Cai, Y.-C., & Li, B. 2013, *MNRAS*, 431, 749
- Clifton, T., Ferreira, P. G., Padilla, A., & Skordis, C. 2012, *PhR*, 513, 1
- Colberg, J. M. 2007, *MNRAS*, 375, 337
- de Felice, A., & Tsujikawa, S. 2010, *LRR*, 13, 3
- Dekel, A., West, M. J., & Aarseth, S. J. 1984, *ApJ*, 279, 1
- Doroshkevich, A. G., Tucker, D. L., Fong, R., Turchaninov, V., & Lin, H. 2001, *MNRAS*, 322, 369
- Einasto, M., Liivamägi, L. J., Tago, E., et al. 2011, *A&A*, 532, A5
- Einasto, M., Saar, E., Liivamägi, L. J., et al. 2007, *A&A*, 476, 697
- Hu, W., & Sawicki, I. 2007, *PhRvD*, 76, 064004
- Huterer, D., & Linder, E. V. 2007, *PhRvD*, 75, 023519
- Jaaniste, J., Tago, E., Einasto, M., et al. 1998, *A&A*, 336, 35
- Kasun, S. F., & Evrard, A. E. 2005, *ApJ*, 629, 781
- Khoury, J., & Weltman, A. 2004, *PhRvD*, 69, 044026
- Knollmann, S. R., & Knebe, A. 2009, *ApJS*, 182, 608
- Krzewina, L. G., & Saslaw, W. C. 1996, *MNRAS*, 278, 869
- Lee, J., & Baldi, M. 2012, *ApJ*, 747, 45
- Lee, J., & Evrard, A. E. 2007, *ApJ*, 657, 30
- Lee, J., & Park, D. 2006, *ApJ*, 652, 1
- Lee, J., Zhao, G.-B., Li, B., & Koyama, K. 2013, *ApJ*, 763, 28
- Li, B., & Barrow, J. D. 2007, *PhRvD*, 75, 084010
- Li, B., Zhao, G.-B., & Koyama, K. 2012a, *MNRAS*, 421, 3481
- Li, B., Zhao, G.-B., Teyssier, R., & Koyama, K. 2012b, *JCAP*, 01, 051
- Linder, E. V. 2005, *PhRvD*, 72, 043529
- Lombriser, L., Slosar, A., Seljak, U., & Hu, W. 2010, *PhRvD*, 85, 124038
- Mota, D. F., & Shaw, D. J. 2007, *PhRvD*, 75, 063501
- Oyaizu, H. 2008, *PhRvD*, 78, 123523
- Park, D., & Lee, J. 2009a, *MNRAS*, 397, 2163
- Park, D., & Lee, J. 2009b, *MNRAS*, 400, 1105
- Planck Collaboration, Ade, P. A. R., Aghanim, N., et al. 2013a, arXiv:1303.5075
- Planck Collaboration, Ade, P. A. R., Aghanim, N., et al. 2013b, arXiv:1303.5076
- Plionis, M., Valdarnini, R., & Jing, Y.-P. 1992, *ApJ*, 398, 12
- Reyes, R., Mandelbaum, R., Seljak, U., et al. 2010, *Natur*, 464, 256
- Salvatelli, V., Marchini, A., Lopez-Honorez, L., & Mena, O. 2013, *PhRvD*, 88, 023531
- Schmidt, F., Vikhlinin, A., & Hu, W. 2009, *PhRvD*, 80, 083505
- Shapiro, C., Dodelson, S., Hoyle, B., Samushia, L., & Flaugher, B. 2010, *PhRvD*, 82, 043520
- Shim, J., & Lee, J. 2013, *ApJ*, 777, 74
- Song, Y.-S., & Koyama, K. 2009, *JCAP*, 01, 048
- Sotiriou, T. P., & Faraoni, V. 2010, *RvMP*, 82, 451
- Tempel, E., Tago, E., & Liivamägi, L. J. 2012, *A&A*, 540, A106
- Wang, Y. 2008, *JCAP*, 05, 021
- Wei, H., Liu, J., Chen, Z.-C., & Yan, X.-P. 2013, *PhRvD*, 88, 043510
- Wei, H., & Zhang, S. N. 2008, *PhRvD*, 78, 023011
- West, M. J. 1989, *ApJ*, 347, 610
- Wojtak, R., Hansen, S. H., & Hjorth, J. 2011, *Natur*, 477, 567
- Wray, J. J., Bahcall, N. A., Bode, P., Boettiger, C., & Hopkins, P. F. 2006, *ApJ*, 652, 907
- Zhang, P., Liguori, M., Bean, R., & Dodelson, S. 2007, *PhRvL*, 99, 141302
- Zhao, G.-B., Li, B., & Koyama, K. 2011a, *PhRvL*, 107, 071303
- Zhao, G.-B., Li, B., & Koyama, K. 2011b, *PhRvD*, 83, 044007
- Zhao, G.-B., Pogosian, L., Silvestri, A., & Zylberberg, J. 2009, *PhRvL*, 103, 241301