

Transferability of Policies to Control Agricultural Nonpoint Pollution in Relatively  
Similar Catchments

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30 nitrate pollution (NP) in two relatively similar mixed farming Scottish catchments with a  
31 diffuse nitrate pollution problem, the Motray and Brothock.

32

33 At present a variety of policy mechanisms to achieve GECS are being assessed by UK  
34 regulators. Since cost-effectiveness is a WFD criteria and there is evidence of the cost-  
35 effectiveness of economic instruments in the literature (see below), regulators have  
36 considered the role economic instruments can play (NERA, 2006). However, concerns exist  
37 over the environmental effectiveness, transactions costs and political acceptability of  
38 economic instruments to reduce nutrient pollution. Thus presently, regulators have employed  
39 a range of managerial controls (regulatory codes of good practice, general binding rules, best  
40 management practices etc.), including limits on fertiliser applications and timings, limitations  
41 on stocking rates etc. (under various cross-compliance schemes).

42

43 There is a growing consensus among UK policy makers/regulators<sup>1</sup> (DEFRA, EA and SEPA)  
44 and catchment stakeholders (rivers trusts, farmers' unions etc.) that a one size fits all  
45 agricultural diffuse pollution policy for catchments characterised by different agricultural  
46 systems, weather patterns etc. is inappropriate and cost-ineffective. However, unfortunately  
47 the high transaction costs of formulating and enforcing catchment specific policies may also  
48 be arguably prohibitively expensive. Thus recent and on going research in the UK<sup>2</sup> has  
49 focused on identifying cost-effective policies that can be applied to similar catchments, i.e.  
50 with similar agricultural systems, weather patterns and hydrogeology.

51

52 Economists have undertaken numerous single catchment studies to assess the cost-  
53 effectiveness of instruments to control NP. Yet, for practicality and wider consistency,  
54 regulators are looking for cost-effective policies that are in general consistently efficient

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<sup>1</sup> Department for Environment, Food & Rural Affairs (DEFRA), Environment Agency (EA) and Scottish Environment Protection Agency (SEPA).

<sup>2</sup> E.g. DEFRA's Demonstration Test Catchment research platform.

55 across relatively similar water bodies<sup>3</sup>. We investigate the characteristics and consistency of  
56 policies, in particular mixed instruments, to control NP in two relatively similar catchments.  
57 The transferability of cost-effective policy instrument rankings across catchments is not  
58 something economists have addressed conclusively as previous cross catchment studies  
59 have been limited by their realism, modelling assumptions, simulated regulatory policies  
60 and/or ability to model farmer's response to them.

61  
62 Moreover, cost-effective instrument ranking has not always been consistent in the empirical  
63 literature. This inconsistency could be attributed to differences in biophysical economic  
64 modelling sophistication, realism, assumptions (scale, resolution, fate, transport and  
65 hydrological modelling, heterogeneity, soil dynamics, livestock management, crop rotations,  
66 input substitution, transformation of regulatory concentration standards into load (mass)  
67 equivalents, farmer's behavioural response options etc.), economic incentives (prices,  
68 subsidies etc.), regulatory restrictions, geophysical catchment characteristics (Martinez and  
69 Albiac, 2004), and/or importantly the catchment weather patterns that drive the stochastic NP  
70 processes etc. In considering the stochastic nature of NP studies have made different  
71 distributional assumptions in estimating deterministic equivalents in chance-constrained  
72 optimisation models. Such differences affect the cost-effectiveness of regulatory instruments  
73 and render a comparison of NP policies in separate studies inappropriate, e.g. it is not  
74 meaningful to compare results of a study in semi-arid Spain (Martinez and Albiac, 2004) or  
75 California (Larson et al., 1996) with a high rainfall UK catchment (Kampas and White, 2004).  
76 Thus, in this research the modelling, assumptions and policy options were kept consistent  
77 enough to compare two separate catchments that differ in terms of scale, soils, crop  
78 rotations, arable to grassland ratio, agricultural activities, diffuse pollution levels, and

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<sup>3</sup> The high transaction costs/political acceptability of tailoring policies to individual catchments necessitates this. Moreover, in practice operational EU "river-basin areas" can be considerably larger, e.g. Scotland comprises of only two river-basin (Scottish-Government, 2015).

79 importantly weather – but not drastically. Thereby allowing a meaningful comparison to help  
80 identify consistently cost-effective instruments across two relatively similar<sup>4</sup> catchments.

81  
82 By using nonlinear stochastic biophysical economic modelling this paper 1) examines the  
83 cost-effectiveness and transferability of policies to control NP in two relatively similar  
84 catchments based on estimates of daily river concentration (mg/L) for 10 continuous years;  
85 2) accounts for physical mixing, retention and lags in the diffuse pollutant transport process  
86 without assuming an underlying pollutant distribution - which is likely to distort instrument  
87 cost-effectiveness; 3) investigates the characteristics of mixed instruments (MI), comprising  
88 of economic instruments and managerial/regulatory controls, that make them more suited to  
89 being applied across catchments; and; 5) estimates pollution swapping (or substitution) of  
90 catchment phosphorus (P) and potassium (K) consumption from implementing policies to  
91 control NP. This is important as farmer's response to regulation may have unintended  
92 consequences and actually prevent attaining GECS.

93

## 94 **2. Previous Work**

95 Past research on the economics of NP control has largely focussed on single instrument  
96 policies and concluded that economic instruments are generally cost-efficient under a range  
97 of restrictive conditions (Balana et al., 2011; Shortle and Horan, 2001; Weersink et al., 1998).  
98 Previous studies have also detailed the efficiency gains of using policies that combine two or  
99 more economic incentives to control NP. However, in practice the information, monitoring  
100 and enforcement transaction costs of such policies have prevented their uptake. One study  
101 reported the superiority of MI in 'wet weather' conditions and improvements in their relative  
102 cost-effectiveness at higher regulatory targets (RT) under 'mean weather' (Aftab et al., 2010).  
103 These results were based on weekly averages of NP for just one representative 'wet' and  
104 'mean' year's weather, which may not realistically capture the stochastic nature of NP over

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<sup>4</sup> Identifying a set of relatively similar catchment characteristics that ensure the cost-effective transferability of policies is beyond the scope of this study. This would require an assumptions/methodologically consistent analysis of numerously more catchments with different characteristics.

105 time. This paper improves on these limitations and uses more realistic modelling  
106 assumptions to determine whether the cost-effectiveness of MI and other policies across  
107 relatively similar catchments is consistent and thus more broadly implementable.

108

109 Previous large-scale studies have provided valuable insights and modelled catchments by  
110 using either an econometric or applied general equilibrium approach. However, both  
111 approaches have their limitations. Econometric studies have been limited by: extremely  
112 broad classifications of land use incapable of differentiating between crops, grassland,  
113 livestock or setaside etc. (Langpap et al., 2008); unrealistically large land units of  
114 assessment (Wu et al., 2004); not permitting land use to change in response to policies  
115 (Fezzi et al., 2010). While an applied general equilibrium approach requires numerous  
116 simplifying assumptions, such as arbitrarily converting the loads of different pollutants into  
117 one generic nutrient unit (Brouwer et al., 2008). A few cross catchment comparison studies  
118 have used a biophysical economic modelling approach. These have been limited by: the  
119 absence of livestock and manure management (Brady, 2003); a simple linear economic  
120 model and infeasible high transaction costs policies (Volk et al., 2008); very small study  
121 areas as well as the assumption that livestock types and amounts remain constant (Vatn et  
122 al., 1997)<sup>5</sup>. More importantly, these studies estimate average pollutant loads<sup>6</sup> and do not  
123 consider pollutant concentration, river mixing and the probability of achieving a concentration  
124 standard with a specific certainty as well as its impact on the cost-effectiveness of policies.  
125 Most assume an arbitrary average annual load reduction equates to compliance with an  
126 environmental concentration standard. Pollutant loads are not necessarily reliable proxies for  
127 concentration and environmental impact. There is a trade-off between the complexity/realism  
128 and the scale of modelling (Brady, 2003). Generally, an econometric approach is restrictive  
129 in: capturing diffuse pollution processes; the type of policies that can be simulated and the  
130 ability to model farmers' behavioural response to policies. Whereas landscape scale

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<sup>5</sup> It compares annual pollutant loads in two catchments with a combined area of 4313ha.

<sup>6</sup> Although Volk et al. estimate the concentration of total N they do not report how the stochastic variation impacts on the cost-effectiveness of policies (Volk et al., 2008).

131 biophysical economic approach is more interdisciplinary, data intensive and, as discussed  
132 earlier, involves assumptions that can vary across studies and affect the cost-effective  
133 rankings of policies.

134

135 Most of the diffuse water pollution chance constrained (stochastic), biophysical economic  
136 literature (Elofsson, 2003; Milon, 1987) involves imposing a deterministic equivalent on the  
137 optimisation problem by assuming that the distribution of pollution estimates are normal  
138 (Gren et al., 2000), log-normal (Kampas and White, 2004) or truncated normal (Kataria et al.,  
139 2009). The normality assumption is motivated by the central limit theorem, i.e., the statistics  
140 of sample loads will asymptotically converge to a normal distribution, while the log-normality<sup>7</sup>  
141 and truncated normal assumption is justified by the need to avoid the possibility of negative  
142 pollution loads. Alternatively, a distribution-free approach uses the Chebyshev's inequality to  
143 approximate the probabilistic constraint (Wets, 1983). The literature is inconclusive and often  
144 contradictory as to which distribution should be used. Besides probabilistic programming  
145 models are sensitive to such distributional assumptions (Gren et al., 2002; Kampas and  
146 White, 2004; Xu et al., 1996; Zhu et al., 1994). More recent research has estimated that the  
147 assumed distribution can bias results by as much as 60% (Kataria et al., 2009). Moreover, a  
148 review of environmental data concluded there was little support for a general use of either  
149 the log-normal or normal distribution (Reimann and Filzmoser, 2000).

150

151 Although numerous studies have investigated controlling P (Goetz and Keusch, 2005; Iho  
152 and Laukkanen, 2012; Johansson et al., 2004; Schleich et al., 1996), and the joint  
153 management of P and nitrogen (N) pollution has been conceptually considered (Heathwaite  
154 et al., 2000), few empirical studies have used detailed biophysical economic modelling to  
155 consider the trade-off between their consumption (Kampas et al., 2002; Vatn et al., 1997).  
156 We consider the consequences of policies to control diffuse N pollution on farm P and K

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<sup>7</sup> A 'theory of successive random dilutions' attempts to explain how lognormal distributions may arise from physical processes responsible for generating pollutant concentrations in the environment (Ott, 1990). However, more recent work by the US EPA has confirmed that such environmental datasets are not necessarily lognormally distributed (Simon, 2014).

157 consumption. Coordinating policies targeted at different agricultural externalities is critical  
158 (Aftab et al., 2007). This also emphasises the importance of attaining a final ecological  
159 outcome, the stated WFD intention, instead of realising a specific nutrient standard. K, unlike  
160 N and P, is not usually a limiting macronutrient in rivers and less likely to contribute to  
161 eutrophication. However, the amount of K in rivers is known to play a role in species  
162 composition and impact river ecology, even though previous studies have highlighted the  
163 possible contribution of elevated K to river eutrophication (Czernas, 1978; Leentvaar, 1980).

164

### 165 **3. Study Area**

166 The relatively similar catchments are approximately 39.03km apart and share reasonably  
167 similar farming practice, weather, ground water base flow and comparable soil profiles (table  
168 1). The Motray is entirely underlain by lavas and tuffs, rising to over 300 m, with lower areas  
169 mantled by fluvioglacial deposits. While the Brothock is underlain mostly by a permeable  
170 geology of sandstones in the lower areas, supporting fertile soils and mixed farming, while  
171 the upper catchment, rising to 150 m, is underlain by lavas and supports a mix of rough  
172 grazing and forestry. The catchments suffer from low flow in summer from surface water  
173 potato irrigation. Both catchments are also in Nitrate Vulnerable Zone (NVZ)<sup>8</sup> designated  
174 areas and infrequent SEPA spot sampling indicates a risk of exceeding the WFD nitrate  
175 standard from NP (see 4.4). Information on catchment crops, rotations, tillage and livestock  
176 was collected from Scottish Agricultural College regional field agronomists as well as surveys  
177 of farmers in the catchments.

178

### 179 **4. Biophysical Economic Modelling**

#### 180 *4.1 Farming Activities*

181 Six main arable crops (winter wheat, spring barely, winter barley, winter oilseed rape, ware  
182 potatoes and seed potatoes), seven different livestock types (dairy, sheep, lowland suckler  
183 and four types of beef cattle), and three types grasslands (permanent grazing grass,

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<sup>8</sup> NVZ require a maximum of 250kg N/ha/yr of organic manure and 170kg N/ha/yr averaged over the farm; fertiliser management plans and restrictions on the storage/application of slurry.



184 temporary grassland (silage) and hay) were modelled<sup>9</sup>. Crop-soil specific production  
185 functions were derived from the literature (Chambers and Johnson, 1990). Farms also had  
186 the option to purchase silage from the market. Livestock waste is accounted for as a source  
187 of N, P and K on grassland and relevant farm subsidies (e.g. Scottish Beef Calf Scheme),  
188 were included. Potatoes are the only irrigated crop and the variable costs of contracting the  
189 supply of irrigation water is incorporated. Catchment agronomic practices and parameters,  
190 crop rotations and the existing baseline scenario were taken from the literature and  
191 catchment farm survey data. Field level crop data for both catchments were collected from  
192 the IACS-SAF database (2000-2010) while livestock numbers were based on lower  
193 resolution parish level data (2008-2010). Approximately 150 crop rotations in each catchment  
194 were considered. For practical reasons these were simplified to catchment specific crop-pair  
195 rotations. Crop-pairs account for the N applied to both crops in a two crop rotation. The  
196 Motray was modelled as 34 crop-pair and the Brothock as 33 catchment specific crop-pair  
197 rotations for each of the three catchment specific soil types. Considering the previous crop in  
198 the rotation accounts for soil N dynamics (Martinez and Albiac, 2004).

199

#### 200 *4.2 Farming Heterogeneity*

201 The Motray's (4743 ha) and Brothock (3580 ha) was modelled as 5 and 7 farms respectively.  
202 The farms represent hypothetical aggregated land use categories since individual farm data  
203 are not made available due to confidentiality concerns. They denote heterogeneity in farming  
204 practice across catchments in terms of farming knowledge, experience, spatial  
205 characteristics, preferences and capital/infrastructure considerations etc. (Wossink et al.,  
206 2001). These heterogeneous farms differ in terms of acreage, distribution of soil types, crop  
207 mix, crop rotations, livestock types, stocking densities, arable to grassland ratios, amount of  
208 non-agricultural sources of NPS nitrate pollution from forestry, rough grazing and urban  
209 areas (FRU). Modelling farm heterogeneity allows more realistic approximation of farms'  
210 responses to regulatory policies, especially since farming practice is notoriously varied.

211

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<sup>9</sup> Spring oats, a relatively minor crop, was the only catchment crop that as not modelled. Note all crops are conventionally tilled.

### 212 4.3 Pollutant flux

213 Fluctuations in daily river N concentrations are driven by temporal interactions between farm  
214 management practices, stochastic weather patterns and crop growth demands. The link  
215 between land use and nitrate run-off was simulated using NITCAT (DEFRA, 2001).  
216 Regressing the N load estimates of catchment specific crop/soil combinations against a  
217 range of nitrogen input levels provided nitrogen leaching functions. Three separate soil  
218 classes for each catchment were determined based on HOST<sup>10</sup> classification, profile water  
219 column, and representative soil type. Daily water balance was calculated for 4 catchment-  
220 specific crop transitions (crop-pair rotations) using the IRRIGUIDE model (Bailey and  
221 Spackman, 1996) for 10 years from 1985/6 to 1993/4<sup>11</sup>. Four water balance classes  
222 appropriately approximated reality without excessively complicating the aggregation of  
223 estimates at the catchment scale. Each crop-pair was assigned to the most appropriate  
224 water balance class.

225  
226 Daily time series of water balance and nitrate loss from soils units via rapid (shallow) and  
227 slow (deep) drainage pathways were routed using the EvenFlow (Anthony et al., 2009)  
228 model. EvenFlow is a semi-distributed, catchment scale, conceptual model of effective  
229 rainfall delivery to a river system by building on: SLIMMER (Anthony et al., 1996), an elution  
230 model; a crop water use/drainage model based on elements of the MORECS (Field, 1983)  
231 and IRRIGUIDE (Bailey and Spackman, 1996) models, and crop-soil specific leaching  
232 functions from NITCAT. This framework simulates a daily time-series of river flow and  
233 nitrate-N concentrations and was validated by the EUROHARP project (DEFRA, 2005). Soil  
234 retention, transfer delays and mixing of base flow helped reproduce the river hydrograph and  
235 concentrations resulting from mixing the two drainage pathways. Although sewage inputs  
236 were not considered emissions from FRU were factored. This framework<sup>12</sup> estimated daily

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<sup>10</sup> Hydrology of Soil Types classification of the soils of the UK, assigns soils to classes on the basis of their physical properties and their effects on the storage and transmission of soil water (Boorman et al., 1995).

<sup>11</sup> This time period afforded the best river flow, river N sampling and continuous weather data in both catchments.

<sup>12</sup> Further details of the modeling framework can be found in the online appendix at [WEB ADDRESS](#).

237 average nonpoint N pollution in the river for 10 years of continuous weather in each  
238 catchment.

239

#### 240 *4.4 Water quality calibration*

241 Infrequent spot ambient water quality sampling by SEPA reveals that the EU nitrate standard  
242 is breached around 49% of the time in the Motray (Figure 1). However, since this includes  
243 contribution from sewage treatment works and other sources not captured by our modelling  
244 this figure is likely to overestimate agricultural NP. Moreover, in-stream measurements may  
245 also overestimate actual pollution because there is a bias towards sampling in winter months  
246 that are more prone to diffuse N peaks. Brothock sampling revealed the standard is violated  
247 approximately 11% of the time. Generally, the simulated baseline provides a reasonable fit to  
248 the actual data, especially the winter patterns, which are more likely to violate the nitrate  
249 standard. Comparing SEPA's actual river concentration data with the distribution of modelled  
250 river concentration (Figure 2 with Figure 1) suggests the modelled data reproduces key  
251 features of the river's actual N concentration distribution. Moreover, simulated hydrograph  
252 peaks and troughs reasonably matched actual in-stream flow patterns. Overall considerable  
253 effort was made to improve the realism of the biophysical catchment processes relative to  
254 previous studies.

255

#### 256 *4.5 Underlying pollutant distribution assumption*

257 We do not assume any underlying distribution and instead empirically estimate the  
258 distribution of daily river N concentration using 10 years' continuous weather data.  
259 Generating a large sample of river concentration under different regulatory policies provides  
260 a more realistic approximation of the natural variability in the stochastic diffuse pollution  
261 process (formation, transport and fate) in each catchment. This way we avoid any bias in the  
262 ranking of regulatory instruments from imposing distributional assumptions about the  
263 pollutant. We also compared the nonparametric kernel density of the empirical (modelled)

264 river concentration with an assumed normal, truncated normal and log-normal distribution<sup>13</sup>  
 265 and report the results in section 5.5. Moreover, our methodology is also superior to imposing  
 266 a standard on the leachate in or below the root zone - a common assumption in the literature  
 267 due to the difficulty of modelling pollutant fate and transport to the receiving water body. It  
 268 also avoids having to convert the EU WFD nitrate standard (concentration - mg/L) into a  
 269 mass equivalent which requires making simplifying and distorting assumptions (Kampas and  
 270 White, 2004). Nor do we assume that the distribution of the pollution load (mass - mg) in the  
 271 root zone approximates the distribution of N concentration in the river, which is likely to  
 272 distort instrument cost-effectiveness and policy ranking. Also, since our approach does not  
 273 involve approximating the deterministic equivalent of a probabilistic constraint in a chance  
 274 constrained programming framework, therefore we don't have to estimate the correlation  
 275 coefficient between emissions (Kampas and White, 2003).

276

#### 277 4.6 Economic modelling

278 (1) Minimise

$$279 \sum_f \Pi_f - \sum_f \left[ \sum_{r,c,s} (Y_{frcs} P_c - w^n N_{frcs} L_{frcs}) + \sum_b a_{fb} P_b - w^n \left( \sum_{r,t,s} u_{frts} m_{frts} \right) - \sum_c C_{fc} L_{fc} - \sum_k A_{fk} R_k + T_f \right]$$

280 Catchment farms are modelled as economic decision makers ( $f$ ), who are assumed to  
 281 maximise individual farm profits ( $\Pi_f$ ), by endogenously determining land and fertiliser (NPK)  
 282 allocation to productive activities<sup>14</sup> on each soil type, in response to different regulatory  
 283 controls. The regulator's policy objective is to minimise the catchment abatement cost of  
 284 achieving a particular RT (probability of exceeding the EU 11.3 mg N/l ambient nitrate  
 285 concentration regulatory standard), i.e. the difference between the unrestricted catchment  
 286 profit  $\left( \sum_f \Pi_f \right)$  and the catchment profit different pollution control policies. Thus, (1)

<sup>13</sup> The parameters for the normal and lognormal distributions were estimated from the data's mean and the mean of the log, respectively, whereas those of the truncated normal over the interval of concentration greater than 2 mg/L (arbitrarily chosen) were obtained by maximum likelihood. The nonparametric density, which closely follows the data, was obtained using a normal kernel with a bandwidth of 0.5. Empirical frequency refers to the number of observations that exceed the standard.

<sup>14</sup> Productive activity refers to crops, livestock production (grassland) and LR.

287 determines the social cost of regulation (Baumol and Oates, 1988; Beavis and Walker,  
 288 1983). If a policy achieves a particular RT at lower social cost than another policy, then it is  
 289 more cost-effective and in a second best world more efficient (Ribaudo et al., 1999).  $\Pi_f$  is  
 290 the outcome of an unrestricted run of the model without any regulation, other than existing  
 291 mandatory restrictions (NVZ etc.), on farm  $f$ . Catchment profit in the objective function is the  
 292 sum of the return to each producer's management and allocation of resources minus the cost  
 293 of total farm nitrogen consumption ( $\sum_{r,c,s} w^n N_{frcs} L_{frcs}$  (arable crops),  $w^n \sum_{r,t,s} u_{frts} m_{frts}$  (silage and  
 294 grazing grass)), cost of land retirement ( $\sum_k A_{fk} R_k$ ) and all other crop specific secondary  
 295 farming costs  $C_{fc}$  including the cost of potato crop irrigation, sprays, K and P fertiliser  
 296 application, etc. Land retirement area  $A_{fk}$  and the per hectare cost of land retirement,  $R_k$  are  
 297 indexed over land retirement type  $k$  (permanent, temporary good and temporary bad).  
 298  
 299 Exogenous terms in (1) include  $P_c$  the market price of arable crop  $c$ , and  $P_b$  the market  
 300 return from livestock unit<sup>15</sup> (LU) type  $b$ . Agricultural prices were set to the 2009/10 price  
 301 level (SAC, 2009). The number of livestock on each farm is represented by  $a_{fb}$ .  $w^n$  is the  
 302 market price of nitrogen fertiliser,  $N_{frcs}$  and  $L_{frcs}$  is respectively the nitrogen applied and land  
 303 allocated to arable crop  $c$  (excluding grasslands) on soil type  $s$  in crop pair rotation  $r$ .  
 304 Likewise,  $Y_{frcs}$  is the yield for each crop, soil, rotation combination on each farm. Whereas  
 305  $m_{frts}$  and  $u_{frts}$  refer respectively to land and nitrogen allocated to grassland type  $t$   
 306 (permanent, temporary, and hay).  $T_f$  refers to all transfer payments (positive for IT). Such  
 307 transfer payments are not included in estimates of abatement costs. The non-linear  
 308 optimization model was written in GAMS (Brooke et al., 1998) and solved using the

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<sup>15</sup> A livestock unit is defined in terms of the metabolised energy requirement. With one unit being the maintenance of a mature 625 kg Friesian cow and the production of a 40–45 kg calf, and 4500 l of milk at 36 g/kg of butterfat and 86 g/kg s.n.f. Based on this the LU unit values of all livestock are calculated, e.g.: suckler cow (1 LU), ewe (0.15 LU), male cattle < 2 years (0.6 LU), male cattle > 2 years (1 LU).

309 CONOPT 3 solver<sup>16</sup> (Stolbjerg-Drud, 1993). Overall the model estimates the cost-  
310 effectiveness of policy control instruments to attain RTs. The 10% RT means the NP  
311 standard must be met at least 90% of the time etc. The social (resource) cost of policy  
312 controls are reported as percentage reductions from the baseline profitability. Figure 3  
313 provides a diagrammatic representation of the biophysical economic modelling.

314

315 We simulated the following policies: 1) nitrogen input taxation (IT); 2) farm livestock stocking  
316 density reduction (SDR), and; 3) a minimum percentage farm permanent land retirement  
317 (LR) requirement. Three types of MI policy packages that combine economic incentives with  
318 managerial controls (regulation), were simulated: a) LR with IT, b) SDR and IT and c) LR,  
319 SDR with IT. All of the control instruments were uniformly applied and simulated as iterative  
320 runs of the model. Impractical high transaction cost policies such as emission taxation (Aftab,  
321 2010) and nitrogen input quotas were also simulated but their results are not reported.

322

#### 323 *4.7 Land use and livestock calibration*

324 The model's baseline allocation was calibrated to farm level survey data on cropping and  
325 livestock intensities. Both catchment models' baseline simulations reflected actual farm  
326 practice in each catchment. The Motray's baseline percentage deviation from actual average  
327 catchment data was: -0.38% for arable crops and 2.99% for catchment livestock units (LU).  
328 The Brothock's baseline percentage deviation from actual average catchment data was: -  
329 11.79% for arable crops and -7.94% for catchment livestock units. The Motray's baseline  
330 arable to grassland ratio is 2.6 to Brothock's 4.45.

331

## 332 **5. Results**

333 Figures 4 and 5 illustrate the social cost of regulation as a percentage reduction from  
334 baseline catchment profit, £3.26m and £2.59m, under different pollution control policies for  
335 the Motray and Brothock respectively. The strictness of nitrate RT increases when moving  
336 from left to right along the x-axis in both figures. The probability of the standard being

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<sup>16</sup> Robustness checks were undertaken and results were verified by using the MINOS 5 solver.

337 exceeded is the number of days in the 3650 days of simulation that violate the standard. MI  
 338 are represented by discontinuous lines. The highest pollution level for each simulated control  
 339 policy is represented by top left-most starting point of its line. The control policies deliver  
 340 different minimum levels of compliance, e.g. the MI: [SDR (1.98) + IT] over achieves the 10%  
 341 RT by ensuring at least 8% compliance at all times. Table 2 ranks each policy's relative cost-  
 342 effectiveness and associated reduction in catchment profit relative to the catchment baseline.  
 343 The 10%, 5%, 3% and 1% RTs were arbitrarily chosen to illustrate the effect of progressively  
 344 stricter enforcement, with the 1% RT being the tightest.

345

### 346 *5.1 Motray results*

347 In figure 4, among single instrument stand-alone policies IT is clearly most efficient while LR  
 348 is the least cost-effective at mitigating pollution. Both stand-alone SDR and LR are inefficient  
 349 at achieving the 10% and 5% targets and incapable of achieving stricter RTs unless essential  
 350 crop rotation constraints are relaxed - unfeasible given the role of crop rotations in minimising  
 351 crop disease. The efficiency difference between economic and managerial policies as well as  
 352 between SDR and LR increases as the RT is tightened.

353

354 Interestingly, as the RT is increased MI outperform. IT is the most cost-effective control  
 355 instrument until the 16% RT after which there is a 'cross-over' and [LR (0.99%) + IT]  
 356 becomes more efficient. From the 15% target onwards various MI optimise social cost. Both  
 357 two instrument mixed instruments (2MI), [SDR + IT] and [LR + IT], are more cost-effective at  
 358 delivering the 15% RT and higher RTs. In fact, even though [SDR (1.98) + IT] over achieves  
 359 and actually meets the 5% RT, it is still more efficient than IT at the 10% target. This  
 360 efficiency difference between the two instruments extends from 0.46% at the 10% RT to  
 361 16.03% at the 1% RT. At the extreme, 2% RT and 1% RT, the three instrument mixed  
 362 instrument (3MI) [LR + SDR + IT] policy packages excels. E.g. at the strictest 1% RT the  
 363 efficiency gain between IT and [LR (0.96%) + SDR (1.97) + IT]<sup>17</sup> is 17.95%. Thus adding a

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<sup>17</sup> [LR (0.96%) + SDR (1.97) + IT] refers to a MI comprising of the requirement to retire 0.96% of farmland, a maximum stocking density of 1.97 GLU/ha on grassland and an N input tax.

364 further control instrument to the MI policy package improves efficiency as regulatory  
365 stringency is increased. Additionally, this efficiency gap widens considerably as the RT  
366 increases (figure 4 and table 2). Overall, across the RT considered in table 2, [SDR (1.98) +  
367 IT] is clearly the most efficient overall. Overall, the ‘crossovers’ are insignificant and policies  
368 tend to outperform in very distinct RT ranges. Such distinct cost-effectiveness frontiers make  
369 it easier to set RT specific policies.

370

### 371 *5.2 Brothock results*

372 The Brothock exhibits greater clustering of instruments in a narrower efficiency range, i.e. the  
373 difference in cost-effectiveness of policies is not as well defined (figure 5). LR is the least and  
374 IT is the most efficient single instrument. IT is marginally the most efficient control policy until  
375 the 10% RT after which various MIs maintain a small efficiency advantage. In table 2, [SDR  
376 (1.98) + IT] is marginally more efficient at the 5%, 3% and 1% level. The 3MI [LR (0.2%) +  
377 SDR (2.1) + IT] is clearly the most cost-effective policy at the strictest 1% level, delivering a  
378 cost saving of 0.82% over IT. Thus overall, within the considered RT range the [SDR + IT] MI  
379 is the most efficient. Two additional MI were simulated in the Brothock catchment: [SDR (2.1)  
380 + IT] and [LR (0.2%) + SDR (2.1) + IT]. These additional MI were set at SDR and LR levels  
381 that were “optimal” for the Brothock - illustrating that efficiency gains from tailoring instrument  
382 levels to each catchment. SDR is considerably more efficient in the Brothock and even  
383 outperforms IT from the 2% RT onwards.

384

385 Intriguingly, a pattern of instrument efficiency frontiers emerges which is entirely consistent  
386 with the Motray frontier. IT is the most cost-effective control instrument for small reductions in  
387 diffuse pollution from the baseline (14%-9% RT), whereas 2MI [SDR (2.1) + IT and SDR  
388 (1.98) + IT] outperform in achieving mid-range abatement (8%-2% RT), and 3MI [LR (0.2%)  
389 + SDR (2.1) + IT] is most cost-effective at the strictest regulatory target (1% RT). Such  
390 efficiency frontiers are catchment specific and depend on catchment characteristics.

391

### 392 *5.3 Cross catchment comparison*



393 In both catchments MIs outperform IT, SDR and LR at stricter RTs and their efficiency gain  
 394 increases at higher RT. The efficiency gain MIs provide is relatively greater in the Motray, but  
 395 instrument ranking remains largely, but not convincingly, consistent in both catchments.  
 396 Unfortunately, this consistency is not as robust as policy makers would like. Intriguingly, for  
 397 approximately the first 40% of pollution reduction in both catchments IT remains the most  
 398 efficient instrument – reflecting the superiority of IT in making small reductions from baseline  
 399 level of pollution in both catchments. Significantly, in table 2, MI policies, especially 3MIs,  
 400 display the least variation in social cost across the RTs (e.g. from the 10% to the 1% RT in  
 401 the Motray IT's resource cost increases from -3.77% to -23.42%, whereas with [LR (0.96%  
 402 +SDR (1.97) + IT] it rises from -4.05% to -5.47%). Suggesting it may be easier and more  
 403 politically acceptable for regulators to raise the RT with MI than with single instruments like IT  
 404 or LR<sup>18</sup>, due to the relative smaller reduction in catchment profit.

405

#### 406 *5.4 Comparative control instrument levels*

407 Table 3 compares the instrument levels required to induce compliance with the same RT in  
 408 each catchment. The result that higher probabilities of achieving  $E^*$  (stricter RT) require  
 409 higher instruments levels and that they are relatively greater in the Motray is self-explanatory  
 410 - given its higher baseline pollution. E.g. a 332.62% higher IT achieves the 10% RT, rising to  
 411 572.16% at the 1% target, in the Motray than in the Brothock. This difference between  
 412 catchments instrument levels is less apparent with managerial controls - particularly, LR at  
 413 the 5% RT where the Motray's 18.66% LR requirement is comparable to the Brothock's  
 414 17.95% LR requirement.

415

416 Also, the instrument level difference between catchments is considerably less for MI. The  
 417 difference in the IT component of the instruments 2MI [SDR + IT] and 3MI [LR + SDR + IT] is  
 418 44.23% and only 13.45% respectively at the 3% target. Intriguingly, the difference between  
 419 instrument levels required to achieve the same RT in both catchments is the smallest with

---

<sup>18</sup> Compare the increased percentage reduction in the Brothock's resource profit using LR in moving from the 10% RT (-6.5) to the 1% RT (-36.94).

420 3MI, i.e. an IT difference of 19.23%, 13.45% and 28.84% at the 5%, 3% and 1% RT  
421 respectively. Thus, the evidence suggests MIs are more suited to being applied uniformly as  
422 blanket policies across different catchments than IT. Uniform policies have lower transaction  
423 costs than spatially targeted ones, are arguably more enforceable in practice and perceived  
424 to be fairer. This may explain the reluctance of policy makers to adopt economic controls in  
425 isolation. Our results suggest it may be easier to impose a uniform MI policy than a uniform  
426 IT policy across different catchments. Detailed water quality metrics and their interpretation  
427 can be found in the supporting supplementary material.

428

#### 429 *5.5 Estimated pollutant distribution bias*

430 Figure 1 compares the modelled daily baseline river concentration histograms of both  
431 catchments. By comparing the nonparametric kernel density of the empirical (modelled) river  
432 concentration with an assumed normal, truncated normal and log-normal distribution we  
433 found that in the Motray all three assumed distributions underestimate the probability of  
434 exceeding the 11.3 mg/L standard, whereas in the Brothock they overestimate the  
435 probability. This illustrates the bias from assuming an incorrect underlying distribution. This  
436 bias is as much as -19.15% with the normal in Motray and 31.88% when assuming a  
437 lognormal distribution in the Brothock. Such substantial errors are likely to be economically  
438 and environmentally costly. Real data seldom follows standard distributions; excessive  
439 peakedness (with many outliers) and multimodality are more common - as shown in the  
440 actual data (Figure 2). Multimodality occurs naturally in meteorological data (Mardia and  
441 Jupp, 2000; Zocatelli et al., 2011), and is a key driver of river pollution. Furthermore, using a  
442 crude one-sided Chebyshev inequality produces very large upper bounds on the probability  
443 of exceeding the threshold. The inequality provides very limited information and appears  
444 excessively conservative when contrasted with real data.

445

#### 446 *5.6 Associated P and K consumption*

447 Farmers tend to apply fertilisers in fixed ratios or purchase fertiliser mixes containing N, P  
448 and K in recommended ratios. Assuming this, the models estimate the application or load of

449 P and K to each crop/soil combination (including grassland) based on the optimal application  
450 of N<sup>19</sup>. Thus allowing an estimate of the impact of NP control policies on catchment  
451 consumption of P and K at both the intensive and extensive margin inclusive of the P and K  
452 content of livestock waste. This is important as regulatory policies, may affect the intensity of  
453 production and land allocation (proportion of arable to livestock activity) in catchments and  
454 thus the relative use of N, P and K. The purpose of this analysis is not to identify cost-  
455 effective ways to control P and K emissions, but to simply consider the possible  
456 consequences of policies to control NP on P and K losses (pollution swapping).

457  
458 The Motray's baseline N load was 751.22t with a P:N ratio of 0.42 and a K:N ratio of 0.47;  
459 whereas the Brothock's baseline N load was 624.82t with a P:N ratio of 0.41 and a K:N ratio  
460 of 0.49. As expected, in the Motray, achieving higher nitrate RT also reduces catchment P  
461 consumption (table 4). The greatest reduction in catchment P consumption is associated with  
462 IT, whereas LR and in particular SDR do not reduce P utilization as much. Therefore, the LR  
463 and SDR components in MIs explain the slightly greater P consumption when compared to  
464 stand alone IT. The fact that IT primarily reduces catchment pollution by decreasing the  
465 intensive margin whereas LR affects the extensive margin may explain the results. SDR  
466 works by either reducing livestock numbers or increasing the farmland that that sustains  
467 livestock or both depending on which is most profitable. Thus at lower N regulatory targets  
468 SDR may only lower P consumption loads on grassland and not affect arable land P  
469 consumption, thereby achieving less P reduction.

470  
471 Similarly, in the Brothock the P load falls as the N regulatory target is tightened. However,  
472 interestingly, in the Brothock results produce two differences. Firstly, LR produces greater P  
473 reduction than IT. This can be explained by the considerably high levels of LR, mostly at the  
474 expense of winter wheat, which are required to meet the nitrate RT. Secondly, using [SDR +  
475 IT] and in particular stand-alone IT produces a sharp increase in catchment P consumption  
476 at the strictest 1% regulatory target - even exceeding the baseline P load in the case of IT.

---

<sup>19</sup> In practice substitution between N, P and K is limited.

477 3MI, which has a smaller IT component, does not produce a spike in P consumption. This is  
478 because at high N input prices it is more profitable to substitute away from winter wheat to  
479 seed potatoes. Therefore, an unintended consequence of IT is that, while it reduces  
480 catchment N consumption, it unfortunately provides a perverse incentive to shift from winter  
481 wheat (NPK/ha ratio 200:70:70) to seed potatoes (NPK/ha ratio 90:200:150) - which requires  
482 relatively less N but more P. Both P and N are nutrients that contribute to eutrophication and  
483 achieving GECS. This highlights the risk of pollution swapping and the need to consider the  
484 broader impact of policies as they may paradoxically provide perverse incentives that  
485 produce detrimental water quality consequences from pollution swapping.

486  
487 The results for K are similar but not as pronounced as the P results. They are similar in that  
488 Motray's K consumption decreases at higher N regulatory targets; this reduction is greatest  
489 with IT and less so with LR. Among the single instruments considered SDR produces the  
490 least reduction in K consumption. 2MI and especially 3MI display much lower catchment K  
491 application. Again the Brothock displays a similar increase in K consumption at the highest  
492 1% RT – although not as significant as the P increase. Overall, this is evidence of the need  
493 to coordinate environmental regulation and consider the complementary regulation of other  
494 polluting nutrients. As clearly, controlling N may inadvertently change P and K consumption  
495 and prevent attaining the intended ecological outcome.

496

## 497 **6. Discussion**

498 Regulation will simpler if consistently cost-effectives policies across a range of water bodies  
499 with similar characteristics can be identified. In this paper, we investigate the consistency of  
500 policy cost-effectiveness across two relatively similar catchments. We account for the  
501 stochastic nature of NP by empirically estimating the distribution of daily ambient river nitrate  
502 concentration using 10 years of continuous weather data, without making distorting a priori  
503 distributional assumptions. This provides a more realistic assessment of the uncertainty  
504 associated with regulatory controls. Additionally, we estimate instrument cost-effectiveness  
505 based on the distribution of river concentration as opposed to pollution loads (mass) in the

506 root zone. We contend that modelling the entire biophysical processes realistically and  
507 imposing environmental standards at the point of environmental impact (river) is critical to  
508 policy analysis. The significance of our results are in the detail, i.e., policy ranking is only just  
509 broadly consistent, even in two relatively similar catchments. That is, the cost-effectiveness  
510 ranking of policies is may not be as robust as policy makers would like.

511 Interestingly, policies tend to outperform in very distinct RT ranges - even though the  
512 instrument levels required to meet RTs differ in catchments. Initial pollution reduction is most  
513 cost-effectively achieved by IT, higher RTs required 2 instrument MIs, whereas the strictest  
514 RTs require 3 instrument MIs. Thus indicating that cost-effective rankings are probably RT  
515 dependent. Such distinct cost-effectiveness frontiers should make it easier to determine  
516 optimal control policies for specific RTs. The presence of crossovers did not significantly alter  
517 the ranking of policies or the identification of efficiency frontiers. Results confirm the previous  
518 literature in that single instruments display efficient abatement fatigue at higher RTs and that  
519 the relative cost-effectiveness of MIs improves as the RT is tightened.

520  
521 A key result is that the difference between instrument levels required to achieve the same RT  
522 in both catchments is the smallest with 3MI. Thus MIs are arguably more suited to being  
523 applied as uniform policies across different catchments than IT. Interestingly, MIs also  
524 display the least variation in catchment resource cost across RTs, implying it might easier to  
525 raise environmental quality (higher RT) with a MI policy. The standard deviation of river  
526 pollution under MIs is also less than IT in both catchments. In considering the impact of  
527 policies to control diffuse N pollution on farm P and K consumption our results suggest that  
528 IT does significantly reduce P and K consumption, but LR and SDR do not. However, at the  
529 strictest RT, IT produced perverse land allocation incentives that may produce spikes in the  
530 consumption of P and K. Another benefit of MIs was the absence of such spikes. It is  
531 apparent that there are trade-offs between policies to control NP and the consumption of P  
532 and K, which in turn can paradoxically prevent meeting GECS – providing another reason to  
533 coordinate policy across pollutants. Admittedly consumption of P & K is a proxy for pollutant  
534 loads entering the river and future research would benefit from modelling P and K river

535 concentrations or better yet ecological impact. Whilst in a sense a favourable case has been  
536 considered here (i.e. relatively comparable catchments in geographical proximity), the results  
537 suggest that an overall consistent ranking is found across policy instruments. Unfortunately,  
538 it may not be as as robust as regulators and stakeholders would like or assume. Differences  
539 in the absolute level of instruments across catchments are considerable but intuitively  
540 correct. Ideally policy packages should be tailored to specific catchments, as the efficiency  
541 gains are theoretically considerable – however real world transaction costs may render this  
542 infeasible at present.

543  
544 The advantages of MI are reinforced when you consider a) the secondary environmental  
545 benefits from the managerial component of MIs, and b) the political sensitivity of  
546 implementing economic instruments in isolation. Properly managed LR can help mitigate NP  
547 pollution while promoting farmland biodiversity (Burt and Haycock, 1993; Ribaud et al.,  
548 1994). CAP has imposed minimum LR and SDR conditions in the past and LR maybe return  
549 under recent ‘greening’ of CAP. Unfortunately, reliable transaction cost estimates of  
550 implementing and enforcing such regulatory policies are not available and thus not  
551 considered. Nor have we factored the stochastic nature of crop yields or the transition period  
552 between policy implementation and its impact. Our analysis would benefit from improved  
553 modelling of farming heterogeneity and groundwater hydrology. More research is required to  
554 analyse the consistency of our results across catchments of differing similarity and to identify  
555 the defining catchment characteristics that determine the transferability of policy cost-  
556 effectiveness.

557

## 558 **7. Conclusion**

559 The paper investigates the transferability of instruments to control NP by comparing the cost-  
560 effective ranking of regulation in two relatively similar agricultural catchments. We use an  
561 approach, which does not necessitate making a priori assumptions about the underlying  
562 distribution of daily stochastic pollutant concentration in rivers. Our results suggest that policy  
563 instrument ranking is broadly but not convincingly consistent across relatively similar

564 catchments but that policies outperform in distinct regulatory target ranges. Notably we find  
 565 that MI policies display characteristics more suitable to wider application across catchments  
 566 (especially at higher RTs), the enforcement of stricter RTs over time and where there are  
 567 ecological concerns about pollution swapping and the consumption of other polluting  
 568 nutrients.

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- 703

Figure 1: Comparison of the modelled daily baseline river concentration histograms of both catchments

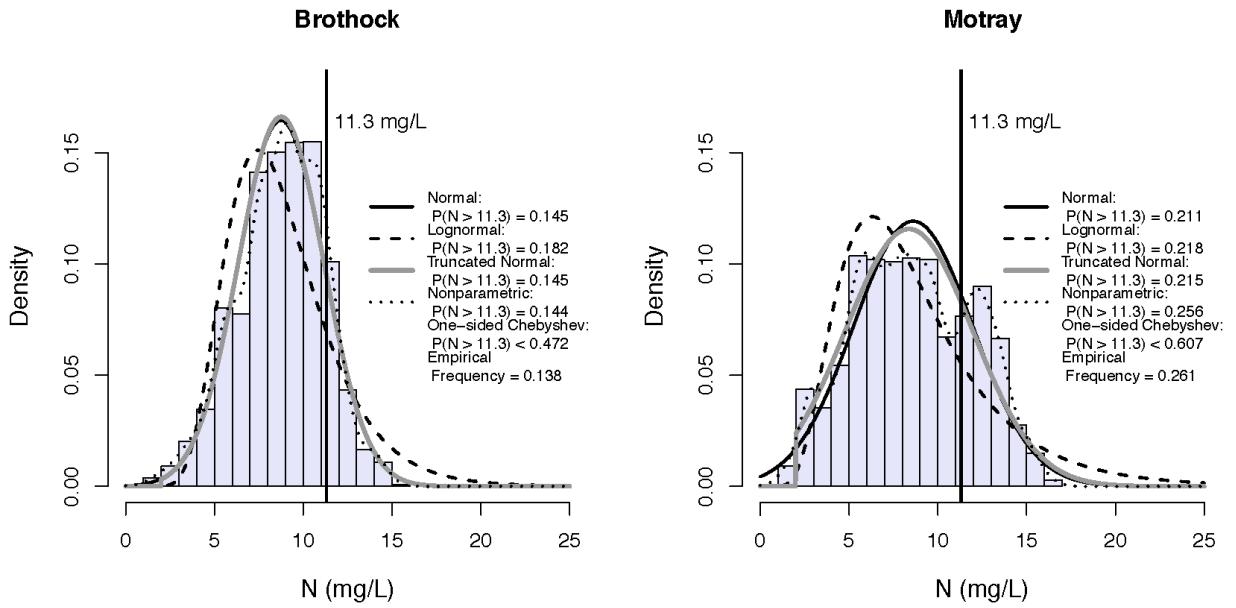


Figure 2: Comparison of the actual sampled river concentration histograms of both catchments

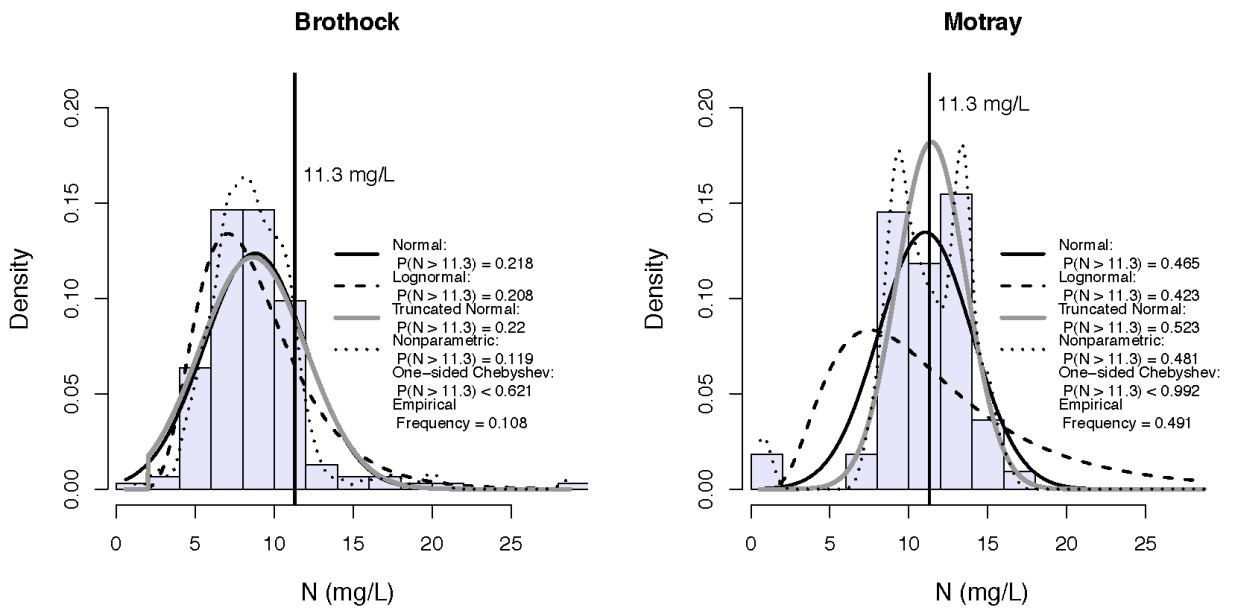
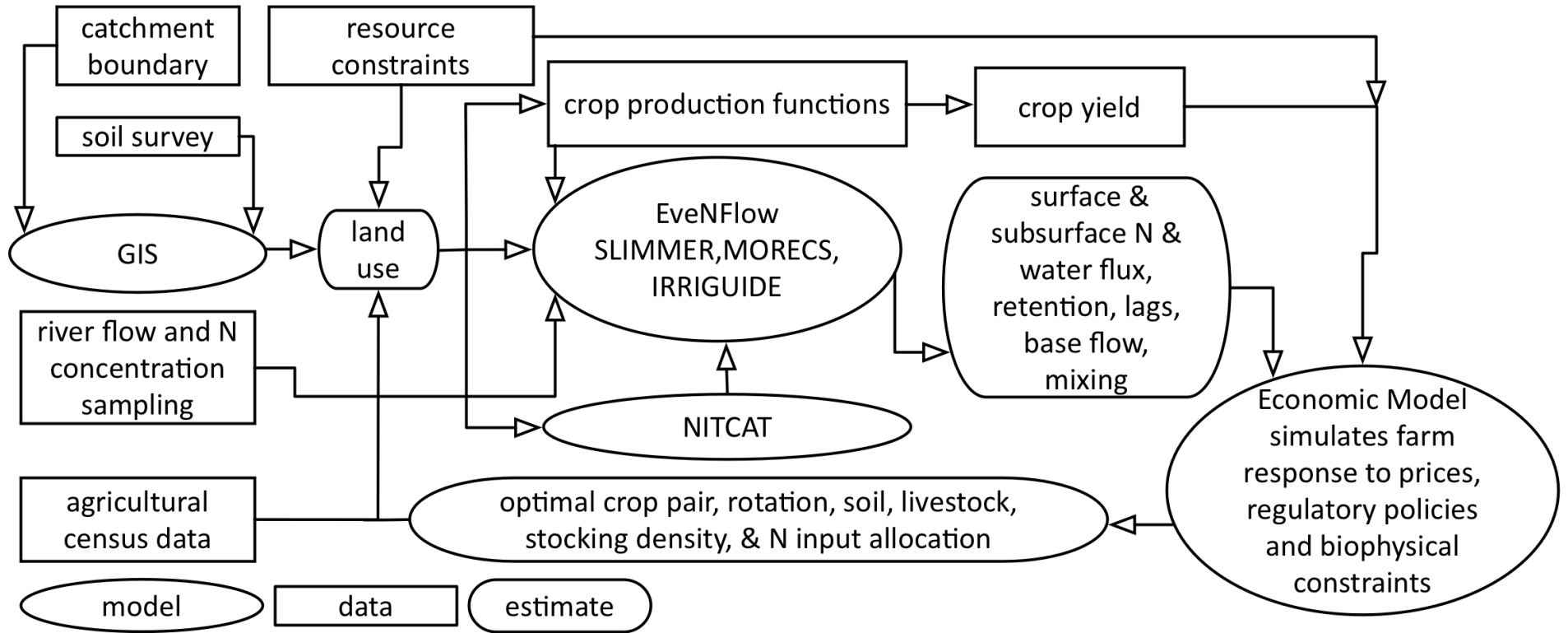
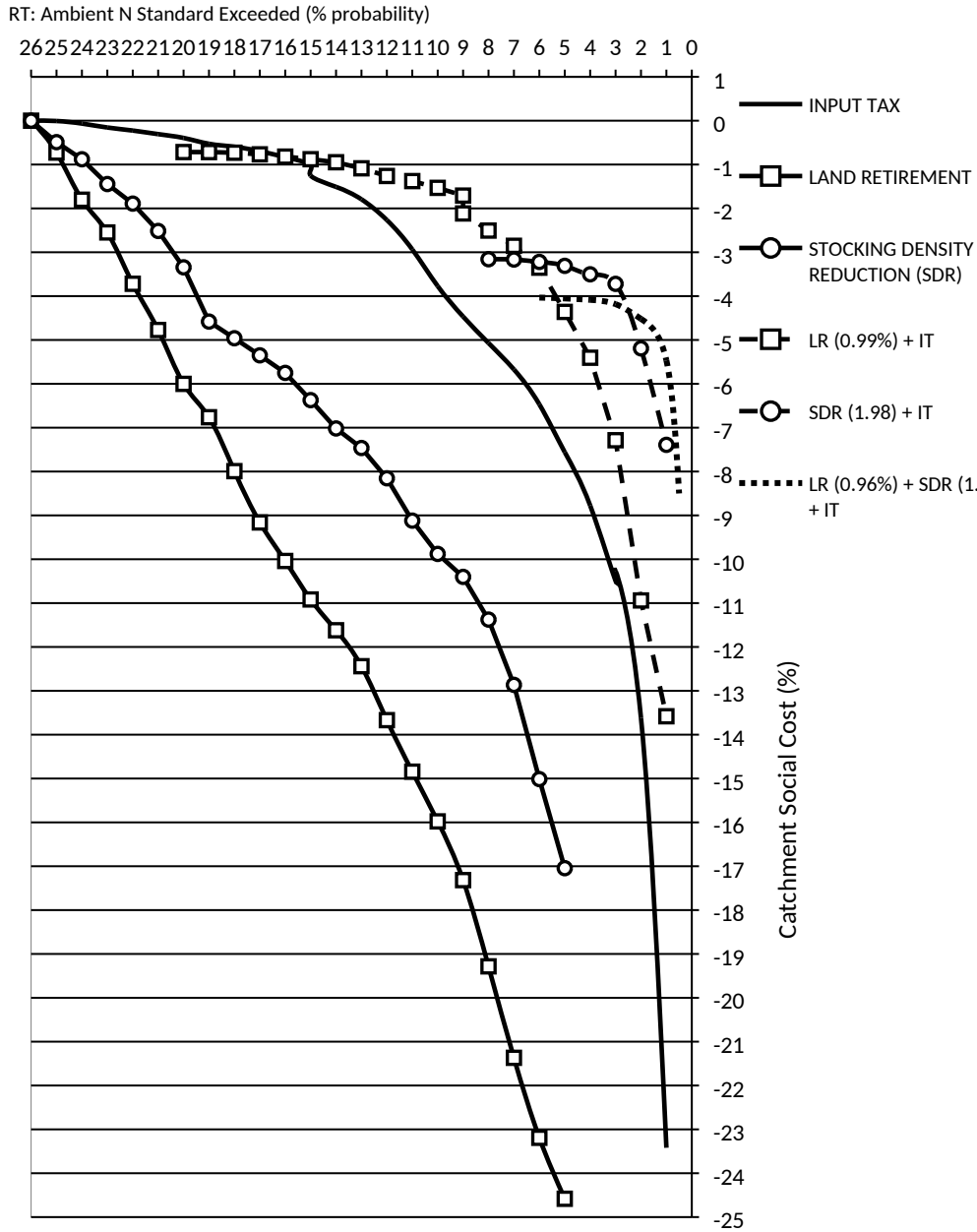


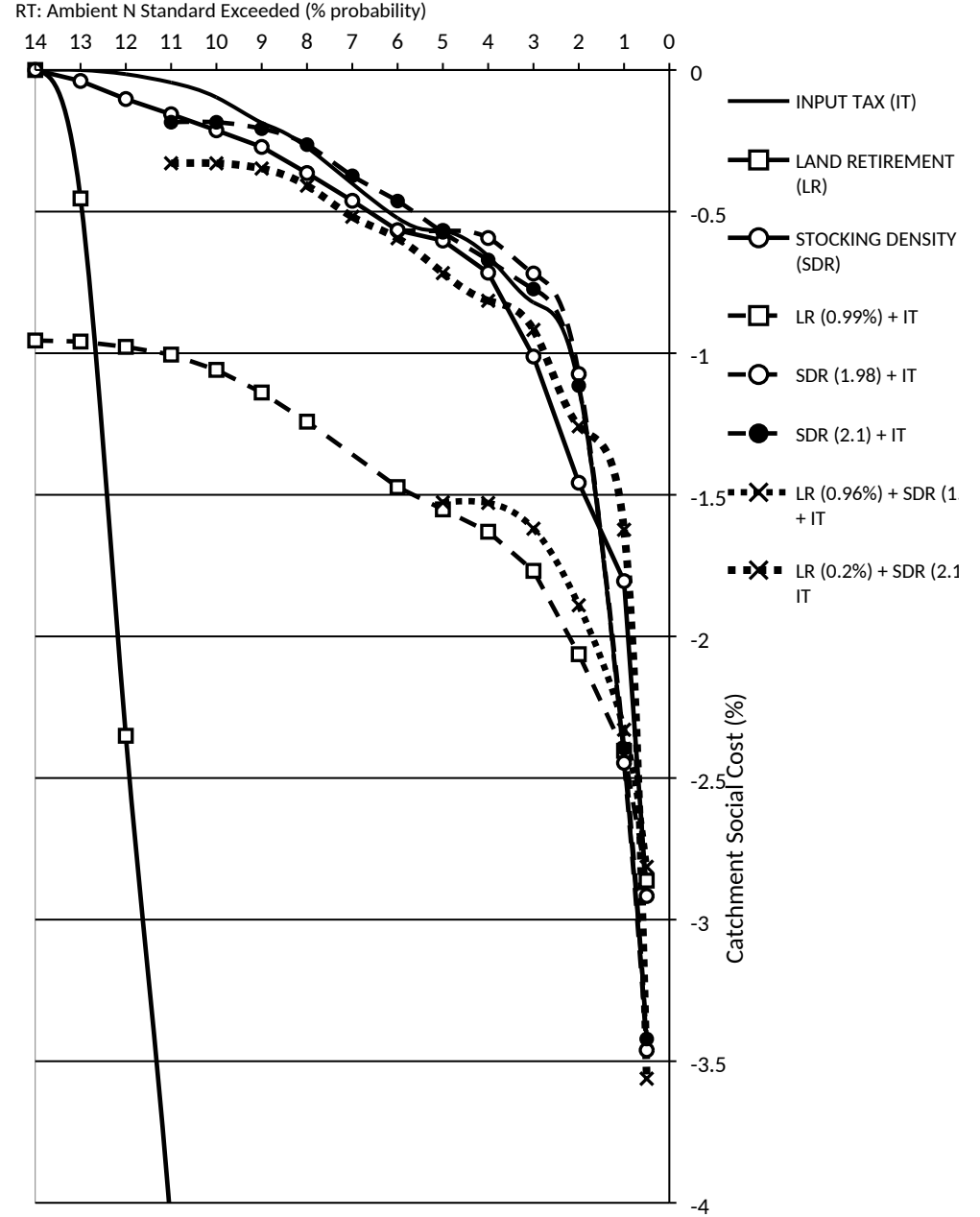
Figure 3: Diagrammatic representation of the biophysical economic modelling



**Figure 4: MOTRAY - REGULATORY TARGETS AND ASSOCIATED CATCHMENT SOCIAL COST**



**Figure 5: BROTHOCK - REGULATORY TARGETS AND ASSOCIATED CATCHMENT SOCIAL COST**



**Table 1: Catchment characteristics**

Catchment	Motray			Brothock		
Size (km <sup>2</sup> )	58.3			44.3		
Arable area* (ha)	4743			3580		
Average annual rainfall (mm)	720			708		
Representative soil classes	Mountboy	Sourhope	Auchenblae	Balrownie	Vinny	Corby
Profile water column (mm)	353	337	219	344	316	193
HOST class	18	22	5	18	16	5
Agricultural area (%)	38	39	23	68	28	4

\* Excluding rough grazing and forestry

**Table 2: Comparative Catchment Ranking of Control Instruments and Associated Percentage Reduction in Catchment Resource Profit**

Catchment	Motray				Brothock			
	Regulatory Target							
Percentage of time	10	5	3	1	10	5	3	1
Input Tax (IT)	2 (-3.77)	4 (-7.56)	4 (-10.50)	4 (-23.42)	1 (-0.10)	3 (-0.57)	3 (-0.82)	6 (-2.44)
Land Retirement (LR)	4 (-15.98)	6 (-24.58)	NA	NA	8 (-6.50)	8 (-18.85)	8 (-26.81)	8 (-36.94)
Stocking Density Reduction (SDR)	3 (-9.88)	5 (-17.04)	NA	NA	3 (-0.21)	4 (-0.60)	5 (-1.01)	2 (-1.80)
LR (0.99%) +IT	1 (-1.53)	3 (-4.36)	3 (-7.29)	3 (-13.58)	5 (-1.06)	7 (-1.55)	7 (-1.01)	4 (-1.80)
<b>SDR (1.98) + IT</b>	OA	1 (-3.31)	1 (-3.72)	2 (-7.39)	OA	1 (-0.57)	1 (-0.72)	7 (-2.45)
SDR (2.1) + IT					2 (-0.18)	2 (-0.57)	2 (-0.77)	5 (-2.40)
LR (0.2%) +SDR (2.1) + IT					4 (-0.33)	5 (-0.72)	4 (-0.92)	1 (-1.62)
<b>LR (0.96%) +SDR (1.97) + IT</b>	OA	2 (-4.05)	2 (-4.18)	1 (-5.47)	OA	6 (-1.53)	6 (-1.62)	3 (-2.33)

(): Associated percentage reduction in catchment resource cost

OA: over achieves regulatory target; NA: does not achieve regulatory target

Note: in the case of SDR and LR not achieving regulatory target does not mean that the two control instruments are incapable of achieving the regulatory target, but only at a very significant cost farming. In terms of the optimisation it means relaxing numerous constraints that are probably not practical (e.g. pest control) or acceptable (high cost) to farmers.

**Table 3: Comparative Control Instrument Levels in Motray and Brothock**

Catchment	Motray				Brothock			
	Regulatory Target (percentage of time)							
Percentage of time	<b>10</b>	<b>5</b>	<b>3</b>	<b>1</b>	<b>10</b>	<b>5</b>	<b>3</b>	<b>1</b>
Input Tax (IT)	373	500	573	726	40.38	76.92	90.38	153.84
Land Retirement (LR)	14.05	18.66	NA	NA	6.40	17.95	22.4	26.9
Stocking Density Reduction (SDR)	24.5	33.18	NA	NA	3.42	8.96	13.58	20.52
LR (0.99%) + IT	103.84	369.23	469.23	626.92	42.30	70.84	90.38	117.30
<b>SDR (1.98) + IT</b>	OA	56.84	96.15	442.30	OA	5.76	51.92	105.77
SDR (2.1) + IT					1.92	75	82.69	117.30
LR (0.2%) +SDR (2.1) + IT					1.92	75	82.69	117.30
<b>LR (0.96%) +SDR (1.97) + IT</b>	OA	19.23	53.84	134.61	OA	0	40.39	105.77

All values are percentage increases relative to baseline levels in each catchment, except SDR for which actual values are presented.

**Table 4: Changes in Phosphorus (P) Consumption Load Associated with Policies to Control Diffuse N Pollution**

Catchment	Motray				Brothock			
	10	5	3	1	10	5	3	1
	<b>PHOSPHORUS</b>							
Input Tax (IT)	-19.03	-23.20	-24.69	-31.68	-4.11	-8.29	-9.76	1.34
Land Retirement (LR)	-14.76	-21.51	NA	NA	-4.90	-14.09	-20.25	-28.18
Stocking Density Reduction (SDR)	-9.61	-14.61	NA	NA	-0.74	-1.94	-3.02	-4.48
LR (0.99%) +IT	-12.16	-19.26	-23.26	-27.61	-4.96	-9.13	-10.36	-13.20
<b>SDR (1.98) + IT</b>	OA	-9.45	-12.89	-22.17		-2.44	-6.90	0.93
SDR (2.1) + IT					-0.85	-8.13	-9.20	1.44
LR (0.2%) +SDR (2.1) + IT					-0.96	-8.22	-9.29	-12.76
<b>LR (0.96%) +SDR (1.97) + IT</b>	OA	-6.95	-10.07	-16.54	OA	-2.64	-6.58	-12.54
	<b>POTASSIUM</b>							
Input Tax (IT)	-24.75	-30.28	-31.88	-39.33	-4.46	-8.81	-10.34	-7.28
Land Retirement (LR)	-13.48	-22.48	NA	NA	-4.10	-12.12	-19.99	-31.06
Stocking Density Reduction (SDR)	-9.09	-15.42	NA	NA	-0.68	-1.74	-2.69	-4.02
LR (0.99%) +IT	-12.58	-24.90	-29.74	-34.10	-5.21	-9.55	-10.85	-13.84
<b>SDR (1.98) + IT</b>	OA	-9.56	-13.53	-28.72		-2.29	-7.13	-7.52
SDR (2.1) + IT					-0.82	-8.63	-9.71	-7.15
LR (0.2%) +SDR (2.1) + IT					-0.91	-8.71	-9.79	-13.47
<b>LR (0.96%) +SDR (1.97) + IT</b>	OA	-6.51	-10.15	-17.43	OA	-2.32	-6.60	-13.06

Phosphorus and Potassium load reductions are presented as percentage reductions from catchment specific baseline phosphorus and potassium loads respectively. Motray's phosphorus (P) baseline load was 313.516 tonnes; Brothock's load was 256.135. Motray's potassium (K) baseline load was 352.608 tonnes; Brothock's load was 306.016 tonnes.



## Glossary

DEFRA	Dept. of Environment Food and Rural Affairs	LR	Land Retirement	P	Phosphorus
EA	Environment Agency	LU	Catchment Livestock Units	RT	Regulatory Target
FRU	Forestry, Rough grazing and Urban areas	MI	Mixed Instruments	SDR	Stocking Density Reduction
GECS	Good Ecological and good Chemical Status	N	Nitrogen	SEPA	Scottish Environmental Protection Agency
IT	Input Taxation	NP	Nonpoint nitrate pollution	2MI	Two instrument mixed instrument
K	Potassium	NVZ	Nitrate Vulnerable Zone	3MI	Three instrument mixed instrument

## SUPPLEMENTARY MATERIAL: Motray and Brothock Modelling Methodology

The modelling of river flow and nitrate concentrations was done using a version of the EveNFlow model, developed by ADAS.

Daily time series of water and nitrate exiting soil units via rapid (shallow) and slow (deep) drainage pathways were routed by the EveNFlow model, introducing transfer delays, to reproduce the river hydrograph and concentrations resulting from the mixing of waters from the two drainage pathways. EveNFlow is a semi-distributed, catchment scale, conceptual model of the delivery of effective rainfall to a river system. The model is constructed so that it may be parameterised in catchments where observed flow data limited or unavailable. Parameterisation of the model requires information on the areas of soils of each HOST class within a catchment or long-term estimates of the BFI from observed flows (Boorman *et al.*, 1995; NERC, 1998). The BFI is conceptualised as a measure of the proportion of flow that travels via the deeper, slower routes to the river system.

The flow routing methodology is based upon an exponential model of the drainage from a non-linear catchment soil water store or reservoir, as derived by Kirkby (1975), in which the instantaneous rate of discharge from the store is calculated as:

$$Q_t = Q_0 \cdot e^{\left(\frac{S_t}{M}\right)} \quad (1)$$

where  $Q_t$  is the rate of discharge at time  $t$ ,  $Q_0$  is the rate of discharge when the soil store is saturated,  $S_t$  is the catchment soil moisture store, and  $M$  is the master recession constant, representing the rate at which the soil store empties and hence the recession of the river hydrograph.

The store is representative of an exponential decline in lateral transmissivity of the soil with depth (Beven *et al.*, 1994). Thus, the change of the rate of discharge is nonlinear with respect to the rate of change of the catchment store. This nonlinear description

enables the model to represent the delivery of water to a river channel via rapid flow routes such as macropores.

In the EvenFlow model, the discharge equation (1) has been simplified to give:

$$Q_t = e^{\left(\frac{S_t}{M}\right)} \quad (2)$$

In this form there is no explicit identification of the state of saturation, and rapid runoff associated with saturation excess overland flow is assumed to be adequately represented by the extension of the soil transmissivity profile above a virtual soil surface.

The instantaneous volume of water in the catchment soil store is calculated as:

$$S_t = M \cdot \log_e Q_t \quad (3)$$

and the mass balance of the catchment soil store is calculated as:

$$\frac{dS}{dt} = H - Q_t \quad (4)$$

where effective rainfall  $H$  is the soil drainage, and represents a constant intensity inflow of water from the root zone to the store.

Kirkby (1975) showed that the instantaneous discharge at time  $t+\Delta t$  is equal to:

$$Q_{t+\Delta t} = \frac{1}{\frac{1}{Q_t} + \frac{\Delta t}{M}} \text{ where } H = 0 \quad (5)$$

and

$$Q_{t+\Delta t} = \frac{H}{1 - \exp\left(-\frac{H \cdot \Delta t}{M}\right) + \frac{H}{Q_t} \cdot \exp\left(-\frac{H \cdot \Delta t}{M}\right)} \text{ where } H > 0 \quad (6)$$

The volume of water discharged to the river system during the time step  $\Delta t$  is calculated by use of equation (13) to determine the net change in the catchment soil water store, taking into account of effective rainfall:

$$\int_t^{t+\Delta t} Q_t = M \cdot \left( \log_e \frac{Q_t}{Q_{t+\Delta t}} \right) + H \cdot \Delta t \quad (7)$$

In this modified form, the parameter  $M$  is used to represent the effect of the combined time delay associated with the lateral movement of water from hillslopes to the river channel and the in-river routing to the mouth of the catchment. The greater the value of  $M$ , the greater the apparent residence time of the water associated with a particular drainage event.

In the modified version of the EveNFlow model used here, each area of a given soil type within a catchment was represented by two EveNFlow soil water stores. The first was driven by additions of both the rapid and slow drainage from the soil profile, and the second by additions of only the slow soil drainage. Total routed flow from the soil area is the output from the first store. The contribution from only rapid flow is the difference in the outputs between the two stores. The contribution from only slow flow is the output from the second store.

Each catchment store  $S$  must be initialised. Each simulation begins on September 1<sup>st</sup>, when the initial value of the soil moisture store can be estimated from the low flow index  $Q_{95}$  as follows:

$$S_{t=0} = M \cdot \log_e(Q_{95} \cdot \bar{H}) \quad (8)$$

where  $\bar{H}$  is the daily mean effective rainfall over the simulation period.

The rate parameter  $M$  for the stores may be determined from iterative optimisation of the fit between the modelled and observed hydrograph. In EveNFlow however, the rate parameter is *not* reliant on an observed flow time series for calibration, but from catchment scale observations of hydrograph shape.

The BFI is a numerical separation of the river hydrograph into a rapid flow and base flow component. The BFI is the volume of base flow, expressed as a proportion of total flow. This published statistic (NERC, 1998), is determined from long-term records of observed flow. The EveNFlow model is based on the observation that the annual BFI and  $Q_{95}$  of hydrographs simulated using the modified flow model are uniquely related to the value of the rate parameter  $M$ , for a given effective rainfall time-series. Flow is simulated on a daily time-step using a given input rainfall time-series and first estimates of  $M$  and the BFI of the hydrograph are calculated. An iterative procedure in the form of a simple bisection method (Press *et al.*, 1992) is invoked that successively modifies the estimate of  $M$  until the BFI of the simulated hydrograph equals the target BFI for the response group HOST class. Parameterisation of  $M$  is based only on the match between the BFI of the simulated hydrograph and the BFI predicted for the soil water store by the HOST database, not by reference to standard model fit criteria. The target BFI of the infiltration excess surface runoff store is set at 0.10, and a separate recession parameter  $M$  is calculated for this store. This value is based upon information in the Flood Studies Report (NERC, 1975) for the response of rivers to storm runoff from urban areas.

The BFI is used to parameterise  $M$  in the EveNFlow system, following studies of hydrograph index variability that have demonstrated that BFI is more stable than  $Q_{95}$ , and that the BFI for individual years are consistently close to the long-term value except in years of extreme drought (Gustard *et al.*, 1987).

The total flow from a catchment is calculated by area weighting of the sum of rapid and slow soil drainage derived flows for each soil area within the catchment.

The methodology described above separates the river hydrograph into components derived from rapid and slow drainage. To simulate mixed nitrate concentrations, the EveNFlow stores were then paired with nitrogen stores. For each store, the nitrogen in storage was increased daily by the quantities in the rapid or slow drainage, as appropriate. The nitrogen in the stores was assumed to be mixed perfectly in the volumes of water held by the EveNFlow stores. Hence, nitrogen was removed from the stores and input to the modelled rivers each day, in proportion to the ratio of the predicted total discharge from and current volume of water in the stores.

Finally, a proportion of nitrate was calculated retained by plant uptake and biochemical processes including denitrification. The proportion of nitrate in the river system remaining after retention was calculated as:

$$P = e^{\frac{-1 \cdot K \cdot 0.26 \cdot [10^{0.0293 \cdot T}]}{V}} \quad (9)$$

where  $K$  is an empirical retention parameter,  $T$  is the daily average air temperature, and  $V$  is the river velocity, calculated according to the methodology of Round et al. (1998).

For further details of the EveNflow methodology, underlying modelling and validation please refer to: Anthony, S., M. Silgram, et al. (2009). "Modelling nitrate river water quality for policy support." *International Journal of River Basin Management* 7(3): 259-275.

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