PAPER • OPEN ACCESS

Coulomb anti-blockade in a Rydberg gas

To cite this article: A D Bounds et al 2019 New J. Phys. 21 053026

View the article online for updates and enhancements.



IOP ebooks[™]

Bringing you innovative digital publishing with leading voices to create your essential collection of books in STEM research.

Start exploring the collection - download the first chapter of every title for free.

of Physics

Deutsche Physikalische Gesellschaft 🕕 DPG

IOP Institute of Physics

Published in partnership

with: Deutsche Physikalische

Gesellschaft and the Institute

New Journal of Physics

The open access journal at the forefront of physics



OPEN ACCESS

RECEIVED 12 February 2019

REVISED 5 April 2019

ACCEPTED FOR PUBLICATION 24 April 2019

PUBLISHED 22 May 2019

Original content from this work may be used under the terms of the Creative Commons Attribution 3.0 licence.

Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.



Coulomb anti-blockade in a Rydberg gas

A D Bounds, N C Jackson, R K Hanley 💿 , E M Bridge, P Huillery and M P A Jones 👘

Joint Quantum Centre Durham-Newcastle, Department of Physics, Durham University, Durham, DH1 3LE, United Kingdom E-mail: a.d.bounds@durham.ac.uk

Keywords: Rydberg, plasma, anti-blockade, strontium

Abstract

PAPER

We perform a comprehensive investigation of the coupling between a Rydberg-dressed atomic gas and an ultra-cold plasma (UCP). Using simultaneous time-resolved measurements of both neutral atoms and ions, we show that plasma formation occurs via a Coulomb anti-blockade mechanism, in which background ions DC Stark shift nearby atoms into resonance at specific distances. The result is a highly correlated growth of the Rydberg population that shares some similarities with that previously observed for van der Waals interactions. We show that a rate equation model that couples the laserdriven Rydberg gas to the UCP via a Coulomb anti-blockade mechanism accurately reproduces both the plasma formation and its subsequent decay. Using long-lived high angular momentum states as a probe, we also find evidence of a crossover from Coulomb anti-blockade to Coulomb blockade at high density. As well as shedding light on loss mechanisms in Rydberg-dressed gases, our results open new ways to create low-entropy states in UCPs.

1. Introduction/motivation

Hybrid quantum systems of ultracold atoms and ions are emerging as a platform for fundamental research in quantum physics [1]. Recently, Rydberg states have received attention as a way to control the coupling between ionic and atomic systems [2–5], for example, using Coulomb blockade from a single ion to suppress Rydberg excitation [6]. Ultracold mixtures of Rydberg atoms and ions have also been studied in the context of cold Rydberg gases, where it was generally found that ions are almost always present due to processes such as collisions between nearby Rydberg atoms and blackbody photoionization. Indeed, studies using resonant laser excitation of Rydberg states have shown an ultra-cold plasma (UCP) under conditions of strong excitation, both in the pulsed [7–9] and continuously driven [10, 11] regimes.

In this paper, we demonstrate that an off-resonant excitation of the Rydberg state can be used to tailor the the interaction between Rydberg atoms and ions in an ultracold gas. We show that plasma formation occurs via a Coulomb anti-blockade mechanism, illustrated in figure 1(b), where background ions DC Stark shift nearby atoms into resonance at specific distances. The result is a highly correlated 'facilitated growth' of the Rydberg population that shares some similarities with that previously observed using van der Waals anti-blockade [12]. A rate equation model that couples the driven Rydberg gas to an UCP via this correlated excitation model accurately reproduces both the initial creation and subsequent decay of the observed ion signal. At longer times, the ionization of long-lived high angular momentum Rydberg states produced in the plasma provides evidence for the interplay between Coulomb blockade [6] and Coulomb anti-blockade in the plasma. In future experiments, controlling this process could provide a route to creating an UCP with a strongly correlated ionic state [13].

Our results also provide a strategy for minimising losses due to ionization in cold Rydberg gas experiments, particularly those aimed at 'dressing' a lower-lying atomic state with properties of a Rydberg state by strong offresonant laser excitation [14–20]. Off-resonant Rydberg dressing has been demonstrated experimentally in alkali metal atoms for two atoms [21] and in optical lattices [22, 23]. However, attempts to observe Rydberg dressing in high-density BECs and 3D lattice gases of alkali metal and alkali earth atoms have been hampered by unexpected loss mechanisms associated with enhanced population of the Rydberg state, which have in general



Figure 1. (a) Relevant energy levels in ⁸⁸Sr. The MOT operates on the 689 nm transition and dressing using 319 nm light offresonantly couples the $|e\rangle = 5s5p$ ³P₁ state to the $|r\rangle = 5s36d$ ³D₁ state. (b) Upper panel: atom–atom (solid purple line) and atom– ion (dashed black line) interaction strength as a function of interparticle separation *r*. Lower panel: the corresponding distancedependent Rydberg excitation fraction for a detuning $\Delta = -(+)12$ MHz for the atom–atom (atom–ion) pair.

limited the achievable lifetime to less than 1 ms [24–27]. Recently our group successfully Rydberg dressed a strontium magneto-optical trap (MOT) using the energy level scheme illustrated in figure 1(a), achieving a lifetime of >1 ms [28]. In that case, selecting a Rydberg state with the correct sign of the DC polarizability was essential in order to avoid the collective ionization mechanisms that we study in detail here. Lastly we note that control of the collisional interaction between trapped ions and ultracold atoms using Rydberg dressing was previously considered in [29].

2. Experimental techniques

The experiments began with the formation of a MOT of ⁸⁸Sr atoms operating on the narrow $5s^2 \, {}^{1}S_0 \leftrightarrow 5s5p \, {}^{3}P_1$ transition. A MOT beam detuning of $\delta_{MOT}/2\pi \approx -175$ kHz and an intensity per beam of $I_{MOT} = 3-50 \, I_{sat}$ (where I_{sat} is the saturation intensity of the transition) resulted in $1/e^2$ cloud radii of 30–60 μ m (100–200 μ m) in the vertical (z) (horizontal (x)) direction, and temperature $T_z = 1 \, \mu$ K. The MOT is loaded from a first-stage MOT operating on the much broader $5s^2 \, {}^{1}S_0 \leftrightarrow 5s5p \, {}^{1}P_1$ transition. By varying the number of atoms captured in the first-stage MOT, the final density of the MOT can be varied independently of the other experimental parameters. More details on the apparatus and loading process can be found in [30–32].

Atoms in the MOT were subsequently coupled to the Rydberg state by off-resonantly driving the 5s5p ${}^{3}P_{1} \rightarrow 5s36d {}^{3}D_{1}$ transition using 50 mW of 319 nm light [33] with a beam waist of 160 μ m (120 μ m) in the vertical (horizontal) direction, resulting in a peak coupling beam Rabi frequency of $\Omega/2\pi = 4$ MHz. The coupling beam detuning was varied from $\Delta/2\pi = -20$ to +20 MHz, allowing observation of the attractive van der Waals interaction of the 36d ${}^{3}D_{1}$ state for negative detunings, and the DC Stark shift due to nearby ions for positive detunings, illustrated in figure 1(b). As we showed in our previous work, laser cooling and trapping forces continue to operate in the Rydberg-dressed MOT [28]. After dressing for a time t_{d} , the cloud was imaged using resonant absorption imaging on the 461 nm transition (figure 1(a)). As the cloud was often optically thick, ballistic expansion was sometimes used to reduce the optical depth of the cloud β before imaging, sacrificing information on the cloud spatial profile. Fitting to the cloud shape, the ground state population N_{g} was measured.

The spontaneous generation of ions in the cloud [8, 34, 35] was studied by continuously counting the ions using a micro-channel plate (MCP) rather than directly (and destructively) probing the Rydberg population through field- or auto-ionization. Spontaneous ionization may occur through several mechanisms including blackbody photoionization, ionizing collisions between nearby Rydberg atoms, and collisions with fast-moving ground state atoms from the atomic beam. Detection was enhanced through a small bias field of ~20 mV cm⁻¹ that draws ions towards the MCP in 30 μ s. Using a fast digital oscilloscope, the arrival of individual ions can be logged with a detection of efficiency of up to 2% [32] and a time-resolution better than 10 ns [36]. However, for most of the data in this paper, the long total acquisition time (>5 ms) necessitated an increase of the time window for detection of a single ion to 40 ns, resulting in a concomitant drop in detection efficiency to 0.5%. The resulting ion signals were then binned according to their arrival times to produce an ion detection rate; by varying the bin width rates could be measured over several orders of magnitude. The combination of non-destructive and time-resolved single-ion detection allows observation of ion detection rates in real-time over the



Figure 2. (a) The fractional change $\beta' = \beta(t = t_d)/\beta(t = 0)$ in optical depth β after dressing for a time $t_d = 5$ ms versus detuning for $\rho_0 = 0.6 \times 10^{10}$ cm⁻³ (black triangles), 2×10^{10} cm⁻³ (purple circles) and 7×10^{10} cm⁻³ (pink squares). Here $\delta_{MOT}/2\pi = -210$ kHz, $I_{MOT} = 50$ I_{sat} and $\Omega/2\pi = 4$ MHz. (b) Histograms showing the distribution of β' over multiple runs of the experiment for the high density data in (a) (pink squares) for three different values of the detuning $\Delta = -10$ MHz (i), 0 MHz (ii) and +10 MHz (iii).

long timescales relevant to Rydberg-dressing experiments, illustrated in figure 4. By repeating the experiment up to 12 times for a given set of experimental conditions, we gain access to the statistical distribution of the ion signal. In particular, we can evaluate the time-dependent Mandel *Q* parameter given by [37]

$$Q = \frac{\langle (\Delta N(t))^2 \rangle}{\langle N(t) \rangle} - 1, \tag{1}$$

where $\langle (\Delta N(t))^2 \rangle$ and $\langle N(t) \rangle$ are respectively the variance and mean of the ion signal at time *t*. The Mandel *Q* parameter is a measure of the deviation of a repeated measurement from Poissonian statistics, with Q > 0 indicating super-Poissonian signals and Q < 0 indicating sub-Poissonian signals [38]. Super-Poissonian signals, such as those we demonstrate in figure 3, are often associated with anti-blockade and collective excitation; sub-Poissonian signals are often associated with blockade effects and nonlinear excitation suppression, and also detector saturation [39]. We do not correct measured *Q* parameters for detection efficiency.

3. Atom loss and spontaneous ionization

The change in the optical depth of the MOT due to the Rydberg coupling laser is illustrated in figure 2, for three different values of the initial density ρ_0 . The lineshape of the loss feature is asymmetic. For the lowest and intermediate density, additional loss occurs for negative detunings relative to positive detunings.

This result is consistent with the attractive van der Waals interaction [40] shifting nearby pairs of atoms into resonance (anti-blockade) as observed in previous experiments [12, 41]. A density of 2×10^{10} cm⁻³ corresponds to a Wigner–Seitz radius (defined as the radius of a sphere of volume equal to the mean volume per atom) of 2.3 μ m, similar to the 1.6 μ m facilitation radius of the 36d³D₁ Rydberg state for $\Omega/2\pi = 4$ MHz, $\Delta/2\pi = -6$ MHz at which the van der Waals interaction shift is equal to the coupling beam detuning.

As the density was increased further, additional loss also appeared for positive detunings. Unlike for zero detuning, the atom number was observed to fluctuate significantly from shot to shot as shown in figure 2(b). This behaviour cannot be explained through the attractive van der Waals interactions of the $5s36d^{3}D_{1}$ Rydberg state. Instead we attribute this loss to the presence of ions in the cloud; for positive coupling beam detunings the ions DC Stark shift atoms into resonance with the coupling beam, leading to enhanced Rydberg excitation and atom loss from the MOT.

The corresponding ion signals for the data presented in figure 2 are shown in figure 3. The time dependence of both the ion detection rate $\langle \dot{N} \rangle$ and the Mandel Q parameter are shown. The ion detection rate demonstrates a strong density dependence, with negligible ionization at low density. At intermediate densities, ions are only observed on resonance and for negative detunings. This observation is consistent with the enhanced loss for negative detunings observed in figure 2. The ion signal is slightly super-Poissonian, which is consistent with the expected correlated growth of Rydberg excitations due to the anti-blockade effect [39]. This effect has been studied in detail elsewhere [42–44] and we do not examine these results further.





At the highest atom density (figure 3(c)) significant ionization is also observed for negative detunings. In fact for $\Delta < 0$ the detector saturates at high density, leading to the sub-Poissonian statistics observed in the Mandel Q parameter. Of interest for this paper is the appearance of a large ion signal for positive detunings, accompanied by super-Poissonian statistics, which is consistent with the enhanced atom loss observed in figure 2. Furthermore, histograms of the ion signal (figure 2) show that the distribution of the total number of ions detected becomes bimodal at high density and positive detuning. This observation is consistent with an avalanche effect that strongly enhances Rydberg excitation and ionization. Our interpretation is that the correlated growth of Rydberg excitation due to the DC Stark shifts from nearby ions eventually leads to the runaway formation of an UCP, leading to rapid ionization of nearly all the remaining Rydberg atoms.

4. Time dependence of the ion signal

To investigate this effect in more detail, we study the time dependence of the ionization rate for a single detuning. These data were taken with different parameters to figure 2 that are chosen such that the plasma threshold is always reached and the distribution is no longer bimodal. Four different stages can be identified in figure 4.

- Plasma seeding and growth (inset (a))—after a density-dependent delay (the plasma seeding time), the ion signal rapidly rises within the first 20 μ s of dressing.
- Rapid atom loss ((a) and (b))—strong Rydberg excitation results in large ion signals and rapid loss of ground state atoms. The ion signal and the atom number decay at similar rates.
- Dressed MOT—the rate of atom loss reduces abruptly and the ion detection rate stabilises, leaving a relatively long-lived, low density Rydberg-dressed MOT that is similar to that presented in [28].
- Long-lived Rydberg atoms—a long-lived ion signal continues to be observed even when the dressing laser and MOT beams are switched off.

To interpret these stages, we note that previous work has shown that in a spontaneously ionizing Rydberg gas, an UCP is formed once the number of ions exceeds a threshold given by $N_C = E_e \sqrt{(\pi/2)} 4\pi\epsilon_0 \sigma/e^2$, where the electron energy E_e is equal to the Rydberg binding energy, e is the electron charge, ϵ_0 is the electric permittivity of vacuum and σ is the cloud radius [8, 45, 46].

The resulting plasma undergoes rapid expansion driven by disorder-induced heating [47, 48], typically living for just a few tens of microseconds [49]. During the plasma phase, the trapped electrons collide with the remaining Rydberg atoms, leading to rapid ionization and the formation of long-lived high-angular momentum Rydberg states [50].



Figure 4. (a) Ion detection rate versus arrival time for an initial density 6×10^{11} cm⁻³ and $\Omega/2\pi = 4$ MHz, $\Delta/2\pi = +12$ MHz and a dressing time $t_d = 2$ ms (indicated by the dashed line). The inset shows the first 0.1 ms of the same dataset with the plasma seeding time indicated by the shaded area. The 30 μ s for ions to reach the detector has been subtracted. (b) Measured variation in atom number versus t_d . Error bars are too small to be seen. The point at $t_d = 2$ ms corresponds to the data shown in (a). (c) Variation of the total detected ion signal $\langle N \rangle$ with initial atom number for different values of the total power in the MOT beams within the ranges <60 μ W (pink squares), 60–150 μ W (purple circles) and >150 μ W (black triangles).

The density-dependent seeding time thus represents the time taken for the number of ions to reach the plasma threshold. At this point, electron Rydberg collisions become possible, leading to a rapid increase in the ionization rate. The ions in the plasma are replenished from the (decaying) atomic population, until the rate of ionization is no longer high enough to balance the rate of ion loss due to plasma expansion, and the plasma is quenched. Ionization can still proceed through non-collisional processes, but at a much lower rate, and the atom population decay is reduced. Once the dressing laser is switched off, the slow black-body radiation induced ionization of long-lived, high-*l* Rydberg atoms [50] created within the plasma is observed. In figure 4(c) we show that the total number of detected ions exhibits the threshold dependence on the ground state atom number that is characteristic of an UCP.

5. Theoretical description

The coupled evolution of a Rydberg gas and a plasma has been considered theoretically by several groups [10, 11, 51]. A related approach was developed for plasma formation in thermal gases in [52]. However these works have focussed primarily on the role of ions in suppressing, rather than enhancing, the Rydberg excitation rate by DC Stark shifting the resonant Rydberg coupling laser off-resonance with the transition. Here we develop a model based on coupled rate equations for the total number of each of the three key species present in the cloud: ground state atoms $N_{\rm g}$, Rydberg atoms $N_{\rm Ryd}$ and ions in the cloud $N_{\rm ion}$. Solutions of the rate equations can then be compared directly to data such as that shown in figure 4.

The initial atom cloud is assumed to be a spheroid of randomly-distributed ground-state atoms, with uniform density and radius σ . As a further simplifying assumption, the Rabi frequency of the coupling laser Ω is also considered to be uniform across the cloud. A fraction P_E of the atoms are considered to be excited to the $5s5p {}^{3}P_{1}$ state by the cooling light in the MOT. The value of P_E depends on the MOT beam power, and is constrained within the range $0.04 < P_E < 0.5$ by the operation of the MOT [53].

Atoms in the 5s5p ${}^{3}P_{1}$ state are available for excitation to the Rydberg state by the coupling laser. As the timescale to reach the steady state is on the order of the Rydberg state lifetime of $1/\Gamma_{Ryd} \sim 20 \ \mu s$, it is much shorter than the timescale associated with the atom loss and ionization shown in figure 4, allowing us to consider the steady-state Rydberg excitation rate described by the power-broadened ($\Omega \gg \Gamma_{Ryd}$) Lorentzian lineshape:

$$R_{\text{Ryd, }|\textbf{m}_{j}|}(r) = N_{\text{g}} P_{\text{E}} \frac{\Gamma_{\text{Ryd}}}{2} \frac{\Omega^{2}}{\Omega^{2} + 2[\Delta - \Delta_{\text{DC, }|\textbf{m}_{j}|}(r)]^{2}}.$$
(2)



Figure 5. (a) Rydberg excitation rate as a function of distance from an ion, described by equation (4) for $P_E = 0.5$ (black solid line). The one-body rate is indicated by the pink dashed line. Inset shows the excitation rate multiplied by r^2 for the same parameters, reflecting the integral weighting in equation (5). (b) Integrated excitation rate as a function of ion density ρ_{ion} (black solid line). The pink dashed line indicates the one-body excitation rate.

Here the laser detuning Δ is combined with the DC Stark shift of the Rydberg state caused by the presence of an ion at a distance r

$$\Delta_{\rm DC}(r) = -\frac{1}{2} \alpha_{|m_j|} \left[\frac{1}{4\pi\epsilon_0} \frac{e}{r^2} \right]^2,\tag{3}$$

where the polarisability of the Rydberg state is $\alpha_{|m_I|=0(1)} = -2\pi \times 40$ (16) MHz/(V/cm)² for the two 36d ³D₁ $|m_I|$ states [32]. To take into account the anisotropy due to the different static polarizability of the $|m_I| = 0$ and $|m_I| = 1$ sublevels we calculate the total excitation rate

R

$$_{\text{Ryd}}(r) = R_{\text{Ryd},|m_l|=0}(r) + R_{\text{Ryd},|m_l|=1}(r);$$
(4)

assuming that the coupling strength for each is $\Omega/\sqrt{2}$ to reflect that on average only half of the coupling light will be the correct polarisation to excite each sublevel. This term plays a key role in the simulation by allowing for the enhanced growth of Rydberg excitations when $\Delta \approx \Delta_{\rm DC}$, as shown in figure 5 and will occur if the coupling beam detuning Δ is of opposite sign to the Rydberg state polarisability α . To include this effect in the model, we express the Rydberg excitation rate as a function of ion number $N_{\rm ion}$ rather than distance r, by integrating over the distribution of atom–ion separations. We treat ions as uniformly distributed such that the number of atoms around an ion is given by $\rho_{\rm atom} 4\pi r^2 \delta r$. The Rydberg excitation rate is then calculated as a function of ion number:

$$R_{\rm Ryd}(N_{\rm ion}) = \frac{\int_0^{r_{\rm ion}} R_{\rm Ryd}(r) \times \rho_{\rm atom} 4\pi r^2 \delta r}{\int_0^{r_{\rm ion}} \rho_{\rm atom} 4\pi r^2 \delta r}.$$
(5)

The upper limit of this integral is set by the mean distance between ions given by the Wigner Seitz radius $r_{\rm ion} = (3/4\pi\rho_{\rm ion})^{1/3} = \sigma/N_{\rm ion}^{1/3}$, where $\rho_{\rm ion} = 3N_{\rm ion}/4\pi\sigma^3$ is the ion density. The ion Wigner Seitz radius is the radius of a sphere with a volume equal to the mean volume per ion; using this approach is therefore equivalent to considering the cloud as comprised of spheres of atoms surrounding each ion.

The way in which this term leads to density-dependent coupling between Rydberg atoms and ions, along with strong spatial correlations, is shown in figure 5. At low charge densities, corresponding to large typical atom–ion separations, the Rydberg excitation rate follows the one-body rate. At higher charge densities the Rydberg excitation rate rises until at the 'facilitation radius' the detuning Δ is compensated by the DC Stark shift. In figure 5 two peaks appear due to the presence of resonances associated with the $|m_j| = 0$ and $|m_j| = 1$ states. The result is a substantial increase in Rydberg excitation and results in the rapid loss of atoms observed in figure 4. At ion densities above 2.5×10^9 cm⁻³ this effect saturates and the integrated excitation rate begins to fall with density. Atoms are so close to ions that the DC Stark shift is large enough to shift atoms beyond resonance with the coupling laser. For large enough ion density, the integrated excitation rate falls below the one-body rate: this is the Coulomb blockade regime [6]. This suggests that Coulomb blockade may result in a self-limiting Rydberg population similar to that proposed in [11], even when the overall effect is one of avalanche anti-blockade.

To complete the rate equations, we also consider the decay and loss mechanisms for Rydberg atoms and ions. Our experiments have shown that there are two important one-body decay processes that contribute to the overall decay rate of the Rydberg states Γ_{Ryd} . The first is radiative decay, which occurs predominantly to lowlying triplet states that are not connected by dipole-allowed transitions to the ground state. This decay is included in the model by introducing a dark state with associated population N_{dark} . Population in this state does not contribute to absorption images, and appears as an overall loss of atoms from the cloud. The second process is spontaneous ionization. Even in the absence of an UCP (i.e. below threshold), a significant background ionization rate is observed. To quantify the branching ratio between radiative and ionizing decay we have measured the ratio of ions created without autoionization (i.e. through spontaneous ionization) to the total Rydberg population measured using autoionization [31] following a controlled excitation sequence with no plasma or significant ion population present. From this we estimate that approximately $P_{\text{ion}} = 30\%$ of the Rydberg atoms decay to ions, through several mechanisms such as blackbody radiation [34], collision with hot atoms [8] and Penning ionization [35]. A high ionization fraction is consistent with high densities of attractively interacting Rydberg states [54, 55]. The spontaneous ionization process is included in the model as a one body coupling $\dot{N}_{\text{ion}} = P_{\text{ion}} \Gamma_{\text{Ryd}} N_{\text{Ryd}}$ with decay to dark states described as $\dot{N}_{\text{dark}} = (1 - P_{\text{ion}}) \Gamma_{\text{Ryd}} N_{\text{Ryd}}$.

Crucially, above the threshold for plasma formation, Rydberg atoms are also ionized by collisions with trapped electrons [7], resulting in an avalanche process as the rising electron population increases the collision rate. In our simulations, we consider that a plasma forms when $N_{\rm ion} > N_C = E_e \sqrt{(\pi/2)} 4\pi\epsilon_0 \sigma/e^2$, where the electron energy E_e is equal to the Rydberg binding energy [46]. Above this threshold, an additional term proportional to the electron density couples $N_{\rm Ryd}$ and $N_{\rm ion}$, given by $\dot{N}_{\rm ion} = 3\gamma_{\rm coll}N_{\rm Ryd}N_e/4\pi\sigma_{\rm P}^3$, where $N_e = N_{\rm ion} - N_C$ is the number of trapped electrons, and $\sigma_{\rm P}$ is the plasma radius, so that $3N_e/4\pi\sigma_{\rm P}^3$ is the electron density. The rate of ionizing electron-Rydberg collisions is given by $\gamma_{\rm coll} = \sigma_{\rm geo}\sqrt{E_e/m_e}$, where $\sigma_{\rm geo} = \pi n^4 a_0^2$ is the geometric cross-section of the Rydberg atom for a principal quantum number of n [10].

The final components of the model are terms that govern the rate at which ions are expelled from the cloud. We consider two processes. First, an applied electric field of ~20 mV cm⁻¹ extracts ions from the cloud in ~7 μ s. This extraction time gives rise to an ion loss rate of R_{extract} . These ions, labelled N_{free} , are then too far from the cloud to play any further part in the system dynamics so are considered lost. The second process is loss due to expansion of the plasma. Previous experiments on UCPs have shown that the dominant driver of expansion is the back-action of the electrons on the ions (electron pressure) [49], giving rise to a loss term of the form $\dot{N}_{\text{free}} = N_{\text{ion}}N_eR_{\text{repulsion}}$ where $R_{\text{repulsion}}$ is treated as a free parameter.

Taken together, these relationships lead to the following rate equations:

$$\dot{N}_{\rm g} = -R_{\rm Ryd}(N_{\rm ion});\tag{6}$$

$$\dot{N}_{\rm Ryd} = +R_{\rm Ryd}(N_{\rm ion}) - \Gamma_{\rm Ryd}N_{\rm Ryd} - \gamma_{\rm coll}N_{\rm Ryd}N_e / \frac{4}{3}\pi\sigma_{\rm P}^3;$$
(7)

$$\dot{N}_{\rm ion} = +P_{\rm ion}\Gamma_{\rm Ryd}N_{\rm Ryd} + \gamma_{\rm coll}N_{\rm Ryd}N_e / \frac{4}{3}\pi\sigma_{\rm P}^3 - N_{\rm ion}R_{\rm extract} - N_{\rm ion}N_eR_{\rm repulsion};$$
(8)

$$\dot{N}_{\text{free}} = +N_{\text{ion}}R_{\text{extract}} + N_{\text{ion}}N_eR_{\text{repulsion}};$$
(9)

$$\dot{N}_{dark} = +(1 - P_{ion})\Gamma_{Ryd}N_{Ryd}.$$
(10)

If the plasma size σ_P is taken to be equal to the size of the atomic cloud, then only two free parameters are not fixed by measurement or theory: P_E (which is constrained) and $R_{repulsion}$. The ion detection efficiency (a linear scaling between the measured signal and N_{ion}) is also treated as a free parameter, with best fitting found with a factor of 0.1%. The difference between this value and the estimated detection efficiency of 0.5% is attributed to stray electric field reducing the detection efficiency.

Before presenting a detailed comparison of the model with the measured data in the next section, it is insightful to reconsider some of the underlying physics. In particular, we point out that our model assumes that the formation of the plasma introduces an additional ionization channel, but does not modify the iondependent excitation process. In order for this to be the case, the length scale for the correlated excitation of Rydberg atoms due to nearby ions must be shorter than the Debye screening length $\lambda_D = \sqrt{\epsilon_0 k_B T_e/e^2 n_e}$ [45]. The electron temperature is given by T_e , and n_e is the electron density. For typical values, we expect a Debye length greater than 10 μ m, much greater than the interparticle separations. Consequently, we do not expect electrons within the plasma to screen atoms in the cloud from the presence of nearby ions, and do not consider them to modify the steady-state Rydberg excitation rate.

6. Comparison with experimental data

In this section, we compare solutions of the rate equations (equations (6)–(10)) to experimental measurements of the atom number and ion signal. The best fit illustrated in figure 6 was obtained with $R_{\text{repulsion}} = 10^4 \text{ e}^{-1} \text{ s}^{-1}$ and $P_{\text{E}} = 0.5 (0.3)$ for a MOT beam intensity of $I_{\text{MOT}} = 26 I_{\text{sat}} (I_{\text{MOT}} = 9 I_{\text{sat}})$. This value of



Figure 6. Ground state atom number (a), (c) and ion detection rate (b), (d) as a function of dressing time for different initial atom numbers at $\delta_{MOT}/2\pi = -110$ kHz, $\Delta/2\pi = +12$ MHz, $\Omega/2\pi = 4$ MHz and MOT beam intensities of $I_{MOT} = 9 I_{sat}(a)$, (b) and $I_{MOT} = 26 I_{sat}(c)$, (d). Model results are shown as solid lines and different colours and markers indicate the initial atom number, shown on the *y*-axis of (a) and (c).

 $R_{\text{repulsion}} = 10^4 \text{ e}^{-1} \text{ s}^{-1}$ corresponds to ions leaving the cloud in 1 μ s for an electron population of 100, which is consistent with plasma expansion velocities observed in UCPs [49]. The plasma size σ_P was also treated as a free parameter. For the case of $I_{\text{MOT}} = 9 I_{\text{sat}}$, we see good agreement with a constant plasma size of 45 μ m, consistent with the cloud size of 50 μ m by 100 μ m 1 e⁻² vertical and horizontal radii. However, in the case of higher MOT beam power, we observe best agreement allowing the plasma size to rise with initial atom number from 40 to 50 μ m, suggesting that at sufficiently high ion production rates the plasma size is a function of ion production rate.

Figure 6 shows that the simulation accurately reproduces the temporal behaviour of the atom number and the ion signal over several orders of magnitude, at least for the first ~1 ms of dressing. This includes both the rapid rise of the ion signal during the initial growth phase, and the subsequent decay, including regions where this decay deviates from a simple exponential. Importantly, examining each of the terms in this model enables us to understand which processes are important in each phase.

The density-dependent plasma seeding time defined in figure 4 is also quantitatively reproduced by the model, as shown in figure 7. The model shows that the seeding time and subsequent rapid loss depend critically on the existence of the Coulomb anti-blockade mechanism illustrated in figure 5. As shown in figure 7(b), the rise in the Rydberg population only occurs if the correlated growth of the Rydberg fraction due to ions is taken into account. The delay between the rise in Rydberg fraction and the rise in ion population is attributed to the time taken for ionization of Rydberg atoms to occur. When the plasma threshold is reached, the model predicts a sharp spike in the number of ions that dissipates due to plasma expansion that we do not observe, likely due to ions spreading out on their way to the detector.

Once the plasma has formed, collisional ionization of Rydberg atoms by electrons becomes a dominant process. The population in the Rydberg state drops as the ionization rate due to Rydberg-electron collisions dominates. The result is a largely exponential decay of the atom number, which since the ions are continually lost from the cloud is also mirrored in the ion signal. A quantitative comparison between the model and the data in this regime was made by fitting an exponential decay to the experimental and simulated data shown in figure 6.

8



Figure 7. (a) Measured plasma seeding time against simulated plasma seeding time, for $I_{MOT} = 9 I_{sat}$ (circles) and $I_{MOT} = 26 I_{sat}$ (crosses). Colours indicate initial atom number and correspond to the colours used in figure 6. The 30 μ s time for ions to reach the detector has been subtracted. (b) The simulated Rydberg fraction (black line) and the ion population (purple dashes) as a function of dressing time, simulated for $I_{MOT} = 9 I_{sat}$ and an initial atom number of 0.3 million. The dotted black line shows the Rydberg fraction in the absense of charges.



The resulting 1/e lifetimes are compared in figure 8(a), and the overall agreement is very good. We also observe a rise in plasma and cloud lifetime with increasing initial atom number, shown in figure 8(b). At first glance this result is suprising. The origin of this effect is the switch from Coulomb anti-blockade to Coulomb blockade for charge densities above 2.5×10^9 cm⁻³ shown in figure 5(b). As the atom number increases, the charge density increases above this value, leading to a reduction in the Rydberg fraction and an increase in the cloud and plasma lifetime. The plasma simulation predicts a peak charge density of up to 4×10^9 cm⁻³ across the plasma, sufficient to reach the self-limiting regime. This self-limiting effect is also responsible for the deviation from exponential decay in atom number and ion detection rate observed in figure 6, which is observed in both the data and the model. Further evidence of the important role of this density-driven cross-over from anti-blockade to blockade to blockade to matching the model is presented in section 7.

Eventually, the number of ions in the cloud decays to below the plasma threshold, and the plasma terminates, resulting in the abrupt change in the slope of the decay for atoms and ions that is observed in the atom number between 0.5 and 1 ms (figure 6). After this point, the role of ions in the excitation and decay processes becomes insignificant due to the low atom and ion density, and the rate equation model is no longer appropriate. Instead, the losses from the cloud are dominated by mechanical effects that originate from the combined effect of the AC Stark shift due to the dressing laser, and the ongoing laser cooling. A quantitative model for this regime was provided in our previous work on Rydberg dressed laser cooling [28].

Lastly, we note that in figure 6 we observe a factor of ~2 between the observed atom number and the modelled atom number at the point of plasma termination. We hypothesise that this difference is due to the finite extent of the UCP, which our fits suggest is less than the size of the atom cloud. Depletion of the atom number due to the plasma therefore occurs preferentially at the centre of the cloud, leaving the wings untouched. This effect is not included in the model. Since we ballistically expand the cloud before imaging, we are unable to





study the spatial dependence of the loss. In future experiments it may be possible to directly probe the spatial dependence of the Rydberg excitation in the cloud [36].

In summary, the rate equation model successfully reproduces the plasma formation and decay processes in this complex coupled system. The agreement is good across multiple observables, including the time dependence of the atom number and ion signal and their dependence on cloud density and MOT beam power. The role of ions in the cloud is critical throughout this process, influencing both the seeding of the plasma and the enhancement and partial suppression of Rydberg excitation within the plasma-coupled cloud.

7. Long-lived Rydberg population

A final probe of the plasma dynamics is the long-lived Rydberg population observed after the coupling laser is turned off (shown in figure 4). Long-lived Rydberg atoms may form in an UCP due to three-body recombination or electron-Rydberg collisions. Although previous studies of continuously driven plasmas have found that three-body recombination can modify the plasma dynamics [51], we do not expect three-body recombination to be significant at the charge density that we reach [56]. Instead we attribute the formation of long-lived Rydberg states to the population of high-angular momentum states by electron-Rydberg collisions, which are significant even at low plasma density [9]. Once created, these high angular momentum states are slowly ionized by blackbody radiation, giving rise to an ion signal that can be observed several milliseconds after the dressing laser is turned off [50]. The long-lived Rydberg population thus contains information about the initial plasma dynamics even several milliseconds after the plasma disperses.

Figure 9(a) shows ion detection rates after the coupling laser has been turned off for the data given in figure 6 and taken at $I_{MOT} = 9 I_{sat}$ with two different initial atom numbers of 3.4 and 0.3 million. Despite this order of magnitude difference in atom number, the number of ions detected after the dressing laser is switched off is essentially identical. As illustrated in figure 9(b), the decay rate of the long-lived component of the ion signal is also independent of the atom number and the dressing time. Based on these results, we use the ion detection rate 2 ms after dressing began $\langle \dot{N} \rangle_{2ms}$ as a proxy for the total long-lived Rydberg population, and study its variation with dressing time and atom number (figure 9(c)).

The most striking observation in figure 9(c) is that in the first 200 μ s of dressing the rate of creation of longlived Rydberg atoms is almost independent of atom number. The ground state atom number varies by an order of magnitude but $\langle N \rangle_{2ms}$ rises with dressing time at a largely constant rate until the plasma terminates, which occurs sooner for clouds with lower atom number. The electron-Rydberg collision rate is expected to be proportional to the product of the Rydberg population and electron density. Since the plasma is nearly neutral the electron density is related to the ion density less the plasma threshold. The implication is that the fraction of atoms in the Rydberg state must fall with increasing atom number in order to maintain the constant electron– Rydberg collision rate observed figure 9(c). Such a reduction is indeed predicted by our correlated growth model as shown in figure 5(b); for large ion densities the Rydberg excitation rate falls as the DC Stark shift begins to reduce rather than enhance the Rydberg excitation rate, leading to a cross-over to a Coulomb blockade effect for large enough densities. The long-lived ion signal therefore provides independent confirmation of this cross-over that was included in the rate equation model that successfully reproduced the formation and decay of the UCP in figures 6–8. In particular it confirms our interpretation of the dependence of the plasma lifetime on the initial atom number in figure 8.

8. Conclusion

In summary, we have used non-destructive and time-resolved ion detection to probe the spontaneous formation of ions in a Rydberg-dressed atomic cloud, and their impact on Rydberg excitation and atom loss. Charges created within the cloud can DC Stark shift nearby atoms into resonance with the excitation laser, leading to strong Rydberg excitation. This Coulomb anti-blockade effect eventually leads to the formation of an UCP, resulting in further ionization and atom loss. The existence of a plasma was evidenced by an ionization threshold and the formation of long-lived high angular momentum Rydberg states. At high density, there is a cross-over to a Coulomb blockade region, where the DC Stark shift from neighbouring ions is large enough to shift nearby atoms out of resonance with the excitation laser. The growth in the ion density with atom number therefore becomes self-limiting.

A key consequence of these results is that careful consideration of the relative sign of the van der Waals interaction and the DC Stark shift is essential in order to minimize charge induced losses in Rydberg dressing experiments. The success of this approach is shown in [28], where the choice of the appropriate Rydberg state led to a significant increase in lifetime.

More interestingly, the quantitative agreement between our model and the experimental data opens the possibility of tailoring the spatial correlation function of Rydberg atoms and ions in the cloud via the Coulomb blockade and anti-blockade mechanisms. Divalent atoms offer a powerful toolkit of techniques such as autoionization [9, 36] and ion imaging [48, 57] that can be used to study these correlations, which may offer new routes to the suppression of disorder-induced heating in plasmas [13]. Coulomb anti-blockade may also be useful to Rydberg-based focused ion beam experiments e.g. [58], enabling higher Rydberg excitation/ion production rates than are allowed due to Rydberg blockade, whilst suppressing disorder-induced heating.

Acknowledgments

Financial support was provided by EPSRC Grant No. EP/J007021. This project has also received funding from the European Union's Seventh Framework (Grant Agreement No. 612862-HAIRS) and Horizon 2020 (Grant Agreements No. 660028-EXTRYG and No. 640378- RYSQ) research and innovation programmes. The data presented in this paper are available for download¹.

ORCID iDs

R K Hanley (https://orcid.org/0000-0001-8373-1025

References

- Tomza M, Jachymski K, Gerritsma R, Negretti A, Calarco T, Idziaszek Z and Julienne P 2019 Cold hybrid ion-atom systems arXiv:1708. 07832
- [2] Wang L, Deiß M, Raithel G and Denschlag J H 2019 Controlling cold atom-ion collisions using a Rydberg state arXiv:1901.08781
- [3] Schmid T, Veit C, Zuber N, Löw R, Pfau T, Tarana M and Tomza M 2018 Rydberg molecules for ion-atom scattering in the ultracold regime Phys. Rev. Lett. 120 153401
- [4] Ewald N V, Feldker T, Hirzler H, Fürst H and Gerritsma R 2018 Observation of interactions between trapped ions and ultracold Rydberg atoms arXiv:1809.03987
- [5] Mukherjee R 2019 Charge dynamics of a molecular ion immersed in a Rydberg-dressed atomic lattice gas arXiv:1901.06288
- [6] Engel F, Dieterle T, Schmid T, Tomschitz C, Veit C, Zuber N, Löw R, Pfau T and Meinert F 2018 Observation of rydberg blockade induced by a single ion *Phys. Rev. Lett.* **121** 193401
- [7] Vitrant G, Raimond J M, Gross M and Haroche S 1982 Rydberg to plasma evolution in a dense gas of very excited atoms J. Phys. B: At. Mol. Phys. 15 L49
- [8] Robinson M P, Tolra B L, Noel M W, Gallagher T F and Pillet P 2000 Spontaneous evolution of Rydberg atoms into an ultracold plasma Phys. Rev. Lett. 85 4466–9
- [9] Millen J, Lochead G and Jones M P A 2010 Two-electron excitation of an interacting cold Rydberg gas *Phys. Rev. Lett.* **105** 213004
- [10] Robert-de Saint-Vincent M, Hofmann CS, Schempp H, Günter G, Whitlock S and Weidemüller M 2013 Spontaneous avalanche ionization of a strongly blockaded Rydberg gas Phys. Rev. Lett. 110 045004

¹ 10.15128/r1vh53wv77q

- [11] Weber T M, Niederprüm T, Manthey T, Langer P, Guarrera V, Barontini G and Ott H 2012 Continuous coupling of ultracold atoms to an ionic plasma via Rydberg excitation *Phys. Rev. A* 86 020702
- [12] Amthor T, Giese C, Hofmann C S and Weidemüller M 2010 Evidence of antiblockade in an ultracold Rydberg gas Phys. Rev. Lett. 104 013001
- [13] Bannasch G, Killian T C and Pohl T 2013 Strongly coupled plasmas via Rydberg blockade of cold atoms Phys. Rev. Lett. 110 253003
- [14] Santos L, Shlyapnikov G V, Zoller P and Lewenstein M 2000 Bose–Einstein condensation in trapped dipolar gases Phys. Rev. Lett. 85 1791–4
- [15] Bouchoule I and Mølmer K 2002 Spin squeezing of atoms by the dipole interaction in virtually excited Rydberg states Phys. Rev. A 65 041803
- [16] Johnson J E and Rolston S L 2010 Interactions between Rydberg-dressed atoms *Phys. Rev.* A 82 033412
- [17] Henkel N, Nath R and Pohl T 2010 Three-dimensional roton excitations and supersolid formation in Rydberg-excited Bose–Einstein condensates Phys. Rev. Lett. 104 195302
- [18] Pupillo G, Micheli A, Boninsegni M, Lesanovsky I and Zoller P 2010 Strongly correlated gases of Rydberg-dressed atoms: quantum and classical dynamics Phys. Rev. Lett. 104 223002
- [19] Honer J, Weimer H, Pfau T and Büchler H P 2010 Collective many-body interaction in Rydberg dressed atoms Phys. Rev. Lett. 105 160404
- [20] Glaetzle A W, Nath R, Zhao B, Pupillo G and Zoller P 2012 Driven-dissipative dynamics of a strongly interacting Rydberg gas Phys. Rev. A 86 043403
- [21] Jau Y-Y, Hankin A M, Keating T, Deutsch I H and Biedermann G W 2015 Entangling atomic spins with a Rydberg-dressed spin-flip blockade *Nat. Phys.* **12**71
- [22] Zeiher J, van Bijnen R, Schauß P, Hild S, Choi J-Y, Pohl T, Bloch I and Gross C 2016 Many-body interferometry of a Rydberg-dressed spin lattice Nat. Phys. 12 1095–9
- [23] Zeiher J, Choi J-y, Rubio-Abadal A, Pohl T, van Bijnen R, Bloch I and Gross C 2017 Coherent many-body spin dynamics in a longrange interacting ising chain Phys. Rev. X 7 041063
- [24] Aman J A, DeSalvo B J, Dunning F B, Killian T C, Yoshida S and Burgdörfer J 2016 Trap losses induced by near-resonant Rydberg dressing of cold atomic gases *Phys. Rev. A* 93 043425
- [25] Goldschmidt E A, Boulier T, Brown R C, Koller S B, Young J T, Gorshkov A V, Rolston S L and Porto J V 2016 Anomalous broadening in driven dissipative Rydberg systems *Phys. Rev. Lett.* 116 113001
- [26] Helmrich S, Arias A and Whitlock S 2018 Uncovering the nonequilibrium phase structure of an open quantum spin system Phys. Rev. A 98 022109
- [27] Boulier T, Magnan E, Bracamontes C, Maslek J, Goldschmidt E A, Young J T, Gorshkov A V, Rolston S L and Porto J V 2017 Spontaneous avalanche dephasing in large Rydberg ensembles *Phys. Rev.* A 96 053409
- [28] Bounds A D, Jackson N C, Hanley R K, Faoro R, Bridge E M, Huillery P and Jones M P A 2018 Rydberg-dressed magneto-optical trap Phys. Rev. Lett. 120 183401
- [29] Secker T, Ewald N, Joger J, Fürst H, Feldker T and Gerritsma R 2017 Trapped ions in Rydberg-dressed atomic gases Phys. Rev. Lett. 118 263201
- [30] Boddy D 2014 First observations of Rydberg blockade in a frozen gas of divalent atoms PhD Thesis Durham University
- [31] Sadler D 2016 Many-body interactions in a dissipative frozen strontium Rydberg gas PhD Thesis Durham University
- [32] Alistair Bounds A 2018 Rydberg-dressed magneto optical trap PhD Thesis Durham University
- [33] Bridge E M, Keegan N C, Bounds A D, Boddy D, Sadler D P and Jones M P A 2016 Tunable cw UV laser with <35 kHz absolute frequency instability for precision spectroscopy of Sr Rydberg states Opt. Express 24 2281–92
- [34] Beterov I I, Tretyakov D B, Ryabtsev I I, Entin V M, Ekers A and Bezuglov N N 2009 Ionization of Rydberg atoms by blackbody radiation *New J. Phys.* 11 013052
- [35] Amthor T, Reetz-Lamour M, Giese C and Weidemüller M 2007 Modeling many-particle mechanical effects of an interacting Rydberg gas Phys. Rev. A 76 054702
- [36] Lochead G, Boddy D, Sadler D P, Adams C S and Jones M P A 2013 Number-resolved imaging of excited-state atoms using a scanning autoionization microscope Phys. Rev. A 87 053409
- [37] Mandel L 1979 Sub-poissonian photon statistics in resonance fluorescence Opt. Lett. 4 205-7
- [38] Malossi N, Valado M M, Scotto S, Morsch O, Arimondo E and Ciampini D 2014 Strongly correlated excitation of a quasi-1d Rydberg gas J. Phys.: Conf. Ser. 497 012031
- [39] Viteau M, Huillery P, Bason MG, Malossi N, Ciampini D, Morsch O, Arimondo E, Comparat D and Pillet P 2012 Cooperative excitation and many-body interactions in a cold rydberg gas Phys. Rev. Lett. 109 053002
- [40] Vaillant C L, Jones M P A and Potvliege R M 2012 Long-range Rydberg–Rydberg interactions in calcium, strontium and ytterbium J. Phys. B: At. Mol. Opt. Phys. 45 135004
- [41] Ates C, Pohl T, Pattard T and Rost J M 2007 Antiblockade in Rydberg excitation of an ultracold lattice gas Phys. Rev. Lett. 98 023002
- [42] Malossi N, Valado M M, Scotto S, Huillery P, Pillet P, Ciampini D, Arimondo E and Morsch O 2014 Full counting statistics and phase diagram of a dissipative Rydberg gas *Phys. Rev. Lett.* 113 023006
- [43] Urvoy A, Ripka F, Lesanovsky I, Booth D, Shaffer J P, Pfau T and Löw R 2015 Strongly correlated growth of Rydberg aggregates in a vapor cell *Phys. Rev. Lett.* 114 203002
- [44] Simonelli C, Valado M M, Masella G, Asteria L, Arimondo E, Ciampini D and Morsch O 2016 Seeded excitation avalanches in offresonantly driven Rydberg gases J. Phys. B: At. Mol. Opt. Phys. 49 154002
- [45] Killian T C, Kulin S, Bergeson S D, Orozco L A, Orzel C and Rolston S L 1999 Creation of an ultracold neutral plasma Phys. Rev. Lett. 83 4776–9
- [46] Wenhui Li et al 2004 Evolution dynamics of a dense frozen Rydberg gas to plasma Phys. Rev. A 70 042713
- [47] Murillo M S 2001 Using fermi statistics to create strongly coupled ion plasmas in atom traps Phys. Rev. Lett. 87 115003
- [48] Simien C E, Chen Y C, Gupta P, Laha S, Martinez Y N, Mickelson P G, Nagel S B and Killian T C 2004 Using absorption imaging to study ion dynamics in an ultracold neutral plasma Phys. Rev. Lett. 92 143001
- [49] Kulin S, Killian T C, Bergeson S D and Rolston S L 2000 Plasma oscillations and expansion of an ultracold neutral plasma Phys. Rev. Lett. 85 318–21
- [50] Dutta S K, Feldbaum D, Walz-Flannigan A, Guest J R and Raithel G 2001 High-angular-momentum states in cold Rydberg gases Phys. Rev. Lett. 86 3993–6
- [51] Siercke M, Oon F E, Mohan A, Wang Z W, Lim M J and Dumke R 2014 Density dependence of the ionization avalanche in ultracold Rydberg gases Phys. Rev. A 89 022701

- [52] Weller D, Shaffer J, Pfau T, L"ow R and K"ubler H 2019 The interplay between thermal Rydberg gases and plasmasarXiv: 1901.07850
- [53] Loftus T H, Ido T, Boyd M M, Ludlow A D and Ye J 2004 Narrow line cooling and momentum-space crystals Phys. Rev. A 70 063413
- [54] Reinhard A, Cubel Liebisch T, Younge K C, Berman P R and Raithel G 2008 Rydberg–Rydberg collisions: resonant enhancement of state mixing and penning ionization *Phys. Rev. Lett.* **100** 123007
- [55] Viteau M, Chotia A, Comparat D, Tate D A, Gallagher T F and Pillet P 2008 Melting a frozen Rydberg gas with an attractive potential Phys. Rev. A 78 040704
- [56] Killian T C, Lim M J, Kulin S, Dumke R, Bergeson S D and Rolston S L 2001 Formation of Rydberg atoms in an expanding ultracold neutral plasma Phys. Rev. Lett. 86 3759–62
- [57] McQuillen P, Zhang X, Strickler T, Dunning F B and Killian T C 2013 Imaging the evolution of an ultracold strontium Rydberg gas Phys. Rev. A 87 013407
- [58] Murphy D, Scholten R E and Sparkes B M 2015 Increasing the brightness of cold ion beams by suppressing disorder-induced heating with Rydberg blockade Phys. Rev. Lett. 115 214802