1	Formation and erosion of sediment cover in an experimental bedrock-alluvial
2	channel
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11 Abstract

Sediment grains in a bedrock-alluvial river will be deposited within or adjacent to a 12 sediment patch, or as isolated grains on the bedrock surface. Previous analysis of 13 grain geometry has demonstrated that these arrangements produce significant 14 differences in grain entrainment shear stress. However, this analysis neglected 15 potential interactions between the sediment patches, local hydraulics and grain 16 entrainment. We present a series of flume experiments that measure the influence of 17 sediment patches on grain entrainment. The flume had a planar bed with roughness 18 19 that was much smaller than the diameters of the mobile grains. In each experiment sediment was added either as individual grains or as a single sediment pulse. Flow 20 was then increased until the sediment was entrained. Analysis of the experiments 21 22 demonstrates that: 1) for individual grains, coarse grains are entrained at a higher discharge than fine grains; 2) once sediment patches are present, the different in 23 entrainment discharge between coarse and fine grains is greatly reduced; 3) the 24 sheltering effect of patches also increases the entrainment discharge of isolated 25 grains; 4) entire sediment patches break-up and are eroded quickly, rather than 26 through progressive grain-by-grain erosion, and 5) as discharge increases there is 27 some tendency for patches to become more elongate and flow-aligned, and more 28 randomly distributed across the bed. One implication of this research is that the 29 30 critical shear stress in bedrock-alluvial channels will be a function of the extent of the sediment cover. Another is that the influence of sediment patches equalises critical 31 shear stresses between different grain sizes and grain locations, meaning that these 32 factors may not need to be accounted for. Further research is needed to quantify 33 interactions between sediment patches, grain entrainment and local hydraulics on 34 rougher bedrock surfaces, and under different types of sediment supply. 35

37 **1. Introduction**

Semi-alluvial channels are identified by their predominantly bedrock channel 38 boundaries and partial alluvial cover (Turowski et al., 2008). The total extent of 39 sediment cover within a semi-alluvial channel is a function of the sediment supply 40 relative to transport capacity, although the exact form of this relationship is debated 41 (Sklar and Dietrich, 2004; Turowski et al., 2007; Chatanantavet and Parker, 2008; 42 Hodge and Hoey, 2012). The spatial arrangement of the sediment cover within the 43 channel is in turn the result of interactions between the bedrock topography, channel 44 45 hydraulics and sediment transport processes (Hodge et al., 2011; Nelson and Seminara, 2012; Inoue et al., 2014; Johnson, 2014; Zhang et al., 2015). These two 46 factors, the total extent and spatial arrangement of sediment cover, are inter-related 47 48 in ways that have yet to be investigated. As with alluvial bedforms, sediment patches can develop in response to boundary shape (analogous to 'forced' bars in alluvial 49 50 literature; Seminara 2010; described as externally controlled by Wohl, 2015) or as a result of the interactions between flow, bedform morphology and sediment transport 51 (equivalent to 'free' bars). To date, emphasis has been on how forced sediment 52 accumulations, whether due to irregular bedrock topography (Turowski and 53 Rickenmann, 2009; Siddigui and Robert, 2010; Hodge and Hoey, in revision) or large 54 immobile boulders (Carling and Tinkler, 1998; Carling et al., 2002; Chatanantavet 55 and Parker, 2008; Papanicolaou et al., 2012) affect flow and sediment cover. To 56 interpret sediment accumulation and erosion in natural channels (e.g. Hodge and 57 Hoey, in revision) which are always likely to have a component of morphological 58 forcing of sediment cover, understanding of how self-formed 'free' bedforms function 59 in semi-alluvial channels is required. 60

The location of a grain within a semi-alluvial channel can have a significant effect on 61 that grain's critical shear stress (τ_c) and hence the ease with which it is entrained by 62 the flow. Isolated sediment grains on a smooth bedrock surface can have values of 63 τ_c that are an order of magnitude less than comparable grains in an alluvial patch 64 (Hodge et al., 2011). This difference is the result of the differing pocket geometries 65 on grain exposure and pivot angle. Differences in roughness, and hence flow profiles 66 and local shear stress, over the alluvial and bedrock surfaces are also likely to 67 exacerbate differences in grain transport potential (Inoue et al., 2014; Johnson, 68 69 2014). The spatial pattern of roughness elements in semi-alluvial channels is very variable (Chatanantavet and Parker, 2008; Inoue et al., 2014), complicating attempts 70 to develop empirical relationships for controls over patch development. 71 Consequently, we focus here on sediment patches on planar, relatively smooth, 72 surfaces in order to isolate the effects of grain-scale interactions on patch 73 development and erosion. 74

75 From the perspective of grain geometry, the distribution of isolated grains and 76 sediment patches across a bedrock surface determines the distribution of τ_c for the population of grains (Hodge et al., 2011), and hence the sediment flux at low 77 78 discharges. At higher discharges when the applied shear stress (τ) is much greater than τ_c , all sediment will be fully mobile and the range of τ_c is no longer significant. 79 However, the typical lognormal distribution of flow events in a river combined with 80 low values of τ_c for isolated grains means that low flow events can have a more 81 significant impact on the total sediment flux than is the case in alluvial rivers with the 82 same sediment sizes (Lisle 1995; Hoey and Hodge, in prep). Theoretical modelling 83 has demonstrated that by distributing the same amount of sediment cover in different 84 ways (i.e. different proportions of grains in bedrock and alluvial positions) the 85

resulting average sediment fluxes range from less than to greater than the average sediment flux in a comparable alluvial river (Hoey and Hodge, in prep). An understanding of the development of sediment cover in semi-alluvial channels is therefore necessary in order to predict sediment fluxes in these systems.

There is little empirical data with which to constrain the most likely distributions of 90 sediment cover, however, previous research has identified some first order 91 tendencies. Higher values of τ_c for grains in alluvial patches are likely to produce a 92 net flux of grains from bedrock surfaces to alluvial patches (Nelson and Seminara, 93 2012). Sediment is thus most likely to form alluvial patches, with only a small fraction 94 of the grains remaining isolated on bedrock surfaces. This pattern is consistent with 95 field sediment tracer data (Hodge et al., 2011). The position and form of alluvial 96 patches will be controlled by both the underlying bedrock topography and 97 98 interactions between the patch roughness and the local hydraulics (Finnegan et al., 2007; Johnson and Whipple, 2010; Hodge and Hoey, in revision). Alluvial bedforms 99 100 such as pebble clusters affect the local hydraulics, causing a downstream separation zone and coherent flow structures with well-defined spatial characteristics (Strom 101 and Papanicolaou, 2007; Lacey and Roy, 2008). Similar processes will occur around 102 alluvial patches, amplified by the potential contrast in roughness between bedrock 103 and alluvial regions and the topographic expression of patches on a bedrock surface, 104 so affecting the growth and shape of the patches and local sediment transport. 105 Whether flow conditions are steady or varying, it is unclear how the bedforms 106 interact and whether these interactions are predominantly regenerative (maintaining 107 bedforms of a given size) or constructive (tending to merge bedforms into a smaller 108 number of larger features) (Kocurek et al., 2010). 109

To begin to address the issues raised above, in this paper we present results from 110 flume experiments on the development and erosion of sediment cover on a bedrock 111 surface. We simplify conditions to assess the fundamental process controls over free 112 bedforms, and use uniform channel width, slope and roughness. In each experiment, 113 a fixed volume of sediment was introduced at the upstream end of a flume with a 114 plane bed of constant low roughness, which resulted in sediment patches 115 developing. Once sediment cover had developed, flow was increased at a known 116 rate and the sediment cover was eroded. The aims of the experiments are to: 1) 117 quantify the impact of grain size and position on τ_c , which is recorded by the flow at 118 which different grains are entrained; and, 2) quantify patch geometry and how this 119 changes as patches are eroded. Results are reported from three sets of 120 experiments: Set 1, control experiments using single grains and no sediment 121 patches; Set 2 with a uniform coarse grain size; and Set 3 with different mixtures of 122 two uniform sediments, one coarse and one fine. 123

124 **2. Methods**

Three sets of experiments (Sets 1, 2 and 3; Table 1) were carried out in a 0.9 m wide 125 flume which has a working length of 8 m and maximum flow of 75 l s⁻¹. A flat plywood 126 bed was installed in the flume, with small-scale roughness added by fixing a layer of 127 < 0.5 mm sand to this using varnish. Flume slope was 0.0067 (Sets 1 and 3) and 128 0.0050 (Set 2). Uniform flow was established throughout the operational section at 129 the start of each run by setting discharge to be close to the sediment transport 130 threshold and adjusting the elevation of the flume tail gate until water depth was 131 constant through the measuring section. Under the initial low flow conditions, flow 132 depths varied from 9 to 40 mm. As flow increased, maximum flow depths were 133 between 50 and 80 mm. Flow properties vary according to the sediment cover on the 134

bed. With no sediment cover, flows across the experimental range of 8.5 to 40 I s^{-1} had a Froude number between 1.27 and 1.33, and Reynolds number of 9100 to 40300. As sediment patches develop, flow may become subcritical. Under the extreme condition of full sediment cover (which is more cover than seen in the experiments), flows from 5.4 to 33 I s⁻¹ have Froude numbers between 0.20 to 0.48 and Reynolds numbers from 5400 to 30300.

Figure 1 outlines the experimental procedure. Set 1 experiments (Table 1) were a 141 control to measure the entrainment threshold for the material used in later 142 experiments when introduced as single, isolated grains. Two very angular sediments 143 (0.2 on the Krumbein roundness scale; Krumbein, 1941) with uniform grain sizes 144 were used for the experiments. Coarse sediment (C) has $D_{50}=15$ mm and fine 145 sediment (F) has $D_{50} = 8.5$ mm. In each Set 1 experiment a single, randomly 146 selected, grain was placed on the centreline of the flume ~4 m from the flume 147 entrance and flow was increased until the grain was entrained. Fifty measurements 148 were made, twenty five with each of the fine and coarse grains. 149

In Set 2 and 3 experiments, a known volume of sediment was introduced at the initial 150 discharge, and allowed to developed patches of sediment cover in the measurement 151 section which extended from 5.5 to 5.8 m along the flume and across the entire width 152 of the flume (a total area of 0.27 m², determined by the video camera field of view). 153 Sediment cover in the measurement area was representative of that in the rest of the 154 flume. Furthermore, each experiment was repeated at least three times. The initial 155 discharge was maintained until there was little temporal variation in cover extent, 156 which typically took about 15 min to form. Sediment cover extent ranged from 13% to 157 23%. Flow was then increased at a rate of 1.2 I s^{-1} per minute until the maximum 158 159 capacity of the pump was reached to erode the sediment grains and patches. Patch formation and erosion was recorded by vertical video photography. Set 2 consisted of 21 repeat experiments each using 20 kg of coarse sediment C. Set 3 used the sediments C and F mixed in the following proportions (where the numbers refer to the percentage of each size fraction in the mixture): 100C, 75C/25F, 50C/50F, 25C/75F, 10C/90F and 100F. Each set 3 experiment used 6 kg of sediment, although the proportion of this that formed sediment patches the measuring section varied between runs. Up to 5 repeats were performed of each experiment in Set 3.

Two main approaches were used to analyse the video of the experiments in Sets 2 167 and 3. The first was watching the erosion of the sediment cover, and identifying the 168 169 time and hence discharge at which isolated grains, and those in patches, were eroded. Isolated grains were defined as being those with contact with ≤ 2 other 170 grains in Set 2, and as one grain diameter from any other grain in Set 3. These 171 different definitions reflect differences in the typical behaviour of the coarse and fine 172 grains. In runs with both coarse and fine grains, patches were classified by grain 173 sizes within the patch (coarse, fine or mixed). The analysis noted the time (and 174 hence discharge), of the first entrainment of isolated grains (defined as three grains 175 moving a distance of one or more grain diameters), and the first break up of a stable 176 177 alluvial patch. In Set 3, the timing of the entrainment of all grains within the imaged area was also recorded. In both sets grains entering the frame from upstream were 178 ignored. 179

The second analytical approach was to measure the sediment cover and the patch geometry. Stills from the videos of the experiments were analysed using two different methods. In the first, the software ImageJ (http://imagej.nih.gov/ij/index.html) was used to segment automatically the grains from the background using the Trackmate algorithm (Crocker and Grier, 1996). Isolated grains were manually identified, and

their areas calculated by the software. The algorithm results were visually assessed 185 to ensure that grains were being identified correctly. The segmentation algorithm 186 was applied to images of high flows over an empty bed to quantify phantom cover 187 caused by scattered light, and this amount of cover was removed from the total 188 calculated from subsequent images. In the second approach, grains were digitised 189 by manually marking the centre of every grain in the frame, and identifying whether 190 the grain was fine or coarse. Image aberration due to the water surface was not 191 explicitly accounted for because it was possible to visually identify the location of all 192 193 grains.. All grains within one grain diameter were identified as being members of the same patch, and isolated grains were those that were more than one grain diameter 194 from any neighbouring grain (Figure 1). 195

The two techniques give comparable estimates of the proportion of sediment cover, 196 197 with the RMS error between estimates from 65 frames being 0.026. The similarity between the two sets indicates that the automated segmentation techniques are 198 robust. In Set 2 experiments, changes in the proportion of sediment cover were 199 assessed in 142 frames using Image J. In Set 3 experiments, digitisation of grains 200 was carried out on twelve runs; two of each sediment mixture. For each run, frames 201 202 from one, five and every subsequent five minute interval after the onset of the flow increase were analysed. 203

A number of patch statistics were calculated from the digitised Set 3 images: dimensions, orientation and Ripley's *K* statistic. Patch dimensions were calculated using the Matlab function regionprops, which fits an ellipse with the same second moments as the patch area (where the second moment of an area reflects the distribution of material within the area), and provides the major and minor axis lengths and major axis orientation. This method takes into account all sediment

within the patch, rather than just at the extremes as a bounding box approach would 210 do, and provides an estimate of patch size that is less sensitive to patch shape. 211 Ripley's K statistic is a measure of how points are distributed across a surface, 212 describing whether points are more evenly distributed or more clustered than a 213 random spacing (Hajek et al., 2010; L'Amoreaux and Gibson, 2013). The K statistic 214 is calculated at a range of lags in order to identify whether the distribution changes 215 as a function of spatial scale. The statistic is estimated for lag r (defined here as a 216 number of grain diameters) using: 217

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$$\widehat{K}(r) = \frac{1}{\widehat{\lambda}N} \sum_{\substack{i=1\\i\neq j}}^{N} \sum_{\substack{j=1\\i\neq j}}^{N} w(s_i, s_j)^{-1} \partial_{ij}(r)$$
[1]

219 (Cressie, 1991; L'Amoreaux and Gibson, 2013) where *N* is the total number of 220 events in the study area, $\hat{\lambda}$ is the density of events in the study area, and s_i , s_j are 221 two different events within the area. The weighting factor $w(s_i, s_j)$ accounts for edge 222 effects and ∂_{ij} serves as a counting function being 1 when the distance between s_i 223 and s_i is \leq 1, otherwise $\partial_{ij} = 0$. *K* is then re-scaled using:

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$$\hat{L}(r) = \left(\hat{K}(r)/\pi\right)^{0.5} - r$$
 [2].

A spatially random distribution has $\hat{L}(r) = 0$ and values > 1 indicate more clustering and values < 1 more regular spacing, than a random distribution. A Monte Carlo approach is used to calculate a confidence interval for the K statistic. For each digitised image, 100 datasets with the same number of points as the image, but with the points at random locations are produced. *K* statistics at different spatial lags are calculated for these datasets, and the 2.5th to 97.5th percentile envelope of these lags produces a 95% confidence interval.

232 **3. Results**

3.1. Grain entrainment shear stress

Results of the conditions under which grain entrainment occurred are mainly 234 reported in terms of discharge, rather than shear stress. The shallow flow depths 235 236 relative to the grain size produced non-uniform flow over the sediment patches, meaning that du Boys' approximation of shear stress is not applicable for Sets 2 and 237 3. However, in Set 1 the single isolated grains did not significantly disrupt the uniform 238 flow in the flume, and so du Boys' approximation is valid. Flows were also too 239 shallow to measure local velocity profiles that could be used to calculate shear 240 241 stress.

Figure 2 shows the distributions of discharge at which isolated grains and alluvial patches first began to move in experimental Sets 1 and 2. In Set 1, fine and coarse isolated grains move at mean discharges of $5.8 (\pm 0.31) | s^{-1}$ (one standard error) and $8.3 (\pm 0.81) | s^{-1}$ respectively. These are equivalent to shear stresses of 0.95 (±0.02) and 1.12 (±0.05) Pa, and dimensionless shear stresses of 0.007 (±0.0002) and 0.004 (±0.0002). These entrainment discharges for the coarse and fine grains are significantly different (t-test, p = 0.007).

In Set 2, isolated coarse grains start to move at a discharge of 10 l s⁻¹, with coarse 249 grains in patches beginning to move at a significantly higher discharge of 21 l s⁻¹ (t-250 test, p <0.0001). Entrainment discharges of isolated coarse grains in Set 2 are higher 251 than for isolated coarse grains in Set 1, although this is not statistically significant (t-252 test, p = 0.057). This 20% increase in discharge between Sets 1 and 2 is equivalent 253 to approximately a 10% rise in shear stress (assuming that shear stress is 254 proportional to flow depth and that this scales with $Q^{0.5}$, and remembering that du 255 Boys' approximation cannot be applied to Set 2). 256

Distributions of entrainment shear stresses from Set 3 are shown in Figure 3. In 257 these boxplots, data from the different replicate runs are amalgamated. Such 258 amalgamation is supported by application of the Kruskal-Wallis test, which was used 259 to compare the entrainment discharge for grains of the same size and in the same 260 location between different replicates. In 6 out of the 23 combinations of sediment 261 mixture and grain position, there was no significant difference (p > 0.05) between 262 any of the different replicate runs. In 14 of the other combinations, application of 263 Tukey-Kramer revealed that within each set of replicates, only one distribution was 264 265 significantly different to the other ones.

In Set 3, across all sediment mixtures, fine grains in both isolated and patch 266 locations start to be entrained at a discharge of around 9 I s⁻¹ (Figure 3). Coarse 267 grains in isolated and patch locations show a similar behaviour when there is up to 268 269 50% fines in the sediment mixture, and this behaviour is comparable to the behaviour of the coarse grains in Set 2. However, when more than 50% of the 270 271 mixture is fine sediment, coarse isolated grains and coarse patches start to be entrained at higher discharges. Figure 3 also shows the variation in initial 272 entrainment between replicate runs. Across all sediment mixtures, isolated fine 273 grains have initial entrainment over a range of 3.6 I s⁻¹, whereas for coarse isolated 274 grains there is more variability and the range is 7.6 I s⁻¹. There is most variability in 275 the initial entrainment from fine and coarse patches, with ranges of 19.7 and 19.6 l s 276 ¹. Initial entrainment from mixed patches has similar values and range to that of 277 course isolated grains. Such variability in initial motion is consistent with that 278 observed in the field by Richardson et al. (2003). 279

280 Consolidating the above interpretation (Figure 3), the Kruskal-Wallis test indicates a 281 significant difference (p < 0.05) between the minimum discharges for different grain sizes and positions in runs 100C/0F, 10C/90F, 50C/50F and 25C/75F. Additional use of the Tukey-Kramer test confirms that the main differences are between patch and isolated grains. An alternative grouping of the data by grain size and location, and hence comparison between sediment mixtures, showed that the only significant variation in minimum discharge with sediment mixture is for coarse isolated grains.

In Set 3, grain size and location affects the discharge (value and variability) at initial grain entrainment. In contrast, the mean discharge at which grains are entrained is less variable between different grain sizes and locations. As before, there is most variation in the replicate runs for grains in fine and coarse patches. Grains in these patches are also the most affected by the composition of the sediment mixture; as the percentage of fines increases, the mean entrainment shear stress for grains in fine and coarse patches decreases and increases respectively.

Application of the Kruskal-Wallis test to the full distributions of entrainment 294 discharges for all mobile grains revealed that for each sediment mixture, there were 295 296 significant differences between grains in different locations ($p \le 0.02$). Further analysis with Tukey-Kramer revealed that in all cases the significant differences were 297 between grains in isolated and patch positions. For each sediment mixture, there 298 was no significant difference between the distributions of entrainment discharge for 299 coarse and fine isolated grains if both were present. For each mixture there was also 300 no significant difference between grains in the various types of patches, with the 301 exception of the fine and mixed patches in 10C/90F. 302

The analysis of sediment entrainment has demonstrated that: 1) the impact of grain size on entrainment discharge become less important once there are sediment patches present; 2) the presence of sediment patches increases the entrainment

discharge for isolated grains as well as for patch grains, indicating the impact of
patches on hydraulics; 3) grain location has a greater impact on the minimum
entrainment discharge than on the mean; and 4) fine and coarse patches become
relatively less and more stable respectively as the proportion of fines in the sediment
mixture increases.

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3.2. Erosion of sediment cover

The extent of sediment cover at steady state was an average of 22.4 (±0.24)% (one 312 standard error) in Set 2 experiments and 15.6 (±0.6)% in Set 3 experiments. In Set 3 313 runs, over 80% of initial sediment cover was in patches. This proportion decreased 314 as the sediment was eroded. In Set 3, the extent of sediment cover did not vary 315 systematically with the proportions of coarse and fine sediment, although the most 316 extensive covers were produced by mixtures of coarse and fine sediment. As 317 discharge increased, erosion decreased the areal extent of sediment cover. In Set 2 318 experiments, the total area occupied by patches remained approximately constant 319 until a discharge of $\sim 20 \text{ I s}^{-1}$, after which the area decreased approximately linearly. 320 Erosion of isolated grains commenced as soon as discharge began to increase, and 321 no isolated grains remained once discharge exceeded 25 I s⁻¹. Set 3 experiments 322 show a similar overall pattern, although the areal extent of patches begins to 323 decrease as soon as the discharge begins to rise rather than only after a threshold 324 value as in Set 2. As in Set 2, isolated grains in Set 3 are mostly removed by a 325 discharge of 25 I s⁻¹. In both Set 2 and Set 3, there is variability between runs, 326 reflecting specific grain arrangements that occurred as the patches developed. 327

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3.3. Sediment patch geometry

The digitised grain data from the Set 3 experiments show how patch geometry (number, area, orientation and elongation) changed during erosion (Figure 5). As the

patches are eroded, there is a systematic decline in the number of patches (Figure 331 5a), and the remaining patches become more flow-aligned (Figure 5c). In most runs 332 there is a concurrent decrease in patch area (Figure 5b), but this decrease is less 333 consistent between the different runs. Finer sediment mixtures tend to have more, 334 smaller, patches. Average patch elongation (major:minor axis length, Figure 5d) has 335 an initial value of 2.4 in all runs. As erosion occurs, elongation generally remains 336 between 2 and 3, apart from a small number of runs in which significantly more 337 elongate patches develop when discharge > 20 I s⁻¹. 338

Within-run analysis of these properties (Figure 6) shows considerable variability on 339 340 top of the trends in Figure 5. In some cases there is an observable change in the distribution of patch properties as discharge increases and patches are eroded 341 (Figure 6a and b); and in other cases the distributions remain the same (Figure 6c). 342 In most runs the size of the largest patch decreases with increasing discharge. 343 Changes in the distribution of patch orientation with increasing discharge are 344 statistically significant in four of the twelve digitised runs (p < 0.05; Kruskal-Wallis 345 test). Changes in the distributions of patch elongation and area were only each 346 statistically significant in one of the twelve runs (p < 0.05; Kruskal-Wallis test). There 347 348 is no systematic relationship between how patch properties change as patches are eroded, and the composition of the sediment mixture. 349

The decrease in number of patches and consistent patch area suggest that as the primary erosion mechanism is the removal of entire patches, rather than patches becoming smaller through erosion round the edges. The change in patch orientation indicates some preferential erosion and local reworking, with grains being removed from patch flanks and deposited in downstream lee locations. The heterogeneity of patch behaviour demonstrates the influence of patch position relative to other

patches, with sediment from upstream erosion potentially resulting in simultaneousaccretion and erosion.

The interactions between sediment patches and local hydraulics will affect the spatial 358 distribution of grains across the bed. This distribution is quantified using Ripley's L 359 statistic. At one minute into the increase in discharge, variations in L(r) as a function 360 of spatial lag (Figure 7) show that at lags equivalent to one or two coarse grain 361 diameters, values of L(r) are significantly negative. Such values indicate that grains 362 are more dispersed than a random distribution. This is partly because the diameter 363 of the grains determines the minimum distance between grain centres, whereas in 364 365 the random simulations there is no minimum distance between points. The result may also indicate that there is a minimum spacing between grains in the flume, i.e. 366 that grains are not in contact. For all sediment mixtures, at lags greater than about 367 368 three grain diameters, there is a rapid transition to significant positive L(r) values, indicating clustering of the grains in patches. 369

The distribution of L(r) changes as the sediment patches are eroded (Figure 8 and 370 Figure 9); examples are shown from 100C/0F and 50C/50F, but the overall trends 371 are common to all runs. As the patches are eroded, L(r) starts to decrease. In run 372 100C/0F (Figure 8), sediment grains are randomly distributed by 20 minutes into the 373 increasing flow regime. Run 50C/50F, shows the same trend for reduced clustering, 374 although the values of L(r) are still above the simulated confidence interval at 25 375 minutes. The reduction in L(r) starts at the larger lags, indicating that grains are 376 377 becoming less clustered at this spatial scale, but retaining their clustering at smaller scales. This suggests that the erosion of entire sediment patches dominates over 378 grain-by-grain erosion processes. If the latter process were dominant, L(r) would 379 380 decrease at smaller, as well as larger, lags. The interpretation of Figure 7, Figure 8

and Figure 9 is thus that there is clustering between the initial patches, but as erosion proceeds and patches are removed the spacing of the patches becomes more random. There are not, however, changes to the clustering of sediment grains within a patch.

385 4. Discussion

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4.1. Controls on grain entrainment

Data from the three sets of experiments show that when sediment patches are 387 present, the location of a grain in either an isolated or a patch position has a larger 388 impact on the discharge at which it is entrained than does its diameter (Figure 3). 389 390 The difference between isolated fine and coarse grains is far greater in the control experiments with single grains (Set 1) than in Set 3 when patches are present. 391 Furthermore, the presence of patches also affects the discharge at which isolated 392 grains are entrained, with isolated coarse grains being entrained at higher 393 discharges in Set 2 than in Set 1 (Figure 2). This small but notable effect is evidence 394 395 of the impact of sediment patches on hydraulic conditions across the measurement area. The impact of sediment patches is therefore twofold; grains in the patches 396 have an increased critical shear stress through the combined effects of changed flow 397 398 hydraulics and inter-grain friction, but isolated grains also have a reduced mobility as a result of the significant secondary effect of patches in changing the reach-scale 399 hydraulics. 400

The impact of patch formation may be greater for the fine isolated grains, as expressed by the proportionally larger increase in discharge between Sets 1 and 3 because their size makes them more likely to be sheltered from the flow by upstream patches. The spatially variable pattern of shear stresses experienced by the isolated grains which results from the arrangement of other grains on the bed is displayed in

406 the difference between the minimum and mean discharges at which isolated grains are entrained (Figure 3). In Set 3, isolated fine grains have the largest difference 407 between minimum and mean discharge, indicating that although many grains are 408 409 affected by the patches, some grains still occupy areas of the bed with similar hydraulics to those in Set 1. For the coarse isolated grains and all patches, there is a 410 smaller, but notable, difference between the minimum and mean discharges, 411 indicating that there is a similar level of local shear stress variation within the patches 412 as there is in the areas surrounding them. Furthermore, the mean discharges are 413 414 similar in all locations, meaning that once the impact of grain geometry is accounted for, the forces experienced by grains in a patch could actually be higher than those 415 experienced by isolated grains at the same discharge. This impact of the patch 416 417 geometry on the flow, and the overriding of grain size effects, is similar to that observed in steep channels with immobile boulders by Yager et al. (2012), who also 418 found that sediment patch grain size was not always a good predictor of sediment 419 420 mobility. The experiments also show that the sediment composition had an impact on the stability of fine and coarse patches, with patches being most stable when their 421 composition is most different to the bulk composition (e.g. fine patches are most 422 stable at 75C/25F). For fine grains, it follows that as the sediment coarsens, the 423 relative roughness of the bed will increase, and patches of fine sediment will become 424 425 relatively more sheltered. For coarse patches the phenomenon is harder to explain, as coarse grains will become relatively more exposed as the sediment mixtures fine, 426 but may be related to the tendency of the finer sediment to form more numerous, 427 smaller, patches (Figure 5), which may more consistently increase roughness across 428 the entire measurement area. 429

430 **4.2. Sediment cover and patch geometry**

As the sediment cover is eroded, sediment patches are removed through the erosion 431 of discrete patches, and the distribution of patches across the bed becomes more 432 random. There is also some evidence that patches become more elongate and 433 aligned with the flow direction. The interaction between patches is constructive 434 (Kocurek et al., 2010), and elements of merging, cannibalization and remote transfer 435 are all seen in our experiments. However, our experiments are limited to short 436 reaches and there is no upstream feed of sediment during erosion. Should a 437 continuous feed, at a rate equal to the erosion rate from the observed reach, be 438 439 introduced then regeneration and self-organisation of the bedforms may occur.

440 The form of the equilibrium between patch size, flow and sediment supply is likely to involve different bedform geometries under different boundary conditions (Nelson et 441 al., 2009; Dreano et al., 2010; Hodge, in press), so cannot be predicted from present 442 443 experiments. The process of patch removal suggests that patches may be sensitive to the entrainment of key grains, either in the patch or an upstream location, which 444 change the local hydraulics and/or grain geometry. Positive feedback by which the 445 erosion of grains destabilises surrounding grains means that a patch can be rapidly 446 removed, as has been reported for particle clusters in alluvial rivers (Strom et al., 447 448 2004; Tan and Curran, 2012; Heaves et al., 2014). Further analysis of the videos could attempt to identify the size and locations of these grains. 449

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4.3. Feedbacks between flow and sediment patches

The development and erosion of sediment patches is a function of the feedbacks between flow, bed morphology and sediment transport (Werner, 2003; Kocurek *et al.*, 2010). These experiments have demonstrated that under the idealised conditions in the flume, sediment patches can override the effects of grain size on grain entrainment, and can influence entrainment conditions in locations beyond the patch,

as well as within the patch itself. Consequently, the patches act to equalise the 456 development and erosion of sediment cover across a range of sediment mixtures. 457 The range of entrainment discharges demonstrated by both isolated and patch 458 grains indicates that the patches induce spatial variation in flow conditions, both 459 within and between the patches. As such these results provide some insight into the 460 mechanisms by which patches self-organise, and provide physical support for rule-461 based models that have demonstrated the formation of such patches and other 462 coarse bedforms (Werner and Fink, 1993; Hodge and Hoey 2010). 463

The observed impact of sediment patches on the critical grain entrainment discharge 464 465 might suggest that with continual sediment supply, extensive sediment cover can rapidly develop as a result of runaway feedback mechanisms (Chatanantavet and 466 Parker, 2008; Hodge and Hoey, 2010). Such cover does not occur in these 467 experiments because of the limited duration and volume of sediment input. The 468 erosion of sediment cover demonstrates the same mechanism in reverse, with rapid 469 470 destabilisation of sediment patches. These mechanisms suggest that bedrockalluvial rivers would tend to have binary sediment cover, with either limited or 471 extensive cover, in the absence of larger-scale roughness elements that drive forced 472 patch (bar) formation. 473

However, in these experiments, the bed developed a stable sediment cover of around 25% under the initial input conditions; the consistency between experiments in set 2 provides evidence that this was an equilibrium configuration. The development of this cover demonstrates that a relatively low spatial density of sediment grains is necessary to disrupt the hydraulics and create conditions suitable for the maintenance of that cover. This could suggest that under the limited and/or intermittent sediment supply common to many bedrock-alluvial rivers (Lague, 2010),

partial sediment covers may be common. This is further supported by the spatially 481 variable conditions induced by the sediment cover. The observed grain entrainment 482 will reflect the conditions of areas of the bed where grains were initially deposited, 483 i.e. those with lower flow velocities. The areas between the grains may be subject to 484 local flow acceleration as a result of grain blockages in other locations, which would 485 discourage deposition in these areas and the development of complete sediment 486 cover. Such preferential pathways for bedload transport have also been observed in 487 the field and flume under conditions of reduced sediment supply (Richardson et al., 488 489 2003; Nelson et al., 2009).

490

4.4. Implications for bedrock-alluvial rivers

These experiments demonstrate that even a relatively low density of sediment grains 491 can have a significant impact on flow hydraulics and sediment patch development. 492 493 Consequently, relatively small inputs of sediment into a channel could have notable impacts on channel roughness, flow and sediment transport. The importance of the 494 495 development of patches will depend on the channel topography, with patches being likely to have less of an impact in channels with a rougher bedrock topography 496 (Inoue et al., 2014; Johnson, 2014). Under rough topographies, sediment patch 497 development could instead smooth the channel bed, producing a different set of 498 feedbacks. However, even within a channel with a grain-rough (sensu Inoue et al., 499 2014) topography, there will still be areas of the bed that are locally flat at a scale 500 larger than that of the sediment grains, and in these locations the relationships these 501 experiments are likely to still apply. 502

These experiments have demonstrated that a single pulse of sediment can produce a partial sediment cover. There are questions as to how this behaviour upscales to a bedrock river with a fluctuating discharge and sediment supply. There are also

questions about the interactions between flow, sediment cover and sediment entrainment under conditions of greater partial cover. The extent to which sediment patches disrupt the flow is likely to be a non-linear process, with maximum disruption occurring once a large proportion of the bed is affected by the wakes from patches. As cover increases further, the bed will effectively become smoother again, reducing the disruption.

512 These experiments also have implications for predicting sediment transport in bedrock-alluvial rivers. The limited impact of grain size on grain entrainment in the 513 experiments with patches is consistent with previous observations that in channels 514 515 with partial sediment cover, sediment transport is independent of grain size (Hodge et al., 2011). In addition to potentially disregarding grain size, the experiments also 516 suggest that, in a mixture of isolated and patch grains, it may be appropriate to use a 517 single entrainment shear stress for both; however, this is not the case if the two 518 populations occur in distinct areas of the bed. The experiments do, however, suggest 519 that the magnitude of the critical shear stress will be a function of the extent of 520 sediment cover. 521

522 **5. Conclusions**

These experiments show that under idealised conditions (flat bed and maximum of 523 two grain sizes) the production and erosion of sediment patches on a flat surface is 524 affected by complex interacting processes. Isolated sediment grains away from the 525 influence of any other sediment are entrained at lower discharges than grains in 526 sediment patches. However, when sediment patches have formed in the flume, 527 isolated grains are entrained at a comparable mean discharge to grains in the 528 sediment patches. This is because of the influence of the sediment patches on the 529 530 local flow conditions.

The rate at which sediment patches are eroded as discharge is increased is approximately linear. The main reduction in sediment cover is through removal of entire patches, rather than grain-by-grain removal from patches. Sediment patches are reshaped as erosion progresses, becoming more flow orientated and sometimes more elongate. Grains are clustered at lags equivalent to a small number of grain diameters, but over time grain spacing at larger lags becomes more random.

Increasing understanding of the way in which sediment cover is produced and eroded on flat bedrock surfaces requires further research on the impact of sediment grains on the local flow, and consequent feedbacks on sediment transport processes. When there is an amount of sediment on the bed, these feedbacks appear to be the dominant control on patch stability, overriding the impact of grain size and whether grains are isolated or in a cluster.

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Experimental property	Set			
	1	2	3	
Sediment mixtures	Single grains C	100C	100C,	
	and F		75C/25F,	
			50C/50F,	
			25C/75F,	
			10C/90F &	
			100F	
Sediment size(mm)	Coarse = 15	Coarse = 15	Coarse = 15	

	Fine = 8.5		Fine = 8.5
Sediment mass supplied per	single grain	20	6
run (kg)			
Bed slope	0.0067	0.0050	0.0067
Flow rate during patch	n/a	7.5 – 8.5	8.8
development (I s ⁻¹)			
Flow depth (mm)	9 – 20 (F)	~30 (input)	~ 20 – 40
	15 – 35 (C)	~ 50 - 80	(input)
		(final erosion)	~ 50 – 80 (final
			erosion)
Time for sediment cover to	n/a	~15	~15
develop (min)			
Time for erosion (min)	n/a	~30	~30
Number of repeats	Coarse: 25	21	100F: 5
	Fine: 25		100C &
			10C/90F: 3
			Others: 4

Table 1: Properties for the experimental runs.



Figure 1: Outline of the experimental procedure used in all experiment runs. In Set 1, 658 individual grains were introduced, whereas in Sets 2 and 3 volumes of sediment 659 660 were added. Insets show examples of digitised grains, taken from video stills of the measurement area. A patch is defined such that all grains in a patch are less than 661 662 one grain diameter from a neighbouring grain. Different patches are shown with different colours, but colours are not consistent between time periods. Video stills 663 and proportion of sediment cover data are from a 50C/50F run. The inset photo is of 664 the bed at 1 minute into the increase in flow. 665



666

Figure 2: Distributions of discharges at which grains in Set 1 (n=25) and Set 2 (n=21) 667 experiments were entrained. Set 1 consisted of individual grains, whereas Set 2 668 comprised a mixture of isolated grains and sediment patches. For Set 2, the 669 discharge is that at which sediment started moving. Whiskers show 5th and 95th 670 percentiles, circles show minimum and maximum, and stars show mean. In Set 1 the 671 difference in entrainment discharge between fine and coarse grains is statistically 672 significant (t-test, 0.007), as is the difference between coarse isolated and coarse 673 patch grains in Set 2 (t-test, p < 0.0001). The difference between the entrainment 674 discharge for coarse isolated grains in Set 1 and Set 2 is not statistically significant 675 (t-test, p = 0.057).676



Figure 3: Distributions of discharges at which grains were entrained in Set 3 678 experiments. Data are grouped by sediment mixture, and grain size and location. 679 The box plots show the combined data from all replicates with that sediment mixture. 680 Whiskers show 5th and 95th percentiles, and black circles show maximum. Grey 681 crosses and squares respectively show minimum and mean values from individual 682 replicates; there is more variability for sediment in patches than for individual grains. 683 The Kruskal-Wallis test indicates a significant difference (p < 0.05) between the 684 minimum discharges for different grain sizes and positions in runs 100C/0F, 685 10C/90F, 50C/50F and 25C/75F. The Kruskal-Wallis test also shows that, for each 686 sediment mixture, there are significant differences between the full distributions of 687 entrainment discharges for grains in different locations ($p \le 0.02$). 688



Figure 4: Decrease in sediment cover with increasing discharge for experiments in a)
Set 2 and b) Set 3. In both, circles are cover from patches and triangles are cover
from isolated grains. Dashed line in a) shows a polynomial fit to the patch data.



Figure 5: a) Number of patches, b) mean patch area, c) orientation and d) elongation as a function of changing discharge for selected Set 3 experiments. Orientation is measured relative to the downstream direction: 90° is perpendicular to flow and 0° parallel to flow. Area is the total bed area containing all the patch grains, not just the area of the grains themselves, and so includes areas of exposed bed within the patch outline. Elongation is the ratio of the lengths of patch major to minor axes. Error bars are one standard error of the mean.



Figure 6: Examples of the changes in patch properties as a function of increasing
discharge. In a. and b. there is a significant difference between the distributions
(Kruskal-Wallis, p < 0.05). c. shows a representative example, but the differences
are not significant.



Figure 7: Values of Ripley's *L* at increasing spatial lags for the sediment grain 707 708 distributions one minute into the flow increase. Values greater than zero indicate greater clustering than random, and values less than zero indicate greater dispersion 709 than random. Solid line is for all grains. Fine line with short dashes is just fine grains, 710 fine line with large dashes is just coarse grains. Grey areas are a 95% confidence 711 interval, calculated from 100 repeat simulations with random spacing of n grains 712 (where n is the number of digitised grains). Grain diameter (D_c) is the coarse grain 713 diameter in all cases. 714



Figure 8: Values of Ripley's L(r) at increasing spatial lags for the sediment grain distributions at increasing discharge in run 100C/0F. See caption of Figure 7 for further information.



Figure 9: Values of Ripley's L(r) at increasing spatial lags for the sediment grain distributions at increasing discharge in run 50C/50F. See caption of Figure 7 for further information. Note different vertical axis scales in e. and f.