The shape of galaxy dark matter haloes in massive galaxy clusters: insights from strong gravitational lensing

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ABSTRACT

We assess how much unused strong lensing information is available in the deep *Hubble Space Telescope* imaging and *Very Large Telescope/Multi Unit Spectroscopic Explorer* spectroscopy of the *Frontier Field* clusters. As a pilot study, we analyse galaxy cluster MACS J0416.1–2403 (z = 0.397, $M(R < 200 \text{ kpc}) = 1.6 \times 10^{14} \text{ M}_{\odot}$), which has 141 multiple images with spectroscopic redshifts. We find that many additional parameters in a cluster mass model can be constrained, and that adding even small amounts of extra freedom to a model can dramatically improve its figures of merit. We use this information to constrain the distribution of dark matter around cluster member galaxies, simultaneously with the cluster's large-scale mass distribution. We find tentative evidence that some galaxies' dark matter has surprisingly similar ellipticity to their stars (unlike in the field, where it is more spherical), but that its orientation is often misaligned. When non-coincident dark matter and stellar haloes are allowed, the model improves by 35 per cent. This technique may provide a new way to investigate the processes and time-scales on which dark matter is stripped from galaxies as they fall into a massive cluster. Our preliminary conclusions will be made more robust by analysing the remaining five *Frontier Field* clusters.

Key words: gravitational lensing: strong – galaxies: clusters: Individual (MACSJ0416.1-2403) – galaxies: evolution – dark matter – cosmology: observations.

1 INTRODUCTION

Galaxies are profoundly transformed by infall into a cluster. As evidenced by the typically smooth distributions of cluster light, infalling subhaloes have their gas content efficiently removed to the intra-cluster medium (ICM) by ram-pressure stripping, even while they pass the virial radius (Smith et al. 2010; Wu et al. 2013). In these cluster outskirts, stripping occurs at a rate consistent with simulations. The mass of an L* galaxy is reduced by $\sim 10^{13}$ to $\sim 10^{12}$ M_{\odot} as it falls from a radius of 5-1 Mpc (Limousin et al. 2007; Natarajan et al. 2009). However, predictions from simulations disagree when the galaxy continues to the central hundreds of kiloparsecs (e.g. Diemand, Kuhlen & Madau 2007; Peñarrubia, McConnachie & Navarro 2008; Wetzel, Cohn & White 2009). The time-scale on which dark matter is eventually stripped by tidal forces remains highly uncertain (Bahé et al. 2012), but the different time-scales of infall phases means that the relative ellipticity and alignment between galaxies' stellar and dark matter haloes are likely to change

Galaxy clusters are the largest observable structures in the Universe (e.g. Shaye et al. 2015). Comprising of thousands of galaxies embedded within a hot X-ray emitting gas halo and the largest concentrations of mass observed, they have become important test beds for theories of structure formation (Jauzac et al. 2015a, 2016, 2017; Natarajan et al. 2017) and dark matter (e.g. Markevitch et al. 2004; Harvey et al. 2015). The mass of a galaxy cluster can exceed $M > 10^{15}$ M_{\odot} (e.g. Bourdin et al. 2011; Jauzac et al. 2012,2015b; Medezinski et al. 2013; Umetsu et al. 2016), heavily distorting the curvature of local space–time. As a result, geodesics to objects behind the cluster become bent, and often split – resulting in multiple, highly distorted images of background galaxies (Schneider 1985; Bartelmann 2010; Kneib & Natarajan 2011; Hoekstra et al. 2013). This effect is known as strong gravitational lensing. Since the image distortion is directly related to the gradient of the gravitational po-

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⁽Pereira & Bryan 2010). Galaxies in the field are predicted to have dark matter haloes more spherical than their stars, and misaligned semimajor axes (Tenneti et al. 2014; Velliscig et al. 2015). However, the situation is again more complex inside clusters, with different measurement techniques yielding incompatible results (e.g. Hao et al. 2011; Sifón et al. 2015; West et al. 2017).

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tential causing it, it is possible to use this information to reconstruct the distribution of all matter along the line of sight, including dark matter (e.g. Richard et al. 2014; Sharon & Johnson 2015; Lagattuta et al. 2017; Mahler et al. 2017).

This paper attempts, for the first time, to implement a method proposed by Harvey, Kneib & Jauzac (2016, hereafter H16) to measure infalling galaxies' stellar and dark matter properties using strong gravitational lensing in exceptionally deep, highresolution observations. For this, we exploit Hubble Space Telescope (HST) Frontier Fields survey (HFF; Lotz et al. 2017) imaging of galaxy cluster MACS J0416.1–2403 (z = 0.397, $M(R < 200 \,\mathrm{kpc}) = (1.60 \pm 0.01) \times 10^{14} \mathrm{M_{\odot}};$ Jauzac et al. 2014, hereafter J14). All six HFF clusters have seven-band HST imaging to unprecedented depth. MACS J0416 also has spectroscopy from the Multi Unit Spectroscopic Explorer (MUSE) at the Very Large Telescope (VLT), which provides spectroscopic redshifts for a large number of strongly lensed galaxies (Caminha et al. 2017). This exceptional information density has led to one of the best-constrained cluster mass models, free from the two usual systematic errors: (1) the unknown distance between the lensed galaxy and the observer and (2) the misidentification of counter images. Using simulations specifically of MACS J0416, H16 showed that perturbations of member galaxies' ellipticity, orientation, position, and size can shift multiple images by up to 1 arcsec. Thus, it may be possible to simultaneously constrain the distribution of mass both in the cluster halo and also in individual galaxies.

This paper is organized as follows. In Section 2, we describe the strong-lensing mass models we use for our analysis. In Section 3, we present our findings. In Section 4, we discuss their implications. Throughout this paper, we assume a Λ cold dark matter cosmological model, with $\Omega_m = 0.3$, $\Omega_{\Lambda} = 0.7$, and Hubble constant $H_0 = 70 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$. We note that there currently exists some tension in the measured values of these parameters (e.g. Riess et al. 2016; Planck Collaboration XVI 2014). However, while variations in cosmological parameters affect the overall *normalization* of the inferred lens mass, they do not affect the shapes, position angles, and positions of haloes studied here. Simultaneously constraining cosmological parameters is beyond the scope of this paper.

2 STRONG-LENSING MASS MODELS

2.1 Figures of merit

This analysis compares various models of the mass distribution in MACS J0416. To qualitatively evaluate the accuracy of each model, we adopt several statistical figures of merit.

Following a Markov Chain Monte Carlo (MCMC) search of model parameter space, we calculate the Bayesian evidence, *E*, and the Bayesian likelihood, \mathcal{L} , of the best-fitting model. For these statistics, higher values mean better models. However, note that none of these figures of merit can compare models with different inputs (such as multiply imaged galaxies or cluster member catalogues). For the maximum likelihood model, we also compute the root-mean-square discrepancy between the predicted and observed positions of lensed galaxies in the image plane, $\langle rms_i \rangle$. For this statistic, lower values mean better models.

To compare models with different parameters, we also calculate the Bayesian Information Criterion (BIC):

$$BIC = -2\log(\mathcal{L}) + k\log(N), \tag{1}$$

where N is the number of constraints and k is the number of free parameters. We then calculate the Akaike Information Criterion

(AIC):

$$AIC = -2\log(\mathcal{L}) + 2k, \tag{2}$$

which is a more robust estimate of overfitting. We finally consider the AIC corrected

AICc = AIC +
$$\frac{2 k (k+1)}{(N-k-1)}$$
, (3)

which corrects the AIC for a finite number of free parameters. For these figures of merit, lower values should also be preferred. All three include a penalty term for models with too many free parameters that overfit noise rather than capture additional information. This penalty term is larger with BIC and AICc than with AIC. Note that these figures of merit were developed for fits to models with linear parameters. Strong gravitational lensing is highly non-linear, so we report these values but interpret them with caution.

2.2 Fiducial model

As a fiducial model of the mass distribution in MACS J0416, we adopt the CATS model v4 from the *Frontier Fields* Mikulski Archive for Space Telescopes (MAST) archive.¹ The *HST* observations of MACS J0416 were taken under Proposal ID 13396 (PI: Lotz). This was created using LENSTOOL (Jullo et al. 2007) to best reproduce the observed position of 141 multiple images from 51 strongly lensed galaxies. At least one of the multiple images in each system has a spectroscopic redshift. Counter images of each system are either confirmed by a spectroscopic redshift or identified using their geometry, colour, and morphology (Limousin et al. 2007; Richard et al. 2011).

The cluster mass distribution is built from three cluster-scale haloes. We include 96 member galaxies with mass-to-light ratios fixed by the Faber & Jackson (1976) relation (grey circles in Fig. 1). Two more galaxies close to multiple images are modelled individually, i.e. not assuming the Faber & Jackson (1976) relation, as they are showing clear signs of galaxy–galaxy lensing. Every component is modelled as a pseudo-isothermal elliptical mass distribution (Elíasdóttir et al. 2009), characterized by a spatial position (x, y), ellipticity ϵ , orientation θ , core radius $r_{\rm core}$, scale radius $r_{\rm s}$, and velocity dispersion σ .

In previously published mass models, galaxies are represented by a single halo containing all of their mass. Parameters describing the shape and size of each halo are fixed from the distribution of light in the F814W band; the velocity dispersion is fixed from the F814W-band flux, such that a galaxy's total mass follows the Faber & Jackson (1976) relation. For the first time, we separate galaxies into components of dark and stellar matter. We preserve total mass, and fix stellar mass to values measured by the ASTRODEEP survey, using spectral energy density (SED) fitting to multiband photometry (Castellano et al. 2016; Merlin et al. 2016). This photometry includes seven optical and near-infrared bands from HST/ACS and VLT/Hawk-I, plus Spitzer/IRAC 3.6 and 4.5 µm bands. The SED fitting measures physical properties using six different methods to minimize residual systematics. Initially, we assume the two components are coincident, so the model has no extra free parameters. Figures of merit for this model are listed in Table 2.

¹https://archive.stsci.edu/pub/hlsp/frontier/macs0416/models/cats/ This is similar to the model in Jauzac et al. (2014), but has been re-optimized after redshifts for more multiple images were confirmed by new *VLT/MUSE* spectroscopy (Caminha et al. 2017).



Figure 1. Composite *HST*/ACS colour image of MACS J0416 (axes show right ascension and declination in degrees). Grey circles show the cluster galaxies included in our mass models, assuming the Faber & Jackson (1976) relation between luminosity and mass. Green diamonds highlight the nine galaxies individually optimized for the 'Ellipticity' model. Orange ellipses highlight the nine galaxies individually optimized for the 'Position Angle' model: the ellipse is oriented following the best-fitting value of θ . The red crosses show the nine galaxies for which the dark matter halo position (*x*, *y*) is constrained: they are centred on the best-fitting position of the dark matter halo, the size of the bars correspond to the 95 per cent error on that position. Cyan squares show the positions of strongly lensed images of background galaxies that we used to optimize our models.

2.3 Models with additional free parameters

We shall now model the distribution of dark matter in some galaxies independently of their distribution of stars. With a parameter space spanning up to seven parameters for each of 96 galaxies, optimization could rapidly become impossible. To make the calculation tractable, we prioritize galaxies to model individually.

We first identify cluster member galaxies whose distribution of dark matter might be constrainable without prior bias. To be conservative in this proof-of-concept analysis, we exclude from consideration galaxies with ellipticity $\epsilon < 0.2$ or stellar-to-halo-mass ratio, SHMR > 0.3. The first cut is because of the way LENSTOOL parametrizes ellipticity as (ϵ, θ) , with a strict bound $\epsilon > 0$. For example, after randomly perturbing the positions of multiple images,

galaxies that are nearly circular appear to gain a best-fitting ellipticity that is biased high by this bound. The second cut is because scatter in the Faber & Jackson (1976) relation leads to unphysical values of our simple SHMR estimates, which prevent us from splitting a galaxy's total mass between stellar and dark matter components in a consistent way. These cuts lead to a catalogue of 29 galaxies, spread fairly uniformly throughout the cluster. Both limitations could be avoided in principle, and a few additional galaxies could be considered in future work.

To identify galaxies whose distribution of dark matter will be constrained with statistical significance, H16 suggests finding all those near multiple images – but notes that some configurations of strong lensing are more constraining than others. To avoid missing

Table 1.	Coordinates of the individually optimized galaxies.	We also high-
light which	ch one is being optimized by which model(s).	

RA (deg)	Dec. (deg)	Ellipticity	Position angle	Position
64.029 693 60	-24.083 408 36	бХ	Х	Х
64.036 865 23	-24.080 665 59)	Х	Х
64.031 967 16	-24.077 428 82	2 X	Х	Х
64.031 822 20	-24.077 793 12	2	Х	
64.029 380 80	-24.079 008 10)	Х	Х
64.038 101 19	-24.067 483 90) X	Х	Х
64.041 316 67	-24.071 607 78	3		Х
64.039 451 60	-24.069 332 12	2 X	Х	Х
64.032 676 70	-24.070 148 47	Х		
64.026 557 92	-24.070 133 21		Х	
64.046 363 83	-24.067 058 56	бХ		
64.048 713 68	-24.065 114 97	Х		Х
64.042 694 09	-24.065 128 33	3 X		
64.045 188 90	-24.062 135 70) X	Х	Х

any constrainable galaxies, we implement a two-step process. First, for all 29 eligible galaxies, we use LENSTOOL to vary the ellipticity ϵ , orientation θ , and position (x, y) of dark matter within broad priors. The parameter space is highly dimensional, so the posterior probability density function (PDF) remains noisy after any reasonable amount of computing time. However, we can predict which parameters will be constrainable in a second optimization, by fitting Gaussians to the noisy PDF. We identify nine galaxies whose 1D PDF has width $\sigma_{\epsilon} < 0.3$, nine galaxies with $\sigma_{\theta} < 60^{\circ}$, and nine galaxies with $\sigma_x < 2$ arcsec and $\sigma_y < 2$ arcsec. They are not the same nine galaxies in each case, because different lensing configurations constrain different properties of a local mass distribution (it is a coincidence that each requirement leads to nine galaxies). The galaxies in each set are shown by the different symbols in Fig. 1 (green diamonds for ellipticity, orange ellipses for position angle, and red crosses for position). Their coordinates and the overlap between sets are listed in Table 1. The overlap is also illustrated in Fig. 2.

Finally, we re-initialize the MCMC for three last optimizations. The cluster-scale haloes are being optimized with the two galaxies responsible for galaxy–galaxy lensing, galaxy-scale haloes are optimized following the Faber & Jackson (1976) relation, however for nine galaxies simultaneously, we optimize either the dark matter ellipticity ϵ , orientation θ , or spatial position (*x*, *y*).

3 RESULTS

We shall now discuss the results of each re-optimization, and compare each best-fitting model with the fiducial one. Figures of merit for these models are listed in Table 2.

3.1 Varying the ellipticity of galaxies' dark matter

Allowing nine galaxies' dark matter haloes to have a different axis ratio than its stars improves the best-fitting $\langle rms_i \rangle$ by ${\sim}13$ per cent compared to the fiducial model. The 2 per cent decrease in BIC and 6 per cent decrease in AICc suggest that this improvement is not simply due to overfitting noise, but reflects real inadequacy in the fiducial model.

We find that about half the galaxies have dark matter that is more spherical than the stars, as expected (Fig. 3). However, the other half of the galaxies have dark matter with ellipticity similar to that



Figure 2. Venn diagram showing the overlap between the three sets of nine galaxies being considered for ellipticity, orientation, and spatial position optimization.

of their stellar haloes, in contradiction with numerical simulations which predict dark matter haloes to be more spherical than the stellar ones (e.g. Tenneti et al. 2014; Velliscig et al. 2015). Note that the extreme end of one or two galaxies' PDFs in Fig. 3 may be truncated by priors, but this effect appears robust to excluding those. Multiplying the PDFs together, to represent the net galaxy population, yields a mean value $\langle \epsilon_{\rm DM} - \epsilon_* \rangle = 0.01 \pm 0.05$.

A subtlety of ellipticity measurement is that parametric fits (as obtained from LENSTOOL) give ~ 10 per cent higher absolute values for the same distribution than moment-based measurements (as obtained for ASTRODEEP using SEXTRACTOR; Bertin & Arnouts 1996). For the fairest comparison, this analysis therefore reports stellar ellipticities instead measured using the CIAO 4.9 fitting tool SHERPA (Freeman, Doe & Siemiginowska 2001). This does not change our qualitative conclusion.

3.2 Varying the orientation of galaxies' dark matter

Allowing nine galaxies' dark matter haloes to be rotated with respect to the stars improves $\langle rms_i \rangle$ by ~9 per cent compared to the fiducial model. The decrease in BIC and AICc is similar to the previous test.

We find that the dark matter in about half (5/9) of the galaxies is aligned with the stars. However, dark matter in two of the galaxies is significantly misaligned with (~45° from) the stars, and in two of the galaxies it is consistent with being maximally misaligned by 90°. The net galaxy population has a mean misalignment $\langle \theta_{\rm DM} - \theta_{\star} \rangle = 48 \pm 8$.

3.3 Varying the position of galaxies' dark matter

Allowing nine galaxies' dark matter haloes to be spatially offset from the stars adds twice as many free parameters as the other tests, but improves $\langle rms_i \rangle$ by ~ 35 per cent compared to the fiducial model. BIC and AICc decrease by 19 per cent and 28 per cent, again suggesting that a more complex model is not simply fitting noise. However, individual galaxies' PDFs remain broad, and it is difficult to quantify the error in the position of a dark matter halo due to the complex configuration of multiple images (Harvey et al. 2017). There is no net preferred direction along which to average spatial offsets from the entire sample.

4 DISCUSSION AND FUTURE WORK

Parametric models are widely used to fit the mass distribution in galaxy clusters. They are the most successful at reproducing observed positions of multiple images in simulated clusters

Table 2. Figures of merit for each model considered in this paper. Columns show the number of degrees of freedom (d.o.f.), the number of free parameters (*k*), the total number of parameters (*N*), Bayesian evidence (log *E*), and likelihood (log \mathcal{L}), the rms deviation of predicted multiple-image positions from their observed positions in the image plane (rms_i), the BIC, the AIC, and the corrected AIC. We also quote the improvement on several parameters compared to the fiducial model: on the (rms_i), δ_{rms_i} , the BIC, δ_{BIC} , and the AICc, δ_{AICc} . A value of δ_{BIC} and δ_{AICc} greater than 10 reflects a significant improvement of the model compare to the fiducial one.

Model	d.o.f.	k	Ν	$\log E$	$\log \mathcal{L}$	$\langle rms_i \rangle$	BIC	AIC	AICc	$\delta_{ m rms_i}$	δ_{BIC}	δ_{AICc}
Fiducial	154	26	180	-493.07	-245.91	0.80″	627	543	553	_	_	_
Ellipticity	145	35	180	-280.24	-216.81	0.74''	615	503	521	8 per cent	12	32
Position angle	145	35	180	-271.08	-217.76	0.74''	617	506	523	8 per cent	10	30
Position (x, y)	136	44	180	-209.49	-140.29	0.52''	509	369	398	35 per cent	118	155



Figure 3. Top panel: probability distribution of the ellipticity as a function of the difference between the ellipticity of the stellar halo and the ellipticity of the dark matter halo for the nine galaxies that have constrained ellipticities from the model. The black line corresponds to the mean over all galaxies. Bottom panel: probability distribution of the acute angle θ between the major axes of a galaxy's stars and its dark matter.

(Meneghetti et al. 2017), and ostensibly reach a statistical precision of 1 per cent. These models are exploited to study physical processes in the cluster itself (e.g. Jauzac et al. 2015a; Ogrean et al. 2015; Annunziatella et al. 2017) or to use its gravitational lensing as a natural telescope to observe the high-redshift Universe (e.g. Atek et al. 2015; Ishigaki et al. 2015; Kawamata et al. 2016). We have demonstrated that the latest high-resolution, deep images of galaxy clusters contain a lot more information than is accounted for by parametric models. Commonly used figures of merit such as $\langle rms_i \rangle$ can be improved dramatically by the introduction of relatively few extra free parameters.

If the parameters are chosen well, the additional information content could be used to model the distribution of mass in cluster member galaxies. One tentative, but potentially interesting result from our analysis is that some cluster galaxies appear to have an equally high dark matter haloes axis ratio as their stellar companions. In field galaxies, the distribution of dark matter is more spherical than the stars. This discrepancy could potentially help to constrain the mechanisms and time-scales for the stripping of dark matter from galaxies during infall into clusters. On the other hand, we find that the orientation of galaxy's dark matter haloes is often misaligned, which could also provide an alternate probe to the physics of harassment during galaxy infall.

Alternatively, the additional information could indicate (and quantify) deficiencies in the models used to fit galaxy clusters. We also find that our model of MACS J0416 dramatically improves by 35 per cent when we let the position of the dark matter to separate from that of the stars. This improvement however has no common trajectory or obvious physical origin so we therefore attribute this to the lack of complexity for the cluster-scale haloes imposed by the parametric approach. Parametric models can span only a limited range of mass distributions, and cannot capture the full complexity seen in simulations around the most massive structures in the Universe. While their statistical precision may approach 1 per cent, their accuracy may not be as good.

We are optimistically inclined to believe that the information is truly connected to galaxy properties, because the improvements in fit come from all over the cluster rather than one (perhaps poorly modelled) region. One way to distinguish between these scenarios will be to repeat our test, but starting from free-form mass models (e.g. Diego et al. 2014) that already have sufficient flexibility to capture more substructures. It would then be necessary to add individual haloes for each galaxy that are as orthogonal as possible to existing free parameters.

It will also be necessary to expand our analysis to more galaxy clusters. To complete a proof of concept, this paper analysed a single *HFF* cluster, MACS J0416. The limited statistical significance of our results does not yet support robust conclusions. However, the surprisingly large improvement in figures of merit such as $\langle rms_i \rangle$ clearly demonstrates the available information content that is being missed by current analyses, and justifies an expansion of the study. At best, this information will provide a useful new tool to investigate the properties of galaxies' dark matter, as they are transformed by their infall into massive clusters. At worst, better statistics will quantify systematic effects in current studies of the high-redshift, gravitationally lensed Universe.

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REFERENCES

- Annunziatella M. et al., 2017, ApJ, 851, 81
- Atek H. et al., 2015, ApJ, 814, 69
- Bahé Y. M., McCarthy I. G., Crain R. A., Theuns T., 2012, MNRAS, 424, 1179
- Bartelmann M., 2010, Class. Quantum Gravity, 27, 233001
- Bertin E., Arnouts S., 1996, A&A, 117, 393
- Bourdin H. et al., 2011, A&A, 527, A21
- Caminha G. B. et al., 2017, A&A, 600, A90
- Castellano M., Amorín R., Merlin E., Fontana A., McLure R. J., Mármol-Queraltó E., 2016, A&A, 590, A31
- Diego J. M., Broadhurst T., Molnar S. M., Lam D., Lim J., 2014, MNRAS, 447, 3130
- Diemand J., Kuhlen M., Madau P., 2007, ApJ, 667, 859
- Elíasdóttir Á. et al., 2009, ApJ, 697, 1725
- Faber S. M., Jackson R. E., 1976, ApJ, 204, 668
- Freeman P., Doe S., Siemiginowska A., 2001, in Starck J.-L., Murtagh F. D., eds, Proc. SPIE Vol. 4477, Astronomical Data Analysis, SPIE, Bellingham, p. 76
- Hao J., Kubo J. M., Feldmann R., Annis J., Johnston D. E., Lin H., McKay T. A., 2011, ApJ, 740, 39
- Harvey D., Courbin F., Kneib J. P., McCarthy I. G., 2017, MNRAS, 472, 1972
- Harvey D., Kneib J. P., Jauzac M., 2016, MNRAS, 458, 660
- Harvey D., Massey R., Kitching T., Taylor A., Tittley E., 2015, Science, 347, 1462
- Hoekstra H., Bartelmann M., Dahle H., Israel H., Limousin M., Meneghetti M., 2013, Space Sci. Rev., 177, 75
- Ishigaki M., Kawamata R., Ouchi M., Oguri M., Shimasaku K., Ono Y., 2015, ApJ, 799, 12
- Jauzac M. et al., 2012, MNRAS, 426, 3369
- Jauzac M. et al., 2014, MNRAS, 443, 1549
- Jauzac M. et al., 2015a, MNRAS, 446, 4132

- Jauzac M. et al., 2015b, MNRAS, 452, 1437
- Jauzac M. et al., 2016, MNRAS, 463, 3876
- Jauzac M. et al., 2017, MNRAS, preprint (arXiv:1711.01324)
- Jullo E., Kneib J.-P., Limousin M., Elíasdóttir Á., Marshall P. J., Verdugo T., 2007, New J. Phys., 9, 447
- Kawamata R., Oguri M., Ishigaki M., Shimasaku K., Ouchi M., 2016, ApJ, 819, 114
- Kneib J.-P., Natarajan P., 2011, A&AR, 19, 47
- Lagattuta D. J. et al., 2017, MNRAS, 469, 3946
- Limousin M. et al., 2007, ApJ, 668, 643
- Lotz J. M. et al., 2017, ApJ, 837, 97
- Mahler G. et al., 2017, MNRAS, 473, 663,
- Markevitch M., Gonzalez A. H., Clowe D., Vikhlinin A., Forman W., Jones C., Murray S., Tucker W., 2004, ApJ, 606, 819
- Medezinski E. et al., 2013, ApJ, 777, 43
- Meneghetti M. et al., 2017, MNRAS, 472, 3177
- Merlin E. et al., 2016, A&A, 590, A30
- Natarajan P., Kneib J.-P., Smail I., Treu T., Ellis R., Moran S., Limousin M., Czoske O., 2009, ApJ, 693, 970
- Natarajan P. et al., 2017, MNRAS, 468, 1962
- Ogrean G. A. et al., 2015, ApJ, 812, 153
- Pereira M., Bryan G., 2010, ApJ, 721, 939
- Peñarrubia J., McConnachie A. W., Navarro J. F., 2008, ApJ, 672, 904
- Planck Collaboration et al., 2014, A&A, 571, A16
- Richard J., Jones T., Ellis R., Stark D. P., Livermore R., Swinbank M., 2011, MNRAS, 413, 643
- Richard J. et al., 2014, MNRAS, 444, 268
- Riess A. G. et al., 2016, ApJ, 826, 56
- Schaye J. et al., 2015, MNRAS, 446, 521
- Schneider P., 1985, A&A, 143, 413
- Sharon K., Johnson T. L., 2015, ApJ, 800, L26
- Sifón C., Hoekstra H., Cacciato M., Viola M., Köhlinger F., van der Burg R. F. J., Sand D. J., Graham M. L., 2015, A&A, 575, A48
- Smith G. P. et al., 2010, A&A, 518, L18
- Tenneti A., Mandelbaum R., Di Matteo T., Feng Y., Khandai N., 2014, MNRAS, 441, 470
- Umetsu K., Zitrin A., Gruen D., Merten J., Donahue M., Postman M., 2016, ApJ, 821, 116
- Velliscig M. et al., 2015, MNRAS, 454, 3328
- West M.J, Propris R.D, Bremer M.N, Phillipps S, 2017, Nat. Astron., 1, s41550
- Wetzel A. R., Cohn J. D., White M., 2009, MNRAS, 395, 1376
- Wu H.-Y., Hahn O., Wechsler R. H., Behroozi P. S., Mao Y.-Y., 2013, ApJ, 767, 23

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