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## Dipolar glass and magneto-electric coupling within a $\pi$ -stacked organic system<sup>†</sup>

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There is much interest in the search for novel materials that show ferroelectric as well as magneto-electric coupling, such as that observed in multiferroics. Within organic based materials the electronic polarisation can originate from a charge distribution across a molecule or molecules, and so one must search for systems that have an electronic (and magnetic) dipole that is intrinsic. One such material is tetraethylammonium bis-7,7,8,8-tetracyanoquinodimethane (TEA(TCNQ)<sub>2</sub>) which is a charge transfer system with a single electron that is delocalised across a TCNQ dimer. We show that dielectric measurements yield anomalies at the cation freezing structural distortion and when singlet-triple excitations freeze. In both cases the electric response is glassy and at low temperature the corresponding magnetic measurements evidence the strong magneto-electric coupling within the material showing scaling behaviour similar to spin glass systems.

### 1 Introduction

Pure organic systems have a great advantage over their inorganic or oxide counterparts in that organic molecules can be easily modified via simple chemical substitutions which can lead to dramatic changes of their properties. Therefore, there is a drive to gain a fundamental understanding of these materials to enhance their technological potential. The ferroelectric behaviour in various organic based samples is due to the polarisability of electron density across molecules, rather than displacements of charged species within the unit cell as is common in inorganic oxides<sup>1,2</sup>, which then leads to a change in polarisability. Thus the search for high performance organic ferroelectrics is exceptionally challenging yet vibrant<sup>3</sup>. Within inorganic systems there are many ex-

amples of ferroelectric materials displaying glassy interactions between electronic dipoles leading to a relaxor ferroelectric state<sup>4,5</sup>; However this can be due to impurities or from doping. Organic materials tend to be cleaner, as crystallisation reduces the level of impurities, and thus any glassy relaxation will often be due to a different mechanism to those observed in inorganic materials. Recent reports have shown that cluster glass type behaviour within organic samples can be observed where there is charge frustration that originates from a triangular lattice of electronic states<sup>6</sup>.

Magneto-electric (ME) coupling is a good indication of multiferroic behaviour where recent work on  $\kappa$ -(BEDT-TTF)<sub>2</sub> Cu[N(CN)<sub>2</sub>]Cl (denoted  $\kappa$ -Cl and where BEDT-TTF is bis(ethylenedithio)tetrathiafulvalene), the structure of which comprises of layers of BEDT-TTF cations that undergo anti-ferromagnetic ordering at 23 K<sup>7</sup>, displaying coupling of the magnetism and electronic charge states<sup>8</sup>. This is achieved through a freezing of electron density across a molecular dimer within these layers and a coupling through the triangular lattice. MEM(TCNQ)<sub>2</sub> (MEM = N-methyl-N-ethylmorpholinium) also shows an anomaly in the dielectric constant (at 9 GHz) at the spin-Peierls transition<sup>9</sup>, however no data is available on the frequency dependence. In order to investigate other systems, similar or not, for the potential to show ME coupling, one must consider samples that show strong magnetic interactions between anions; here we consider the charge-transfer salt tetraethylammonium

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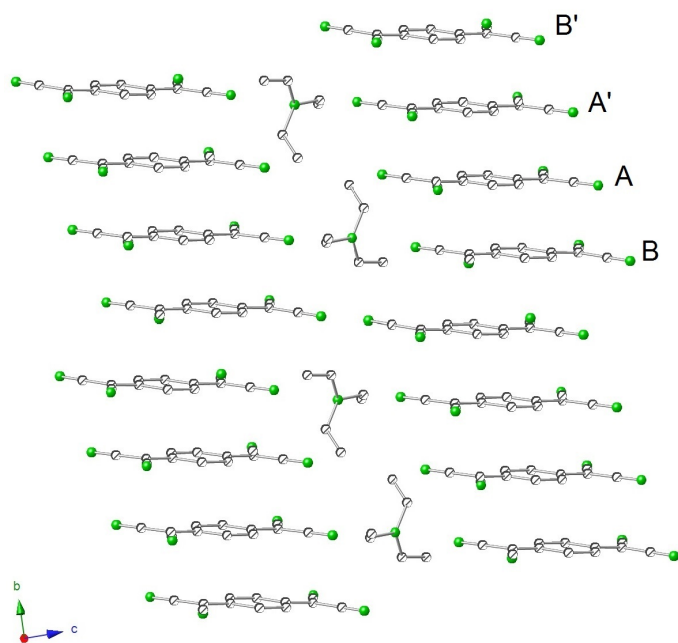
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**Fig. 1** Crystal structure of TEA(TCNQ)<sub>2</sub> showing the inherent tetramerisation and stacking of the TCNQ molecules along the *b*-axis at room temperature. Note that this shows the average structure as below 220 K, there is a freezing of the TEA cations into one of two positions refined in reference<sup>15</sup>.

bis-7,7,8,8-tetracyanoquinodimethane (TEA(TCNQ)<sub>2</sub>), which seems to be an ideal model system.

TEA(TCNQ)<sub>2</sub> shows TCNQ stacking along the *b*-direction (see Figure 1) where the TCNQ stacks are in sets of 4 (denoted BAA'B' with an inversion centre between the A and A' molecules)<sup>10</sup>, thus creating favourable tetramerisation where a single electron is delocalised across a TCNQ dimer<sup>10,11</sup>. As the temperature decreases, there is a gradual increase in the tetramerisation of the TCNQ units along the stack. The TEA cations fluctuate between two different configurations within the crystal structure and at 220 K, they freeze into a disordered state<sup>10,12–14</sup> that also effects the TCNQ stack and each dimer behaves as an  $S = 1/2$  entity. The magnetism is dominated by singlet-triplet excitations and this crossover temperature is from  $\sim 120$  K (This transition is from herein denoted as  $T_{ST}$ ), the system shows strong antiferromagnetic coupling (i.e. a singlet state is formed) between the BAA'B' dimers<sup>13,16,17</sup>. One interesting feature of the TCNQ dimer is that the single electronic charge is split across the molecular unit unevenly over the temperature range from 395 to 110 K<sup>10,18</sup>. As the temperature increases ( $T > 345$  K) one may expect this charge distribution to become equal. However, at 295 K it is split at  $q_A/e = 0.58$  and  $q_B/e = 0.42$  ( $q_A$  and  $q_B$  denote the charge on the A and B TCNQ molecule respec-

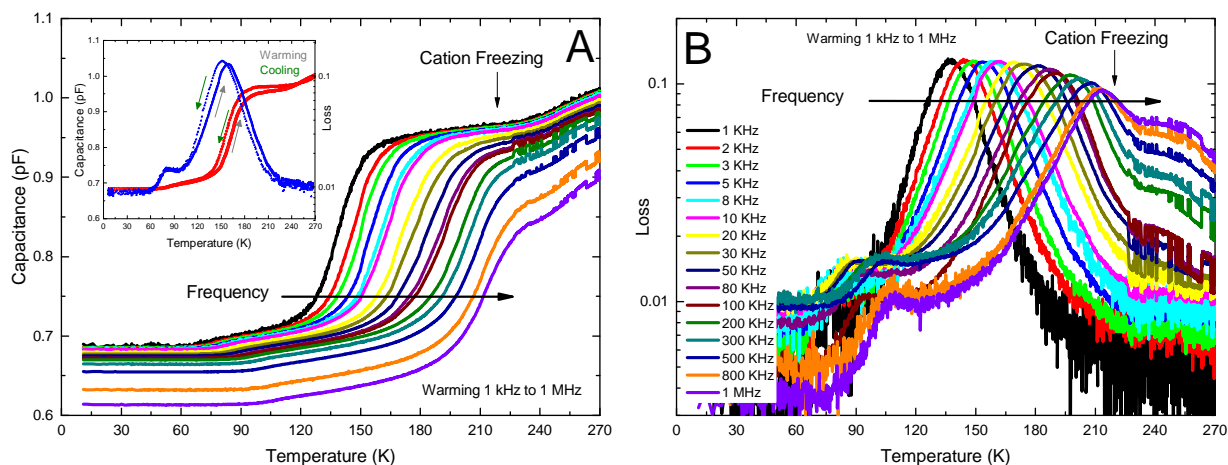
tively and  $e$  is the elementary charge) and is most pronounced at 110 K where  $q_A/e = 0.72$  and  $q_B/e = 0.28$ . Consequently this provides much encouragement, as the search for organic ferroelectrics hinges on a polarisation of electron density across a molecule and as such within TEA(TCNQ)<sub>2</sub> this may be intrinsic across the TCNQ dimers. Thus this warrants further investigation in order to determine whether there is evidence for ferroelectric behaviour and ME coupling within this material, and whether these strongly interacting TCNQ based systems may be a good model to pursue with regards to novel ferroelectric or even multiferroic samples. Within this work we show dielectric measurements on TEA(TCNQ)<sub>2</sub> that display features at both the cation freezing and singlet-triplet transitions. In both cases there is a strong frequency dependence which can be explained by a glassy dipolar state which at low temperatures is coupled with singlet-triplet excitations.

## 2 Experimental Methods

The samples were prepared using a method detailed by Melby *et al.*<sup>19</sup> and were in the form of long purple/black needles of the order of a few millimetres in length. Dielectric measurements were performed using an Agilent E4980A Precision LCR meter where the sample (approximately 3 mm length) was mounted on a gold capacitor circuit evaporated onto a piece of sapphire (see supplementary information). One must bear in mind therefore, that the capacitance will include that of the substrate and contacts, however, a background scan showed this contribution to be negligible and so the circuit can be considered to be a single resistor and capacitor in parallel. From the experiment both the capacitance and loss can be measured, which is a measure of the real and imaginary part of the dielectric constant. The capacitance is a measure of the dynamics of the polarisability of the sample, and the loss measures the phase shift of the impedance of the electronic polarisability to the applied AC field. Therefore, when the electric dipole moments can no longer keep up with the oscillating field, this will feature as a component within the loss. Note that although the capacitance ( $C$ ) and loss could be measured, the area of the sample is unknown as there is no well defined cross-sectional area of the crystal; because of this one cannot calculate the dielectric constant. This should however not effect the conclusions from our measurements since

$$\epsilon = \frac{Cd}{\epsilon_0 A}, \quad (1)$$

where  $\epsilon$  is the dielectric constant,  $\epsilon_0$  is the vacuum permeability,  $A$  is the area and  $d$  is the distance between capacitor plates. Thus  $\epsilon \propto C$  and the changes in  $C$  or the loss should correspond to changes in both the real and complex parts of  $\epsilon$ . An AC electrical field was applied to the long axis of the crystal which is along the stacking direction of the TCNQ molecules as determined from



**Fig. 2** Capacitance (A) and loss (B) data for TEA(TCNQ)<sub>2</sub> showing anomalies at ~220 K and ~100 K. *Inset*: Warming and cooling data for the capacitance and loss at 10 kHz, the green arrows and grey arrows correspond to the cooling and warming curves respectively.

X-Ray diffraction (see Figure 1), so the field will be causing the electronic dipoles to oscillate perpendicular to the flat-plane of the TCNQ molecules. This is advantageous as the application of the electric field perpendicular to the stacking direction showed strong anisotropy when studying both the optically excited vibrational modes<sup>20</sup> and the DC electrical conductivity<sup>21</sup>. However, our work focuses on the dynamics associated with electrical polarisation.

### 3 Results and Discussion

The raw data are shown in Figure 2 and clear anomalies at approximately 220 and 100 K are observed in both  $C$  (Figure 2A) and the loss (Figure 2B). The dielectric experiments measure changes of the electronic polarisation within the sample as a function of frequency and so every change in the data corresponds to the sample undergoing a change related to the electronic polarisation within material. Below 60 K the response is flat and this includes a background contribution. There is a strong frequency dependence at both anomalies, which can be a clear indication of some glassy or relaxor type behaviour related to the electric dipole interactions<sup>22</sup>. The warming and cooling data taken at 10 kHz shows hysteretic behaviour at the high temperature transition (220 K) that could point towards two possible scenarios; the first is that the transition is first order in nature, i.e. a pure structural distortion, and the second is that the relaxor/glassy nature of the sample dominates, as the relaxation time diverges. The structural study by Filhol and Thomas<sup>10</sup> showed no evidence of a sudden change in the lattice parameters that would indicate a first order transition and since the cooling and warming rates were different, it may be that the latter, glassy scenario, is more likely. Within the loss, the behaviour at high frequencies ( $T > 240$  K) is likely due to the sample being semiconducting or metallic above

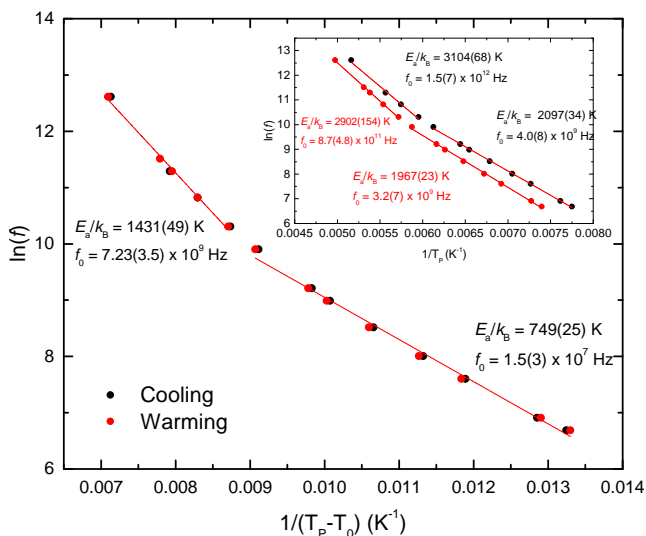
this cation freezing transition. As an estimate to gain the magnitude of the dielectric constant<sup>23,24</sup>, the crystal dimensions could be approximated as  $3 \times 0.5 \times 0.2$  mm in length. This results in a permittivity of  $2.4 \times 10^3$ , if one assumes a capacitance of 0.7 pF, which is a fairly large value but is in agreement with what is expected for a ferroelectric, although an order of magnitude lower than that of a colossal permittivity material<sup>25</sup>.

Although both anomalies will be considered, we will firstly discuss the frequency dependent behaviour at ~220 K. As mentioned previously, there is some form of hysteretic behaviour associated with the transition and so when taking the temperature of the maximum of the peak ( $T_p$ ) within the loss, two values will be obtained corresponding to heating and cooling of the sample. Using the Arrhenius equation, it is possible to analyse the data to obtain a value for the energy gap associated with the statistical population of the excited and ground states. A plot of  $\ln(f)$  vs.  $1/T_{max}$  was made (see inset to Figure 3) and within the plot there are two clearly different regimes with a difference in slopes that occur between 20 kHz and 30 kHz. Fitting to the data provides unreasonable values for the activation energy ( $E_a$ ) and nominal time scale of the fluctuations/attempt frequency ( $f_0$ ), as shown in the inset of Figure 3. Instead a better model is the Vogel-Fulcher law (VF);

$$f = f_0 \exp\left(\frac{E_a}{(T_p - T_0)}\right), \quad (2)$$

which accounts for a  $T_0$ , or a freezing temperature of the dipolar glassy interactions<sup>26</sup>. For the cooling and warming data,  $T_0 = 53$  and 60 K respectively. By choosing different values of  $T_0$  these curves can be made to overlap showing the scaling relation, whereas the Arrhenius type analysis has no flexible parameters, thus it makes it also makes it harder to parameterise the system.

At  $\ln(f) \approx 10$  or  $f \approx 22$  kHz, there is a definite change in slope

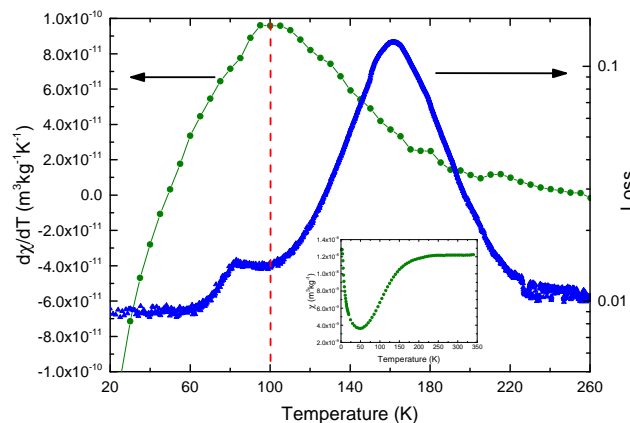


**Fig. 3** Vogel-Fulcher analysis of the cation freezing ( $T_P$ ) at 220 K within the loss data for TEA(TCNQ)<sub>2</sub>. Note that  $T_0 = 53$  and 60 K for the cooling and warming curves respectively and the parameters calculated are more reasonable than for the simple Arrhenius type behaviour. *Inset*: Arrhenius plot of the maximum in the loss that correspond to the cation freezing transition. The parameters for both the warming and the cooling are physically unreasonable and so the VF approach is likely a more accurate description of the underlying physics. *In all cases uncertainties are given in brackets.*

shown clearly in Figure 3. This change in slope may be due to the fact that the measurements are sensitive to different relaxations or processes, although the two processes are likely to be related. Measures of energy gap associated with the transition are of the order of  $\sim 2000$  K<sup>21,27</sup>, therefore one may allocate the high frequency ( $f > 20$  kHz) behaviour to the increasing interactions within the TCNQ stacks. The difference may be due to the different time scales of measurements. The process with an  $E_a = 749$  K from our measurements may therefore be due to the ordering of the TEA cations at  $\sim 210$  K. The lower energy associated with the cation freezing again supports the idea that the structural distortion may be due to the freezing of the cations which in turn causes the interactions between TCNQ dimers and tetramers to increase leading to a strongly coupled Mott state<sup>13</sup>.

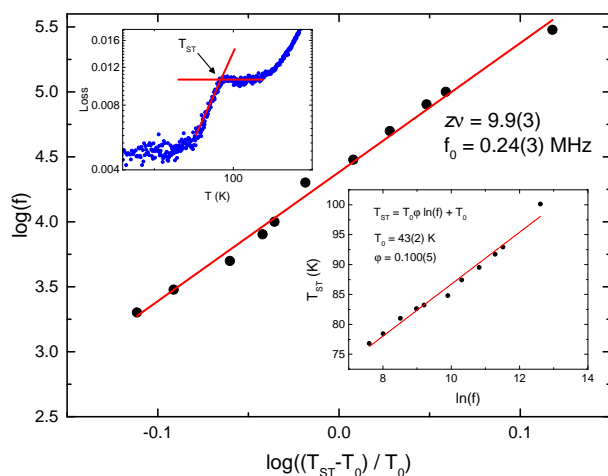
The magnetism of TEA(TCNQ)<sub>2</sub> has been previously studied where there is a gradual tetramerisation of the TCNQ units below 250 K<sup>17</sup>, which is also seen in our data (see inset to Figure 4). When differentiating the magnetic susceptibility data one finds the steepest part of the slope is approximately 100 K which can be considered to be where the freezing of singlet-triple excitations freezes out and the system is locked into a singlet ground state. This transition matches well with the low temperature features seen in the  $C$  and loss data for the sample. This is demonstrated in Figure 4, where the loss and differentiated susceptibility of the

sample are compared and there is a definite correlation between the two datasets. Ultimately this means that the magnetic transition is coupled to the electronic polarisation and the magnetic ordering may trigger an electric dipole ordering.



**Fig. 4** The differentiated magnetisation plotted against  $T$  to show the steepest part of the slope, generally considered as a good indication of a critical temperature compared to the loss at 10 kHz. The onset of the low temperature anomaly within the loss shows coupling to the magnetic transition within the data which is strong evidence for magneto-electric coupling. *Inset*: Magnetic susceptibility of TEA(TCNQ)<sub>2</sub> as a function of temperature in an applied field of 5 T.

The frequency dependence of the peak within the loss can be analysed in a similar manner to the cation freezing distortion above. Note that  $T_{ST}$ , the temperature associated with the condensing of the system into the singlet phase, was from the loss data and defined as the intersection of two straight lines as shown in the upper inset of Figure 5. The strong frequency dependence and the unreasonable fitting parameters from the Arrhenius behaviour (see supplementary information) points to a more glassy or relaxor state. One must therefore use the VF law to describe the data (see supplementary information). In order to calculate a reasonable value for  $T_0$  the frequency dependence of the peak was plotted as it tends to  $f = 0$  (see the lower inset of Figure 5) where  $T_0 = 43(2)$  K. Using the Mydosh criterion one can look at the frequency dependence of the transition where  $\phi = 0.1$ , which is, for the spin glass analogue, similar to cluster glasses or super spin glasses<sup>28</sup>. Within TEA(TCNQ)<sub>2</sub> the sample may undergo a transition where the electric dipoles order in local clustered regions. For the VF analysis it was found that the best fits to the data produced values for  $E_a/k_B$  and  $f_0$  of 423 K and  $4.8 \times 10^8$  Hz respectively. Therefore these represent the energy scales required for an excitation from the ground state, but since both the magnetic and electrical behaviour is coupled, a perturbation in one causes a perturbation in the other.



**Fig. 5** Critical scaling behaviour of TEA(TCNQ)<sub>2</sub> analogous to spin glass systems where the critical temperature varies with frequency. *Top inset:* A graph showing how the transition temperature ( $T_{ST}$ ) was defined. *Bottom inset:* Mydosh-type analysis of through the transition to study the frequency dependence and to get a value for  $T_0$  within this magnetic transition. *In all cases errors are given in brackets.*

Since there are strong analogies between dipolar and spin glasses, it is worth attempting further analysis of the anomaly in the dielectric loss associated with singlet-triplet transition. One model used within spin glasses is critical scaling behaviour<sup>28</sup>, described by

$$f = f_0 \left( \frac{T_{ST} - T_0}{T_0} \right)^{-z\nu}, \quad (3)$$

where  $f_0$  is the attempt frequency,  $T_0$  is the freezing temperature (43 K) and  $z\nu$  is a critical dynamical exponent. Fits to the data produced values for  $f_0$  and  $z\nu$  of 0.24(3) MHz and 9.9(3) respectively. The value of  $f_0$  is slower than that observed within spin glass systems however it is on the time scale of our measurements and is similar to the frequency of magnetic fluctuations observed in MEM(TCNQ)<sub>2</sub> in the vicinity of  $T_{ST}$ <sup>29</sup>. The value of the dynamical exponent is also of interest as this is well within the limits of that observed for spin glasses<sup>28,30</sup>. However, these parameters have a dependence on the choice of value of  $T_0$ .

Both the cation freezing and singlet-triplet (ST) crossovers are observed in the dielectric data and as mentioned above this implies that in the case of the ST transition, the magnetic and electronic polarisation are strongly coupled. This is evidence that the sample behaves similarly to  $\kappa$ -Cl<sup>8</sup>, which is a multiferroic at low temperatures. The multiferroic behaviour in  $\kappa$ -Cl is dominated by a freezing of electric dipoles across a cationic BEDT-TTF dimer (each BEDT-TTF is an electron donor). The TCNQ dimers within our sample, behave in an opposite manner and are the electron acceptors. Although charge-ordering is common within low dimensional charge transfer salts<sup>31</sup> this can manifest as differences

in critical and ferroelectric transition temperatures. Therefore within TEA(TCNQ)<sub>2</sub>, since a charge difference exists across the TCNQ dimers that results in an electric dipole, which may be able to fluctuate and be polarisable even below the temperature at which the TEA cation configuration freezes. Since the P $\bar{1}$  contains an inversion centre, they may simply represent a spatially averaged structure and one interpretation of the dipolar ordering could come from the local regions where the freezing of the TEA cations produces a static disorder, where the inversion symmetry of the average structure could be broken. At  $T_{ST}$  the magnetic exchange between TCNQ dimers may cause a freezing of the magnetic moments and the system enters a quasi-static state. This in turn causes a freezing or locking of the fluctuations of the electronic dipole moments across the TCNQ dimers. This leads to static electric dipole due to the inequivalent electron density distribution across a TCNQ dimer and could lead to ferroelectric or multiferroic ordering.

## 4 Conclusion

To conclude, we have demonstrated anomalies within the  $C$  and loss data taken on a single crystal of TEA(TCNQ)<sub>2</sub> which correspond to the onset of a cation freezing and of singlet-triplet excitations. The dielectric data show a sensitivity to the high temperature cation freezing distortion where two different relaxation processes were separated; one due to the cation freezing and the other related to the opening of a pseudo-energy gap, which effects the conduction along the TCNQ stacks. At lower temperatures the features within the  $C$  and loss data are due to the onset of a singlet-triplet energy gap opening up resulting from correlations between  $S = 1/2$  TCNQ dimers. On going through the magnetic transition the electric dipole ordering is observed to be glassy with analysis that shows similar characteristics to that of spin glasses. Therefore although the magnetism is considered to be in a frozen coupled state, this may not be the case for the electric dipoles until below  $T_{ST}$  where they freeze into a clustered arrangement.

There is a lot of interest in the search for organic systems for technological applications and we have presented data for a material that highlights the applicability and potential of TCNQ based organic charge transfer salts in which there is a strong magneto-electric coupling. Hopefully the usefulness of these type of  $\pi$ -stacked systems has been highlighted when designing materials where a coupling between the magnetism and electrical properties is desirable, such as within multiferroics.

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