

# Colours and luminosities of $z = 0.1$ galaxies in the EAGLE simulation

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## ABSTRACT

We calculate the colours and luminosities of redshift  $z = 0.1$  galaxies from the EAGLE simulation suite using the GALAXEV population synthesis models. We take into account obscuration by dust in birth clouds and diffuse interstellar medium using a two-component screen model, following the prescription of Charlot and Fall. We compare models in which the dust optical depth is constant to models where it depends on gas metallicity, gas fraction and orientation. The colours of EAGLE galaxies for the more sophisticated models are in broad agreement with those of observed galaxies. In particular, EAGLE produces a red sequence of passive galaxies and a blue cloud of star-forming galaxies, with approximately the correct fraction of galaxies in each population and with  $g - r$  colours within 0.1 mag of those observed. Luminosity functions from ultraviolet to near-infrared wavelengths differ from observations at a level comparable to systematic shifts resulting from a choice between Petrosian and Kron photometric apertures. Despite the generally good agreement there are clear discrepancies with observations. The blue cloud of EAGLE galaxies extends to somewhat higher luminosities than in the data, consistent with the modest underestimate of the passive fraction in massive EAGLE galaxies. There is also a moderate excess of bright blue galaxies compared to observations. The overall level of agreement with the observed colour distribution suggests that EAGLE galaxies at  $z = 0.1$  have ages, metallicities and levels of obscuration that are comparable to those of observed galaxies.

**Key words:** galaxies: general – galaxies: luminosity function, mass function.

## 1 INTRODUCTION

The basic scenario for how galaxies form and evolve is well established: gas accretes on to deepening dark matter potential wells, cools and makes stars. Although this basic paradigm has been accepted for many years (e.g. Rees & Ostriker 1977; White & Rees 1978; White & Frenk 1991), many important aspects are still poorly understood. For example, the shape of the galaxy stellar mass function (GSMF) and of the halo dark matter mass function are quite different, so a simple formation model in which a halo of given mass contains a galaxy whose stellar mass is equal to a fixed fraction of its halo mass is ruled out (e.g. White & Frenk 1991; Benson et al. 2003). In addition, galaxy surveys have revealed the presence of many correlations between the stellar properties of galaxies and

galaxy mass, for example bimodality in the colour–magnitude diagram (CMD) in the form of a blue cloud of star-forming galaxies at lower mass, and a red sequence of mostly passive galaxies at higher mass (e.g. Baldry et al. 2004). Clearly, the dynamics and interaction physics of gas play important roles in determining the properties of galaxies.

It is thought that at the faint end of the GSMF supernovae (SNe) quench star formation in small galaxies (Larson 1974; Dekel & Silk 1986) with reionization effectively preventing galaxies from forming in dark matter haloes below a minimum mass (e.g. Rees 1986; Efstathiou 1992; Thoul & Weinberg 1995; Okamoto, Gao & Theuns 2008). Together these processes shape the GSMF at low stellar masses, with dark matter haloes containing increasingly feeble galaxies with decreasing halo mass, until most haloes remain dark (Sawala et al. 2014). In contrast, at higher galaxy masses it is thought to be the feedback from accreting black holes (BHs) that introduces a near exponential cut-off in the GSMF (Bower et al. 2006; Croton et al. 2006).

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That feedback from star formation and BHs together shape the GSMF is energetically plausible, and semi-analytical models (e.g. Cole et al. 2000; Henriques et al. 2013; Gonzalez-Perez et al. 2014; Porter et al. 2014) and numerical simulations (e.g. Oppenheimer et al. 2010; Puchwein & Springel 2013; Vogelsberger et al. 2014; Schaye et al. 2015) that appeal to these processes are able to produce model GSMFs that compare well to observations at redshift  $z \sim 0$ . However, neither the semi-analytical models nor simulations of cosmological volumes come anywhere near resolving the scales at which SNe and BHs inject energy, and so cannot a priori compute the net efficiency of the resulting feedback. Simulations therefore need to rely on a phenomenological description of these crucial processes occurring on unresolved (‘subgrid’) scales, using observations to calibrate the parameters that appear in the subgrid modules. It is then important to quantify the uniqueness and degeneracies in such modelling (Schaye et al. 2010; Crain et al. 2015), while at the same time use very high resolution simulations (e.g. Hopkins, Quataert & Murray 2011; Creasey, Theuns & Bower 2013, 2015; Martizzi, Faucher-Giguère & Quataert 2015; Rosdahl et al. 2015) to try to bridge the gap between numerically unresolved and resolved scales.

The Evolution and Assembly of GaLaxies and their Environment (EAGLE; Crain et al. 2015; Schaye et al. 2015) suite of simulations uses the  $z \sim 0.1$  GSMF, together with observations of galaxy sizes, to calibrate the subgrid physics modules. The GSMF is however not directly observable, but is inferred from luminosity functions (LFs) after applying corrections for dust obscuration, and using simple stellar population (SSP) synthesis models that involve assumptions about stellar evolution, star formation histories, metallicity dependence of stellar emission, etc. With simulations such as EAGLE, we can take the converse approach, attempting to reproduce the observational relations by inputting physical quantities tracked by the simulation. This has the advantage of allowing one to use properties modelled self-consistently such as gas content, metallicity and age to derive observable quantities, rather than treating them as free parameters in ‘SED fitting’ (e.g. Walcher et al. 2011) to estimate physical properties from observations. The colours of EAGLE galaxies are also an important test of the realism of the fiducial EAGLE model.

In this paper, we examine to what extent mock luminosities computed from EAGLE galaxies using SSP models and a simple correction for dust obscuration reproduce the observed LFs (in a range of broad-bands), as well as galaxy colours. The aim is twofold: to provide a test of the realism of EAGLE, but also to test at some level whether the procedure of going from luminosity to stellar mass is reliable, as investigated in a recent paper by Torrey et al. (2015) using spectral energy distribution (SED) fitting of galaxies from the ILLUSTRIS simulation (Vogelsberger et al. 2014). It is perfectly possible that EAGLE galaxies have the wrong colours but the right stellar masses and stellar ages if errors in dust modelling are severe. However, if masses and colours agree with the data, then this increases our confidence that we can use EAGLE to investigate, for example, the origin of the observed bimodality of galaxy colours, or the nature of the galaxies that lie in between the red sequence and blue cloud in a CMD.

In what follows we compare to photometric data from the Galaxy And Mass Assembly survey (GAMA; Driver et al. 2011). This is a spectroscopic follow-up based on photometric data from the Sloan Digital Sky Survey (SDSS) and the UK Infrared Digital Sky Survey (UKIDSS), with details on the targeting and star–galaxy separation in Baldry et al. (2010) and on the GAMA-processed photometry, including matched aperture photometry from  $u$  to  $K$  in Hill et al. (2011). The GAMA survey has been designed for high uniform

**Table 1.** Numerical parameters of those simulations of the EAGLE suite that are used in this paper. From left to right: simulation identifier, side length of cubic volume  $L$  in comoving Mpc (cMpc), initial mass  $m_g$  of baryonic particles, Plummer-equivalent gravitational softening  $\epsilon_{\text{prop}}$  at redshift  $z = 0$  in proper kpc (pkpc).

Name	$L$ (cMpc)	$m_g$ ( $M_\odot$ )	$\epsilon_{\text{prop}}(z = 0)$ (pkpc)
Ref-L025N0376 (Ref-25)	25	$1.81 \times 10^6$	0.70
Recal-L025N0752 (Recal-25)	25	$2.26 \times 10^5$	0.35
Ref-L100N1504 (Ref-100)	100	$1.81 \times 10^6$	0.70

spectroscopic completeness (Robotham et al. 2010) and provides accurate redshifts (using AUTOz; Baldry et al. 2014) for a catalogue of  $\sim 190\,000$  galaxies, as presented by Taylor et al. (2015).

This paper is organized as follows. We begin with an overview of the EAGLE simulations, with emphasis on those aspects that are most relevant for the SSP modelling. In Section 3, we detail the development of our photometric model, concentrating on emission and absorption in Sections 3.1 and 3.2, respectively. This model is applied to yield an optical CMD and multiband LFs for galaxies, which are plotted and discussed in Section 4. We discuss our findings in Section 5 and summarize in Section 6.

## 2 THE EAGLE SIMULATIONS

Full details of the EAGLE simulations can be found in Schaye et al. (2015, hereafter S15) and Crain et al. (2015, hereafter C15); here we give only a brief overview. The EAGLE simulation comprises a suite of cosmological hydrodynamical simulations of periodic cubic volumes performed with the GADGET-3 TreeSPH code (which is an update of the GADGET-2 code last described by Springel 2005). Simulations were performed for a range of volumes and numerical resolutions. Here we concentrate on the reference model, using simulations at different resolution to quantify numerical convergence. The reference model assumes a  $\Lambda$ CDM cosmology with parameters derived from the initial Planck (Planck Collaboration XVI 2014) satellite data release ( $\Omega_b = 0.0482$ ,  $\Omega_{\text{dark}} = 0.2588$ ,  $\Omega_\Lambda = 0.693$  and  $h = 0.6777$ , where  $H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$ ). Relevant properties are listed in Table 1.

We modified the treatment of hydrodynamics in GADGET-3 to use the conservative pressure–entropy SPH formulation of Hopkins (2013), the artificial viscosity switch introduced by Cullen & Dehnen (2010), an artificial conduction switch inspired by Price (2008), the  $C^2$  kernel from Wendland (1995) and the timestep limiter of Durier & Dalla Vecchia (2012). Motivation and tests of this ‘ANARCHY’ version of SPH are presented in Dalla Vecchia (in preparation, see also appendix A of S15), whereas Schaller et al. (in preparation) examine the effects of using this modified version of SPH on galaxy properties.

A crucial aspect of EAGLE is that the parameters describing the subgrid modules have been calibrated on the observed  $z \sim 0$  GSMF and galaxy sizes. This good agreement extends to many other observables that were not considered during the calibration, such as specific star formation rates (S15), the evolution of the GSMF (Furlong et al. 2015), molecular hydrogen fractions (Lagos et al. 2015) and absorption by intergalactic metals and neutral hydrogen (Rahmati et al. 2015; S15).

We now briefly describe those aspects of the subgrid model most relevant for this paper.

## 2.1 EAGLE subgrid physics

The subgrid modules of EAGLE are partly inspired by the OWLS and GIMIC simulations (Crain et al. 2009; Schaye et al. 2010). Star formation is implemented as described in Schaye & Dalla Vecchia (2008): above the metallicity-dependent star formation threshold of Schaye (2004), cold enough particles ( $T \sim 10^4$  K) are converted to star particles stochastically at a pressure-dependent rate that reproduces the observed Kennicutt–Schmidt star formation law. Each simulation star particle is assumed to represent a coeval population of stars formed with a Chabrier (2003) initial mass function (IMF), comprising stars with masses in the range  $[0.1, 100] M_\odot$ .

Stellar evolution is implemented as described in S15 and Wiersma, Schaye & Smith (2009b). We follow the production and release into the interstellar medium (ISM) of 11 elements from three channels of stellar evolution (AGB stars, Type I and Type II SNe) using metallicity-dependent stellar lifetimes and stellar yields. We also track a separate ‘total’ metallicity (the mass fraction of elements more massive than helium),  $Z$ , to account for elements not tracked explicitly. When a gas particle is converted into a star particle it inherits the gas particle’s abundances. In addition to a particle metallicity, the simulation tracks smoothed metallicities which are computed using the SPH formalism to partly remedy the absence of mixing in the calculation (see Wiersma et al. 2009b for motivation). The ages, masses and metallicities of the star particles are the main ingredients of the SSPs models used below.

Radiative cooling and photoheating in the presence of an optically thin UV/X-ray background, as computed by Haardt & Madau (2001), is accounted for as described in Wiersma et al. (2009a). The crucial processes of feedback from star formation is implemented by stochastically heating particles by a fixed temperature increment, as described and motivated in Dalla Vecchia & Schaye (2012), and adapted for the simulation as described in S15 and C15. The formation of supermassive BHs and gas accretion on to them is implemented as in Booth & Schaye (2009), with modifications described in Rosas-Guevara et al. (2013) and S15, using a single feedback mode.

## 2.2 Identifying galaxies

To group star particles into ‘galaxies’, we proceed as follows. We begin by identifying dark matter haloes using the friends-of-friends algorithm (Davis et al. 1985) with a linking length of 0.2 times the mean dark matter interparticle spacing to identify regions that are overdense by a factor of  $\sim 200$  (Lacey & Cole 1994). We then use the SUBFIND algorithm (Springel et al. 2001; Dolag et al. 2009) to identify self-bound substructures (subhaloes) within haloes of dark matter, stars and gas, which we identify with galaxies. Massive galaxies in EAGLE have extended density profiles. To assign luminosities to mock galaxies, we only include light emitted within a sphere of radius 30 proper kpc (pkpc), centred on the minimum of potential of each subhalo. The motivation for the choice of aperture is discussed further in Section 3.1.4 and also in S15.

## 3 PHOTOMETRY

This section explains how we compute luminosities and colours for the simulated EAGLE galaxies. We begin by modelling luminosities of star particles, taking into account their ages and metallicities using population synthesis (Section 3.1), the photometric system used to calculate magnitudes for direct comparison to observation (Section 3.1.3) and the effects of dust absorption (Section 3.2). The

results of this section are summarized in Fig. 1, in which we plot histograms of  $g - r$  colours of EAGLE galaxies in narrow stellar mass bins for different models, ranging from a simple emission model without dust, to a model including a multivariate treatment for dust.

### 3.1 Source modelling

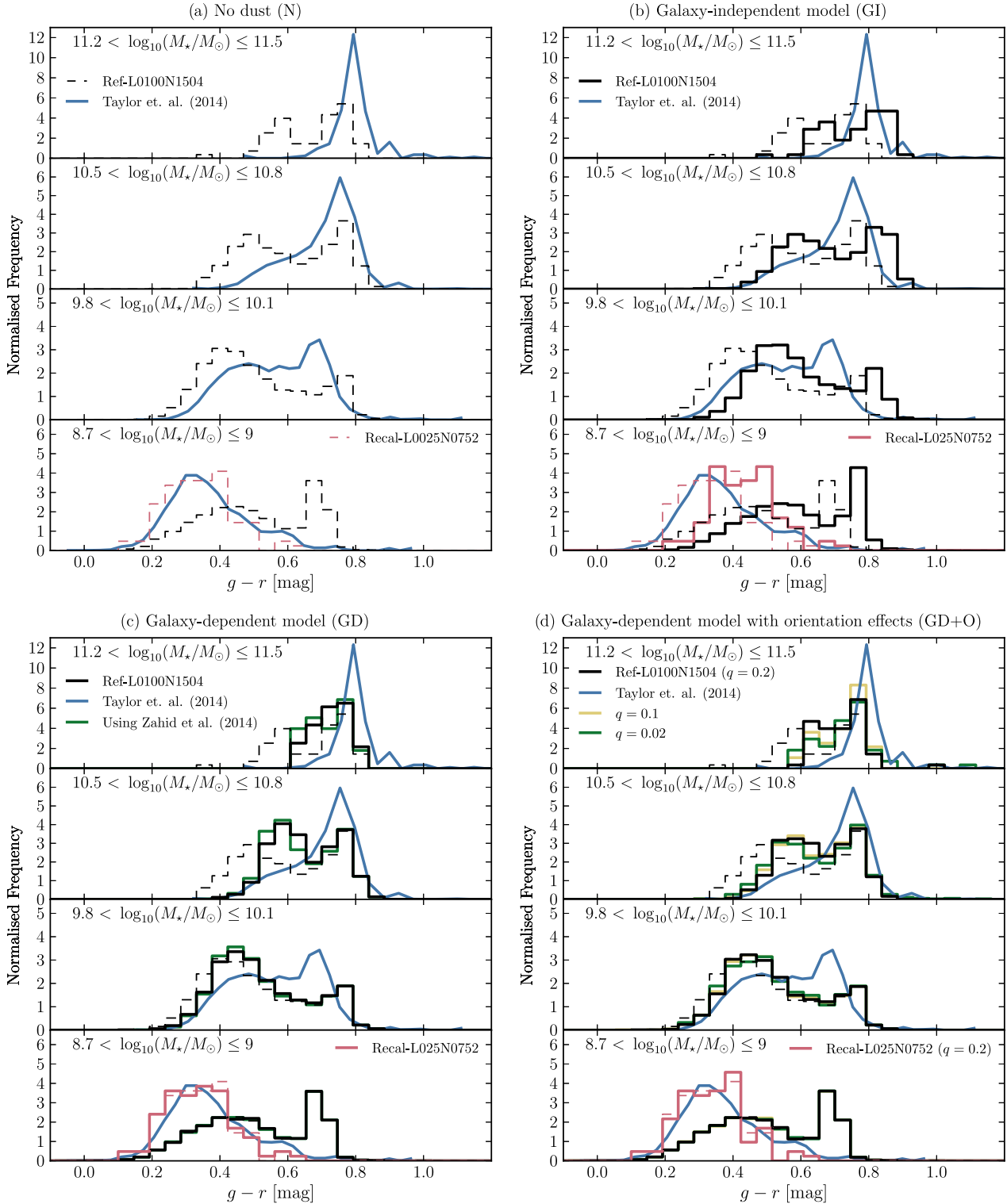
Below we compute luminosities of EAGLE galaxies from the ultraviolet (UV) to the near-infrared (NIR). We limit ourselves to modelling stars, neglecting both nebular emission lines and light from AGN. Light absorbed by dust is assumed to be re-emitted in the far-infrared which we do not study in this paper. As we also neglect scattering by dust, we treat individual wavelength bands independently. This approximation is supported by observations showing that scattering is a negligible contributor to the observed attenuation curve in galaxies (e.g. Fischera, Dopita & Sutherland 2003).

Population synthesis models provide spectra for a discrete range of SSPs (e.g. Leitherer et al. 1999; Bruzual & Charlot 2003; Maraston 2005). These SSPs represent populations of stars characterized by their total initial mass, formation time and composition while assuming some stellar IMF. By decomposing the stellar component of an observed galaxy into a superposition of SSPs, the SED of an entire galaxy can be approximated. In EAGLE, we treat each star particle as an SSP with given initial stellar mass, metallicity and age. These values are set and held fixed from the instant a star particle is formed, where the star particle inherits the gas particle mass and metallicity at the time of formation. The parametrization of the SSP models are elaborated further below.

#### 3.1.1 SSP ingredients

Given our implementation of star formation, where gas particles are wholly converted into star particles, the typical mass of an EAGLE star particle is  $\sim 10^6 M_\odot$ . Stars are assumed to form with a Chabrier (2003) IMF (for consistency with the evolutionary models used in EAGLE), and they inherit the SPH-smoothed metallicity,  $Z$ , from their parent gas particle. The mass of a newly formed star particle is purely set by numerical resolution; the particle should not be thought of as representing a star cluster. In fact,  $10^6 M_\odot$  is higher than the stellar mass formed in giant H II regions (e.g. Relaño & Kennicutt 2009; Zaragoza-Cardiel et al. 2014). This poor sampling of star formation can adversely affect luminosities of EAGLE galaxies. Indeed, a single recently formed star particle can affect the colour of a galaxy. We try to mitigate this numerical artefact by employing a finer sampling of the star formation history of recently formed stars. We do this by assuming that the star formation rate of gas particles is constant over the past 100 Myr, and randomly spawning star particles of mass  $10^4 M_\odot$ , that on average represent this constant star formation rate. We do the same for recently formed star particles (age  $< 100$  Myr), using the star formation rate of the progenitor gas particle at the time of birth. We note that this has only a small effect for optical colours and thus for the results presented here.

The metallicity of stars affects their colours resulting in the well-known age–metallicity degeneracy (e.g. Worthey 1994). In addition,  $Z$  affects stellar evolution leading to differences between models, particularly for the AGB phase (e.g. Inoue 2012; Stancliffe & Jeffery 2007). In addition, metallicity of stars in EAGLE galaxies is set by the intricate interaction between enrichment of the ISM, gas accretion and the extent to which galactic winds transport metals into the galaxy’s circum- and intergalactic medium. The details of such metal mixing are still poorly understood and numerically



**Figure 1.** Rest-frame  $g-r$  colour distributions for EAGLE galaxies at redshift  $z = 0.1$ , using four different models (panels a–d) for four non-contiguous ranges in stellar mass as indicated in the legend (top to bottom). Black lines indicate the fiducial Ref-100 galaxy population, while red lines indicate the higher resolution Recal-25 simulation. Dashed lines denote the unobscured SED (model N); these are repeated in each panel for comparison. Models shown are: model N without dust (panel a, see Section 3.1.5), model GI with galaxy independent dust (panel b, see Section 3.2.1), model GD where the dust obscuration depends on gas fraction and metallicity (panel c, Section 3.2.2), and model GD+O that in addition takes into account orientation effects (panel d, Section 3.2.3). Green and yellow lines show model variations in panels (c) and (d) (see sections 3.2.2–3.2.3 for details). Blue lines represent observed galaxy colours for the volume-limited sample of GAMA galaxies from Taylor et al. (2015). The figure shows the subtle quantitative effects that our different dust models have on the colour distributions of EAGLE galaxies in various  $M_*$  regimes, as is discussed further in the text.



challenging to model. Hence, there is no a priori guarantee that EAGLE yields realistic stellar metallicities.

The stellar mass–metallicity ( $M_*$ – $Z_*$ ) relations provide a useful way of characterizing stellar abundances as a function of galaxy mass, and as shown in S15, the Ref-100 model yields stellar and gas-phase metallicities consistent with observations (Tremonti et al. 2004; Gallazzi et al. 2005; Zahid et al. 2014) for stellar masses  $M_* \gtrsim 10^{10} M_\odot$ . However, lower mass galaxies in EAGLE tend to be more metal-rich than observed, with numerical resolution playing a role: the higher resolution Recal-25 simulation agrees with the data for  $M_* \lesssim 10^9 M_\odot$ . It should also be noted that there are large systematics on the observed mass–metallicity relations (e.g. Kewley & Ellison 2008). We investigate the impact of stellar metallicity ( $Z_*$ ) on EAGLE colours in more detail in Appendix B. In our analysis, we use the EAGLE SPH-smoothed metallicities (Wiersma et al. 2009a) for each particle, which yield less noisy estimates of  $Z_*$ .

### 3.1.2 Stellar population synthesis (SPS) modelling

We adopt the GALAXEV population synthesis models of Bruzual & Charlot (2003), which provide the SED per unit initial stellar mass of an SSP for a discrete grid of ages (ranging from  $t = 10^5$  to  $2 \times 10^{10}$  yr) and metallicities (ranging from  $Z_* = 10^{-4}$  to 0.05). We compute the SED for each stellar particle by interpolating the GALAXEV tracks logarithmically in age and  $Z_*$ , and multiplying by the initial stellar mass. The simulated stellar metallicities reach higher values than the models of Bruzual & Charlot (2003) can represent, with  $\sim 1.5$  per cent of star particles possessing superenriched values. We extrapolate the model to predict colours for the highest metallicities.<sup>1</sup> We note that the more conservative approach of not extrapolating introduces a bias.

The GALAXEV spectra are based on stellar emission alone. These models are widely used, and have been shown to fit the local galaxy population in the optical bands with reasonable star formation and enrichment histories when used in conjunction with a dust model (e.g. Charlot & Fall 2000; Cole et al. 2000). The choice of population synthesis model has been shown to be largely unimportant for low-redshift galaxy populations, especially in optical bands (e.g. Gonzalez-Perez et al. 2014). The effect of different models (e.g. Maraston 2005; Conroy, Gunn & White 2009), and in particular the more uncertain impact of thermally-pulsing AGB stars (TP-AGB) on the SED, should however be considered when surveying higher redshift ( $z \gtrsim 1$ ) galaxy populations (e.g. Maraston 2005; Gonzalez-Perez et al. 2014).

The Bruzual & Charlot (2003) models specify  $Z_*$  values as absolute metal–mass fractions, where  $Z_*$  affects the colours of stars through its impact on stellar structure and evolution – for example via the opacity, equation of state and mean molecular weight – and on stellar atmosphere models. Even so, the metallicity of the Sun ( $Z_\odot$ ) does enter the population synthesis models because some parameters, such as the mixing length, are calibrated based on solar observables (Bressan et al. 1993). Recent literature determinations of  $Z_\odot$  have shown significant variability, with a minimum of  $Z_\odot \sim 0.0126$  (e.g. Asplund et al. 2004) from the traditional value of  $Z_\odot = 0.02$  assumed in Bruzual & Charlot (2003). Although the EAGLE simulations do not make use of any particular solar abundance pattern or  $Z_\odot$  value, a relatively low value of  $Z_\odot = 0.0127$  (Allende

Prieto, Lambert & Asplund 2001) has been assumed in analysis for consistency with Wiersma et al. (2009a) (S15). The variation of  $Z_\odot$  generally results from a different determination of the abundance of some important element, such as O, N, C or Fe which also implies a variation of the abundance partition in the Solar model. In principle, one should use GALAXEV SSP models with an abundance partition consistent with the assumed value of  $Z_\odot$ , and take into account effects arising from the different mixing length calibration, to compute colours self-consistently. For now we neglect any such changes and use the original GALAXEV SEDs, as the effects of this change on broad-band colours are expected to be small, as long as one makes use of the absolute value of the metallicity (Bressan 2014, private communication).<sup>2</sup>

### 3.1.3 Photometric system

Given the SED for each star particle in the simulation, and a model for attenuation due to dust as a function of wavelength, we could compute the SED for each galaxy, and calculate a broad-band magnitude by convolving with a broad-band filter. Here we use a much simpler method, namely we first convolve the GALAXEV spectra (for each value of age and metallicity) with broad-band filters to obtain ‘un-obscured’ broad-band luminosities. We use these to obtain a broad-band luminosity for an EAGLE galaxy. We only then take into account dust attenuation (as described below). If, as we assume, the wavelength dependence of the dust attenuation is not very strong (i.e. the optical depth does not vary strongly over the wavelength extent of the filter), then these two approaches yield very similar results. For the dust models discussed below, we verified that this is indeed the case (Section 3.2).

We use the *ugrizYJHK* photometric system for optical and NIR photometry, to enable a direct comparison to the GAMA survey (described in Driver et al. 2011; Hill et al. 2011). This survey is based on the photometry of SDSS (technical description in York et al. 2000) and UKIDSS, (technical description in Lawrence 2007). Note that when calculating photometry below, filter transmission curves include atmospheric absorption to enable a like-for-like comparison of simulation and observation. All magnitudes are calculated as rest frame and absolute in the AB-system (Oke 1974) in which the apparent magnitude  $m_{AB}$  is defined as

$$m_{AB} \equiv -2.5 \log_{10}(F_\nu) - 48.6, \quad (1)$$

where  $F_\nu$  is the isophotal flux density (in cgs units) in a particular band (e.g. Tokunaga & Vacca 2005).

### 3.1.4 Choice of aperture

Individual EAGLE ‘galaxies’ are identified as described in Section 2.2. We select galaxies with at least 100 star particles, whose stellar mass is reasonably well converged numerically (S15). The line of sight is chosen consistently to lie along an axis of our simulation coordinates, yielding an essentially randomised orientation for each galaxy.

Massive galaxies ( $M_* \gtrsim 10^{10.5} M_\odot$ ) in EAGLE have up to  $\sim 40$  per cent of their stellar mass in an extended halo beyond 30 pkpc of the galaxy centre (‘intracluster light’ since most of these massive galaxies are at the centre of a group or cluster). Observationally, such galaxies also tend to have extended light distributions

<sup>1</sup> We find that the effect of extrapolating metallicities, as opposed to clipping metallicities to that of the highest metallicity GALAXEV spectra, has a small ( $\lesssim 2$  per cent) effect on our optical colours.

<sup>2</sup> We are grateful to S. Charlot and A. Bressan for their detailed explanation of the impact of  $Z_\odot$  on the GALAXEV model.

and, unsurprisingly, the luminosity assigned to them depends on how such light is taken into account (e.g. Bernardi et al. 2013). We apply a constant aperture of 30 pkpc centred on the minimum of the gravitational potential of each subhalo for measuring the total luminosity,  $L$ , of a galaxy. The luminosity and colour of a galaxy with a significant intracluster light component do depend on whether we apply a 2D aperture or a 3D aperture. This change in colour is due to colour gradients but also due to the inclusion or exclusion of small blue satellite objects below the significance of those identified by SUBFIND. This is a similar issue to that encountered when isolating galaxies in astronomical data using software such as SExtractor (Jackson et al. 2010). We choose to apply a 3D spherical aperture, consistent with our previous analysis (Furlong et al. 2015; S15). Such an aperture is shown in S15 to yield similar stellar masses to a Petrosian aperture, often used in observational studies.

The aperture definition is not standardized in observations, and can make a difference when a considerable fraction of stellar material lies outside the aperture. This is illustrated for the Kron and Petrosian apertures in Driver (2012), where luminous galaxies with high Sérsic indices yield different magnitudes. Similarly, when analysing our simulations, the luminosities of EAGLE galaxies with  $M_* \gtrsim 10^{11} M_\odot$  are sensitive to the exact choice of aperture size. However, this is not the case for lower mass galaxies, for which the fraction of light in an extended halo is much lower.

### 3.1.5 Model N

The procedure for obtaining EAGLE galaxy photometry outlined above (Sections 3.1.1–3.1.4) provides a model with no consideration of dust effects. This is hereafter referred to as model N. Model N provides a basis for comparison with photometry corrected for dust attenuation, as described below (Sections 3.2.1–3.2.3). Panel (a) of Fig. 1 shows the  $g - r$  colour distribution of EAGLE galaxies for this model.

## 3.2 Dust model

We develop a simple *empirically calibrated* model for dust absorption, as opposed to a more physical modelling using ray-tracing, which we will present elsewhere. One advantage of such a model is that we can easily disentangle the effects of dust from those of the SPS modelling on galaxy colours. In addition, if we model dust attenuation using galaxy parameters that are provided by EAGLE but can also be inferred through observation, then we may calibrate the reddening of EAGLE galaxy colours empirically to reproduce observed trends. Keeping our dust model parametrization independent of certain quantities, such as the gas distribution, also allows us more freedom to investigate the extent to which certain assumptions affect galaxy colours.

In our modelling, dust corrections are applied as a multiplicative factor that reduces a given broad-band luminosity. This factor is estimated at the effective wavelength of each filter (SDSS filter parameters taken from Doi et al. 2010, UKIRT filter parameters taken from Hewett et al. 2006), for a given dust prescription (neglecting changes in the dust opacity within a broad-band filter is a good approximation provided the dust model has a smooth wavelength dependence). In this way, dust obscuration depends on the subhalo properties of a galaxy alone, and we avoid handling entire SEDs and generating a new interpolation grid for each galaxy. This makes the analysis process very efficient. The approximation that reddening can be applied *after* the spectrum has already passed through a

filter affects the  $g - r$  optical colours by  $\lesssim 0.02$  mag over the whole interpolation grid for the constant optical depth model discussed below.

### 3.2.1 Model GI: galaxy-independent dust model

We begin by discussing the simplest dust model introduced by Charlot & Fall (2000, hereafter CF). This model includes two contributions to the dust optical depth in a galaxy ( $\hat{\tau}_d$ ): (i) a transient component due to dust in stellar birth clouds ( $\hat{\tau}_{bc}$ ), and (ii) a constant dust screen that represents dust in the ISM ( $\hat{\tau}_{ism}$ ). The transmission  $T$  of this model is

$$T(\lambda, t') = \begin{cases} \exp\left(-[\hat{\tau}_{bc} + \hat{\tau}_{ism}]\left(\frac{\lambda}{\lambda_v}\right)^{-0.7}\right), & \text{for } t' \leq t_{\text{disp}}, \\ \exp\left(-\hat{\tau}_{ism}\left(\frac{\lambda}{\lambda_v}\right)^{-0.7}\right), & \text{for } t' > t_{\text{disp}}. \end{cases} \quad (2)$$

Here,  $t'$  is the stellar particle's age,  $t_{\text{disp}}$  is the dispersal time of the stellar birth cloud,  $\lambda$  is the wavelength of light and  $\hat{\tau}_{ism}$  and  $\hat{\tau}_{bc}$  characterize the total dust optical depth (due to ISM and birth-cloud, respectively), at wavelength  $\lambda_v$ . When a model SED of a galaxy is fitted to an observed galaxy,  $\hat{\tau}_{ism}$  and  $\hat{\tau}_{bc}$  can be used as fitting parameters to model dust (e.g. da Cunha, Charlot & Elbaz 2008). Alternatively, these parameters can be assigned constant values to model dust for a given population of galaxies as in Bruzual & Charlot (2003), but this does then not allow for variations between galaxies.

As a first approximation we simply take  $\hat{\tau}_{ism}$  and  $\hat{\tau}_{bc}$  to be constants,

$$\begin{aligned} \hat{\tau}_{bc} &= 0.67 \\ \hat{\tau}_{ism} &= 0.33, \end{aligned} \quad (3)$$

with  $\lambda_v = 5500 \text{ \AA}$  and  $t_{\text{disp}} = 10^7 \text{ yr}$ , which were calibrated to fit starburst galaxies and were used for the recent analysis of the ILLUSTRIS simulations (Vogelsberger et al. 2014) by Genel et al. (2014) and Torrey et al. (2015). With the optical depths fixed, the colours of an EAGLE galaxy will only depend on the SSP modelling. Such an approximation was also used in the development of the GALAXEV model, where it was shown to work well when SED fitting a subset of the SDSS survey at  $z = 0.1$  (Bruzual & Charlot 2003). The effect of this simple dust model on  $g - r$  colours can be seen by comparing panels (a) and (b) in Fig. 1, and is discussed in more detail below.

In this simple model (model GI), the strength of the two screen components are fixed for each galaxy (and hence do not depend on e.g. its gas mass or metallicity) and are also independent of orientation. We discuss refinements of the dust model next.

### 3.2.2 Model GD: ISM-dependent dust model

To account for variations in metal enrichment in the ISM of galaxies, we use the mass-weighted SPH-smoothed metallicity (Wiersma et al. 2009a) calculated for star-forming gas in each EAGLE subhalo,  $Z_{\text{SF}}$ . This metallicity calculation is chosen to imitate observational measurement techniques (Tremonti et al. 2004; Zahid et al. 2014). As demonstrated in S15, the mass–metallicity relations in EAGLE are significantly affected by resolution, with the Recal-25 simulation showing better agreement with the observed  $Z_g - M_*$  relation from

Tremonti et al. (2004) than Ref-100 for  $M_* \ll 10^{10} M_\odot$ .<sup>3</sup> Near the knee of the mass function, however, the EAGLE mass–metallicity relation agrees well with observation (see S15).

We take the analytic expression for the  $M_*$ – $Z_g$  mass–metallicity relation at  $z = 0.1$  of Zahid et al. (2014),  $Z_{14}(M_*)$ , evaluated at the Milky Way stellar mass,  $M_{\text{MW}} = 6.43 \times 10^{10} M_\odot$  (McMillan 2011), as the ISM metallicity represented by the optical depth values of equation (2). Assuming optical depth is proportional to metallicity, we then scale the optical depths  $\hat{\tau}_{\text{bc}}$  and  $\hat{\tau}_{\text{ISM}}$  that appear in equation (2) by the factor

$$\begin{aligned}\hat{\tau}_{\text{bc}} &\rightarrow \frac{Z_{\text{SF}}}{Z_{14}(M_* = M_{\text{MW}})} \hat{\tau}_{\text{bc}} \\ \hat{\tau}_{\text{ISM}} &\rightarrow \frac{Z_{\text{SF}}}{Z_{14}(M_* = M_{\text{MW}})} \hat{\tau}_{\text{ISM}},\end{aligned}\quad (4)$$

for each EAGLE galaxy.

Making the dust optical depth depend on metallicity is physically well motivated, as it is indicative of the fraction of ISM mass in dust grains. Therefore, we must also take account of the gas mass to quantify how much dust is available for obscuration. We do so by making the dust optical depth dependent on the *cold gas* mass – but still neglect how that gas is distributed.

We approximate the cold gas mass,  $M_{\text{ISM}}$ , by the mass in star-forming gas, which in EAGLE means gas above a given metallicity-dependent density threshold and below a given temperature (see S15). We then scale the birth cloud and ISM dust optical depths by the ratio of  $M_{\text{ISM}}$  for the galaxy over the value for the Milky Way (which we take to be 10 per cent of  $M_*$ ; Mo, van den Bosch & White 2010; McMillan 2011). This scaling is derived from observations indicating that optical depths approximately scale with the overall gas surface density ( $\Sigma_g$ ) of galaxies (e.g. Boquien et al. 2013; Grootes et al. 2013). By taking  $\Sigma_g$  as approximately  $\propto M_{\text{ISM}}/R_*^2$ , and since the  $z = 0.1$  stellar mass–size relation is relatively flat for both EAGLE (S15) and observed galaxies (Shen et al. 2003), we approximate that  $\tau \propto \Sigma_g \propto M_{\text{ISM}}$ . Neglecting the  $R_*^{-2}$  dependence maintains a relatively simple parametrization, and appears to have little effect on galaxy colours, due to the limited mass range over which reddening is significant.

Such a scaling has the desired effect of reddening gas-rich spiral galaxies more than gas-poor elliptical galaxies at the same  $M_*$ . The galaxy  $g - r$  colour distributions for the model including metallicity and gas fraction dependent reddening (model GD) are shown in Fig. 1(c). For comparison, we also show the  $g - r$  colour distributions for EAGLE galaxies where the value of  $Z_{14}(M_*)$  is used in equation (4), instead of  $Z_{\text{SF}}$ . Because low  $M_{\text{ISM}}$  values provide low optical depths for the stellar mass range where EAGLE and observed mass–metallicity relations differ ( $M_* \ll 10^{10} M_\odot$ ), both treatments produce similar distributions.

### 3.2.3 Model GD+O: ISM-dependent dust model with orientation effects

Finally, we represent the dependence of obscuration on orientation with a simple toy model. We assume the dust geometry to be an oblate spheroid, with major to minor axial ratio of  $q = a/b = 0.2$ .

This  $q$  value is commonly used to represent an axial ratio typical of the intrinsic stellar distribution in disc galaxies (e.g. Tully & Fisher 1977). We assign to each EAGLE galaxy an orientation  $w = \cos(\theta)$ , where  $\theta$  is the angle between the galaxy’s minor axis and the line of sight. To obtain a random orientation, we randomly sample  $w$  from a uniform distribution over the interval  $[-1, 1]$ . The line-of-sight depth through the dust spheroid is then

$$l(w) = a \frac{q}{\sqrt{q^2 + (1 - q^2)w^2}}. \quad (5)$$

We then scale  $\hat{\tau}_{\text{ISM}}$  as

$$\hat{\tau}_{\text{ISM}} \rightarrow \frac{l(w)}{\langle l \rangle} \hat{\tau}_{\text{ISM}}, \quad (6)$$

so that the mean optical depth does not change. This scaling reduces the amount of dust obscuration for most galaxies by a small amount, yet increases  $\tau$  by a factor of  $\sim 2$  for a small number of ‘edge-on’ systems. We assume a value of  $q$  that is appropriate for discs, but we note that elliptical galaxies – provided they have little cold gas – are not strongly reddened anyway, hence this orientation correction is not important for them. The  $g - r$  colour histograms including orientation effects are shown as model GD+O in Fig. 1(d). We also show the colour distributions produced using more oblate geometries, with axial ratio values  $q = 0.1$  and  $q = 0.02$ , for comparison.

## 4 RESULTS

In this section we examine the effects of dust modelling on the colours, luminosities and CMDs of EAGLE galaxies taken from the Ref-100 and Recal-25 models at redshift  $z = 0.1$ .

### 4.1 Galaxy colours as a function of stellar mass

We contrast  $g - r$  colours for EAGLE galaxies in narrow (0.3 dex) bins of  $M_*$  for different models of dust absorption in Fig. 1 (panels a–d). In all panels, the blue line corresponds to the observed distribution from the GAMA survey (Taylor et al. 2015). Different panels show models with no dust (model N, panel a), a dust model that is independent of galaxy type (model GI, panel b), a model in which dust opacity depends on metallicity and gas fraction (model GD, panel c), and finally a model that in addition accounts for orientation effects (model GD+O, panel d). All models are shown as histograms, normalized to have unit integral. Models including dust are plotted as solid histograms, while the dashed histograms represent model N in all panels. Ref-100 distributions for the fiducial dust models are plotted in black, whereas Recal-25 distributions are plotted (for the lowest mass bin) in red. Model variations are also plotted for Ref-100, with a model using the observed mass–metallicity relation in panel (c) shown in green (see Section 3.2.2) and models with alternative  $q$  values in panel (d) shown in green and yellow (see Section 3.2.3).

The observed  $g - r$  colours shift from very red massive galaxies (usually termed the ‘red sequence’), to a broader distribution in colours for  $10^{9.8} \lesssim M_*/M_\odot \lesssim 10^{10.8}$ , and finally a blue population (usually termed ‘blue cloud’) at lower stellar masses. There is little evidence for a strong ‘bimodality’ in observed colours even though the data is often interpreted that way. Such an interpretation is perhaps due to the bimodality seen at a fixed optical magnitude, where blue galaxies are pushed into higher luminosity bins.

Before comparing the models to the data, we investigate the effects of dust modelling, going from high- to low-mass galaxies (top to bottom rows in panels a–d). The most massive galaxies

<sup>3</sup> Note, however, that the observed mass–metallicity relation suffers from calibration uncertainties that exceed the difference between Tremonti et al. (2004) and Ref-100 (Kewley & Ellison 2008) and that the more recent re-analysis by Zahid et al. (2014) falls in between Ref-100 and Tremonti et al. (2004, see fig. 13 of S15).



( $10^{11.2} \lesssim M_*/M_\odot \lesssim 10^{11.5}$ , top rows) have a relatively extended intrinsic colour distribution (model N). Including a model with dust reddening independent of galaxy properties incorrectly reddens the reddest galaxies even more (model GI) but taking into account the relatively low cold-gas masses of these galaxies returns the colours to close to their intrinsic values (model GD). The tail of bluer massive galaxies is significantly affected by dust, yielding a monomodal distribution in the highest mass bin. Including orientation effects (model GD+O) gives a slightly broader colour distribution for the fiducial axial ratio value of  $q = 0.2$ .

A similar trend is noticeable for galaxies in the second most massive bin ( $10^{10.5} \lesssim M_*/M_\odot \lesssim 10^{11.2}$ , second row from the top). Though the fiducial value of  $q = 0.2$  for GD+O produces a similar distribution to GD in this bin, varying  $q$  values appears to have the strongest effect here. Smaller  $q$  values show a more pronounced bimodality, as the majority of galaxies are subject to less reddening, while a minority of ‘edge-on’ galaxies are heavily reddened to  $g - r$  colours  $\gtrsim 0.8$ .

The third bin ( $10^{9.8} \lesssim M_*/M_\odot \lesssim 10^{10.1}$ , third row from the top) also behaves similarly: the intrinsically bluest galaxies get reddened slightly more than the intrinsically red galaxies with scatter due to orientation having a negligible effect.

Finally, the colour distribution for galaxies in the least massive bin ( $10^{8.7} \lesssim M_*/M_\odot \lesssim 10^9$ , bottom row) is also shown for the Recal-25 simulation. There is a large difference in colours between Ref-100 and Recal-25 for the least massive galaxies, which is predominately a resolution effect: at the resolution of Ref-100 the star formation rates in these low-mass galaxies is underestimated (S15) which makes the simulated galaxies too red. This striking resolution dependence is not surprising. In Ref-100, galaxies of mass  $M_* \sim 10^9 M_\odot$  are represented by only  $\sim 10^3$  star particles, and for a typical cold gas fraction of 10 per cent, by only 100 star-forming gas particles. We demonstrate in Appendix A that red and blue sequence colours for galaxies across the  $10^{9.8} \lesssim M_*/M_\odot \lesssim 10^{10.1}$  range<sup>4</sup> are quite similar in Ref-100 and Recal-25 – which gives us confidence that Recal-25 gives numerically converged answers for the bottom row of Fig. 1. However, the different environments probed by the Ref-100 and Recal-25 models also contribute to the difference in colours, in particular the strength of the red sequence, because the larger volume contains a population of satellite galaxies in massive haloes. This is also shown in Appendix A and discussed further in Section 5. Taking into account dust obscuration and orientation effects has little effect on the colours in Recal-25 for these low-mass galaxies, with model GD+O and N yielding nearly identical colour distributions.

We now turn to comparing the colours of EAGLE galaxies to the data, going from top (most massive) to bottom (least massive) bins in stellar mass and focusing on model GD+O, Fig. 1 d). At the massive end, the observed red sequence galaxies are about 0.05 mag redder in the data than in EAGLE. As the optical colours of old ( $\gtrsim 10$  Gyr) stellar populations are dominated by metallicity effects (Bell & Rodgers 1969), this small colour difference is attributable to SSP metallicities. The  $M_* - Z_*$  relation for EAGLE galaxies (S15) is seen to lie slightly below (by less than 0.1 dex) observational data in galaxies with  $M_*/M_\odot > 10^{11}$ , resulting in a slightly bluer red sequence colour. The data also has a tail to even redder colours not present in EAGLE. In contrast, the most massive EAGLE galaxies have a tail to bluer colours resulting from recent star formation. It could

be that such star formation is shielded more effectively in the data (i.e. the value of  $\hat{\tau}_{bc}$  used is too low), or alternatively that our AGN feedback scheme does not quite suppress star formation sufficiently. The higher than observed gas fractions for galaxy clusters in EAGLE (S15) could also contribute to the enhanced SFR of some simulated BCGs.

The red sequence of galaxies with  $10^{10.5} \lesssim M_*/M_\odot \lesssim 10^{10.8}$  is very similar in the data and the simulation, but in EAGLE there are significantly more blue galaxies. The blue cloud starts to appear in the data for galaxies with  $10^{9.8} \lesssim M_*/M_\odot \lesssim 10^{10.1}$ , and its colour is very similar in EAGLE. However, in EAGLE the blue peak is stronger and the red peak occurs at a slightly redder colours ( $g - r = 0.75$  compared to the observed value of 0.7). Using smaller values of  $q$  in GD+O does not improve agreement with observation here. Dust reddening and orientation effects already play little role in setting the colours of EAGLE galaxies in this mass bin. Finally, in the lowest mass bin,  $10^{8.7} \lesssim M_*/M_\odot \lesssim 10^9$ , there is excellent agreement in the colour distributions of simulation and data and once more our dust reddening models are unimportant in setting EAGLE colours.

This level of agreement between galaxy colours in the simulation and the data is encouraging. By including metallicity and orientation effects in our dust treatment, we prevent the significant colour shift seen in the simple GI model. The validity of our dust model is discussed further in Section 5. Despite the good agreement, there are some clear discrepancies between EAGLE and the GAMA colour distributions. These can be seen in the widths and relative strengths of red and blue populations. The latter discrepancy reflects the finding of S15 that the transition from actively star-forming to passive galaxies occurs at slightly (by a factor of  $\sim 2$ ) too high mass in EAGLE.

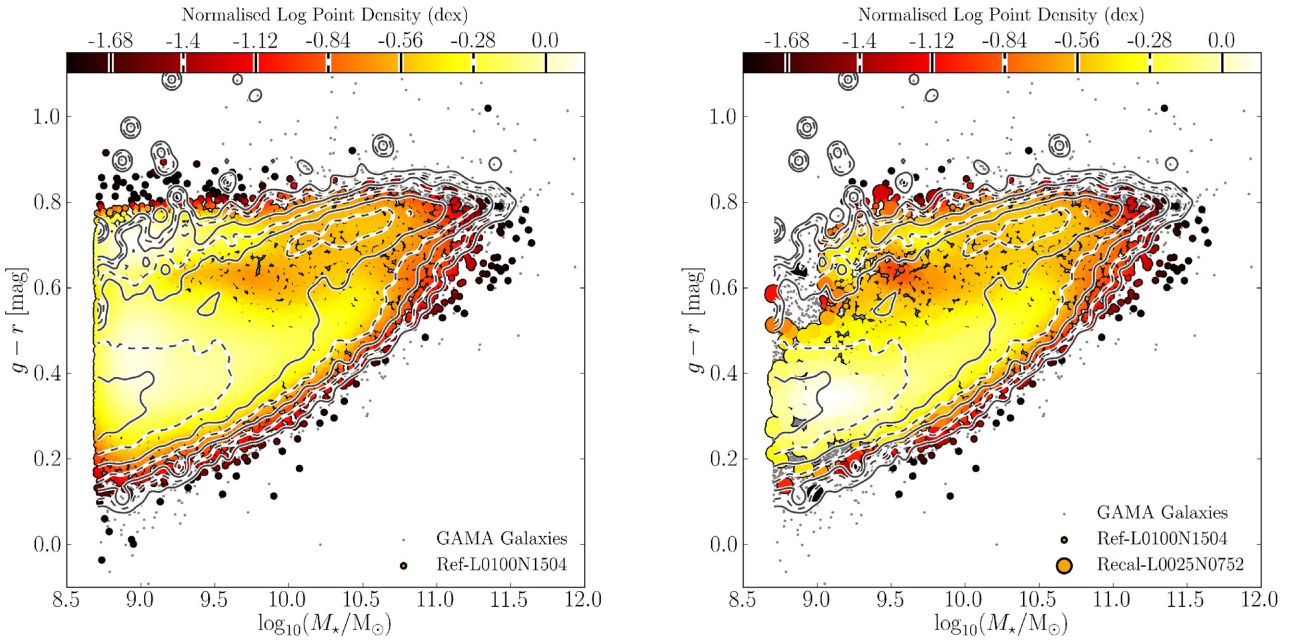
The dependence of galaxy colours on stellar mass is further illustrated in Fig. 2, where the number density of galaxies in EAGLE with given rest-frame  $g - r$  colour (computed using model GD+O) and stellar mass is compared to a volume-limited sample of GAMA galaxies taken from Taylor et al. (2015). Results are plotted down to stellar masses of  $10^{8.7} M_\odot$ , below which volume corrections due to the influence of line-of-sight structure become increasingly uncertain in the data (Taylor et al. 2015). The colour bar shows the point density of EAGLE galaxies and how these map to the Taylor et al. (2015) contours.

The left-hand panel shows the galaxies taken from simulation Ref-100. The simulation reproduces the trend seen in the data from galaxies being red above a stellar mass of  $M_* \sim 10^{10.5} M_\odot$  to being predominantly blue below that. However, as also seen in the previous figure, there is a population of red ( $g - r \sim 0.7$ ) low-mass ( $M_* \sim 10^9 M_\odot$ ) galaxies in EAGLE that is not seen in the data. These galaxies are modelled using only  $\sim 1000$  star particles; the right-hand panel of Fig. 2 therefore uses the higher resolution simulation Recal-25 for galaxies below  $10^9 M_\odot$  and Ref-100 above  $10^9 M_\odot$ , cross-fading one simulation into the other. This is achieved by interpolating the frequency at which galaxies are randomly sampled from the simulations for our scatter plot linearly in  $\log(M_*)$  between two values at  $10^9 M_\odot$  and  $10^{10} M_\odot$ . This is from 1 to 0 for the Ref-100 simulation and from 0 to 32 for Recal-25 simulation, respectively.<sup>5</sup> With this we aim to show the colour–mass distribution

<sup>4</sup> A larger mass range is used in Appendix A than in the third row of Fig. 1 so that Ref-25 and Recal-25 are sufficiently sampled.

<sup>5</sup> The sampling frequency of Recal-25 galaxies in this plot are weighted a factor of 64 higher than Ref-100 galaxies to account for the smaller volume and a further factor of 2 lower to account for the boosted number counts in Recal-25 caused by poor sampling of large-scale power in the smaller volume. This means that for masses  $< 10^9 M_\odot$  each Recal-25 galaxy





**Figure 2.** Rest-frame  $g-r$  colour-stellar mass diagrams for EAGLE galaxies using photometry and dust reddening from model GD+O at  $z = 0.1$  for simulation Ref-100 (left-hand panel), and a composite set of EAGLE galaxies obtained by combining the higher-resolution model Recal-25 for galaxies with  $M_* \lesssim 10^9 M_\odot$  and Ref-100 for  $M_* > 10^9 M_\odot$  (right-hand panel), cross-fading the sampling probability of the two galaxy populations linearly in  $\log_{10}(M_*/M_\odot)$  (see text for details). Colours represent the point density of EAGLE galaxies of given  $M_*$  and  $g-r$  colour (see text for details), with black points representing individual outlying EAGLE galaxies. Contours represent the colour- $M_*$  distribution for a volume-limited set of GAMA galaxies from Taylor et al. (2015), with grey points representing individual outlying galaxies. The masses of observed galaxies are obtained through SED fitting, see Taylor et al. (2015). The colours are mapped to their equivalent contours in the colour bar. The colour bar covers 2 dex in point density with a contour spacing of 0.28 dex. A lack of numerical resolution makes lower-mass EAGLE galaxies too red in the left-hand panel. The transition of colours of observed galaxies, from the red-sequence at stellar masses above  $M_* \sim 10^{10.5} M_\odot$  to the blue cloud at lower stellar masses, is reproduced in the simulation, although the blue cloud extends to slightly higher  $M_*$ .

for a larger range of well-resolved galaxies ( $\gtrsim 1000$  star particles), while avoiding a discontinuity that renders the overall distribution less clear. This cross-fading is only intended to help in visualizing the overall distribution of  $g-r$  colours in EAGLE, taking advantage of the higher resolution at low-mass end and of the larger volume run at the high-mass end. A quantitative analysis of the colour distribution of EAGLE galaxies is shown in Figs 1 and 5, and discussed below.

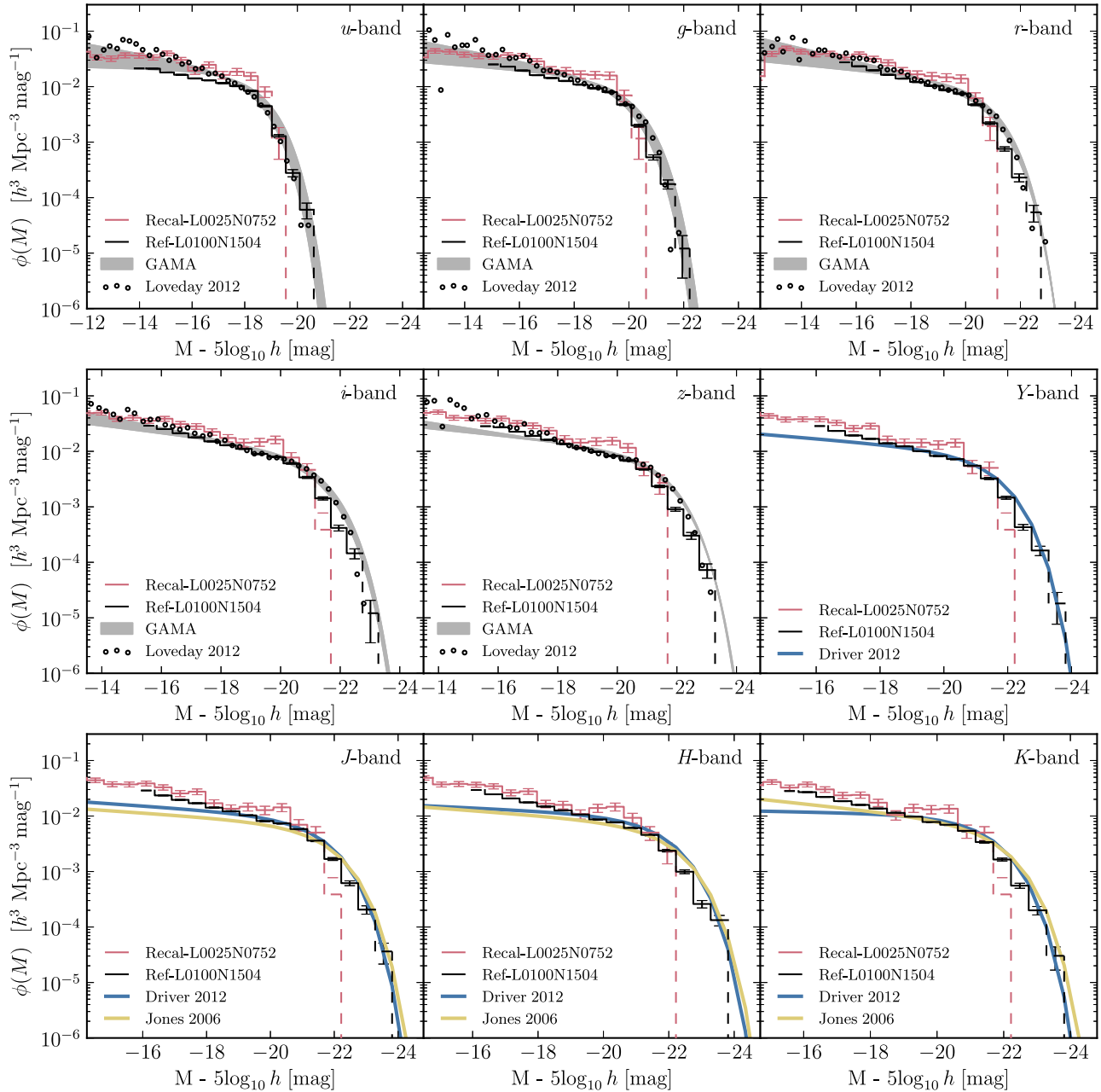
Combining these two resolutions, the colours of EAGLE galaxies at given  $M_*$  track the data from the GAMA galaxies (Taylor et al. 2015) well. Both display a red sequence of massive galaxies which becomes redder with increasing stellar mass, and  $g-r \sim 0.7$  at  $M_* \sim 10^{10.5} M_\odot$ . The simulation also reproduces the width of that sequence, albeit with a shallower slope. A blue cloud of galaxies appears both in EAGLE and GAMA below  $M_* \sim 10^{10.5} M_\odot$ , with  $g-r \sim 0.45$  at  $M_* = 10^{10.5} M_\odot$ . At decreasing stellar mass, the location of the blue cloud becomes bluer, reaching  $g-r \sim 0.35$  at  $M_* = 10^9 M_\odot$ . Overall we find that EAGLE reproduces the mean trends in galaxy colours well. Though the eradication of the faint red sequence in this sample is at least partly due to improved sampling, it also comes about because these galaxies are much less abundant in the higher resolution Recal-25 simulation (further discussion of the origin of this faint red population can be found in Section 5 and Appendix A).

contributes a factor of 32 more to the point densities in Fig. 2 than a Ref-100 galaxy at mass  $> 10^9 M_\odot$ . This weighting is chosen to yield approximately the same number of galaxies plotted per unit stellar mass in the right-hand panel of Fig. 2 as in the left.

In addition to the mean location of galaxy colours, there are outliers in both data and simulation. The GAMA data display a scatter to extremely red colours ( $g-r > 1$ ) at all stellar masses only seen for one high-mass outlier in EAGLE. There is also a scattering of galaxies  $\sim 0.1$  mag bluer than the main locus in GAMA that appear in EAGLE as well. Finally, EAGLE has some very massive, relatively blue galaxies ( $M_* \sim 10^{11.5} M_\odot$ ,  $g-r \sim 0.6$ ); although there are such galaxies in GAMA as well, they are more numerous in EAGLE, as is more easily seen in Fig. 1. We suggested before that these either imply too little dust reddening in star-forming regions in EAGLE, or simply that some of these massive EAGLE galaxies are undergoing too much star formation despite the inclusion of AGN feedback.

## 4.2 Luminosity functions

LFs for model GD+O in rest-frame  $ugrizYJHK$  broad-band filters are plotted using absolute AB magnitudes in Fig. 3. The simulations Ref-100 and Recal-25 at redshift  $z = 0.1$  are shown with Poisson error bars as solid black and red histograms, respectively, becoming dashed when there are fewer than 10 galaxies per  $\sim 0.6$  mag bin. For Recal-25 the bins are correlated, as can be seen for example in the  $u$  band for bins  $M - 5 \log(h) = -17.5$  to  $-18.5$ , due to poor sampling of large-scale modes in the small volume. There is generally good agreement between the two runs, with Recal-25 typically less than a factor of 2 (0.3 dex) higher at the faint end, and by much less for the redder bands. Note that this higher-resolution simulation does not sample the exponential cut-off at high luminosities because of its small volume. Differences in resolution are most noticeable in bluer colours, particularly in  $u$ . As discussed



**Figure 3.** LFs in each band of the *ugriZYHJK* photometric system plotted for the fiducial 100 Mpc simulation (Ref-100) in black and the re-calibrated high-resolution 25 Mpc simulation (Recal-25) in red, both at redshift  $z = 0.1$ , using the GD+O dust model. The Ref-100 function is plotted down to the faintest magnitude bin at which most galaxies are represented by  $>100$  star particles. The simulation results from *ugriZ* SDSS bands are compared to the Petrosian GAMA survey LFs taken from Loveday et al. (2012),  $k$ -corrected to rest-frame magnitudes and plotted as empty circles. The region bound by the Schechter fits to the Driver (2012) and Loveday et al. (2012) LFs is shaded in grey. As these two LFs are measured using Kron and Petrosian magnitudes, respectively, the grey area indicates the difference due to aperture definition. Schechter fits for UKIDSS band LFs are taken from GAMA (Driver et al. 2012) and from 6DF+2MASS (Jones et al. 2006) where available. All magnitudes are in the AB system. Error bars reflect Poisson errors with dashed lines indicating bins containing  $<10$  simulation galaxies. The *EAGLE* LFs are similar to the observed fits across the spectral range, with some discrepancies discussed in Section 4.

before, in small galaxies the stellar feedback events driving outflows are poorly sampled and the star-forming components are poorly resolved. As a result star formation rates and thus intrinsic colours are subject to considerable resolution effects. We see that the higher-resolution simulation yields higher star formation rates and hence

bluer colours. We again note that this is not just a resolution issue: the Ref-100 volume contains a population of faint red quenched satellites of massive galaxies, which are simply not present in the much smaller Recal-25 volume, as discussed further in Appendix A. LFs in longer wavelength bands are consistent in shape between

**Table 2.** Best-fitting Schechter function (equation 7) parameters for EAGLE AB-magnitude LFs in the  $r$  band for different dust models in simulation Ref-100 at redshift  $z = 0.1$ , and the observed LF from Loveday et al. (2012). The EAGLE and observed LFs are all fit over the magnitude range  $-23.2 < r < -14.2$ ,  $1\sigma$  errors on the best-fitting parameters were computed using jackknife sampling. Best-fitting parameters to *ugrizYJHK* LFs can be found in Appendix C.

Model	Description	$\phi_*$ [ $h^3 \text{ cMpc}^{-3} \text{ mag}^{-1}$ ]	$r$ band $\alpha$	$-2.5 \log_{10}(L_*/h^2)$ [mag]
N	No dust	$8.1^{+1.0}_{-0.9} \times 10^{-3}$	$-1.24^{+0.03}_{-0.03}$	$-21.0^{+0.1}_{-0.1}$
GI	Galaxy-independent dust model	$7.5^{+0.9}_{-0.9} \times 10^{-3}$	$-1.25^{+0.03}_{-0.03}$	$-20.7^{+0.1}_{-0.2}$
GD	$Z$ and $M_{\text{ISM}}$ dependent	$9.3^{+1.2}_{-1.1} \times 10^{-3}$	$-1.21^{+0.03}_{-0.03}$	$-20.7^{+0.1}_{-0.2}$
GD+O	GD with orientation dependence	$9.5^{+1.5}_{-1.3} \times 10^{-3}$	$-1.21^{+0.04}_{-0.03}$	$-20.7^{+0.2}_{-0.2}$
Data	Loveday et al. (2012)	$9 \pm 0.7 \times 10^{-3}$	$-1.26 \pm 0.01$	$-20.7 \pm 0.03$

the two simulations (despite the small volume simulation being noisier).

Observed LFs from Loveday et al. (2012) are plotted in each of the *ugriz* bands, which we fit with a single Schechter (1976) function,

$$\frac{1}{L_*} \frac{dn}{dL} = \phi_* \left( \frac{L}{L_*} \right)^\alpha \exp(-L/L_*) \frac{dL}{L_*}. \quad (7)$$

Single Schechter function fits are also taken from Driver (2012) and Jones et al. (2006). For the *ugriz* bands these are shown as grey shaded regions, which are bounded by the fits to the observed LF of Loveday et al. (2012) and Driver (2012), both based on data from GAMA. The differences between these observed LFs result from the use of Kron and Petrosian magnitudes, respectively. The thickness of the grey band is thus a measure of how these different aperture choices affect the Schechter fit. For the *YJHK* band, we plot published Schechter fits, which are based on UKIDSS data.

There appears to be some discrepancy between Schechter fits from the observational papers and directly observed LFs in the optical, as can be seen by comparing the Loveday et al. (2012) data with the Schechter fits. In particular, the data points appear systematically higher than the Schechter fit at the faint end and below the fit at the bright end. This is most visible in the  $z$  band where the shaded region is narrowest. This could be a consequence of intermediate magnitude bins dominating the fit as this is where observational errors are minimal. It also shows that the single Schechter function is not a good fit to the observational data. In particular, it is unable to represent the observations at the faint end accurately (e.g. Loveday 1998). The Driver (2012) and Jones et al. (2006) fits agree reasonably well, except for the faint-end slope in the  $K$  band. The single Schechter fits are used here as simple indicators of the shape, position and normalization of the observed LFs, but clearly their exact location depends on details of how galaxies are identified in the data, and possibly on the range and assumed errors used in the fitting procedure. We compare the parameters of Schechter fits to EAGLE LFs to observational fits in Table 2.

From Table 2, we see that the dust treatment has little effect on the shape of the  $r$ -band LF. The effect of including dust using the GI model makes the knee position,  $-2.5 \log_{10}(L_*)$ , 0.3 mag fainter and decreases the normalization,  $\phi_*$ . Scaling dust absorption by galaxy properties in GD serves to increase  $\phi_*$  for the same  $L_*$  value. The GD and GD+O model LFs provide  $L_*$  and  $\phi$  parameters that agree with the observational values within the errors. The faint-end slope,  $\alpha$ , shows some variation between dust models, but remains within  $\sim 1\sigma$  of the observational value. Information on the fitting

and best-fitting parameters to each *ugrizYJHK* LF for GD+O can be found in Appendix C.

Comparing the GD+O EAGLE LFs to the data in Fig. 3 shows a striking overall consistency from the UV to the NIR bands. The deviations are mostly of the same order as differences in fits to the published LFs of different authors. The agreement is particularly good in the optical bands *ugriz*, where EAGLE tends to fall mostly inside the grey band that represents the dependence of the LF on the choice of aperture. The excellent agreement over such a wide range of colours suggests that EAGLE forms the correct number of galaxies of a given stellar mass and that those galaxies have realistic star formation histories and metallicities.

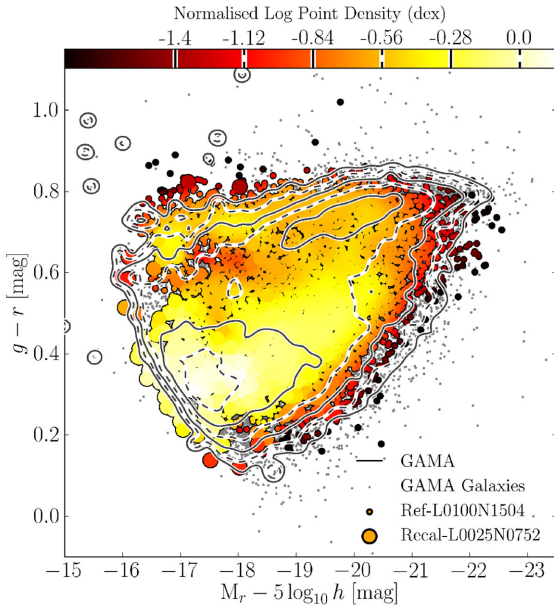
Comparing blue bands ( $u - g$ ) to redder bands ( $J - K$ ) at the faint end, we notice that the EAGLE Ref-100 LFs tend to be slightly low in blue bands relative to the data, but high in the red bands. This is a consequence of Ref-100 producing slightly too many low-mass galaxies (S15) which have too low star formation rates (Furlong et al. 2015). Resolution also plays a role: we plot galaxies with more than 100 star particles, where we know that the stellar feedback events generating outflows and star formation rates at the faint end are poorly resolved. In addition, even fainter galaxies with high star formation rates cannot scatter into the faint-end bins since we impose a cut in mass and not in magnitude.

The EAGLE LF tends to drop below the observations at the ‘knee’ ( $L_*$ ) in the Schechter function, particularly in the bands red-ward of  $r$ . This is consistent with a slight underestimate in the masses of more massive EAGLE galaxies, as seen in the mass function plotted in S15.

The *JHK* bands also appear to have generally somewhat steeper faint-end slopes (parameter  $\alpha$  in equation 7) in EAGLE than the Schechter fits to the data. However, the data itself also show a upturn at the faint end relative to the observed Schechter fits (circles in Fig. 3, see also Driver 2012). Generally, the single Schechter function fit tends to underestimate the LF at the faint end (Loveday 1998). This is more pronounced in the *JHK* bands where the NIR sky is relatively bright (e.g. Sivanandam et al. 2012), leading to large uncertainties in the faint end data.

### 4.3 The $g - r$ colour-magnitude distribution

The CMD of model GD+O for EAGLE is plotted in Fig. 4. As in the right-hand panel of Fig. 2, we combined faint galaxies from the higher resolution simulation Recal-25 for galaxies with  $M_* < 10^9 M_\odot$  with galaxies from simulation Ref-100 at higher masses. As before, colours represent the number density of EAGLE galaxies in this plane, whereas contours show the corresponding

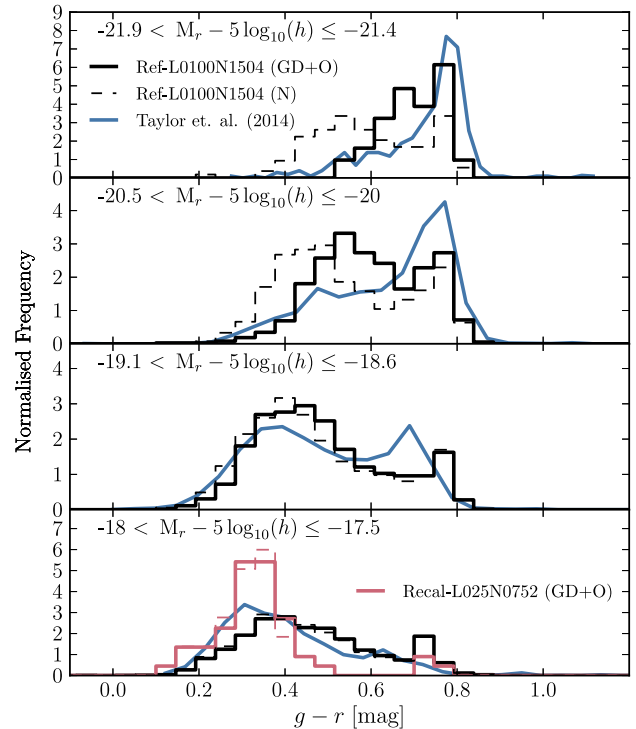


**Figure 4.** Rest-frame  $g-r$  colour as a function of  $r$ -band absolute magnitude for EAGLE galaxies (colours) compared to a volume-limited sample of GAMA galaxies (Taylor et al. 2015, contour lines). Contours and point shading is the same as in Fig 2, with the normalized contour levels indicated on the colour bar. EAGLE photometry is obtained using the GD+O model. A composite EAGLE galaxy population is used, consisting of galaxies from Ref-100 at  $M_* > 10^9 M_\odot$  and Recal-25 at  $M_* < 10^9 M_\odot$  as in the right-hand panel of Fig 2. There is general agreement between EAGLE and GAMA in the location and slope of the red-sequence ( $g-r \approx 0.7$  at  $M_r - 5 \log_{10} h = -20$ ), the appearance of a blue cloud of galaxies with  $g-r \sim 0.45$  at that magnitude, which becomes increasingly blue ( $g-r \sim 0.3$ ) for the fainter galaxies with  $M_r - 5 \log h \sim -17.5$ .

data from the volume-limited catalogue of GAMA taken from Taylor et al. (2015). For both simulation and data, we only show galaxies with stellar mass  $M_* > 10^{8.7} M_\odot$ . Fig. 4 now contains only ‘observable’ quantities for GAMA galaxies,<sup>6</sup> and in particular does not require any SED fitting. The overall agreement between EAGLE and the data is generally very good, exhibiting similar galaxy densities across the colour–magnitude plane.

We also plot colour distribution histograms in Fig. 5 for a more quantitative comparison, now in 0.5 mag bins of absolute  $r$ -band magnitude. The location of the red-sequence is within  $\sim 0.1$  mag of the observations in each panel. In a similar manner to Fig. 1(d), we measure a slightly shallower red-sequence slope than observed with systematically redder colours at the faint end. A transition between a predominately red to predominately blue distribution occurs, but at slightly brighter magnitudes than observed ( $M_r - 5 \log(h) \sim -20.5$ ). In the lowest  $M_r$  bin, the colours and magnitudes of EAGLE galaxies also agree generally well with the data. To avoid the stellar mass cut affecting blue galaxies significantly, our faint end bin is chosen to have galaxies brighter than  $M_r = -17.5$ . The Recal-25 simulation does not appear to show superior agreement with observation relative to the Ref-100 simulation in this bin. It should be noted that the number of galaxies in this bin are lower for both simulation volumes than in the lowest mass bin of Fig. 1(d).

<sup>6</sup> In practice, the diagram still depends to a small extent on the applied cut in stellar mass at the faint end and on the choice of aperture to measure magnitudes.



**Figure 5.** Rest-frame  $g-r$  colour distributions for EAGLE galaxies at redshift  $z = 0.1$  for four non-contiguous ranges in  $r$ -band magnitude as indicated in the legend (top to bottom). Black lines indicate the fiducial Ref-100 galaxy population, while red lines indicate the higher resolution Recal-25 simulation. Dashed lines denote the N photometry with solid lines representing the fiducial GD+O. Blue lines represent observed galaxy colours for the volume-limited sample of GAMA galaxies from Taylor et al. (2015).

The  $g-r \sim 0.3$  colours of the faint blue galaxies appears to be well reproduced. The bright blue population in EAGLE become slightly more discrepant with data for the  $-21.9 < M_r < -21.4$  bin than in the high-mass bin of Fig. 1(d), due to the fact that bluer galaxies generally possess brighter  $r$ -band magnitudes for the same  $M_*$ .

The level of agreement between simulation and data in the CMD shown in Figs 4 and 5 is remarkable and suggests that these EAGLE simulations provide a relatively realistic population of galaxies at low redshift, and that the modelling of emission and dust obscuration in model GD+O works reasonably well.

## 5 DISCUSSION

The EAGLE simulations were calibrated to reproduce the local GSMF and galaxy sizes by appropriate choice of the parameters in the subgrid model for feedback. As stellar mass is closely linked to NIR luminosity, the consistency of GSMF proxies such as the  $K$ -band LF shown in Fig. 3 is not surprising, at least at  $z \sim 0$ . However, consistency with the LFs in other broad-band filters is not automatic because stellar mass, star formation history, metallicity and dust obscuration all play a role.

In Section 4, we focused on our GD and GD+O photometric models where dust absorption is approximated by a simple two component screen, with optical depths that vary with galactic gas content, metallicity and orientation (GD+O only). The colour distributions as a function of stellar mass and  $r$ -band magnitude for model GD+O in Figs 1, 2, 4 and 5 show a level of agreement between simulated galaxies and observations that appears unprecedented for



hydrodynamical simulations, and comparable to that achieved for semi-analytical models (e.g. González et al. 2009; Henriques et al. 2014). The EAGLE LFs also agree well with observations over a range in wavelengths from optical to NIR (Fig. 3). The relatively good agreement for number density, luminosity and colour, suggests that in EAGLE each dark matter halo forms a galaxy with stellar mass, age and metallicity close to those inferred from observation. The similar level of agreement in observed colour–magnitude space also rules out a potential circularity resulting from using the same photometric model to infer stellar mass from observational data as is used in the simulations. Even though the overall level of agreement is good between EAGLE and the data, there are discrepancies.

There is an excess of bright ( $M_r - 5 \log_{10} h \lesssim -20$ ) blue ( $g - r \lesssim 0.6$ ) EAGLE galaxies relative to data, apparent in e.g. Fig. 5. Such an excess is seen in all our photometric models (see Fig. 1), but is least apparent for model GD+O where the recent star formation, that is the root cause of the blue colours, is most strongly obscured by dust. This parallels the findings of S15, that the fraction of passive EAGLE galaxies is too low at the high-mass end, relative to observations. It may be that massive EAGLE galaxies are too highly star forming, perhaps as a consequence of insufficient suppression of star formation by AGN. The colours of these galaxies can be sensitive to a low level of recent star formation. A 10 Gyr population requires a specific star formation rate of  $\sim 0.025 \text{ Gyr}^{-1}$  over a 0.1 Gyr period to move from  $g - r \sim 0.8$  to 0.6 at a fixed metallicity of  $Z = 0.02$ , corresponding to  $2.5 \text{ M}_\odot \text{yr}^{-1}$  for a galaxy of  $M_* = 10^{11}$ . Whether the good agreement in the colour of the blue cloud, despite the underestimate of the median star formation rates at these masses (S15), suggests underestimated reddening is discussed further below.

The EAGLE red sequence, at  $g - r \sim 0.75$ , is flatter than observed, both when plotted as a function of stellar mass (Fig. 2) and when plotted as a function of absolute magnitude (Fig. 4). The flatter slope may be attributable to the dependence of stellar metallicity on galaxy mass,  $Z_*(M_*)$ ; although stellar metallicities of EAGLE galaxies agree well with the data at the massive end, they fall less rapidly with decreasing stellar mass compared to the observational data of Gallazzi et al. (2005), as shown in S15. Numerical resolution may play a role here, because the  $Z_*(M_*)$  of the higher resolution simulation Recal-25 does agree with the data; see S15.

There is an abundant population of red ( $g - r \sim 0.7$ ), low-mass ( $M_* \sim 10^9 \text{ M}_\odot$ ) galaxies in simulation Ref-100 that is not observed (see Fig. 2 a). The comparison of simulations Ref-25 and Recal-25 in Appendix A shows that this is at least partially due to a lack of numerical resolution. Indeed, star formation and outflows driven by feedback in these galaxies are poorly resolved and poorly sampled, leading to too low values of the specific star formation rate (and correspondingly too high passive fractions) and too high metallicities (see S15). We include a re-sampling technique, described in Section 3.1.1, in all models to try to mitigate poor sampling. Although this goes some way towards improving the modelling, it does not eliminate the discrepancy. Because the re-sampling is a post-processing step, it cannot help with the poor sampling of stellar feedback in these low-mass systems within the simulation. Related resolution problems are more intractable, and higher-resolution simulations are required to alleviate them.

Comparing simulations Ref-100 and Ref-25 that have identical numerical resolution (and the associated poor sampling of star formation in  $M_* \sim 10^9 \text{ M}_\odot$  galaxies), yet differ in simulated volume size, allows us to isolate the effects of environment (see Appendix A). Although on average the colours of galaxies agree well between these simulations, the presence of faint red galaxies is

much more pronounced in the larger volume. This is because many of these galaxies are satellites of more massive systems that are absent in the smaller volume. The fraction of satellites increases at lower stellar masses, and in the range  $10^{8.7} \text{ M}_\odot < M_* < 10^9 \text{ M}_\odot$  comprises  $\sim 46$  per cent of the galaxy population in the Ref-100 simulation and  $\sim 33$  per cent in Ref-25. Evidently, satellites contribute significantly to the colour distribution at low masses. At present we cannot verify whether improved resolution will also reduce the suppression of star formation in, or decrease the metallicities of, small satellite galaxies, which would improve the colours of  $M_* \sim 10^9 \text{ M}_\odot$  galaxies compared to data. We conclude that the redder colours of low-mass galaxies in EAGLE relative to data is at least partially a result of resolution, stemming from poor sampling of star formation and feedback. The improved agreement with the data that comes about from using a composite sample of Recal-25 and Ref-100 galaxies relative to using the Ref-100 sample alone is thus mainly due to improved numerical resolution, but also to the exclusion of red satellite galaxies that are not present in the smaller volume. The relationship between galaxy colours and environment in EAGLE is clearly an important test of the simulation, and will be explored further in future work.

The level of agreement between EAGLE colours and the data also depends on the realism of our dust reddening model. Fig. 1 illustrates how dust reddening depends on the assumptions made in models N (no reddening) to model GD+O (gas metallicity, gas mass and orientation-dependent reddening). Differences between these models are typically of order  $\Delta(g - r) \sim 0.1$ . A dust model that is independent of galaxy properties (such as GI) incorrectly reddens red galaxies. A reddening model that takes into account the gas mass (GD) resolves this inconsistency, with most of the remaining effects of reddening affecting blue bright galaxies. Overall, we find that the details of the dust treatments make relatively little difference to galaxy colours so that differences with observations are more likely due to the ages and metallicities of the stars rather than dust obscuration. This may be due to the relatively small effect of dust at redshifts  $z \sim 0.1$ . We leave the investigation of evolution of colours and luminosities in EAGLE to a future work.

Taken at face value, the specific star formation rates of star-forming galaxies in EAGLE are lower than inferred from observations by  $\sim 0.2$  dex (S15). The fact that the colours of those same galaxies nevertheless agree with the data might imply that we underestimate dust reddening. Indeed, an underestimate of the gas fraction would lead to both an underestimate of the specific star formation rate and, at fixed metallicity, the attenuation. Lagos et al. (2015) have shown that at  $M_* \sim 10^{10} \text{ M}_\odot$  the median  $\text{H}_2$  fraction in EAGLE is about 0.2 dex lower than observed, and that this discrepancy goes away at higher masses and for the higher resolution Recal-25 model.

Systematically lower attenuation for faint galaxies could thus be attributable to their low gas masses in the simulations. However, more complex models yield non-zero levels of attenuation even for very low gas surface densities (e.g. Boquien et al. 2013). The realism of mixed screen models as used here has been shown to break down when screens are optically thick (e.g. Disney, Davies & Philipps 1989). As dust optical depths are expected to be higher in blue bands, our dust prescription may be too crude to reproduce the data at higher levels of obscuration. This could contribute to the bluer colours of massive galaxies in EAGLE.

However, it is also possible that the levels of obscuration are realistic, but that star formation rates are overestimated in the data due to the absolute calibration of observed tracers of star formation. The calibration of star formation rates from tracers rely on assumptions about the intrinsic UV continuum (from population synthesis

modelling) and absorption at short wavelengths, as well as an assumed form for the IMF (e.g. Kennicutt 1998). The cumulative build-up of stellar mass in *EAGLE* is lower than observed by about 0.1 dex, whereas the star formation rate is lower than that observed by 0.2–0.4 dex, depending on redshift (Furlong et al. 2015). This slight tension may suggest a small overestimate of the observationally inferred star formation rates. Estimating intrinsic properties from observables of simulated galaxies (such as star formation rates) may help to clarify these issues, see e.g. the recent study by Torrey et al. (2015).

The dust model we developed here was designed to be as simple as possible, yet to avoid unrealistic levels of reddening. The model assigns a single value of reddening per galaxy without taking into account the non-uniform distributions of dust apart from that assigned to birth clouds. It is possible to make much more detailed estimates of reddening using 3D radiative transfer (RT) calculations (e.g. Baes, Dejonghe & Davies 2005; Jonsson, Groves & Cox 2010). We postpone comparisons of the current simple model to those obtained with the RT code *SKIRT* (Baes et al. 2005) to future work.

## 6 SUMMARY AND CONCLUSIONS

We have calculated broad-band luminosities of simulated galaxies taken from the *EAGLE* suite of hydrodynamic simulations (C15; S15), and compared them to observations of the redshift  $z \sim 0.1$  galaxy population. The model uses SSP modelling based on the *GALAXEV* population synthesis models of Bruzual & Charlot (2003). To marginally reduce sampling noise arising from single young star particles in poorly resolved galaxies, we use a re-sampling procedure for the young stellar component. In all models, galaxy luminosities are found by summing the particle luminosities within a 30 kpc radius spherical aperture for consistency with previous analysis (Furlong et al. 2015; S15), which has been shown to mimic Petrosian apertures. Absolute magnitudes are presented in the AB system.

We compare and contrast three models of dust obscuration and to model N which neglects dust. Model GI, inspired by Charlot & Fall (2000), includes contributions to the dust optical depth from the birth clouds of young stars and from a constant dust screen, with parameters that are independent of the galaxy properties. Applying a single diffuse dust correction to all galaxies incorrectly reddens ellipticals and we avoid this with model GD in which dust reddening depends on gas phase metallicity as well as gas mass. Finally, model GD+O uses a simple geometric model to account for orientation effects, which are however small.

These simple models allow us to investigate the dependence of galaxy colours on stellar metallicities and ages, gas metallicities and dust obscuration. Our main conclusions are as follows.

(i) The GI dust prescription which applies a reddening that is independent of galaxy properties, and was used by e.g. Torrey et al. (2015), excessively reddens the red-sequence population of galaxies. As a consequence,  $g - r$  colours of massive ( $M_* \gtrsim 10^{10.5} M_\odot$ ) *EAGLE* galaxies are  $\sim 0.1$  mag redder than observed, in spite of having ages and stellar metallicities that are similar to those inferred (Fig. 1b). Scaling dust optical depths with cold gas mass and gas metallicity, as in model GD, is more realistic and improves agreement with observation (Figs 1c and 1d).

(ii) The red sequence in *EAGLE* is  $\sim 0.1$  mag bluer in  $g - r$  than observed for  $M_* \gtrsim 10^{11.2} M_\odot$ , and has a shallower dependence on

stellar mass than observed (Fig. 1). This is most likely a consequence of the dependence of colour on stellar metallicities.

(iii) The appearance of a faint red sequence in the Ref-100 simulation run ( $M_* < 10^{9.75} M_\odot$ ,  $0.6 < g - r < 0.8$ , see left-hand panel of Fig 2) that is not observed, is largely an effect of numerical resolution. Star formation and outflows are not well resolved in galaxies of such low mass.

(iv) A ‘blue cloud’ of star-forming galaxies appears in *EAGLE* below  $M_* \lesssim 10^{10.5} M_\odot$ , with  $g - r$  colour in agreement with the GAMA data from Taylor et al. (2015, left-hand panel of Fig 2).

(v) There is an excess of bright ( $M_r - 5 \log_{10} h \lesssim -20$ ) blue ( $g - r \lesssim 0.6$ ) galaxies in *EAGLE* relative to the data. This may be caused by an underestimate of the reddening in star-forming regions, or an overestimate of the star formation rates in these massive galaxies due to insufficient suppression of star formation by AGN.

(vi) The  $z = 0.1$  galaxies taken from *EAGLE* transition from mostly red ( $g - r \sim 0.7$ ) above  $M_* \sim 10^{10.5} M_\odot$  to mostly blue (ranging from  $g - r \sim 0.5$  at  $M_* \sim 10^{10.5} M_\odot$  becoming bluer with decreasing mass to  $g - r \sim 0.35$  at  $M_* \sim 10^9 M_\odot$ ) at lower masses, follows the colours of GAMA galaxies from Taylor et al. (2015, see Fig. 2). However the blue cloud persists to higher than observed stellar masses, consistent with a similar trend in passive fractions shown in S15.

(vii) The  $z = 0.1$  galaxy LFs constructed from the *EAGLE* population agree well with data from UV to NIR bands, with differences of the order of the difference between using Kron and Petrosian magnitudes in the data (Fig. 3). This level of agreement is similar to the agreement between the *EAGLE* and observed stellar mass functions. In particular, there is a slight underestimate in the number density of galaxies close to the knee of the Schechter fit, and the faint-end tends to be slightly steeper than observed in most bands. We note, however, that the faint-end of the LF is uncertain, especially in NIR bands, and single Schechter fits tend to underestimate the faint-end slope (Loveday 1998). Good agreement was not surprising in the NIR where luminosities are dominated by stellar mass, whereas the good agreement in other bands suggests that the star formation histories and metal enrichment in *EAGLE* galaxies are relatively realistic.

(viii) The  $z = 0.1$   $g - r$  colour versus  $M_r$  magnitude diagram for galaxies with  $M_* \gtrsim 10^9 M_\odot$  yields a level of agreement with data that is comparable to that of current semi-analytic models (Fig. 4; González et al. 2009; Henriques et al. 2014). The similar colour distributions of N and GD+O photometries (Fig. 1d) suggests that the dust model plays only a minor role in this agreement. This further attests to the relatively realistic evolution of the *EAGLE* galaxy population.

The general agreement in the colour and luminosity of *EAGLE* galaxies and observed galaxies suggests that the simulated galaxies have similar star formation histories, metal enrichment processes and current star formation rates as observed galaxies. This makes the *EAGLE* suite well suited to investigate the physical processes that shape galaxies through cosmic time.

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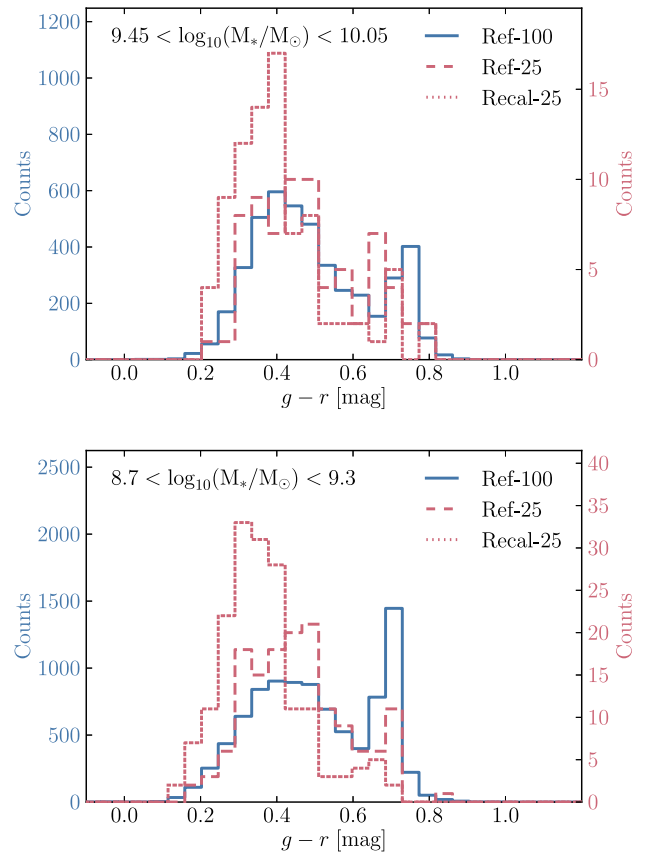
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## APPENDIX A: COLOUR CONVERGENCE

As simulation Recal-25 has a factor of 8 finer mass resolution than the fiducial model Ref-100, the stellar mass threshold above which galaxies are considered well resolved is pushed to lower masses. By comparing colour distributions of the Ref-100, Ref-25 and Recal-25 simulations (Table 1; S15) for galaxies within a certain mass range, we attempt to decouple the effects of simulation volume and resolution on the colours of low-mass galaxies in *EAGLE*. In Fig. A1, we compare colour distributions for galaxies of mass  $9.45 < \log(M_*/M_\odot) \leq 10.05$  and  $8.7 < \log(M_*/M_\odot) \leq 9.3$  in the top and bottom panels, respectively. The histograms for differing simulation volumes have different y-axis ranges, with the 25 Mpc simulation axis range a factor of 64 smaller to account for the differing simulation volumes.

In the  $9.45 < \log(M_*/M_\odot) \leq 10.05$  mass range, the position of the red and blue peaks appear roughly the same in the different simulations. However, the relative strengths of the red and blue populations differ, with the red sequence being significantly weaker than the blue cloud in the high-resolution Recal-25 model compared to Ref-100 and Recal-25. This is consistent with the lower passive fractions in the high-resolution simulation at  $z = 0.1$  shown in S15.

The  $8.7 < \log(M_*/M_\odot) \leq 9.3$  range shows less consistency, with the red sequence becoming practically absent in the Recal-25 model while remaining in the Ref-100 and Ref-25 models. The redder colour and larger scatter of the blue population in the reference model is attributable to poor sampling of star forming gas in these galaxies. The lower star formation rates in the fiducial volume may also account for the different colours. However, we also see a larger difference between Ref-25 and Ref-100 here, particularly in the relative contributions of the red and blue populations. We attribute the higher contribution of the red sequence in the Ref-100 model to the presence of large cluster environments in the Ref-100 simulations, and thus quenched satellite galaxies, that are not sampled by the



**Figure A1.** Comparison of  $g-r$  colour distributions of the Ref-100, Ref-25 and Recal-25 simulations (see Table 1) to assess the weak convergence and volume effects on model colours. Ref-100 and Ref-25 have the same resolution, while Recal-25 has a resolution eight times finer. The top and bottom panels show galaxy stellar mass ranges of  $9.45 < \log(M_*/M_\odot) \leq 10.05$  and  $8.7 < \log(M_*/M_\odot) \leq 9.3$ , respectively. In both panels, the blue and red histograms represent the counts per colour bin in the 100 and 25 Mpc simulations, respectively. The Ref-100, Recal-25 and Ref-25 simulations, are plotted as solid, dotted and dashed lines, respectively. Separate y-axes are labelled and coloured to correspond to the 100 Mpc (left) and 25 Mpc (right), with their ranges scaled by a factor of 64 to account for the differing box volume. Both resolution and box size appear to significantly affect the colour distributions of low-mass *EAGLE* galaxies.

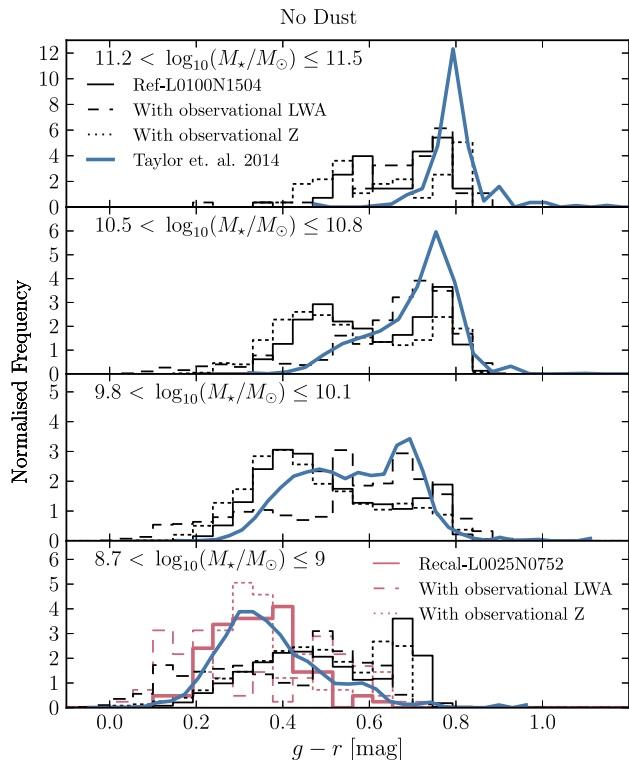
Ref-25 box. This suggests that volume effects also contribute to the weaker red sequence seen in the Recal-25 box. In both plots, the greater area under the Recal-25 histogram is indicative of the systematic shift in galaxy number densities between the simulations, also seen in Fig. 3.

## APPENDIX B: SSP PARAMETER INFLUENCE

As intrinsic galaxy colours are sensitive to star formation histories and elemental abundance patterns, comparing *EAGLE* model colours directly to observed galaxy colours is a difficult way to disentangle the influence of different SSP parameters and to identify the source of any discrepancies.

To go some way towards assessing how the *EAGLE* stellar metallicities and star formation histories influence our mock photometry, we use the simple photometric model without dust (N). Two sets of photometric data are first generated for the simulated galaxy sample using simulation output for one parameter while using empirical





**Figure B1.**  $g-r$  colour distributions for EAGLE galaxies for the dust-free model. The four panels show colour distributions for four bins of stellar mass, as indicated by the legend. The solid, dotted and dashed lines show the EAGLE SSP values and the EAGLE SSP values with Gallazzi et al. (2005) metallicities and ages, respectively. Gallazzi metallicities and ages are assigned to each galaxy, based on the median parameter values at the galactic stellar mass. Z values are simply taken as the observed median value. The LWA values are sampled from a normal distribution with standard deviation taken from Gallazzi et. al. (2005), assuming that the scatter in age and metallicity is uncorrelated. We see that the complex star formation histories of EAGLE provide a better match to the observed colour distributions than a single SSP model using empirical values for age and metallicity.

relations for the other. The galaxy metallicities and light-weighted ages (LWAs) as functions of stellar mass presented by Gallazzi et al. (2005) are used to provide the empirical input. For the LWA values, we include a Gaussian scatter about the median values of the published width, which is assumed to be uncorrelated with metallicities. Clearly the assumption that galaxies may be treated as a single starburst and that the metallicity and age parameters are uncorrelated are poor, so the amount of information that can be drawn from this type analysis is limited. These plots serve as a basic qualitative illustration of the influence of different SSP parameters on galaxy colours.

The colour distributions in four  $M_*$  bins are plotted for the simulation-empirical hybrid photometry models, and are compared to the EAGLE photometry in Fig. B1. The black lines indicate distributions of Ref-100 simulation galaxies. The distributions using the raw emission model with EAGLE ages and metallicities are plotted as solid histograms. The photometry models using observed LWA and  $Z_*$  values are plotted as the dashed and dotted lines, respectively.

The observational data of Taylor et al. (2015) is also plotted in blue for comparison.

We see that the age parameter has the biggest influence on the colour distribution, with the empirical ages introducing a generally larger spread than metallicities, when compared to the pure EAGLE photometry. We have verified that this is still the case when we include the scatter on observed metallicity values. Fig. B1 shows that giving galaxies a single age stellar population using the observational LWA data of Gallazzi et al. (2005, dashed line) works reasonably well in the two most massive bins where stellar populations are old. However in the lower mass bins where galaxies are generally younger they provide a poor fit to the observed colours, inferior to our model photometry using the complex star formation histories of EAGLE (solid line).

The bimodality seen for the full EAGLE photometry in the two most massive bins, but not for in the observational LWA model, shows that the EAGLE populations are intrinsically bimodal in age. This supports the assertion that there is an excess of star-forming galaxies in this regime relative to the observed population. The bluer than observed high- $M_*$  red sequence in the observational LWA model could be a result of the lower metallicities of high- $M_*$  galaxies. The inferior agreement of the observational LWA model relative to the full EAGLE model in the lower mass bins suggests that the complex star formation histories of EAGLE reproduce the data better than an empirical model assuming a single age population.

The observational Z model reveals a poor fit to observation for the two highest mass bins. The red sequence is also much less prominent than seen in the observations and the other models across the  $M_*$  range.

The systematic effect of assuming uncorrelated scatter between the age parameter may also account for the fact that the colour distributions are broader and flatter than observed for this model, especially in the low-mass bins.

The resolution effects that drive much improved agreement between observed low-mass colours and Recal-25 relative to Ref-100 are noted in Section 4 and Appendix A. In the lowest mass bin of Fig. B1, we see that using observed metallicities has less impact on EAGLE colours than using observed LWAs. This indicates that star formation rate resolution is the primary resolution effect on colours, with metallicity resolution secondary to this. The presence of a faint red sequence is due to lower star formation rates and higher stellar ages than found in low-mass Ref-100 galaxies, whereas the position of the red sequence is redder by  $\sim 0.1$  due to the higher than observed metallicities at these masses. The star formation rate resolution is also the main contributor to the redder than observed blue cloud position in Ref-100.

## APPENDIX C: SCHECHTER FITS

Table C1 provides best-fitting Schechter function parameters for the GD+O  $ugrizYJHK$  EAGLE LFs. Each LF is fit over a range indicated in the final column using  $\chi^2$  minimization. In the fitting, Poisson errors are assumed for the  $\phi$  values of each bin and additionally weighted by the median bin luminosity. This weighting causes bins close to  $L_*$  to most strongly constrain the fit, similar to observed LFs.

**Table C1.** Best-fitting Schechter function (equation 7) parameters for EAGLE AB-magnitude LFs in *ugrizYJHK* using the GD+O photometry for simulation Ref-100 at redshift  $z = 0.1$ . The EAGLE LFs are fit over the magnitude range indicated in the final column. Errors on the best-fitting parameters were computed using jackknife sampling.

Band	$\phi_* [h^3 \text{ cMpc}^{-3} \text{ mag}^{-1}]$	$\alpha$	$-2.5 \log_{10}(L_*/h^2) [\text{mag}]$	Range [mag]
<i>u</i>	$13.7^{+1.8}_{-1.5} \times 10^{-3}$	$-1.11^{+0.04}_{-0.03}$	$-18.8^{+0.1}_{-0.2}$	$[-14.0, -21.0]$
<i>g</i>	$11.1^{+1.4}_{-1.3} \times 10^{-3}$	$-1.17^{+0.03}_{-0.03}$	$-20.1^{+0.2}_{-0.2}$	$[-14.0, -22.5]$
<i>r</i>	$9.5^{+1.5}_{-1.3} \times 10^{-3}$	$-1.21^{+0.04}_{-0.03}$	$-20.7^{+0.2}_{-0.2}$	$[-14.2, -23.2]$
<i>i</i>	$7.6^{+0.8}_{-0.8} \times 10^{-3}$	$-1.26^{+0.02}_{-0.02}$	$-21.2^{+0.1}_{-0.2}$	$[-16.0, -24.0]$
<i>z</i>	$6.7^{+0.8}_{-0.6} \times 10^{-3}$	$-1.28^{+0.02}_{-0.02}$	$-21.6^{+0.1}_{-0.2}$	$[-16.0, -24.0]$
<i>Y</i>	$6.2^{+0.7}_{-0.7} \times 10^{-3}$	$-1.29^{+0.02}_{-0.02}$	$-21.9^{+0.1}_{-0.2}$	$[-16.0, -24.5]$
<i>J</i>	$5.9^{+0.6}_{-0.6} \times 10^{-3}$	$-1.29^{+0.02}_{-0.02}$	$-22.0^{+0.1}_{-0.2}$	$[-16.0, -24.5]$
<i>H</i>	$5.5^{+0.6}_{-0.6} \times 10^{-3}$	$-1.30^{+0.02}_{-0.02}$	$-22.3^{+0.1}_{-0.2}$	$[-16.0, -24.5]$
<i>K</i>	$5.6^{+0.6}_{-0.5} \times 10^{-3}$	$-1.29^{+0.02}_{-0.01}$	$-22.0^{+0.1}_{-0.2}$	$[-16.0, -24.5]$

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