



On the Prospect of Using the Maximum Circular Velocity of Halos to Encapsulate Assembly Bias in the Galaxy–Halo Connection

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Abstract

We investigate a conceptual modification of the halo occupation distribution approach, using the halos’ present-day maximal circular velocity, V_{\max} , as an alternative to halo mass. In particular, using a semianalytic galaxy formation model applied to the Millennium WMAP7 simulation, we explore the extent that switching to V_{\max} as the primary halo property incorporates the effects of assembly bias into the formalism. We consider fixed number density galaxy samples ranked by stellar mass and examine the variations in the halo occupation functions with either halo concentration or formation time. We find that using V_{\max} results in a significant reduction in the occupancy variation of the central galaxies, particularly for concentration. The satellites’ occupancy variation on the other hand increases in all cases. We find effectively no change in the halo clustering dependence on concentration, for fixed bins of V_{\max} compared to fixed halo mass. Most crucially, we calculate the impact of assembly bias on galaxy clustering by comparing the amplitude of clustering to that of a shuffled galaxy sample, finding that the level of galaxy assembly bias remains largely unchanged. Our results suggest that while using V_{\max} as a proxy for halo mass diminishes some of the occupancy variations exhibited in the galaxy–halo relation, it is not able to encapsulate the effects of assembly bias potentially present in galaxy clustering. The use of other more complex halo properties, such as V_{peak} , the peak value of V_{\max} over the assembly history, provides some improvement and warrants further investigation.

Unified Astronomy Thesaurus concepts: [Cosmology \(343\)](#); [Galaxies \(573\)](#); [Large-scale structure of the universe \(902\)](#); [Clustering \(1908\)](#); [Observational cosmology \(1146\)](#); [Galaxy evolution \(594\)](#); [Galaxy dark matter halos \(1880\)](#); [Cold dark matter \(265\)](#); [Cosmological models \(337\)](#); [Galaxy formation \(595\)](#); [N-body simulations \(1083\)](#); [Astrostatistics \(1882\)](#)

1. Introduction

In the standard cosmological framework, galaxies form, evolve, and reside in dark matter halos. It is of fundamental importance to understand the relation between galaxies and dark matter halos. How do the galaxies populate the halos? How do the properties of galaxies depend on halo mass or other characteristics of the halos? What role does the environment have in the halo occupation? These questions lie at the core of our understanding of galaxy formation. They are also crucial if we are to take full advantage of the next generation of galaxy surveys aimed at measuring galaxy clustering with unparalleled accuracy. The cosmological constraints from these data will no longer be dominated by statistical errors but rather the accuracy of our theoretical models. Understanding how galaxies relate to the underlying dark matter is thus essential for optimally using galaxies as a cosmological probe.

The formation and evolution of the dark matter halos is dominated by gravity and can be predicted accurately using high-resolution cosmological numerical simulations and analytic models. The formation of the galaxies and their relation to the dark matter halos, however, is more complex and depends on the detailed physical processes leading to the varied observed galaxy properties. Studying in detail the galaxy–halo connection is therefore of paramount importance (see Wechsler & Tinker 2018 for a review).

A powerful approach to explore galaxy formation within dark matter halos is semianalytic modeling (SAM; e.g.,

Cole et al. 1994, 2000; Benson et al. 2003; Baugh 2006; Bower et al. 2006; Croton et al. 2006; Somerville et al. 2008). In such models, halos identified from high-resolution N -body simulations are “populated” with galaxies using analytical prescriptions for the evolution of baryons through cosmic time. These models have been successful in reproducing many measured properties including the galaxy luminosity and stellar mass functions (see, e.g., Bower et al. 2006; Croton et al. 2006; Fontanot et al. 2009; Guo et al. 2011, 2013; Henriques et al. 2015; Lagos et al. 2018; Baugh et al. 2019).

Alternatively, hydrodynamic simulations follow the physical processes which govern the behavior of baryons by solving the fluid equations, while also modeling some of the unresolved processes with subgrid prescriptions (see, e.g., Somerville & Davé 2015). Cosmological hydrodynamical simulations have started to play a major role in the study of galaxy formation and evolution. Two recent efforts, the Illustris Project (Vogelsberger et al. 2014; Pillepich et al. 2018) and the EAGLE simulation (Schaye et al. 2015), have set the state-of-the-art in hydrodynamical calculations. These ambitious simulations are still, however, significantly smaller than large-scale structure dark-matter-only simulations and harder to fine-tune to the observations.

A useful approach to empirically connect galaxies with dark matter halos is the halo occupation distribution (HOD) framework (e.g., Jing et al. 1998; Benson et al. 2000; Peacock & Smith 2000; Seljak 2000; Scoccimarro et al. 2001; Berlind & Weinberg 2002; Cooray & Sheth 2002; Berlind et al. 2003;

Yang et al. 2003; Kravtsov et al. 2004; Zheng et al. 2005). The HOD formalism characterizes the relationship between galaxies and halos in terms of the probability distribution, $P(N|M_{\text{vir}})$, that a halo of virial mass M_{vir} contains N galaxies of a given type, together with the spatial and velocity distributions of galaxies inside halos. The key ingredient is the halo occupation function, $\langle N(M_{\text{vir}}) \rangle$, representing the average number of galaxies as a function of halo mass. The advantage of this approach is that it does not rely on assumptions about the (poorly understood) physical processes that drive galaxy formation and can be directly constrained from the observations.

When considering the halo occupation function it is often useful to separate the contribution of central galaxies, namely the main galaxy at the center of the halo, and that of the additional satellite galaxies that populate the halo (Kravtsov et al. 2004; Zheng et al. 2005; Jimenez et al. 2019). Standard applications assume a cosmology and a parameterized form for the halo occupation functions motivated by predictions of SAMs and hydrodynamic simulations (e.g., Zheng et al. 2005). The HOD parameters are then constrained using galaxy clustering measurements from large surveys, the galaxies abundance and the predicted halo clustering. The approach has been demonstrated to be a powerful theoretical tool to study the galaxy–halo connection, transforming clustering measurements into a physical relation between galaxies and dark matter halos. It has been successful in explaining the shape of the galaxy correlation function, its dependence on galaxy properties and environmental dependence (e.g., Zehavi et al. 2004, 2005, 2011; Berlind et al. 2005; Abbas & Sheth 2006; Skibba et al. 2006; Tinker et al. 2008; Coupon et al. 2012). It has also become an increasingly popular method to create realistic mock catalogs, by populating halos in large N -body simulations (e.g., Manera et al. 2015; Zheng & Guo 2016; Smith et al. 2017; DeRose et al. 2019), important for planning and analysis of current and upcoming surveys.

A central assumption in the standard applications of the HOD framework is that the galaxy content of halos depends only on the host halo mass. The origins of this assumption is in the Press–Schechter formalism (Press & Schechter 1974; Lacey & Cole 1993) and the uncorrelated nature of random walks describing halo assembly, resulting in a correlation of the halo environment with its mass but not with its assembly history (Bond et al. 1991, Lemson & Kauffmann 1999, White 1999). This assumption has been challenged by explicitly demonstrating in large N -body simulations that the clustering of halos varies with halo formation time, concentration, substructure occupation, and spin, at fixed halo mass (Sheth & Tormen 2004; Gao et al. 2005; Wechsler et al. 2006; Gao & White 2007; Jing et al. 2007; Wetzel et al. 2007; Lazeyras et al. 2017; Salcedo et al. 2018; Sato-Polito et al. 2019), an effect that has been generally referred to as “halo assembly bias.”

To what extent is the galaxy distribution impacted by the assembly bias of their host halos is an actively debated topic. If galaxy properties closely correlate with halo formation history this would lead to a dependence of the galaxy content on large-scale environment and a corresponding change in the amplitude of galaxy clustering on large scales. The latter is commonly referred to as “galaxy assembly bias” (a misnomer referring to the manifestation of halo assembly bias in the galaxy distribution; GAB hereafter). The predictions for GAB have been explored with simulated galaxies (e.g., Zhu et al. 2006; Croton et al. 2007; Zu et al. 2008; Zentner et al. 2014;

Chaves-Montero et al. 2016; Romano-Diaz et al. 2017; Xu & Zheng 2019), while the observational evidence for it remains inconclusive and controversial. Several suggestive detections have been put forward (Cooper et al. 2010; Wang et al. 2013; Lacerna et al. 2014a; Hearin et al. 2015; Watson et al. 2015; Miyatake et al. 2016; Montero-Dorta et al. 2017) while other studies indicate the impact of assembly bias is small (Abbas & Sheth 2006; Blanton & Berlind 2007; Tinker et al. 2008; Lacerna et al. 2014b; Lin et al. 2016; Zu & Mandelbaum 2016; Walsh & Tinker 2019) and that previous claimed detections are due to systematics (e.g., Campbell et al. 2015; Sin et al. 2017; Tinker et al. 2017; Zu et al. 2017; Sunayama & More 2019).

If significant, GAB can have direct implications for interpreting galaxy clustering using the HOD framework (Pujol & Gaztanaga 2014; Zentner et al. 2014). The presence of GAB implies a dependence of the halo occupation functions on the secondary halo parameters in addition to mass. This “occupancy variation,” namely the dependence of the galaxy content of halos on additional halo parameters, provides a crucial direct link between halo assembly bias and GAB (Zehavi et al. 2018; Z18 hereafter). Both halo assembly bias and occupancy variation are required to produce GAB.

Z18 explore the predicted occupancy variation in SAMs applied to the Millennium simulation, focusing on the dependence of the galaxy content of halos on large-scale environment and on halo formation time. They find distinct occupancy variations with central galaxies in denser regions preferentially occupying lower-mass halos. A similar, but significantly stronger, trend is found with halo age, where early formed halos are more likely to host central galaxies at lower halo mass. A reverse trend is seen for the occupation of satellites, with early forming halos having fewer satellites. They also examine the overall impact on galaxy clustering (i.e., the GAB signature) in these samples, arising from the combined effect of halo assembly bias and the occupancy variations.

To gain insight on the origin of the occupancy variations, Z18 also investigate the stellar mass–halo mass relation for central galaxies in the SAM, finding a distinct dependence on secondary halo properties, e.g., at fixed halo mass, older halos tend to host more massive galaxies, which drive the centrals occupancy variation. We stress that it is not the amount of scatter, but rather the trends within the scatter as a function of secondary halo properties that cause the occupancy variations. Similar results for the occupancy variation and the dependences of the stellar mass–halo mass relation have also been shown with the cosmological hydrodynamical simulations EAGLE, Illustris, and IllustrisTNG (Artale et al. 2018; Bose et al. 2019).

Similar results are also found when examining the dependence on halo concentration (Contreras et al. 2019, hereafter C19). C19 extend the work of Z18 to study the cosmic evolution of assembly bias and occupancy variation in the Guo et al. (2013) SAM. They explore the redshift range between 0 and 3, considering galaxy samples selected by either stellar mass or star formation rate (SFR), and selecting halos by both halo formation time and halo concentration. At the present epoch, both halo concentration and halo formation time produce similar features when examining either halo clustering or the occupancy variation. However, these two halo properties exhibit different evolutionary scenarios. The GAB signature monotonically decreases when going to higher redshift (and for lower number density samples), reversing its sense in some instances.

Building on the work of Z18 and C19, we set out here to explore a conceptual modification of the HOD approach which shifts from halo mass to an alternative proxy, aimed at encapsulating assembly bias in the galaxy–halo connection. In searching for this proxy, we draw upon abundance matching techniques (e.g., Conroy et al. 2006; Reddick et al. 2013; Chaves-Montero et al. 2016; Lehmann et al. 2017). Such methods typically associate dark matter (sub)halos with galaxies using a monotonic relation between a galaxy property (such as stellar mass or luminosity) and a halo property like its infall halo mass, its maximum circular velocity, V_{\max} , or the peak value of V_{\max} across the assembly of the halo, V_{peak} . These are expected to have a tighter relation with the galaxy properties compared to the virial mass of the halo, M_{vir} .

Given the distinct trends with concentration (or halo age) in the galaxy–halo connection mentioned above and their crucial role in producing the occupancy variations (Z18), we choose V_{\max} as the alternate halo property. V_{\max} , the maximal value of the circular velocity inferred from the halo mass distribution, effectively characterizes the gravitational potential and is closely related to halo concentration. Using the Guo et al. (2013) SAM applied to the Millennium WMAP7 simulation, we explore the extent to which switching from virial mass to the halo’s maximum circular velocity in the HOD is able to encapsulate the main features of assembly bias. We consider all three aspects of this phenomenon: occupancy variation, GAB, and halo assembly bias. While some aspects are certainly improved, we find (spoiler alert) that, regrettably, V_{\max} is unable to “capture” the essence of assembly bias and improve upon the use of M_{vir} in measuring GAB. Still, we think it is useful and educational to go through this exercise.

The overall motivation and potential applications of this work are many. First, we can obtain further insight into assembly bias and on how best to capture its essential features. Beyond the increased theoretical understanding of this complex phenomenon, had this conceptual change to the HOD successfully encapsulated assembly bias, it would have provided varied practical applications. The modified HOD could then have been utilized as an efficient tool for creating mock catalogs from simulations, which would reproduce realistic galaxy clustering while incorporating assembly bias. Moreover, it could have potentially been invaluable for inferring the galaxy–halo connection from galaxy clustering free of the effects of assembly bias.

The outline of the rest of the paper is as follows. Section 2 describes the galaxy samples we use. In Section 3 we present the occupancy variation with halo concentration and age when using V_{\max} instead of halo mass. In Section 4 we examine the relation between stellar mass and the different halo properties. Section 5 presents our results for GAB, and we conclude in Section 6. Appendix A investigates halo assembly bias with V_{\max} . Appendix B includes additional results for SFR-selected samples and samples at higher redshift. Finally, Appendix C shows some results when alternatively using V_{peak} .

2. The Galaxy Samples

2.1. Simulation and Galaxy Formation Model

We use the Millennium WMAP7 N -body simulation (Guo et al. 2013), which is similar to the original Millennium simulation (Springel et al. 2005) but with cosmological parameters consistent with the seven year WMAP data

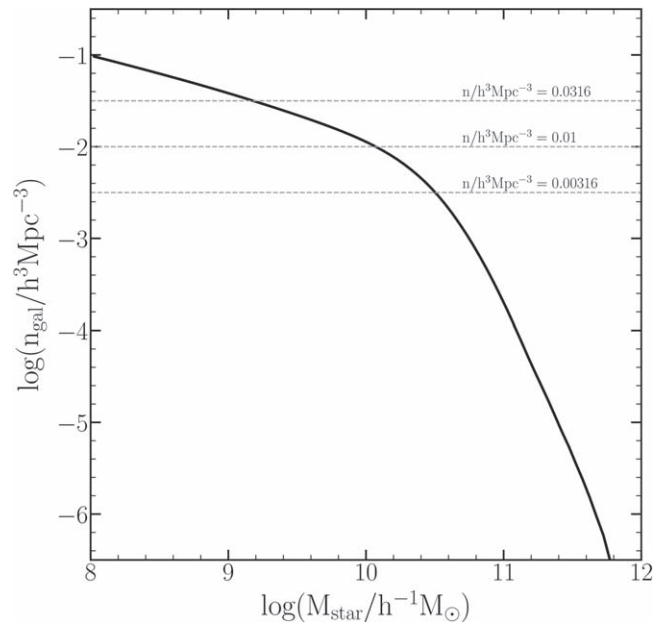


Figure 1. Cumulative stellar mass function predicted by the Guo et al. (2013) SAM. The dashed horizontal lines indicate the number densities of the samples used in this work.

(Komatsu et al. 2011). The simulation has a comoving boxsize of $500 h^{-1} \text{Mpc}$ on a side and follows 2160^3 particles with a mass resolution of $9.36 \times 10^8 h^{-1} M_{\odot}$. Multiple outputs of the simulation are available at different snapshots from redshift 50 to the present day. At each snapshot, halos are identified using a friends-of-friends algorithm (Davis et al. 1985), and SUBFIND (Springerl et al. 2001) is then run on these to identify subhalos. Halo merger trees are constructed by following the evolution of the halos and subhalos with time.

Semianalytic modeling is a fundamental methodology to model the evolution of baryons over cosmic time in a cosmological context (see, e.g., Baugh 2006; Lacey et al. 2016). SAMs aim to model the main physical processes involved in galaxy formation and evolution, grafted onto a halo merger tree. Some of these processes include gas cooling, star formation, feedback from supernovae and active galactic nuclei, chemical enrichment, dark matter halo mergers, and galaxy mergers. The SAM used in our work is that of Guo et al. (2013), which is a version of the L-GALAXIES SAM code of the Munich group, based on Guo et al. (2011) and applied to the Millennium WMAP7 simulation. It is publicly available from the Millennium Archive.⁶

For the main part of our analysis we use galaxy samples with different number densities, ranked by the stellar mass of the galaxies. We use three number densities, 0.0316, 0.01, and $0.00316 h^3 \text{Mpc}^{-3}$, corresponding to stellar mass thresholds of $\sim 1.6 \times 10^9$, 1.2×10^{10} , and $3.4 \times 10^{10} h^{-1} M_{\odot}$, respectively. The samples are approximately evenly spaced in logarithmic number density, and follow the choices made in Z18. Figure 1 shows the cumulative stellar mass function and the three number density cuts used. The galaxies selected in each case are those to the right of the intersection with the corresponding horizontal line. Pertinent results for galaxy samples selected by ranked SFR are shown in Appendix B.

⁶ <http://gavo.mpa-garching.mpg.de/Millennium/>

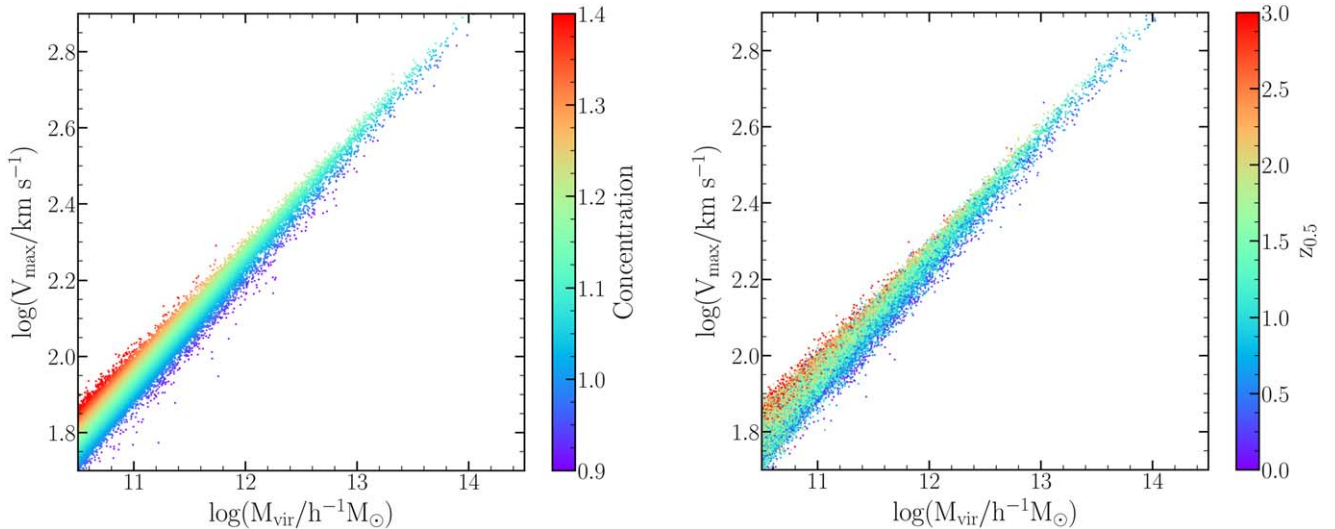


Figure 2. Relation between V_{\max} and M_{vir} , color coded by halo concentration (left) and by halo formation time (right). For clarity and to avoid overcrowding, we plot only 1% of the halos randomly chosen and ordered.

2.2. Halo Properties

We consider as the mass of the halo the virial mass, namely the mass enclosed within the virial radius of the halo corresponding to a density of 200 times the critical density of the universe. This choice, which we denote here as M_{vir} , is largely a matter of convention but has been shown to roughly correspond to the boundary at which halos are in approximate dynamical equilibrium (e.g., Cole & Lacey 1996). We hereafter interchangeably refer to M_{vir} as the halo mass (but see Jiang et al. 2014 for an alternate mass definition). The circular velocity profiles of the halos obtained from the dark matter distribution, $V_c^2 = GM(r)/r$, have a well defined maximum, which serves as a natural halo size scale denoted as V_{\max} . This quantity is robustly defined for simulated halos and effectively characterizes the depth of the gravitational potential (e.g., Bullock et al. 2001; Conroy et al. 2006; Diemand & Moore 2011). We consider here in detail the use of V_{\max} as a proxy for halo mass.

For the secondary parameters, we use the halo concentration and halo formation time, following C19. These are regarded as two fundamental parameters related to the halo assembly often used in assembly bias studies (e.g., Gao et al. 2005; Wechsler et al. 2006; Gao & White 2007; Mao et al. 2018; C19; Bose et al. 2019). The halo concentration characterizes the density profile. It is canonically defined as $C_{\text{vir}} = r_{\text{vir}}/r_s$, where r_{vir} is the virial radius of the halo and r_s is the inner transitional radius appearing in the Navarro et al. (1996) profile, at which the density profile changes slope. It is often alternatively defined as the ratio between V_{\max} and V_{vir} , where V_{vir} is the virial velocity of the halo, $V_{\text{vir}} \equiv V_c(r_{\text{vir}})$. We use the latter definition here, which is directly calculable from simulation data and does not require any model fitting, and can be applied to the lowest-mass halos considered, which might have too few particles to fit a density profile (Bullock et al. 2001; Gao & White 2007; Diemand & Moore 2011).

The formation time of the halo is defined as the redshift at which the main progenitor of the halo first reaches half of its current mass, denoted as $z_{0.5}$. We calculate it from the halo merger trees of the simulation, linearly interpolating the halo mass among the time snapshots available. This definition has been very commonly used in assembly bias studies (e.g., Gao et al. 2005; Croton et al. 2007; Gao & White 2007; Z18;

Han et al. 2019). As we use the halo formation time simply to rank the halos as early forming or late forming we do not anticipate any dependence on the specific definition (however, see the study of Li et al. 2008).

Figure 2 shows the relation between V_{\max} and M_{vir} for the halos in the simulation, color coded either by halo concentration or formation time. We plot only 1% of the halos, randomly chosen and ordered, to avoid overcrowding. As expected, there is a tight relation between the two, with the scatter arising distinctly from the differences in concentration. For fixed halo mass, V_{\max} is directly related to the concentration (by definition), with more concentrated halos corresponding to larger V_{\max} . A similar relation is noted when color coding the halos by formation time, albeit with some scatter in the dependence on halo age, which arises from the scatter between concentration and halo age.

3. Occupancy Variations

We now proceed to examine the halo occupation functions and their variations with halo concentration and age. For each of these properties, we rank the halos by the secondary property in narrow (0.1 dex) bins of halo mass and identify the 20% extremes of the distribution. This factors out the halo mass dependence on these parameters and allows us to examine the occupancy variations for halos of the same mass. We also do the same for fine (0.04 dex) bins in V_{\max} . We have verified for both cases that our results are insensitive to the exact binning choice. Given the tight relation between M_{vir} and V_{\max} there is significant overlap between the identification binned by either mass proxy.

Figure 3 presents the halo occupation functions for the $n = 0.01 h^3 \text{Mpc}^{-3}$ galaxy sample and their variation with concentration. The left-hand side shows the “standard” occupation functions as a function of halo mass. We see that more concentrated halos start hosting central galaxies at lower halo mass, while they host on average fewer satellites per halo. These are in full agreement with previous results explored in detail by Z18 and C19. The uncertainties on the occupation functions, estimated from jackknife resampling, are negligible over the range of halo masses plotted here, and hence they are not included. (They only start becoming noticeable for masses

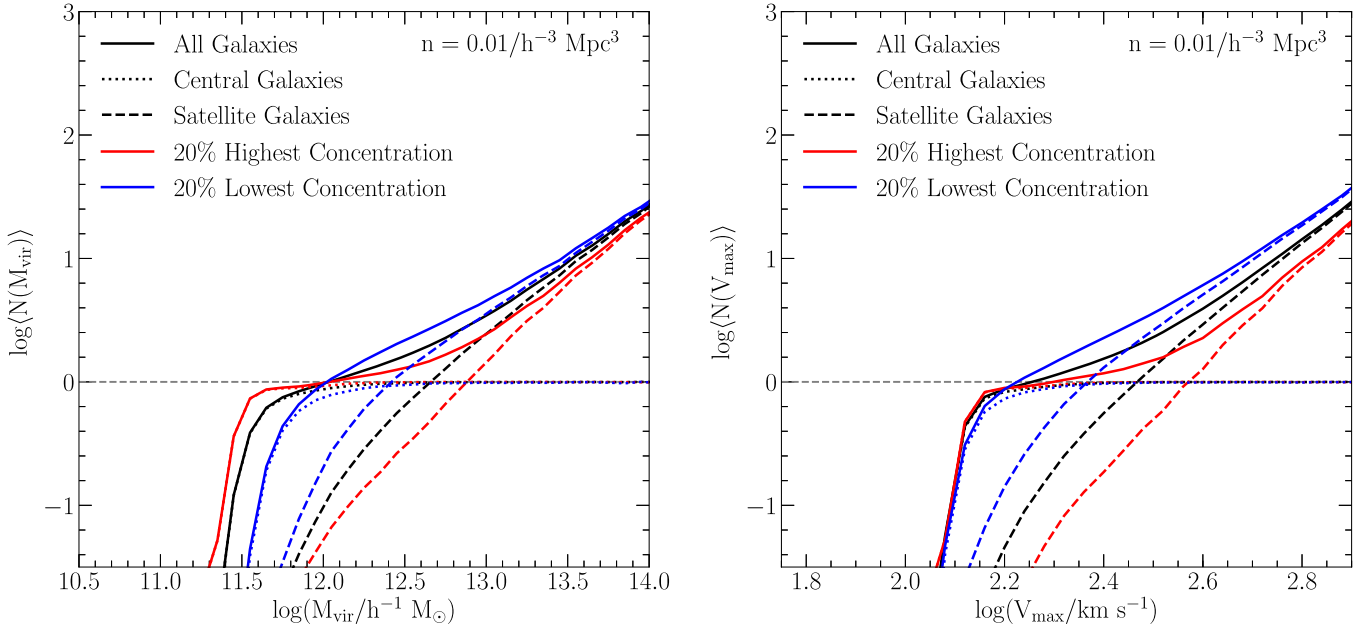


Figure 3. Halo occupation functions for the $n = 0.01 h^3 \text{ Mpc}^{-3}$ galaxy sample, for the full galaxy sample (black), for the galaxies in the 20% most concentrated halos (red), and 20% least concentrated halos (blue). The occupation functions are shown as a function of M_{vir} on the left and V_{max} on the right.

larger than $\sim 10^{14} h^{-1} M_{\odot}$ where there are very few halos; see e.g., Figure 3 of Z18 or Figure 5 of C19.)

The right-hand panel of Figure 3 shows our new results for the halo occupations now using V_{max} as our proxy for halo mass. We see that the general shape of the HOD remains the same. However, there are significant changes to the occupancy variation of central galaxies and satellites. We find that the V_{max} occupancy variation for central galaxies is very nearly diminished in this case, with all halos, most concentrated ones and least concentrated halos exhibiting similar occupation by galaxies. In contrast, the V_{max} occupation functions for satellite galaxies exhibit larger differences, namely, an increased occupancy variation.

We also examine the differences in the occupancy variation for the other galaxy samples in Figure 4, finding some dependence on the number density, or rather stellar mass threshold, of the sample. For the lower number density (more massive galaxies; left-hand side) switching from M_{vir} to V_{max} only partially removes the centrals' occupancy variation, while it increases further the satellites' occupancy variation. While for the higher number density (less massive galaxies; right-hand side) the central occupancy variation is nearly over compensated by the switch to V_{max} , resulting in the least concentrated halos being occupied by central galaxies at slightly lower V_{max} than the most concentrated halos.

This change in behavior is not really unexpected and simply stems from the dependence of the (standard) occupancy variation with number density, as exhibited in the top panels of Figure 4 and studied in detail in Z18. The halo mass occupancy variation for both centrals and satellite galaxies increases with stellar mass (i.e., with decreased number density). Switching from M_{vir} to V_{max} amounts to a roughly constant shift in the mapping from M_{vir} to V_{max} , for the 20% least concentrated halos, as can be seen in Figure 2. This results in the slight over-compensation, nearly full compensation and partial compensation of the V_{max} occupancy variation, respectively, for the three cases with decreasing number density. Thus the nearly diminished V_{max} occupancy variation seen in Figure 3 is somewhat coincidental.

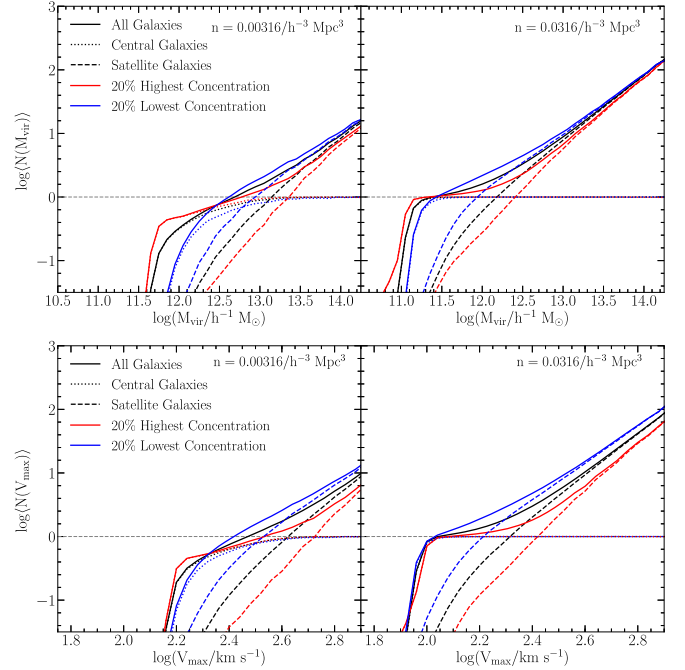


Figure 4. Same as in Figure 3, but for different number density samples, $n = 0.00316 h^3 \text{ Mpc}^{-3}$ (left) and $n = 0.0316 h^3 \text{ Mpc}^{-3}$ (right). The occupation functions with M_{vir} are shown on top and the ones with V_{max} on the bottom.

To get a sense of how general these results are, we explore the occupancy variations when switching to V_{max} also with regard to another fundamental halo parameter, the halo formation time. Figure 5 shows the occupation functions as a function of M_{vir} and V_{max} for the three galaxy samples, now for the 20% early formed halos and 20% late forming halos. When examining the standard HOD as a function of M_{vir} , we find the previously studied variations with age (Z18; C19), with older halos more likely to host central galaxies at lower mass and to have fewer satellites. When switching to V_{max} (bottom panels of Figure 5), the central galaxies' occupancy variation with respect to age is

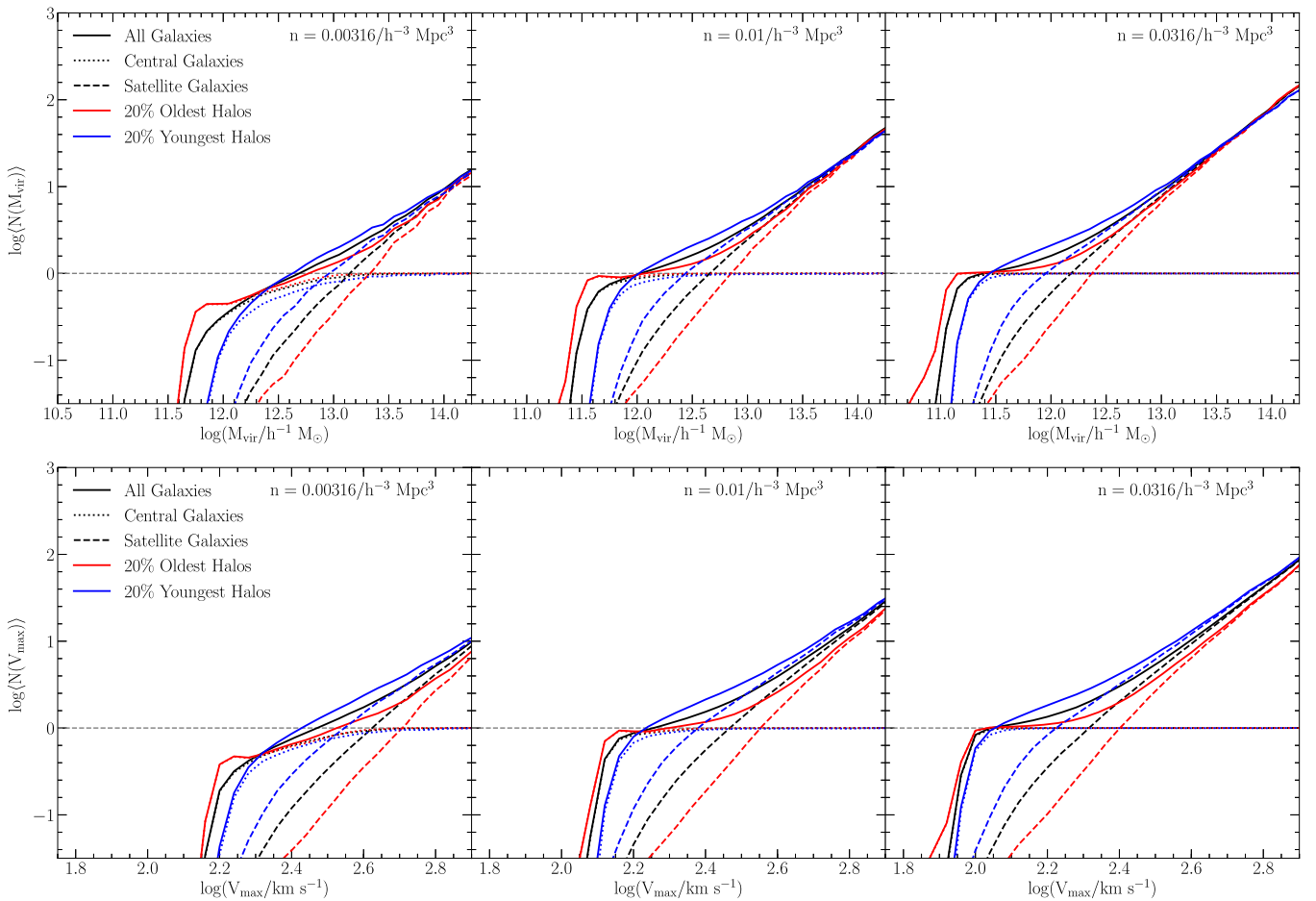


Figure 5. Same as Figures 3 and 4 but now for the occupancy variations with age, for all three number densities. The galaxies in the 20% oldest halos are shown in red, while the ones in the 20% youngest halos are shown in blue. The occupation functions with M_{vir} are shown on top and the ones with V_{max} on the bottom.

reduced, but only partially so, for all number densities. This partial reduction likely arises from the overall correlation between halo formation time and concentration, and hence V_{max} . This correlation of halo age with V_{max} is also seen in the right panel of Figure 2.

4. Relation between Galaxy and Halo Properties

The study of Z18 first showed that the key features of the occupancy variation for central galaxies stem from the dependence of their stellar mass on secondary halo properties at fixed halo mass. They examined the stellar mass–halo mass relation (see their Figure 9 and discussion in Section 4), finding that at fixed halo mass, more massive centrals tend to reside in older or denser halos. This dependence directly produces the changes in occupation we observe, while the level of scatter in these secondary trends controls the strength of the occupancy variation. Similar diagnostics were also utilized in other works such as Matthee et al. (2017), Tojeiro et al. (2017), Artale et al. (2018), and Xu & Zheng (2019).

We revisit this relation in the context of our work. The left panel of Figure 6 examines the relation between stellar mass and host halo mass for the central galaxies in the SAM, and the galaxies are color coded by the halo concentration. In an analogous fashion, we find here that at fixed halo mass, the more concentrated halos tend to host more massive central galaxies. The three horizontal lines mark the stellar mass thresholds used to define our samples. By examining the population of centrals above each threshold, we can visually see how the occupation

variations come about, including the galaxies in the most concentrated halos at lower halo mass and vice versa. The extent of the spread in the horizontal direction also directly correlates with the magnitude of the variations, producing larger variations for the higher stellar mass thresholds (lower number densities), as seen in Figures 3 and 4. We note, however, that the color coding by concentration here is done globally, while when defining the samples for the occupation functions, the 20% extremes are defined as a function of halo mass, so one should be careful when making the comparison.

The right panel of Figure 6 shows the relation between the stellar mass of the central galaxies and V_{max} of their host halos, once again color coded by concentration. The stellar mass– V_{max} relation has overall slightly less scatter, as expected (see Chaves-Montero et al. 2016; Matthee et al. 2017). In this case, we see a less-obvious trend with concentration. Examining the three cases separately (the three horizontal lines), we can obtain some intuition to understand the result for each sample. For the middle sample, there is a very mild trend with concentration. The top sample (lowest number density) has in fact a larger horizontal scatter and trend with concentration (after accounting for the different concentration markings noted above), causing the remaining occupancy variation shown in Figure 4. Going to the lowest stellar-mass threshold we in fact note that the trend reverses with the lower-concentration halos appearing at lower halo mass than the higher concentration ones. Our highest number density sample is just at the cusp of this change.

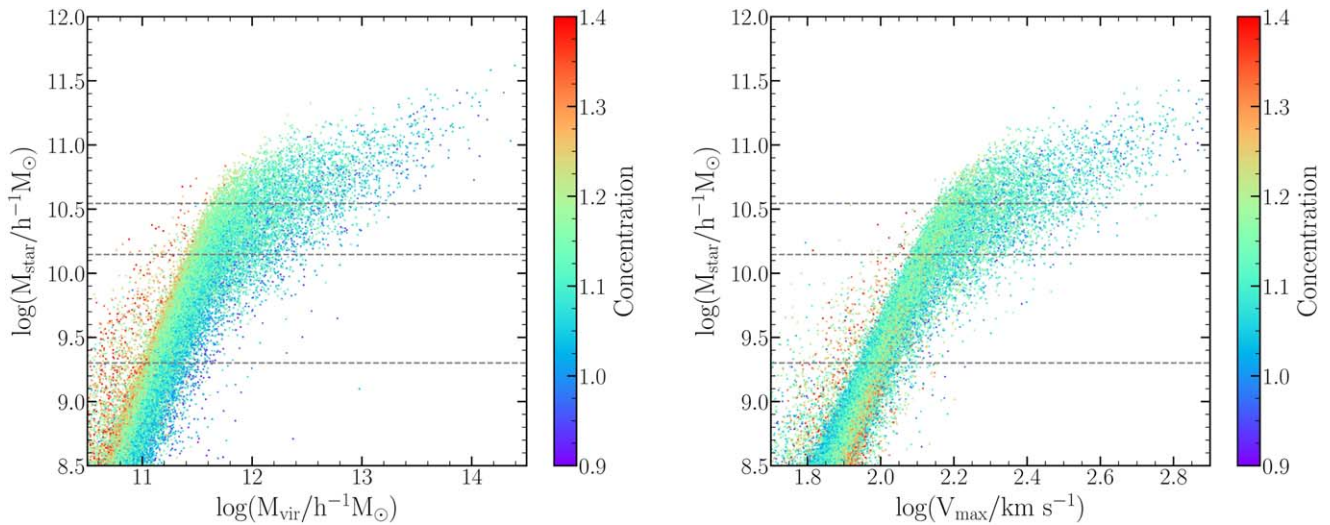


Figure 6. Stellar mass of central galaxies as a function of host halo mass (left) and V_{\max} (right) for galaxies in the SAM applied to the Millennium WMAP7 simulation. Galaxies are color coded by their host halo concentration. For clarity, we use a representative (randomly chosen and ordered) 1% of the central galaxies. The dashed horizontal lines show the stellar mass thresholds used to define the galaxy samples.

5. Galaxy Assembly Bias

Having investigated the behavior of the halo occupation functions and the resulting occupancy variations with V_{\max} , we now proceed to study its net impact on galaxy clustering, namely GAB. For completeness, we also provide a brief investigation of halo assembly bias in Appendix A, showing the concentration-dependent halo clustering with M_{vir} and V_{\max} .

To investigate the impact of assembly bias on galaxy clustering we compare the clustering of galaxies in our sample to that of shuffled galaxy samples. The shuffling follows the methodology of Croton et al. (2007; see also Z18 and C19), randomly reassigning the galaxy content of halos among halos of the same mass. More specifically, the central galaxies are randomly shuffled among halos within the same mass bin. The satellite galaxies are moved together with their original central galaxy, preserving the same distribution, and thus maintaining the same contribution to the correlation function from intrahalo pairs. In order to investigate GAB with respect to V_{\max} , we perform an analogous shuffling procedure in bins of fixed V_{\max} . We present the results using 0.05 dex bins in M_{vir} and 0.044 dex bins in V_{\max} . We verified that the specific bin choice makes no difference to our results.

The shuffling removes any dependence of the galaxy population on secondary properties of the halos (or their assembly history) other than that inherent in halo mass or V_{\max} . The difference between the clustering of the original galaxy sample and the shuffled sample reflects the impact of assembly bias on galaxy clustering, namely the level of GAB. In the idealized extreme case, if V_{\max} encapsulated in full the occupancy variations with respect to all secondary halo properties, there would be no difference between the clustering of the original sample and the V_{\max} -shuffled one.

Figure 7 shows the resulting GAB signatures when shuffling by either M_{vir} or V_{\max} , for the three stellar-mass selected samples we study. The M_{vir} results are identical to the ones examined in C19, showing a $\sim 12\%$ – 16% excess clustering due to assembly bias. This arises from the net combined effect of the occupancy variation and halo assembly bias. For example, with regard to concentration, central galaxies preferentially occupy the more concentrated halos which are more strongly clustered. The surprising, and rather disappointing, results lie

with the V_{\max} case: we find that generally the GAB associated with V_{\max} is unchanged and comparable to that of M_{vir} . This is somewhat puzzling given the significant reduction of the centrals occupancy variation when using V_{\max} .

The uncertainties on this clustering ratio, estimated from jackknife resampling, are again negligible over most of the range (and start becoming noticeable only above separations of $20 h^{-1}$ Mpc; see, e.g., Figure 10 of Z18 or Figure 10 of C19). We estimated as well the uncertainty involved due to randomness of the shuffling procedure, by utilizing 10 independent shuffled samples. The resulting scatter in the clustering ratio is minimal, of the order of 1%, in agreement with previous studies (e.g., Croton et al. 2007). We also note that when comparing GAB measures for the different halo properties, we utilize the same random seed, such that this extra small scatter does not impact our results.

To further assess the situation, we repeat this analysis but now considering only the central galaxies, the results of which are presented in the top panel of Figure 8. Note that we only show here larger scales in the 2-halo regime, since without satellites there are no intrahalo pairs. We see that when considering just central galaxies there is a significant reduction in the GAB signal, of about 40% at $10 h^{-1}$ Mpc scale. The difference between the two curves reflects the amount of assembly bias “captured” by V_{\max} when considering just the central galaxies. The lower GAB signature is perhaps to be expected, given the much reduced occupancy variation with concentration for central galaxies in the V_{\max} case (as shown in Figure 3). Still, most of the GAB signal remains, in accord with the emerging understanding that GAB is not fully governed by a single parameter (or simple combination thereof; Croton et al. 2007; Xu & Zheng 2019).

We demonstrate in Appendix A that the level of halo assembly bias for concentration remains roughly unchanged when switching to V_{\max} . The similar level of GAB for V_{\max} compared to the standard GAB signature for M_{vir} exhibited in Figure 7 is then plausibly related to the increased occupancy variation we find for the satellites, which also contribute to the signal via central-satellite pairs (Zu et al. 2008). The occupancy variations thus provide some insight and physical intuition for the GAB signal, though we caution that the GAB we measure

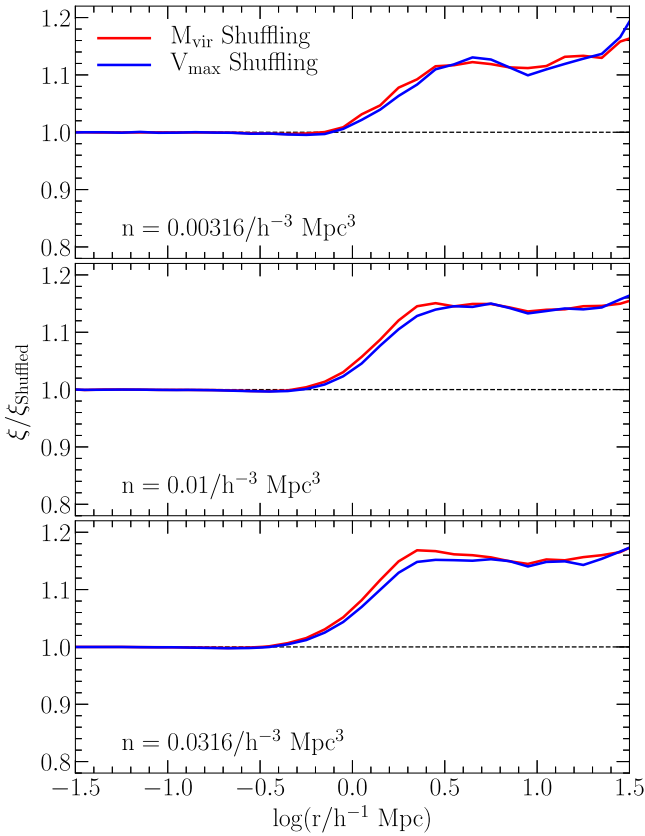


Figure 7. Ratios between the correlation functions of the SAM galaxies and those of the corresponding shuffled galaxy samples (see the text), showing the impact of galaxy assembly bias. These are shown for M_{vir} (red) and V_{max} (blue) for three stellar-mass selected samples as labeled.

is the net effect, potentially impacted from multiple secondary parameters in an intricate fashion.

We also attempt a hybrid shuffling scheme, to potentially remedy the increased contribution from the satellite galaxies, in which the central galaxies are shuffled according to V_{max} while the satellites are shuffled by M_{vir} as before. The result of this hybrid shuffling is shown as the green line in the bottom panel of Figure 8, exhibiting a roughly 15% reduction in GAB on large scales. The slight deviation of the hybrid case from a ratio of unity on small scales arises from changes to the contribution from central-satellite pairs due to the more complex shuffling procedure. One can envision improving this further by finding a different halo property that would diminish the satellites’ occupancy variations, perhaps by utilizing the number of substructures. Alternatively, one may be able to develop a composite new parameter that will simultaneously improve both the centrals’ occupancy variation and the satellites’ one. However, attempts to do this at least in the context of halo assembly bias (e.g., Villarreal et al. 2017; Mao et al. 2018; Xu & Zheng 2018; Han et al. 2019) have shown that this is largely unattainable, and such modeling approaches might be too complex to be practical in any case.

Another potential candidate is V_{peak} , the peak value of V_{max} throughout the accretion history of the halo. This parameter is often used in the context of abundance matching methods (e.g., Conroy et al. 2006; Reddick et al. 2013; Chaves-Montero et al. 2016; Guo et al. 2016) to better connect galaxies to halo substructure. Its main advantage in such methodologies, however, is in connecting satellites to subhalos, which differs

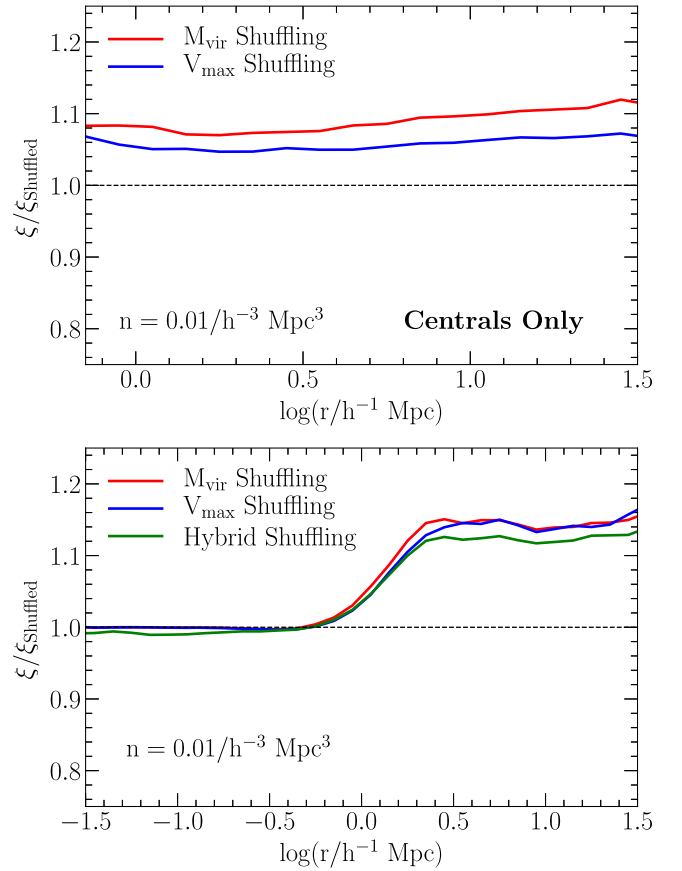


Figure 8. Galaxy assembly bias measurements for only the central galaxies in the $n = 0.01 h^3 \text{Mpc}^{-3}$ sample (top) and a hybrid shuffling method, where the centrals are shuffled by V_{max} and the satellites by M_{vir} (bottom).

from the HOD approach relating both central and satellite galaxies to the main host halo. Still, recent claims have suggested that V_{peak} provides the tightest relation to the stellar mass of galaxies (He 2019) and is free from secondary dependences (Xu & Zheng 2019), touting its use as a better proxy for halo mass. Remaining scatter in the relation is attributed to stochastic baryonic effects (Matthee et al. 2017; Kulier et al. 2019).

Figure 9 shows the resulting GAB, when using V_{peak} as the primary halo property instead of M_{vir} or V_{max} , for the three different galaxy samples. Namely, we calculate the clustering of the galaxies relative to a galaxy sample shuffled according to V_{peak} , where V_{peak} is obtained from the merger tree of each halo. We see that using V_{peak} partially suppresses the GAB signature, mostly in the 1-halo to 2-halo transition region. This effect is more significant with increased number density, as more small galaxies are included. Appendix C shows further analysis of the relation of V_{peak} to other properties, suggesting that the differences arise primarily from low-mass, high-concentration and older halos where V_{peak} varies from V_{max} . This may be related to the existence of splashback galaxies, i.e., galaxies whose halos had their mass accretion histories truncated due to a close encounter with a larger halo. Such halos are thought to have a significant role in halo assembly bias of low-mass halos (Mansfield & Kravtsov 2019), and are likely to impact the intermediate “transition” scales, as these centrals likely reside just outside the virial radius of the larger halo. We defer further investigation of this phenomenon with higher-resolution simulations to future work.

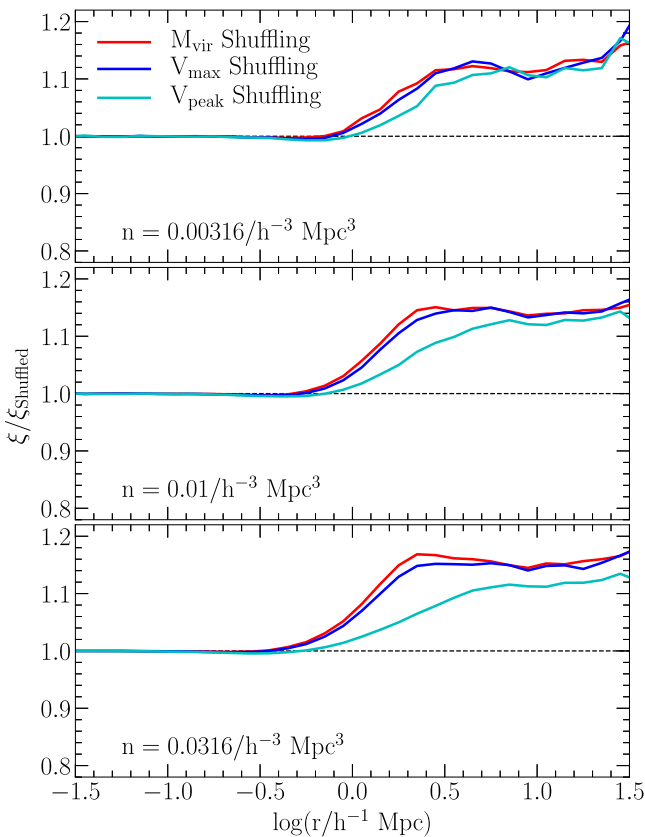


Figure 9. Galaxy assembly bias measurements for V_{peak} (cyan) compared to the results for M_{vir} (red) and V_{max} (blue).

We note, however, that even if V_{peak} can be utilized as a parameter which partially encapsulates assembly bias, determining it in simulations requires calculating the full merger trees of the halos with sufficient mass resolution. In such a scenario, one will likely also have access to other sophisticated modeling techniques which may be more useful. We focused in this work on a property like V_{max} that would be readily available in most N -body simulations commonly used for creating large mock catalogs and for constraining cosmology.

6. Conclusion

We use a state-of-the-art semianalytic galaxy formation model applied to the Millennium simulation to study the prospects of a conceptual modification of the HOD approach, replacing the virial mass of the halo by its maximal circular velocity of the halo, V_{max} . The motivation is that this revised halo occupation function may encapsulate the effects of assembly bias into the formalism, enabling more accurate modeling of the galaxy–halo connection and galaxy clustering, and potentially allow us to produce realistic mock catalogs that incorporate assembly bias. We thus explore the different aspects of assembly bias, namely halo clustering dependence on secondary parameters (halo assembly bias; see Appendix A), the variation in the galaxy content of halos with these parameters (occupancy variation; Section 3), and the impact on galaxy clustering relative to a shuffled galaxy sample (GAB; Section 5). We mostly use here galaxy samples with fixed number density ranked by stellar mass at the present epoch, and for the secondary halo parameters we investigate the variation with halo concentration and halo formation time. To get a

broader understanding of the origins of the occupancy variation, we also examine the relation between stellar mass and the different halo properties (Section 4). Finally, we also investigate the potential of utilizing V_{peak} , the peak value of V_{max} across the halo’s assembly history as the proxy for halo mass.

The main conclusions from our work are summarized as follows:

1. Halo assembly bias, i.e., the dependence of halo clustering on concentration, is largely unchanged when examined in bins of fixed V_{max} versus fixed halo mass. The same holds for V_{peak} .
2. Employing V_{max} significantly reduces the occupancy variation with halo concentration for central galaxies; however, it increases the satellites occupancy variation.
3. The centrals occupancy variation is partially reduced when using halo formation time as the secondary halo property.
4. The change to V_{max} does not reduce the level of GAB, despite the reduction in the central occupancy variation. The GAB signature remains essentially the same when using V_{max} or M_{vir} , irrespective of sample number density.
5. V_{max} does not prove to be a useful quantity also when examining samples selected by SFR or when looking at $z = 1$, with varying results.
6. Using V_{peak} slightly reduces the GAB signal, impacting mostly the 1-halo to 2-halo transition regime, an effect likely related to splashback galaxies. However, the large-scale effect remains largely unmitigated.

Assembly bias remains a challenge for contemporary models of galaxy clustering and the galaxy–halo relation. Perhaps a more intricate parameter can better encapsulate the effects of GAB, however, given the complex nature of the phenomenon this might be hard to achieve and not-trivial to implement in practice. While the level of assembly bias in the universe remains an open and debated issue, the results shown here can help inform theoretical modeling of it and attempts to determine it in observations.

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Appendix A Halo Assembly Bias

We examine the concentration-dependence of *halo* clustering in the simulation, namely halo assembly bias. Following

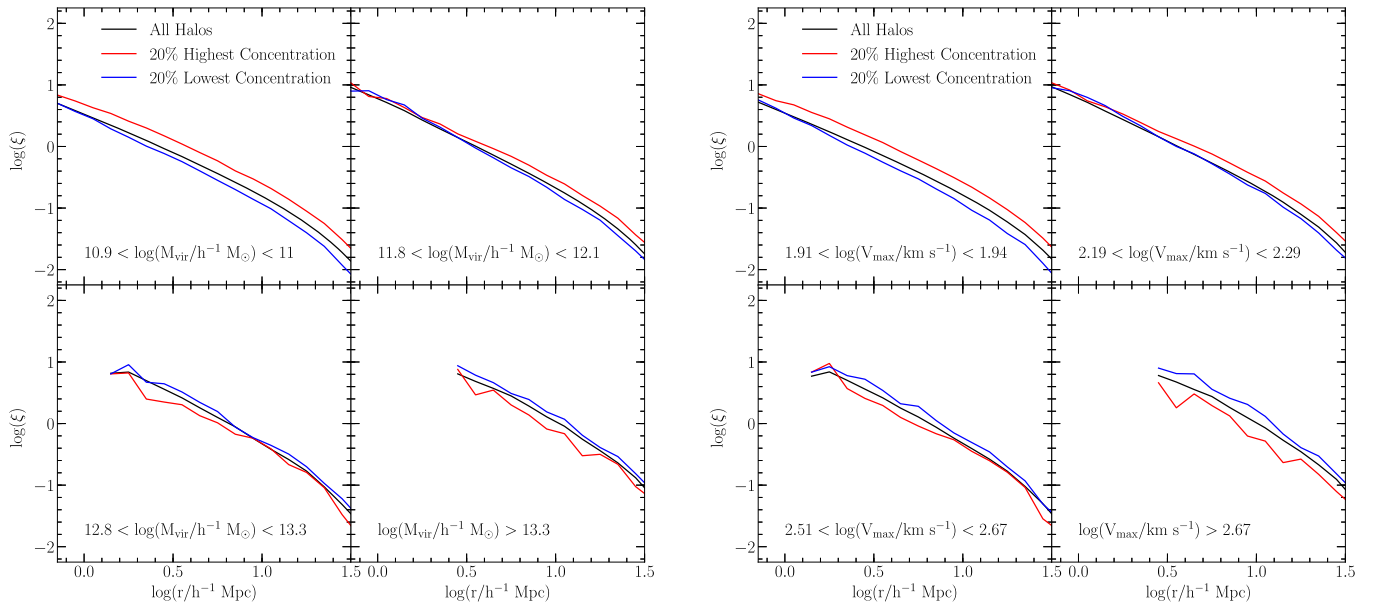


Figure 10. Correlation function of halos in the Millennium WMAP7 simulation and its dependence on concentration, for samples of fixed M_{vir} (left) and fixed V_{max} (right).

Gao et al. (2005), we bin the halos in discrete bins of halo mass and calculate the autocorrelation function of these halo samples and of the 20% most concentrated and 20% least concentrated halos. These are shown in the left-hand side of Figure 10, and exhibit the well-studied concentration-dependent halo clustering (e.g., Wechsler et al. 2006; Gao & White 2007; Mao et al. 2018). We see that for relatively low halo masses, more concentrated halos are more clustered than less concentrated halos. This trend is the strongest for our lowest-mass bin, decreases with increasing mass, then reverses sense and continues to increase in amplitude for the most massive halos.

The right-hand side of Figure 10 repeats this analysis, but now in fixed bins of V_{max} . The bins are chosen to roughly match the halo mass bins according to the relation between V_{max} and M_{vir} (Figure 2) and have identical number densities. We find very similar results for the concentration-dependent halo clustering as a function of V_{max} , with comparable assembly bias amplitudes in all bins and a reversal of the trend at larger V_{max} values. Our results are in good agreement with Sato-Polito et al. (2019) who find a similar behavior with a reversal of the halo assembly bias effect at $M_{\text{vir}} \sim 10^{13} h^{-1} M_{\odot}$ and at $V_{\text{max}} \sim 330 \text{ km s}^{-1}$, using the MultiDark suite of simulations (Klypin et al. 2011), as well as the results of Salcedo et al. (2018) using the LasDamas simulations. For completeness, we also investigate the concentration-dependence of clustering for fixed bins of V_{peak} , the peak value of V_{max} across the halos’ assembly history (not shown here). We find nearly identical results for V_{peak} as for V_{max} . We conclude that switching from M_{vir} to either V_{max} or V_{peak} has no significant impact on halo assembly bias.

Appendix B

Results for SFR Selected Samples and for Redshift $z = 1$

We report here an analogous analysis to the one in the main part of the paper but performed for galaxy samples selected by their SFR, which may be relevant for galaxy selections of upcoming surveys. We use the same three number densities. Figure 11 shows the occupancy variations for one

representative case of the $n = 0.01 h^3 \text{ Mpc}^{-3}$ galaxy sample. The left-hand side shows the standard occupation functions as a function of halo mass. This is the same case presented in Figure 7 of C19. Of note is the characteristic shape of the occupation function, which is different from that of stellar mass selected samples, due to the paucity of star-forming galaxies residing as centrals in massive halos. The occupancy variation for SFR-selected samples is similar to that of stellar mass selected ones, with more concentrated halos preferentially hosting central galaxies at the “knee” of the occupation and having fewer satellites. In the “dip” of the centrals occupation at higher mass, a smaller fraction of the more concentrated halos tends to host star-forming central galaxies.

The right panel of Figure 11 shows the occupancy variation in the V_{max} case. In this case, the occupancy variation for the central galaxies at the “turnover” reverses sense, with low-concentration halos starting to host central galaxies at lower halo mass. The variations in the central occupation at higher halo masses remain similar, but perhaps slightly reduced, while the satellite occupancy variations increase.

The net impact on galaxy clustering is shown in Figure 12, where we show again the ratio of correlation function to that of shuffled samples where the galaxy content was randomly reassigned to halos of the same M_{vir} or V_{max} , which effectively erases the occupancy variations. The overall changes with number density are consistent with those found by C19. We find that for all SFR-selected samples, this ratio slightly decreases for V_{max} with respect to the one for M_{vir} , possibly due to the preferential occupation of centrals in low-concentration halos. Hence we find that, for all cases, the correlation function of the V_{max} shuffled samples is larger than that of the M_{vir} shuffled one. The resulting impact on GAB, however, changes with number density (i.e., SFR threshold). For the highest number density sample, utilizing V_{max} slightly decreases GAB (defined as the deviation from a ratio of unity); for the middle number density it nearly diminishes the GAB signal; while for the lowest number density it increases the GAB effect. Thus it is hard to draw any conclusions on the usefulness of switching to V_{max} .

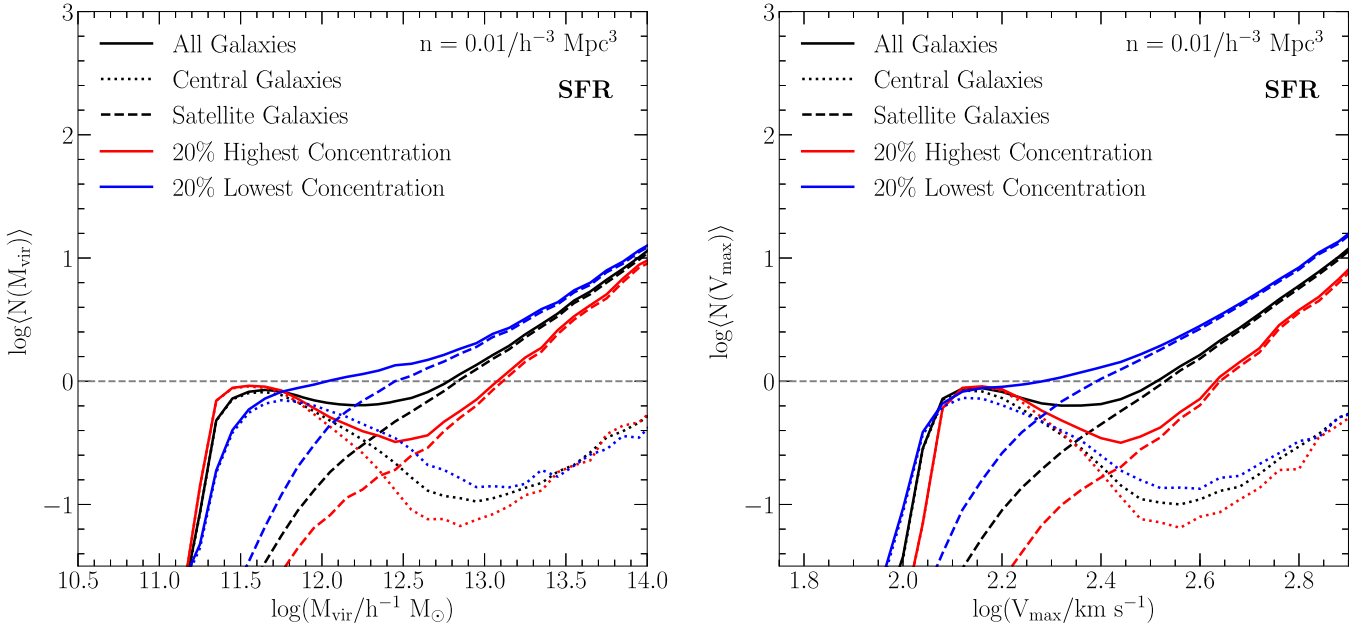


Figure 11. Occupancy variation with concentration for an SFR-selected sample corresponding to a number density of $n = 0.01 h^3 \text{Mpc}^{-3}$, shown for M_{vir} (left) and V_{max} (right).

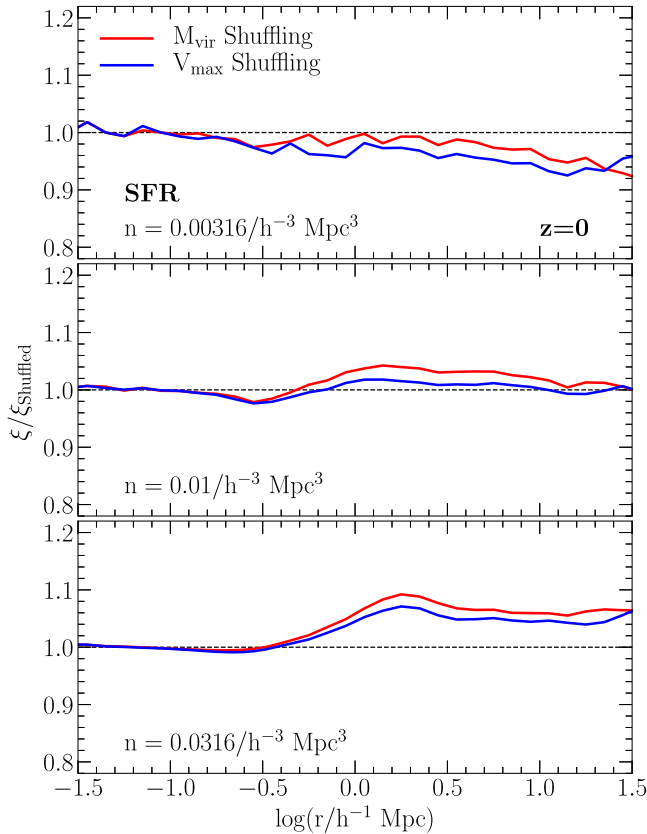


Figure 12. Galaxy assembly bias measurements for M_{vir} (red) and V_{max} (blue), for the three SFR-selected fixed number density samples.

Finally, in the left-hand side of Figure 13 we explore the GAB signatures at a higher redshift of $z = 1$. At $z = 1$ we find that the clustering ratio is now larger for V_{max} than for M_{vir} for all cases, or rather that the clustering of the V_{max} -shuffled sample is lower than that of the M_{vir} -shuffled sample. And, once again, the specific impact on GAB depends on the number density. For completeness, we also show in the right-hand side

of Figure 13 the GAB results for the stellar mass selected samples at $z = 1$. We see that in this case as well, for all number densities, the clustering with respect to the V_{max} -shuffled sample is increased relative to the M_{vir} case, resulting in increased GAB signatures. Overall, the results presented here strengthen our conclusion that, despite its claimed “potential,” V_{max} is unable to encapsulate GAB effects.

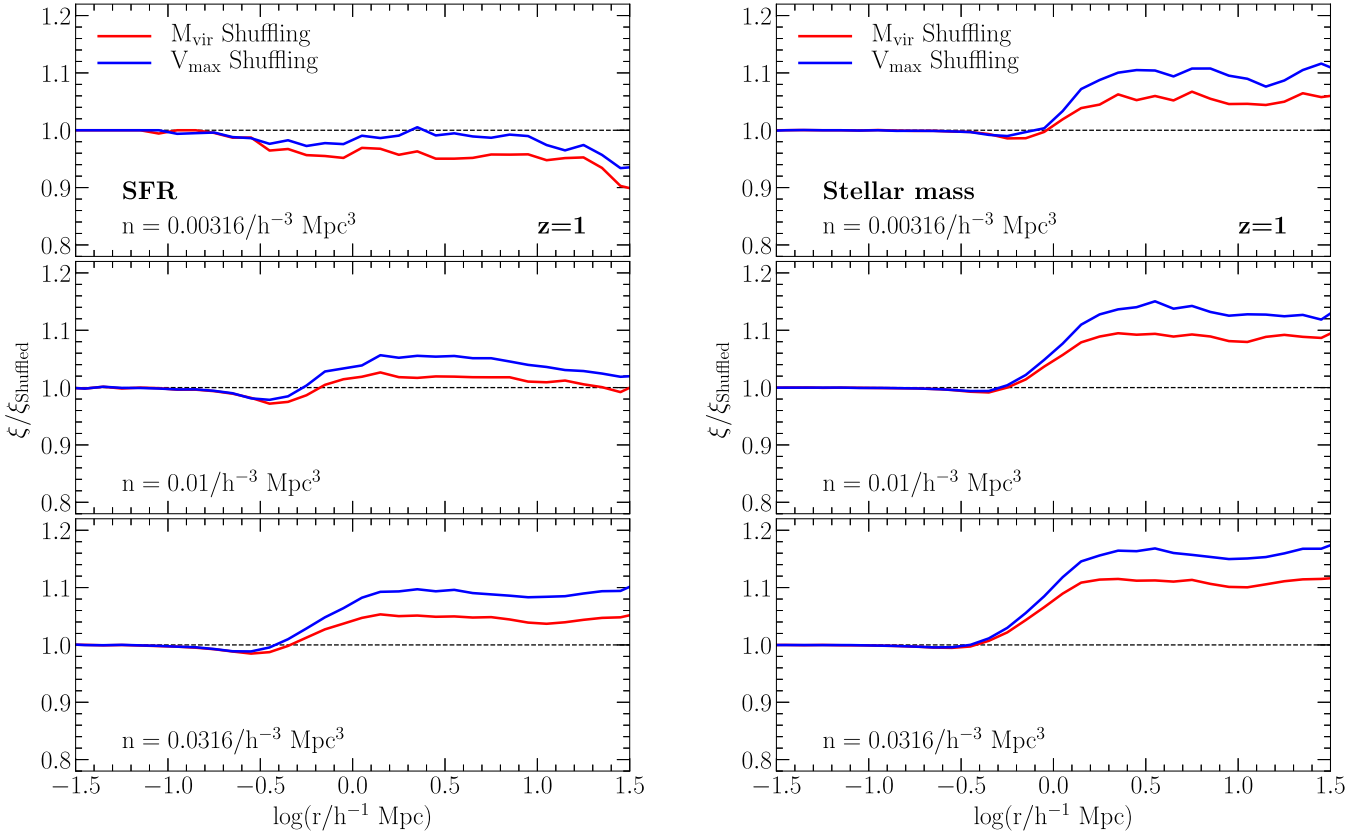


Figure 13. Galaxy assembly bias measurements for M_{vir} (red) and V_{max} (blue) at $z = 1$, shown for the SFR-selected samples (left) and stellar mass selected samples (right).

Appendix C Additional Results with V_{peak}

In this appendix we provide supplementary information regarding using V_{peak} , the maximum value of V_{max} of each halo over its cosmic history, as our proxy for halo mass. Figure 14 presents the $V_{\text{peak}}-M_{\text{vir}}$ relation, color coded by either halo concentration (left) or formation time (right). These relations can be compared to the analogous ones for V_{max} shown in Figure 2. We find that the relations are similar, but with a larger scatter in the V_{peak} case, especially for the low M_{vir} /low V_{peak} range. This arises from the scatter between V_{peak} and V_{max} , primarily for low-mass halos where V_{peak} varies from V_{max} and extends to larger values. It is noteworthy that the low-mass halos with the largest V_{peak} values tend to have higher concentrations and, strikingly, earlier formation times. This supports our hypothesis that these are splashback halos that had a larger mass in the past.

Figure 15 shows the relation between stellar mass and V_{peak} for the SAM central galaxies. This relation is similar to the

analogous one for V_{max} shown in Figure 6. However, it exhibits less secondary dependences on concentration—note the lack of noticeable extremes of the most concentrated halos—in particular for lower values of stellar mass. This is consistent with the slight improvement in GAB seen in Figure 9 and its dependence on number density.

Finally, Figure 16 shows the occupancy variations with concentration for an HOD computed as a function of V_{peak} . Again, we find very similar results to the occupancy variations with V_{max} (Figures 3 and 4). The centrals’ occupancy variation improves (i.e., decreases) to a varying degree for the different samples while the satellites’ occupancy variation increases with respect to the “standard” occupancy variations with M_{vir} . There are slight differences in the level of occupancy variation for V_{peak} with respect to that for V_{max} , with the highest number density sample (lowest stellar mass threshold) exhibiting now nearly diminished centrals occupancy variation, seemingly related to the relatively bigger improvement seen for the GAB measurement in that case (bottom panel of Figure 9).

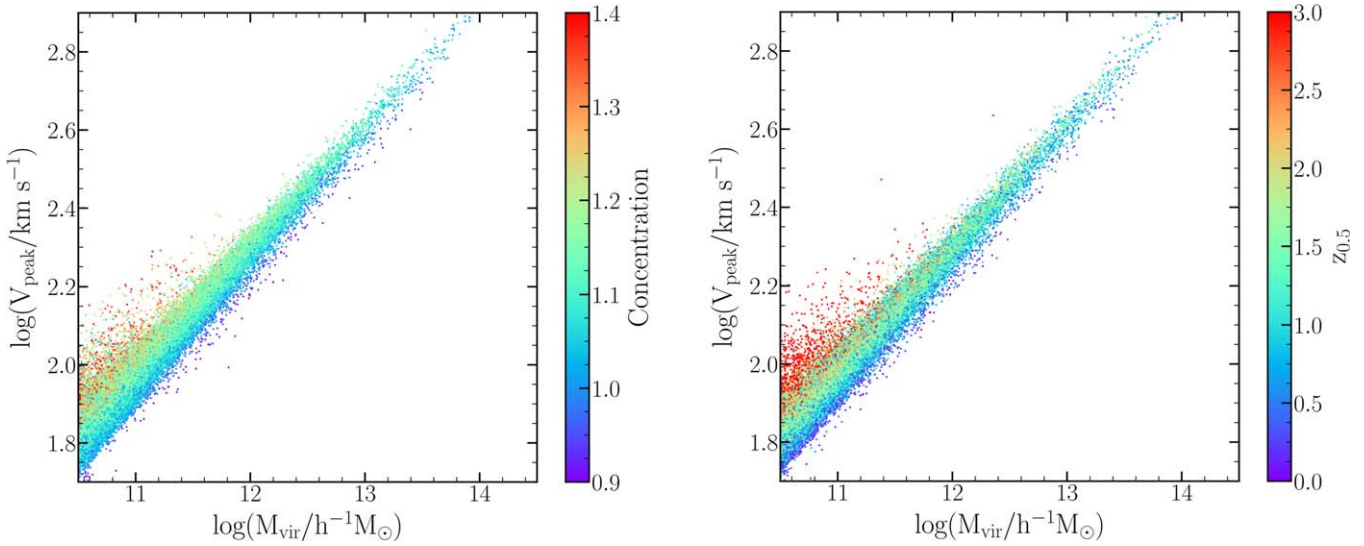


Figure 14. Relation between V_{peak} and M_{vir} color coded by halo concentration (left) and by halo formation time (right). These are the analog of Figure 2 but for V_{peak} instead of V_{max} . For clarity, we plot a representative (randomly chosen and ordered) 1% of the halos.

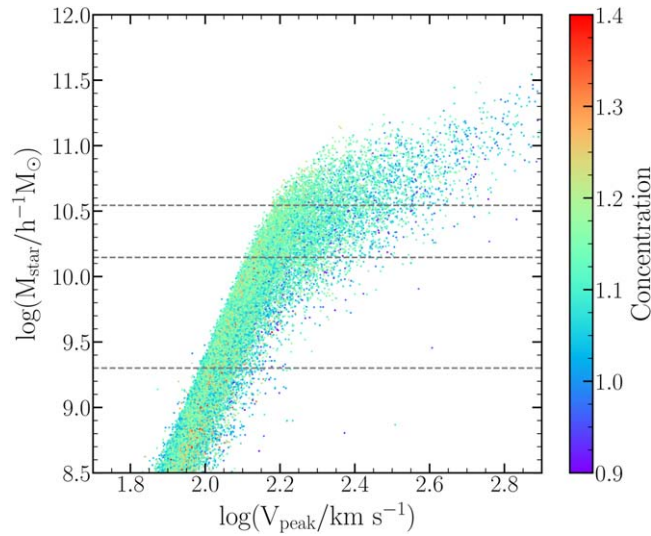


Figure 15. Relation between the stellar mass of central galaxies as a function of host V_{peak} , color coded by concentration. The dashed lines mark the stellar mass thresholds defining our three samples. This figure complements Figure 6. Once again we only plot 1% of the galaxies.

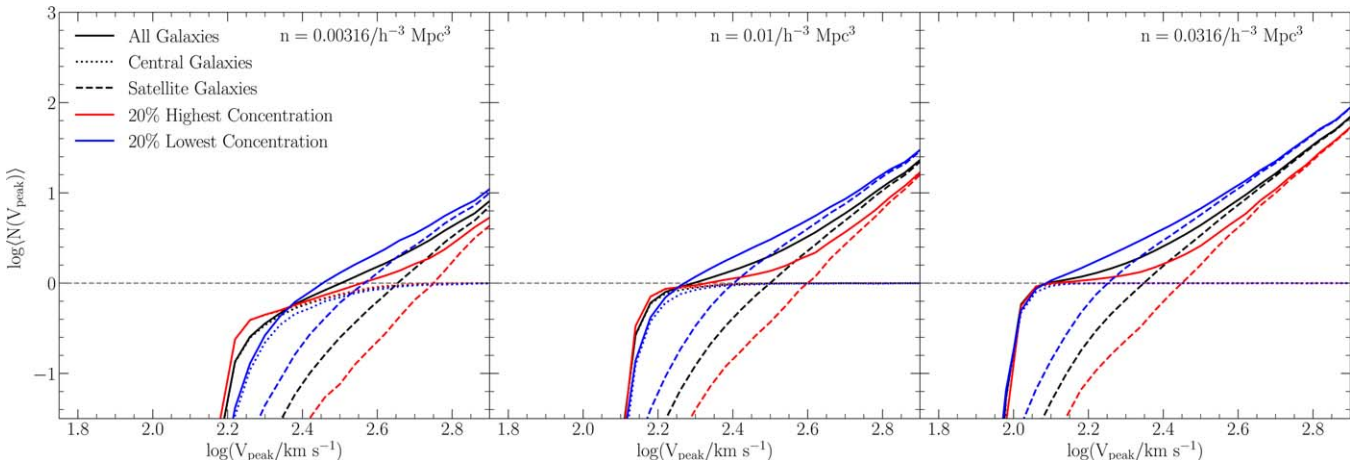


Figure 16. Same as Figures 3 and 4 but now for V_{peak} , namely the halo occupation functions for V_{peak} showing the variations with concentration, for the three number density samples.

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