Quantification of Stereochemical Communication in Metal–Organic Assemblies

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Abstract: The derivation and application of a statistical mechanical model to quantify stereochemical communication in metal–organic assemblies is reported. The factors affecting the stereochemical communication within and between the metal stereocenters of the assemblies were experimentally studied by optical spectroscopy and analyzed in terms of a free energy penalty per “incorrect” amine enantiomer incorporated, and a free energy of coupling between stereocenters. These intra- and inter-vertex coupling constants are used to track the degree of stereochemical communication across a range of metal–organic assemblies (employing different ligands, peripheral amines, and metals); temperature-dependent equilibria between diastereomeric cages are also quantified. The model thus provides a unified understanding of the factors that shape the chirotopic void spaces enclosed by metal–organic container molecules.

By virtue of their hollow interiors, metal–organic container molecules[3] offer great potential for a range of applications,[2] including guest binding and separation, cavity-controlled catalysis, and stabilization of reactive intermediates. In contrast to the many enantioselective transformations catalyzed inside an enzyme’s (chiral) active site, in synthetic hosts the role of stereochemistry[4] has received little attention, with the focus mostly on controlling the size of the host cavity to steer guest binding or catalysis.[5] Reports addressing stereochemistry in metal–organic assemblies have so far mainly dealt with the synthesis of enantiopure cages,[5] (interconverting) diastereomeric species,[6] stereochemical switches,[7] enantioselective catalysis,[8] or guest binding.[9]

To emulate the enantioselectivity displayed by enzymes, insights into the conditions under which chiral ligands induce the formation of an enantiopure metal–organic self-assembled capsule are required. Such rules can guide the design of new container molecules offering enantioselective guest binding or catalysis, and may have implications for the understanding of the origin of biological homochirality.[10] A quantitative analysis based on statistical mechanics has proven useful in the description of chiral amplification in covalent and supramolecular polymers.[11]

The present work provides a quantitative description of the degree of stereochemical information transfer within discrete metal–organic cages. Building upon the pioneering work of Piguet on quantifying subtle thermodynamic effects in the self-assembly of polynuclear complexes,[12] we develop a simple statistical mechanical model that quantifies the effects of various factors, such as the choice of metal, chiral residue, ligand length, and temperature. We start with the phenomenon of amplification of stereochemical information as previously observed in a Fe₆L₆ cage with a strong preference to have all metal centers with the same all-Δ configuration.[13] We then examine this phenomenon in related tetrahedral cages with different metals, ligand lengths, or geometries (Figure 1). We also apply the model to the temperature-dependent diastereomer distributions in tetrahedral cages with weaker stereochemical coupling between metal centers.

Sergeant-and-soldiers experiments (Figure 1, top), involving the substitution of residues of achiral amine a within a racemic Fe₆L₆ cage (2a; Figure 1, bottom) with increasing amounts of a more nucleophilic enantiopure amine (S)-b, resulted in the quantitative induction of a single stereochemical configuration at all Fe³ centers before 100% (12 equiv) of the chiral amine was added, as monitored by the chiroptical response.[13] This effect was shown to be enhanced in the cage with respect to a related mononuclear complex (1a) as a result of stereochemical coupling between metal centers in the cage.

To devise a statistical model to quantify this effect, we separate the two ways in which stereochemical information can be amplified in multimolecular structures. First, at each metal center, intra-vertex amplification can manifest itself when fewer than three chiral amine residues suffice to quantitatively induce a single Δ or Δ stereoconfiguration. Second, inter-vertex communication: the mechanical connection between metal centers by rigid ligands allows stereochemical information to be relayed between vertices in the framework.[14] As a result, the configuration at one metal center can influence or even dictate the configuration of its neighbors. The resulting model is a finite Ising system with...
quenched field disorder controlled by the distribution of chiral amines. Related models\cite{15} have been used to describe the binding of ions to polyelectrolytes\cite{15a,b} and cooperativity in supramolecular chemistry.\cite{15c}

We consider first the case of a mononuclear ML\textsubscript{2} complex which we treat as a two-state system with Δ and Λ states, where Δ is the preferred configuration for all (S)-chiral amines in this work.\cite{13} Taking the Δ state as reference, an (S)-amine attached to a Λ center incurs a free energy penalty, denoted \( f_1 \), in units of the thermal energy \( k_B T \) (where \( k_B \) is the Boltzmann constant). The \( f_1 \) value quantifies the strength of coupling between carbon and metal stereocenters. We treat each amine in a given metal coordination sphere as acting independently, and we take the probability of substitution as equal for all amines in the system.

For tetrahedral cages, we treat each of the four metal centers as a two-state system, as in the mononuclear case. Now, however, there is also inter-vertex communication, as a result of the preference of a ligand to have the same stereoconfiguration at its two ends in a given structure. Taking the Δ and Λ states of a ligand as the reference, we quantify the inter-vertex stereochemical coupling through the parameter \( f_2 \), defined as the free energy of the Δ and Λ states, divided by \( k_B T \). The total dimensionless free energy of a given tetrahedral complex is a multiple of \( f_1 \) plus a multiple of \( f_2 \) depending on the number and location of chiral amines, and the stereoconfiguration at each of its metal centers.

A Boltzmann-weighted average over all stereoconfigurations yields the overall fraction \( x_\Lambda \) of Δ centers in an equilibrium solution of the cages (see Section S3.1 in the Supporting Information). The value of \( x_\Lambda \) depends on the parameters \( f_1 \) and \( f_2 \), providing a physical interpretation of the populations of Δ and Λ centers observed in experiments. For given values of \( f_1 \) and \( f_2 \), the model predicts how the excess chirality (i.e., the relative excess of Δ over Λ metal centers) increases with the fraction \( s \) of substituted amine. Plots of chiral excess as a function of \( s \) approach a limiting form as the \( f_1 \) and \( f_2 \) values become large, that is, the shape of the curve eventually becomes insensitive to the precise values of \( f_1 \) and \( f_2 \) (see Section S3.2).

We first apply the model to analyze sergeant-and-soldiers experiments,\cite{13} which started either with a racemic Fe\textsubscript{III}L\textsubscript{2} complex (1a), or with the racemic cage Fe\textsuperscript{III}L\textsubscript{4} (2a), and to which different amounts of (S)-amine were added (see Section S2 in the Supporting Information). We examined three chiral amines, (S)-b,\cite{13} (S)-c, and (S)-d\cite{16} (Figure 1, bottom), to differentiate between the abilities of the amines to induce a single-metal stereochemical configuration, as expressed by the \( f_1 \) value. Figure 2A shows how the excess chirality, as probed by circular dichroism, varied with the amount of added amine. In these plots, both the experimental
and fitted curves have been renormalized to 1 at a chiral amine concentration of 100% (see Section S3.3). Values of $f_i$ were obtained by least-squares fitting to data from experiments with the $\text{Fe}^\text{II}\text{L}_3$ complexes (Figure S1). These values were then fixed and used in a second fit to the experimental data obtained for the related $\text{Fe}^\text{II}\text{L}_4$ cages (Figure S4), to obtain an $f_2$ value for each cage (Figure 2E).

The model accounts well for the shape of the experimental curves (Figure 2A). The $f_i$ values of 38, 0.90, and 1.4 obtained for amines (S)-b, (S)-c, and (S)-d, respectively, highlight the much stronger ability of amine (S)-b than amine (S)-c in controlling the configuration at the metal center. The free energy penalty of 38kT for (S)-b lies in the limiting regime of a large $f_i$ value, where the sergeant-and-soldiers effect is overwhelming and the chiroptical response is insensitive to the exact value (Figure S8). Between (S)-c and (S)-d, (S)-d exhibited a stronger ability to control the configuration at the metal center, which we attribute to the greater bulk of the side group (cyclohexyl versus isopropyl). We infer that both steric and $\pi$-stacking effects between phenyl and pyridyl rings are responsible for the strong influence of amine (S)-b upon the metal-centered configuration.

Using the $f_i$ values from the $\text{Fe}^\text{II}\text{L}_3$ complexes, experimental data could be fitted for the $\text{Fe}^\text{II}\text{L}_4$ cages 2b and 2c; precipitation during the substitution of cage 2a with (S)-d precluded sergeant-and-soldiers studies with this amine. In these cages the $\text{Fe}^\text{II}$ vertices are held together by the same ligand so similar $f_i$ values are expected as $f_i$ measures the ligand’s ability to mediate stereocchemical communication between the individual metal centers (as explained above). Gratifyingly, the values of $f_2$ for cages 2b and 2c of 0.40 and 0.51, respectively, are similar. We attribute the small difference between the two values to uncertainty in fitting experimental data and to small differences in cage geometry as a result of the different amines.

Next, the effect of metal choice on the degree of amplification was studied by performing substitution experiments with (S)-b on the $\text{Co}^\text{II}$ and $\text{Zn}^\text{II}$-containing analogues of the $\text{Fe}^\text{II}\text{L}_3$ complex 1a (namely 3a and 4a) and the $\text{Co}^\text{II}$-templated analogue of the $\text{Fe}^\text{II}\text{L}_4$ cage 2a (namely 5a; for each metal the chiroptical data were normalized at a different parameter of 1.5, which is significantly higher than the value of 0.55 for the corresponding $\text{Co}^\text{II}\text{L}_4$ cage 5b (Figure 2E). We infer that the tritopic ligands have a strong “gearing” effect within the rigid structure, forcing the four metal centers in the cage to adopt a homochirally pure $\Delta$ state. This strong inter-vertex stereocchemical coupling has been shown to enable stereocchemical memory in a $\text{Fe}^\text{II}\text{L}_4$ cage.

In addition to analyzing the transmission of stereocchemical information in all-$\Delta$ or all-$\Lambda$ cages, we have also applied our model to a set of racemic $\text{Fe}^\text{II}\text{L}_4$ cages (9–12; Figure 1) that have been previously observed to form heterochiral species. These assembled from ditopic achiral ligands (that is, with $f_1 = 0$) based on terphenyl linkers with different methylation patterns. Cages 9–12 were found to exist in solution as an equilibrium between homochiral $T$ ($\Delta\Delta\Delta\Lambda\Lambda\Lambda\Lambda\Lambda\Lambda\Lambda$), heterochiral $C_1$ ($\Delta\Delta\Delta\Lambda\Delta\Delta\Delta\Lambda\Lambda\Lambda$), and achiral $S_1$ ($\Delta\Delta\Delta\Lambda\Lambda\Lambda\Lambda\Lambda\Lambda\Lambda$) diastereomers. Moreover, variable-temperature NMR studies revealed these equilibria to be temperature-dependent.

The model can be employed to make a direct prediction of universal curves for the equilibrium distribution of the three diastereomers as a function of $f_i$ value (Figure 3). We have placed the temperature-dependent distribution of diastereomers for cages 9–12 on these curves by finding the point on the $f_i$ axis where each set of three yields fits best. There is no guarantee that an arbitrary set of three diastereomer fractions could be consistently placed on the curves. Hence, the observation that all data sets, apart from those for cage 9, can be superimposed on the plot provides strong support for the underlying model. The behavior of the four cages is very different. Cage 11 has strongly negative values for $f_i$ ($< -2$), indicating that the ligand prefers to connect two metal centers of opposite handedness, thus favoring the $S_1$ diastereomer (wherein four of the six ligands link metal centers of opposite configuration). Cage 10 shows the opposite behavior: the
homochiral T diastereomer is favored by the positive $f_2$ value (about 0.9 at room temperature). However, raising the temperature decreases the $f_2$ value, thereby increasing the proportions of the $S_1$ and $C_3$ diastereomers at the expense of the $T$ diastereomer. For cage 12 the $f_2$ value was found to be close to 0 (independent of the temperature), resulting in a nearly unbiased statistical distribution (which would be 1:4:3 for $T:S_1:S_3$). For cage 9 some discrepancies between the data and the model were observed for the $S_1$ and $C_3$ diastereomers. However, its behavior can still be characterized by the moderately positive $f_2$ value of 0.35 that slightly favors the $T$ diastereomer.

The direction and sensitivity of the change in $f_2$ value with respect to temperature are determined by the sign and magnitude of the enthalpic contribution to the free energy. The enthalpic and entropic contributions to $f_2$ can be extracted by a Van’t Hoff type analysis and can be shown by our model to relate to all three of the pairwise equilibria\[10\] between the $T$, $S_1$, and $C_3$ states (see Section S6 in the Supporting Information). The generally good agreement between the separatedly determined entropies and enthalpies and those derived from our model further validates the applicability of the model, providing a unifying understanding of the equilibria. Apart from the case of cage 9, we found that it is entropically favorable to have opposite stereocentra at the two ends of each ligand, even when that combination is enthalpically unfavorable.

Our statistical mechanical model thus accounts for the specific nonlinear response of excess chirality in metal–organic tetrahedra due to stereochemical communication within the structures. For the first time for metal–organic cages, the effect of structural features on the degree of stereochemical communication has been quantified in terms of two energy parameters with clearly defined physical meanings, and an overarching description of the temperature-dependent equilibrium between diastereomeric cages has been provided. The general nature of the model allows for its extension to new cage geometries[90] and related structures, such as metal–organic frameworks.\[90] We anticipate that the physical insight our model provides into the nuanced stereochemistry of the chiroptical cavities of these structures will translate into control over stereoselective guest binding and catalysis.\[10,\[90,\[91\]

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Keywords: cage compounds · diastereoselectivity · statistical mechanics · stereochemical communication · supramolecular chemistry

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Figures

**Figure 3.** Experimental diastereomer distribution and predicted distribution as function of the $f_2$ value (diastereomers: $T$ = black; $C_3$ = red; $S_1$ = blue) for cage 9 (●), 10 (○), 11 (△), and 12 (▲). Arrows indicate increasing temperature.

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