

Quality Measures of Reconstruction Filters for Stereoscopic Volume Rendering

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Abstract In direct volume rendering (DVR), the choice of reconstruction filter can have a significant effect on the visual appearance of the images produced and thus, on the perceived quality of a DVR rendered scene. This paper presents the results of a subjective experiment where participants stereoscopically viewed DVR rendered scenes and rated their subjective quality. The statistical analysis of the results focuses on the relationship between the quality of the stereoscopic scene and properties of the filters such as post-aliasing and smoothing, as well as the relationship between the quality of the stereoscopic scene and properties of the rendered images such as shape compactness.

The experiment evaluated five reconstruction filters on four different volumetric data sets. Participants rated the stereoscopic scenes on four quality measures: depth quality, depth layout, minimal jaggyness and sharpness. The results show that the correlation between the quality measures and post-aliasing and smoothing, which are properties associated to each reconstruction filter, is moderate and statistically insignificant. On the other hand, the correlation between the quality measures and compactness, which is a property specific to each rendered image, is strong and statistically significant.

Keywords Direct Volume Rendering, Reconstruction Filters, Stereoscopic, User Evaluations.

1 Introduction

Volumetric data can describe 3D scenes containing various objects of complex shape, which could be semi-transparent and arranged in complex layouts. This can lead to conflicting depth information and can make it difficult for observers to understand the detailed layout of the objects in the scene. Several attempts have been made to aid in the understanding of depth in images produced by direct volume rendering (DVR), including the analysis of semi-transparency [5, 35] as well as the use of stereoscopic displays [7, 12, 16].

The *reconstruction filters* are functions used by the standard DVR algorithms to interpolate between the nodes of a 3D grid of volumetric data. Reconstruction filters have been widely studied in their use for 2D image re-sampling [20] and volume rendering [6, 9, 19, 21, 28]. There is a wide range of proposed reconstruction filters and the type and severity of the various types of visual artefacts they introduce into the produced images is fairly well-understood. Artefacts such as aliasing and blurring can degrade the perception of depth and thus, the choice of reconstruction filter that introduces the artefacts was shown to have an effect on the results of path-searching tasks when used with stereoscopic DVR [28]. However, it is less clear how observers perceive these artefacts and how they may affect subjective measures of the quality of a stereoscopically viewed DVR rendered scene.

This paper presents an experimental study of four quality measures related to stereoscopic volume rendering: depth quality, depth layout, minimal jaggyness and sharpness. We tested five reconstruction filters on four different data sets, three of which are natural data sets and one is computer generated. We then analysed the results looking for relationships between the quality measure scores gathered from the participants on the one hand and the smoothing and post-aliasing of the filters and the shape compactness

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of the images on the other.

The analysis of the results of the experiment suggests that while the perception of the quality of the scene layout is not affected by the choice of reconstruction filter, this is not the case for depth quality. That is, whilst users are able to understand the global layout of objects in the scene regardless of the choice of reconstruction filter, the perception of depth quality depends on that choice. However, when we tried to translate the statistically significant relationships between quality measures filters, into correlations between quality measures and properties of the filters, here smoothing and post-aliasing, we found such correlations to be moderate at best and statistically insignificant. On the other hand, we found that an image specific, rather than filter specific, measure of shape compactness is highly correlated with each of the quality measures.

The implications of the results is firstly that the often quoted smoothing and post-aliasing measures of reconstruction filters for DVR do not necessarily relate to how well observers will perceive the images. Therefore preferences towards reconstruction filters that exhibit high or low post-aliasing or smoothing do not guarantee any particular level of perceived quality. Measures that take into account the rendered images, such as the shape compactness used in this paper, should be preferred instead. Secondly, the shape compactness results suggest that the B-spline approximation filter should be preferred if the smoothing of the initial volumetric data caused by the use of an approximating filter can be tolerated.

We summarise the contributions of the paper as:

- An experimental evaluation of stereoscopic DVR on four quality measures with our results showing that reconstruction filters affect the quality of depth.
- We show that shape compactness measured on rendered images has a stronger correlation to the quality measures assessed than the smoothing and post-aliasing properties of the reconstruction filters.

The rest of the paper is organised as follows. In Sec. 2, we discuss related work and the background to reconstruction filters as well as reviewing evaluations of stereoscopic DVR. In Sec. 3, the compactness measure used in the analysis of the results is described. In Sec. 4, we detail the design of the experiment. Sec. 5 presents the results of the experiment and in Sec. 6 these are discussed. We briefly conclude in Sec. 7 and discuss possible future work.

2 Related Work

2.1 DVR

The classic approach for direct volume rendering for each pixel in the image casts a ray directed towards the volumetric data. Along this ray samples are taken of the volumetric data. As volumetric data is discrete it is necessary to interpolate the data at points away from the grid nodes. To produce values for these off-grid sample points a reconstruction filter is used. If the sample rate along the ray is at or above the Nyquist rate the *sinc* filter can be used for perfect reconstruction. However, the unbounded support of this filter makes it impractical in most cases.

A significant body of research has been done on the design of practical reconstruction filters. This includes a range of windowing schemes for the sinc filter to create a bounded support filter with some of the properties of perfect reconstruction [32]. Methods that use a prefilter prior to reconstruction to improve the quality of the filtered data [4, 9]. As well as a number of spline based filters, including the Catmull-Rom, cubic B-splines and BC-splines [3, 14, 19].

All practical filters will introduce artefacts into the reconstructed image. The nature and severity of such artefacts is usually studied in the frequency domain. A filter smooths if it deviates from the ideal pass-band behaviour and produces post-aliasing if it deviates from the ideal stop-band behaviour in the frequency domain. Visually, in the final rendered images smoothing removes finer details while post-aliasing introduces typical aliasing artefacts. The amount of smoothing and post-aliasing introduced by a filter can be estimated by the metrics in [19]. In Fig. 1(a), the engine data set has been rendered using DVR. Fig. 1(b) shows the data set rendered with the trilinear reconstruction showing aliasing artefacts when zoomed in. In Fig. 1(c) the zoomed in area is noticeably smoother due to using the B-spline filter.

Although reconstruction filters can affect noticeably the visual appearance of DVR images there are surprisingly few studies that assess how observers perceive the differences between the filters or the artefacts produced by them. In [20] a perceptual study was undertaken to see what parameters for the BC-splines causes visual artefacts of blurring, ringing or anisotropy. In a more recent study reconstruction filters were assessed for a path-searching task in 3D [28]. The results there determined that the choice of filter can have an effect on task performance, although it is not clear exactly why the filters produced different results.

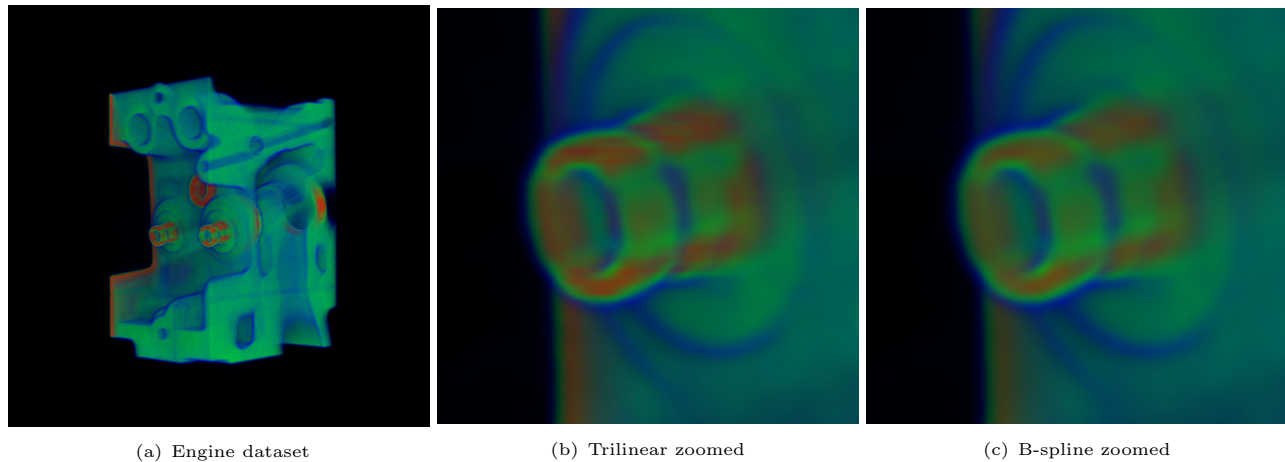


Fig. 1 DVR image of an engine data set illustrating the differences between two reconstruction filters.

2.2 Quality of Stereoscopic DVR

The quality of stereoscopically viewed DVR has been primarily assessed using tasks that require a participant to perform a task related to depth perception. These include the depth ordering evaluations of [5, 7] where volume rendered cylinders are displayed and participants must find their ordering. As well as the more common relative depth tasks requiring participant to find which highlighted feature is closest to themselves [13, 29] and path-searching tasks [2, 28]. These studies give values use the task's accuracy rates to compare the quality of one rendering method or display system over another but do not give any information as to how participants perceive any visual differences.

The literature on the assessment of the perceived quality of stereoscopic DVR is more sparse. In [26] an open comment system was used for participants to remark upon the quality of different display systems used for DVR. Participants positively commented on the quality of a Fishtank display versus a standard 2D display and gave positive comments towards the high levels of immersion in the Cave environment. More formalised quality measures were used in [16] with a Likert scale being used to determine the comfort level, ease of viewing and ease of understanding features in the data sets. The results found that the ease of viewing increased for stereoscopic viewing. The qualitative measures used in these studies are however secondary to the primary task based evaluations performed.

3 Shape compactness

Although there are several methods for defining compactness for planar shapes, the measure used in [18]

is the most widely accepted:

$$C = \frac{4\pi A}{P^2} \quad (1)$$

where A is the area of the shape and P its perimeter. Because of the isoperimetric inequality [23], the compactness value of a shape is always in the range $(0, 1]$. The highest value of compactness is equal to 1 and attained by the disc, while shapes with multiple branching extremities have low values of compactness that approach 0. It is scale invariant and moreover is relatively stable under the almost rigid shape deformations that are common in physical simulations.

3.1 Implementation Details

A simple method for calculating a compactness value for a DVR image is by computing the area and perimeter of the features of the image. By applying a binary thresholding to the DVR image a silhouette of the features is produced. The area of the features is then calculated by counting the number of non-zero pixels while the perimeter is found by applying the Canny edge detection algorithm to the silhouette and counting the number of edge pixels.

We considered two methods of binary thresholding: manual fine tuning for each data set and Otsu's method [24]. Fig. 2 displays the results of the two thresholding methods and the corresponding edge sets returned by the Canny algorithm. Otsu's methods can be seen to be more conservative than manual thresholding. In our analysis we always used Otsu's method since it is fully automatic and thus it was deemed more objective.

Obviously, the compactness values of the DVR images depend heavily on the data set. For example, the engine data set would most likely produce more

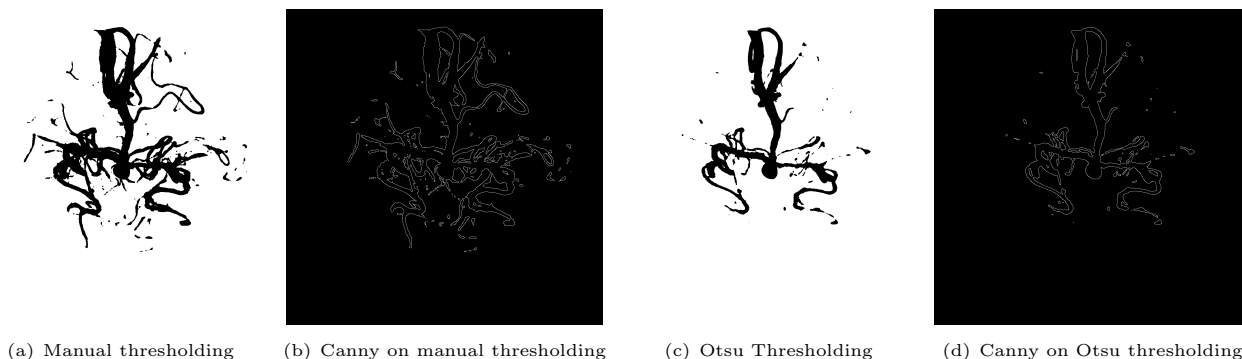


Fig. 2 Thresholding of an angiography data set using the two methods considered.

compact images than the angiography data set, under any reasonable choices of parameter values. On the other hand, and critically for our purposes, the choice of reconstruction filter can also significantly alter the compactness of the rendered images. For example, a filter with a significant smoothing effect can blur and eventually remove from the thresholded image the thinner branches, increasing thus the overall compactness.

4 Experiment Methodology

4.1 Quality Measures

In the assessment of the quality of the stereoscopic volume rendered images and the properties of each reconstruction filter, four different quality measures were used. Tab. 1 shows the descriptions of the quality measures as given to the participants.

The first, depth quality [17], is a critical aspect of stereoscopic viewing and is dependant upon two factors: the stereoscopic image being presented as well as the hardware and viewing settings used to display it. Artefacts such as aliasing and blurring in the image can cause errors between perspective and binocular depth cues [25] and degradation of fine depth perception [8] that may lead to poor depth quality. Low display resolutions and incorrect viewing distances are typical hardware and viewing setting factors that can lead to a poor quality of depth perception.

To determine how reconstruction filters may affect the ability to understand the organisation of the features of the scene, the second measure that was assessed is the depth layout [17]. It characterises how positions and spatial features in a scene are understood. While the depth effect and perspective cues are considered more helpful than stereopsis when determining object positions and how they relate to each other [34], nevertheless, when sampling artefacts

exist, stereopsis combined with linear perspective can provide conflicting depth information to the viewer [25].

The third quality measure was sharpness, which concerns the crispness of details in the stereoscopic images presented. Previous subjective evaluation of stereoscopic images have shown no strong correlations between sharpness and depth quality, necessitating the need for the sharpness and an independent measure [30, 31].

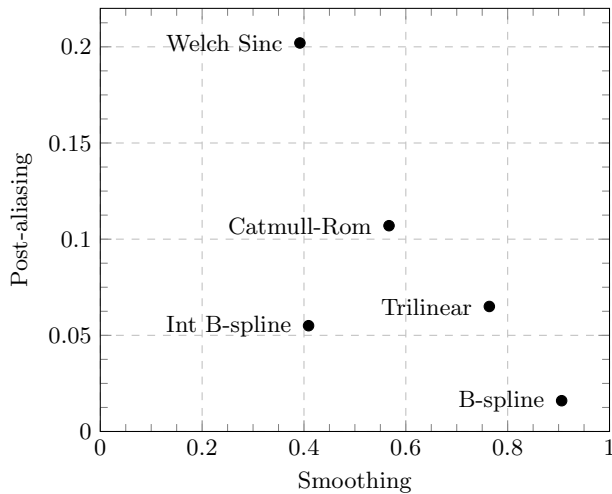
The fourth assessed quality measure assessed was minimal jaggyness. In this case low values of that measure would reflect no jaggy or aliasing artefacts. Increased levels of aliasing in stereoscopic images have been suggested to cause errors in disparity and conflicting depth information [25]. Further, it has been demonstrated that anti-aliasing techniques can increase the ability to perceive depth [11]. One would reasonably expect that reconstruction filters with higher levels of aliasing would lead to higher jagginess scores, however that had to be tested since it has been suggested that a form of binocular averaging occurs between the two eyes that decreases the overall perceived aliasing artefacts [10, 27].

4.2 Reconstruction Filters

Five reconstruction filters have been evaluated: B-spline, trilinear, Catmull-Rom, interpolating B-spline and the Welch windowed sinc. The B-spline filter is an approximation filter and technically not a reconstruction filter, but it is included due to its common usage for noisy data sets. The trilinear filter, being built into GPUs, is the most commonly used filter in DVR. The Catmull-Rom is an interpolating spline with a balance between smoothing and post-aliasing artefacts. The interpolating B-spline uses a prefilter to force the B-spline to interpolate the values at the grid nodes, at the cost of increased post-aliasing artefacts. Finally, the Welch windowed sinc is a windowed version

Tab. 1 Explanations of quality measures given to participants

Quality Measure	Explanation
Depth Quality	is the depth presented in the scene realistic
Depth Layout	how easy is it to understand the organisation of the elements composing the scene
Sharpness	clarity of the details in the image
Minimal Jagginess	excellent if there are no jaggies or staircase artefacts, bad if there are a high number

**Fig. 3** Marschner and Lobb smoothing and post-aliasing values for the five reconstruction filters evaluated. High values indicate high levels of smoothing or post-aliasing.

of the sinc filter that has minimal smoothing but high post-aliasing.

The frequency domain smoothing and post-aliasing metrics of [19] measure the pass-band and stop-band behaviour, respectively. Fig. 3 shows the values of the smoothing and post-aliasing metrics for the five reconstruction filters used in the experiment.

4.3 Stimuli

Four data sets were used in the experiment. Three of them, the angiography, the engine, and the Visible Human are natural and have been created via conventional scanning processes. The volume resolutions of these data sets are $(512 \times 512 \times 512)$, $(256 \times 256 \times 256)$ and $(128 \times 256 \times 256)$ respectively. For each data set the transfer function that assigns colours and opacities has been chosen arbitrarily. Fig. 4(a), Fig. 4(b) and Fig. 4(c) show renderings of each of these data sets using the B-spline reconstruction filter.

The fourth data set, referred to as the graph, is a computer generated data set containing a set of spherical nodes connected to other nodes via cylinders. It has been designed to encapsulate characteristics of natural data sets such as noise, branching and complex

spatial layout. The noise has been introduced by modulating the volume data with a 3D Perlin noise function and the spatial structure of the graph is determined by a graph layout algorithm detailed in [34]. The use of noise and graph layout algorithms produces a volume approximating the irregularities of the natural data sets whilst allowing the overall complexity to be easily controlled by increasing or decreasing the number of nodes. The data set was produced by the publicly available software *vxtl* [22] at a resolution of $(256 \times 256 \times 256)$. The transfer function was designed to have a degree of semi-transparency whilst still displaying clear structures. Fig. 4(d) shows a rendering of the graph data set with the B-spline filter.

4.4 Equipment and Viewing Conditions

To display the 3D images a stereoscopic True3DI 24" HD-SDI display was used with a resolution of 1920×1200 for each eye and refresh rate of $60Hz$. A 17 inch IBM LCD display, used to display the grading scales for the measurement scores, was positioned to the left of the stereoscopic display. Participants wore linear polarized glasses at all times during the experiments and were seated at a distance of $60cm$ from the display. All light levels were kept constant throughout the experiments.

4.5 Participants

Overall, 20 participants took part in the experiment; 14 women and 6 men with ages ranging from 18 to 29. All participants were paid $\pounds 5$ for taking part in the experiment. The Bailey and Snellen chart were used to screen participants for vision and the Titmus fly stereo test was used to screen for stereo-vision.

The participants of the experiment did not have prior experience with analysing volumetric data sets, however some were familiar with stereoscopic displays. In the literature, the choice between novice and expert participants in experiments involving the analysis of volumetric scenes is a matter still open for discussion. Although domain experts can provide highly specific results, novice participants are free of preconceived biases towards particular display methods or rendering

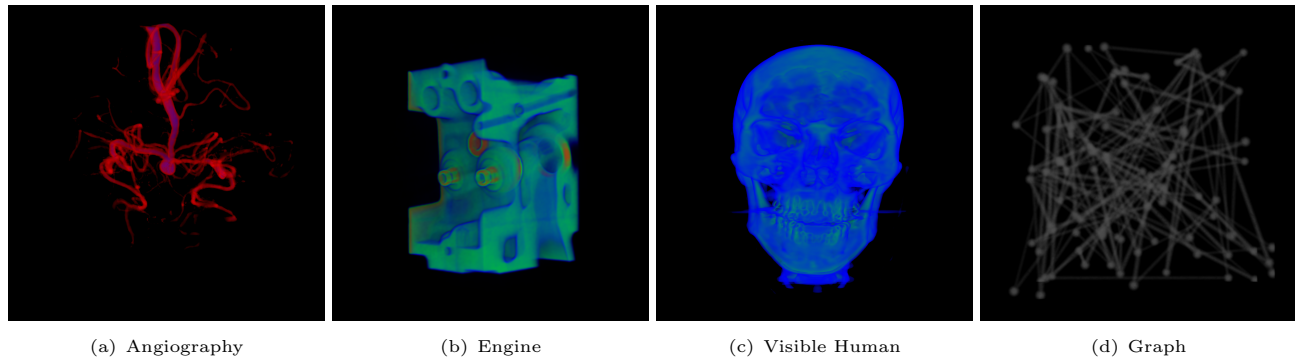


Fig. 4 Example renderings of the four data sets used in the experiment.

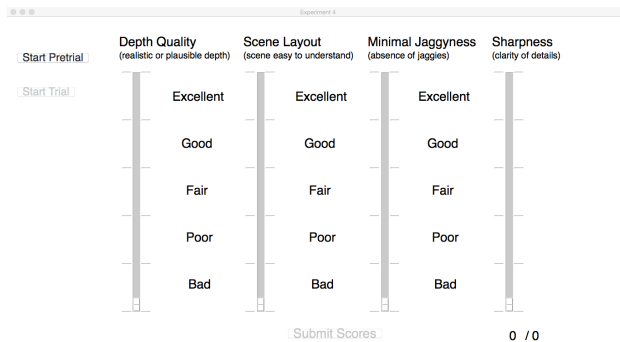


Fig. 5 Grading scales used for the subjective experiment

styles [15, 16].

4.6 Procedure

Before the main experiment, each participant took a pretrial test where five images were displayed and rated for each of the four measurements. For the pretrial test no scores were recorded. In the main experiment, for each participant, the images of each data set were shown as a block sequence, i.e. there was no interleaving between data sets. The ordering of the four data sets for each participant was determined via a Latin Square design, while the ordering of the reconstruction filters for each data set was random.

For each image in the experiment four grading scales were used, one for each of the quality measurements assessed. The sliding scales were divided into five regions labelled Excellent, Good, Fair, Poor and Bad according to the ITU-R BT.500 recommendations [1]. The scale was continuous with values ranging from 0-100, which were not presented to the participant. After submitting the scores for an image, a blank screen was displayed for 3 seconds. Fig. 5 shows the grading scales used for the experiment.

5 Results

Sec. 5.1.1, Sec. 5.1.2, Sec. 5.1.3 and Sec. 5.1.4 present the statistical analysis of the results of the experiment for the Angiography, Engine, Visible Human and Graph data sets, respectively. In Sec. 5.2, we analyse the relationship between the smoothing and post-aliasing of the reconstruction filters and the quality scores. Finally, in Sec. 5.3 we analyse the relationship between the compactness of the test images and the quality scores.

5.1 Results of the Experiment

Prior to performing statistical analysis of the results, the subjective scores from each participant for each measure were transformed to z-scores. This is required because not all participants use the entire range of the scales presented when rating the images, therefore their scores are not directly comparable. To normalize the raw scores into z-scores the values are converted into standard deviation units that represent deviations from the mean [33]. Fig. 6 shows the average z-score values for each data set, quality measure and reconstruction filter.

Following the ITU-R BT.500 recommendations, an analysis of the results per individual participant was performed prior to the main statistical analysis [1]. This was done to potentially remove participants who may have misunderstood the individual quality measures used in the experiment. The β^2 normality test was used for each participant and quality measure separately. The test determined that no participants should be removed prior to full analysis.

For the main analysis, the z-scores for each measure per data set were subjected to a one-way repeated measures of analysis of variance (ANOVA) with the reconstruction filter as the independent variable and the score as the dependent variable. In the cases

when the assumption of sphericity failed after applying Mauchly's Test of Sphericity, the Greenhouse-Geisser correction was applied. When applicable, post-hoc analysis was performed using the pairwise Bonferroni test. In reporting the results, we use the standard notation of F and p for the F -statistic and the p -value, respectively, while for the effect size we report the partial η^2 .

5.1.1 Angiography

The choice of reconstruction filter was found to have a significant effect on depth quality when viewing the angiography data set. The results of the ANOVA were $F(4, 76) = 3.152$, $p = 0.019$, partial $\eta^2 = 0.142$. Despite the interpolating B-spline having the lowest depth quality with a z-score of -0.253 and the Welch windowed sinc having the highest with 0.473 a post-hoc pairwise Bonferroni test revealed no significant interactions between individual pairs of reconstruction filters.

Regarding the sharpness measure, the choice of reconstruction filter was found to have a significant effect with the results of the ANOVA being $F(4, 76) = 2.991$, $p = 0.024$, partial $\eta^2 = 0.071$. Following a post-hoc Bonferroni test, significant differences were found between the trilinear (0.362) and interpolating B-spline (-0.433), $p = 0.044$.

Significant differences were found when analysing the scores for the minimal jaggyness measure with $F(4, 76) = 5.739$, $p < 0.001$ and partial $\eta^2 = 0.232$. According to a post-hoc Bonferroni pairwise test, the B-spline (0.532) was significantly different from the Catmull-Rom (-0.516), $p = 0.008$ and the interpolating B-spline, (-0.559), $p = 0.003$.

There was no statistical significance of reconstruction filters on the depth layout measure for the angiography data set.

5.1.2 Engine

For the engine data set, the choice of reconstruction filter was found to have a significant effect on depth quality. Mauchly's test of Sphericity was violated with $p = 0.005$ and therefore the Greenhouse-Geisser correction was used. The results of the ANOVA were $F(2.492, 47.537) = 3.284$, $p = 0.036$, partial $\eta^2 = 0.147$. No significant interactions between pairs of reconstruction filters were found according to a post-hoc pairwise Bonferroni test. However, the trilinear filter had the lowest depth quality with an average of -0.075 and the interpolating B-spline had the highest with 0.697 .

The choice of reconstruction filter was found to have

a significant effect on sharpness, with the results of the ANOVA being $F(4, 76) = 4.582$, $p = 0.002$, partial $\eta^2 = 0.194$. A follow-up Bonferroni test reported that the sharpness score of the B-spline filter (0.240) was significantly lower than the interpolating B-spline (0.787), $p = 0.025$ and the Welch windowed sinc (0.836), $p = 0.016$.

The results of ANOVA showed that there was no significant effect of the choice of reconstruction filter on depth layout or minimal jaggyness for the engine data set.

5.1.3 Visible Human Data Set

A significant effect was found on depth quality with the ANOVA reporting $F(4, 76) = 4.612$, $p = 0.002$, partial $\eta^2 = 0.195$. Follow-up post-hoc tests revealed no significant interactions between pairs of reconstruction filters, however the Catmull-Rom filter had the lowest average with -0.204 and the interpolating B-spline had the highest with 0.508 .

The ANOVA for minimal jaggyness also reported statistical significance. Sphericity had been violated with $p = 0.005$ and so the Greenhouse-Geisser correction was applied. The ANOVA results were $F(2.678, 50.883) = 3.039$, $p = 0.043$, partial $\eta^2 = 0.138$. No interactions were found between individual reconstruction filters, however the trilinear filter had the lowest average with -0.254 and the B-spline had the highest with 0.482 .

The choice of reconstruction filter had no statistically significant effect on the depth layout and the sharpness scores.

5.1.4 Graph

The choice of reconstruction filter was found to only have an effect on the minimal jaggyness measure with the ANOVA reporting $F(4, 76) = 4.308$, $p = 0.003$. A Bonferroni test reported that the B-spline filter (-0.046) was significantly different from the Welch windowed sinc filter (-0.721) with $p = 0.013$.

No significant results were reported for the depth quality, depth layout and the sharpness measures.

5.2 Correlations with Smoothing and Post-aliasing

The smoothing and post-aliasing introduced by the reconstruction filter correspond to the blurring and aliasing of the features of the rendered images. These artefacts can degrade depth perception when viewing stereoscopic scenes [8, 25]. Here, we investigate whether these properties of the filters are related to how observers perceived the images by measuring the

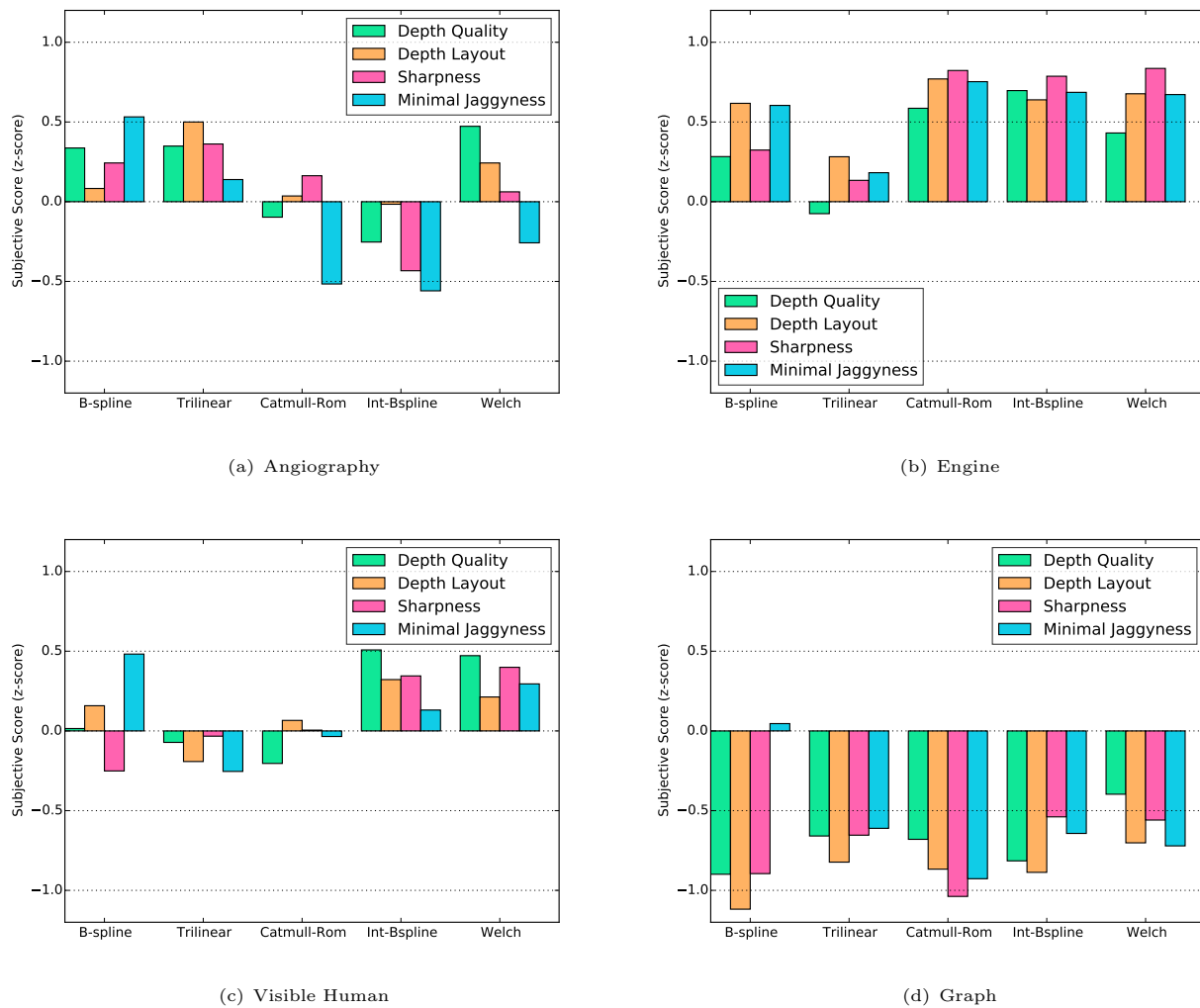


Fig. 6 Plot of average z-score results.

correlation between the smoothing and post-aliasing metrics on the filters proposed in of [19], and the quality scores obtained from the experiment.

The smoothing and post-aliasing values for the reconstruction filters used in the experiment are shown in Fig. 3. The Pearson correlation coefficients were computed to determine if a linear relationship exists between the smoothing and post-aliasing properties and the quality scores obtained from the experiment. A summary of the results can be seen in Tab. 2. There were no strong correlations between either of the frequency domain metrics and the quality scores obtained.

5.3 Correlations with Compactness

The frequency domain metrics used to measure smoothing and post-aliasing are filter specific in that

they are independent of the data set used or images they produces. As an alternative we investigated whether the image specific measure of shape compactness was correlated with the quality scores obtained.

The compactness of each image used in the experiment was computed by the method described in Sec. 3. We found that the compactness analysis gives very similar results when it is applied on the left images of the stereoscopic pairs, or the right images, or on combined cyclopean images. For simplicity, here we only report the analysis for the left images. The compactness measures for each of the twenty images used in the experiment can be seen in Fig. 7(a) and Fig. 7(b). From the results we can see that the Engine and Visible Human data sets have high compactness values where as the Angiography and Graph data sets have low values. In all cases, the use of the B-spline

Tab. 2 Correlations between smoothing and post-aliasing and quality scores

		Depth Quality	Depth Layout	Minimal Jaggyness	Sharpness
Post-aliasing	r	0.210	0.099	-0.166	0.191
	p	0.374	0.677	0.483	0.419
Smoothing	r	-0.192	-0.096	0.249	-0.194
	p	0.418	0.686	0.289	0.412

approximation filter gave the highest compactness.

After computing the compactness measures for the images Pearson correlation coefficients were computed to see if a relationship exists between image compactness and the quality scores. A summary of the results is shown in Tab. 3. There was a moderate positive correlation between the compactness measure and the quality of depth reported by the participant, $r(18) = 0.475$, $p < 0.05$ with compactness statistically explaining 22.563% of the variation in depth quality. A strong correlation was found for depth layout with $r(18) = 0.557$, $p < 0.05$ with compactness explaining 31.025% of the variation in depth layout. Compactness was also found to have a strong correlation with minimal jaggyness with $r(18) = 0.605$, $p < 0.01$ and compactness statistically explaining 36.603% of the variation in scores found. A further strong correlation was found for sharpness with $r(18) = 0.510$, $p < 0.05$ and compactness explaining 26.010% of the variance in sharpness scores.

6 Discussion

From the overall analysis of the results, the largest factor in the differences in quality scores is the data set itself. The natural data sets reported higher scores for the quality measures than for the computer generated data set, implying a preference towards non-computer generated data sets.

However, in many practical situations users do not have control over the data sets they view and it is therefore a significant finding that the choice of reconstruction filter had an effect on the quality scores. Indeed, in the three natural data sets, the choice of reconstruction filter was found to have a significant effect on the depth quality. On the other hand, exactly how the choice of reconstruction filter affects depth quality is still not clear. The interpolating B-spline had the highest depth quality measure for the Engine and the Visible Human data sets, while for the Angiography data set the interpolating B-spline had the lowest score. This suggests that some processing and analysis of the volumetric data is required before choosing the optimal

reconstruction filter for viewing them.

Reconstruction filters were found to have no significant effect on the depth layout scores for any of the data sets used in the experiment. This implies that the differences in the images do not affect the general ability to understand global features in the scene. It also suggests that the perceived relationships between object positions are unaffected by the choice of reconstruction filter.

As expected from an approximating filter, the B-spline had significantly higher minimal jaggyness scores in most cases. This implies that it produces images with the fewest number of perceived aliasing artefacts, meaning that its low Marschner and Lobb post-aliasing value, see Fig. 3, has visual significance.

For the Angiography and Engine data sets the sharpness quality measure was affected by the reconstruction filter, however the results vary considerably between the data sets. This suggests that the data set is the primary factor affecting the values of this measure.

6.1 Smoothing and Post-aliasing

The Pearson correlation coefficients indicate that the smoothing and post-aliasing properties of the reconstruction filters have only small correlations with the quality measures, i.e., r coefficients in or very near the region of $[0.1, 0.3]$. Moreover, these measured correlations are not statistically significant. This suggests that a choice of reconstruction filter based on its smoothing and post-aliasing properties alone does not guarantee any level of quality and that other data set specific factors must be considered.

6.2 Compactness

Unlike smoothing and post-aliasing, the shape compactness measure was found to have a strong correlation to each of the quality measures assessed in the experiment, i.e., r coefficients in or very near the region of $[0.5, 1.0]$. In each case, a high compactness measure implies a high score for depth quality, depth layout, minimal jaggyness and sharpness. If a choice

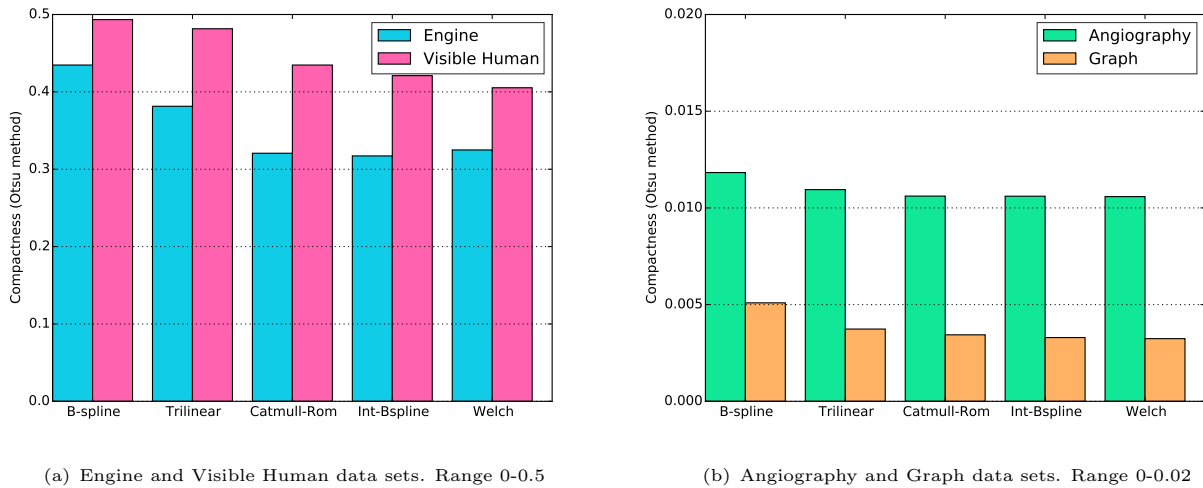


Fig. 7 Plots of compactness measures split into two graphs with different scalings of the y -axis due to the polarization of the results.

Tab. 3 Relations between compactness and quality scores. * denotes significance at 0.05, ** denotes significance at 0.01.

		Depth Quality	Depth Layout	Minimal Jaggyness	Sharpness
Compactness	r	0.475*	0.557*	0.605**	0.510*
	p	0.034	0.011	0.005	0.022

of data set is possible, then data sets with high compactness, such as the Engine and the Visible Human, should be preferred. Of course, in many applications we do not choose the data set. In such cases, the compactness values in Fig. 7 show that the B-spline filter produces the highest compactness across all data sets and so should be preferred. If an approximation filter is not suitable, then according to the results the trilinear filter should be the second preference.

7 Conclusion

In this paper we have evaluated several quality measures on stereoscopic DVR images produced by various reconstruction filters. The results suggest that the choice of reconstruction filter affects the perceived quality of depth in stereoscopic DVR images but not the understanding of the layout of objects in the scene. We have found that the frequency domain measures of smoothing and post-aliasing of individual filters do not correlate with any of the quality measures. Instead, a positive correlation was found between the compactness of the images and each of the quality measures, with the B-spline approximation filter producing the most compact images.

From a practical point of view, the results suggest that we cannot choose an optimal reconstruction filter using the filter specific measures of smoothness and post-aliasing. However, based on the strong correlation between image compactness and depth perception, a possible strategy for choosing reconstruction filter would be to render the dataset with several filters, compute the compactness measure of each rendered image and, finally, present to the viewer the image with the highest compactness.

In the future, we plan to extend the study to include both novices and expert users of DVR to see how the preferences may differ between these groups. Since transfer functions can also have a significant effect on tasks requiring depth perception [5], a second possible extension of the research presented in this paper is to study the effect of the choice of transfer function on the quality measures of stereoscopic DVR.

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