- 1 Short title: Design principle for decoding calcium signals
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13	Article title: Design principles for decoding calcium signals to generate specific gene
14	expression via transcription
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22	One sentence summary: Identification of the design principle by which plant cells decode
23	specific calcium signatures to produce the correct gene expression response.
24	
25	Footnotes
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35 ABSTRACT

The second messenger calcium plays a key role in conveying specificity of signalling 36 pathways in plant cells. Specific calcium signatures are decoded to generate correct gene 37 expression responses and amplification of calcium signatures is vital to this process. It is not 38 known: (1) if this amplification is an intrinsic property of all calcium-regulated gene 39 expression responses and whether all calcium signatures have the potential to be amplified, 40 and (2) how does a given calcium signature maintain specificity in cells containing a great 41 number of transcription factors (TFs) and other proteins with the potential to be calcium-42 43 regulated? The work presented here uncovers the design principle by which it is possible to decode calcium signals into specific changes in gene transcription in plant cells. Regarding 44 45 the first question, we found that the binding mechanism between protein components possesses an intrinsic property that will nonlinearly amplify any calcium signal. This 46 47 nonlinear amplification allows plant cells to effectively distinguish the kinetics of different calcium signatures to produce specific and appropriate changes in gene expression. 48 49 Regarding the second question, we found that the large number of calmodulin (CaM)-binding transcription factors (TFs) or proteins in plant cells form a buffering system such that the 50 51 concentration of an active CaM-binding TF is insensitive to the concentration of any other CaM-binding protein, thus maintaining specificity. The design principle revealed by this 52 work can be used to explain how any CaM-binding TF decodes calcium signals to generate 53 54 specific gene expression responses in plant cells via transcription.

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56 INTRODUCTION

Plants are sessile organisms and therefore they must adapt their metabolism, growth, and 57 architecture to a changing environment. To survive, it is vital for plants to be able to sense 58 and act upon environmental information. Central to this are "second messengers": cellular 59 chemicals that convey information from the outside world to the cells that make up a plant. 60 Second messengers have evolved to trigger the required response of cells to environmental 61 cues. Calcium is a ubiquitous second messenger for activating tolerance mechanisms in 62 63 plants responding to environmental stresses (McAinsh et al., 1995; Allen et al., 2001; Love et 64 al., 2004; Miwa et al., 2006; McAinsh and Pittman, 2009; Dodd et al., 2010; Short et al., 2012; Edel et al., 2017; Yuan et al., 2017; Bender et al., 2018; Kudla et al., 2018). 65

The majority of plant defence responses against stress is realised by changes in gene 66 expression in order to produce proteins required to combat the conditions they encounter. It is 67 68 thus vital that the correct proteins are produced in response to different environmental conditions, i.e. different genes need to be switched on in response to different stimuli. This 69 70 means that the identity of the primary stimulus must be encoded in a "language" that the cell can understand. Most stimuli lead to transient elevation in cellular calcium levels. 71 72 Importantly, different stimuli produce calcium elevations with different characteristics: a unique "calcium signature". Consequently, the specific properties of different calcium 73 signatures have been proposed to encode information on the identity of the stimulus 74 (McAinsh et al., 1995; Allen et al., 2001; Love et al., 2004; Miwa et al., 2006; McAinsh and 75 Pittman, 2009; Dodd et al., 2010; Short et al., 2012) 76

Experimental data showed that calcium signals can be decoded to generate specific gene expression responses (Whalley et al., 2011; Whalley and Knight, 2013) and modelling analysis revealed that amplification of calcium signals is important for decoding calcium signals (Liu et al., 2015; Lenzoni et al., 2018). However, it remains unclear whether or not decoding calcium signatures in plant cells is governed by any general principle.

The complexity for plant cells to decode specific calcium signatures is multifaceted. First, any, even a modest, calcium signature (e.g. in response to ozone (Clayton et al., 1999)) is able to induce gene expression. Second, the specific characteristics of the calcium signatures produced by different stresses encode stimulus-specific information. Experimental evidence demonstrates that Arabidopsis (*Arabidopsis thaliana*) is able to decode specific calcium signatures and interpret them; leading to distinct gene expression profiles (Whalley et al., 2011; Whalley and Knight, 2013). Third, a variety of experimental data show that there

89 are a large number of calmodulin (CaM)- binding proteins (Reddy et al., 2011; Poovaiah et al., 2013; Virdi et al., 2015; Edel et al., 2017; Yuan et al., 2017; Bender et al., 2018; Kudla et 90 al., 2018). CaM has two pairs of Ca²⁺-binding EF-hand domains located at the N- and C-91 termini, respectively (Finn and Forsen, 1995; Valeyev et al., 2008). Some transcription 92 factors (TFs) can bind to Ca²⁺-CaM, allowing them to respond to calcium signals via this 93 Ca²⁺-CaM-TF interaction. Clearly, for transcription factors to decode calcium signals, and 94 95 therefore generate specific gene expression responses, they must be able to distinguish the kinetics of different calcium signals in the context of competing for binding CaM with other 96 97 CaM-binding proteins. However, how this occurs is unknown. In general, the search for basic underlying principles is vital for a better understanding of the regulation of signalling 98 dynamics. Cells navigate environments, communicate and build complex patterns by 99 initiating specific gene expression responses to specific signals (Brophy and Voigt, 2014). 100 Studies in other cellular systems (Savageau, 2001; Salvador and Savageau, 2003; Wall et al., 101 2003; Salvador and Savageau, 2006; Purvis and Lahav, 2013; Tolla et al., 2015; Karin et al., 102 2016) have found that biological networks may be evolutionarily tuned and regulatory 103 architecture of a biological network is optimised following some basic principles underlying 104 evolutionary selection (Salvador and Savageau, 2003; Chubukov et al., 2012). Design 105 106 principles are the underlying properties of network structures that have evolved to endow the network functions. Although experimental data showed that calcium signals can be decoded 107 108 to generate specific gene expression responses (Whalley et al., 2011; Whalley and Knight, 2013) and modelling analysis revealed that amplification of calcium signals is important for 109 110 decoding calcium signals (Liu et al., 2015; Lenzoni et al., 2018), it remains unclear whether or not decoding calcium signatures in plant cells is governed by any general principle. This 111 work uncovers the design principle for decoding calcium signals through changes in 112 transcription by addressing the following two questions: (1) is amplification of Ca^{2+} 113 signatures an intrinsic property of all calcium-regulated gene expression responses and do all 114 calcium signatures have the potential to be amplified? And (2) how does decoding of calcium 115 signals maintain specificity when one messenger (Ca^{2+}) is decoded by many transcription 116 factors and proteins in plant cells? This work establishes the link between the characteristics 117 of CaM (i.e., it has two pairs of Ca²⁺-binding EF-hand domains and it is capable of binding a 118 large number of proteins in plant cells) with the intrinsic properties of Ca²⁺-CaM-TF 119 interactions, to reveal the design principle underpinning how plant cells decode calcium 120 signals to generate specific gene expression response via changes in transcription. We show 121 that both a theoretical simple gene expression system and an empirical system of two plant 122

immunity genes (*enhanced disease susceptibility 1* (*EDS1*) and *isochorismate synthase 1* (*ICS1*)) (Lenzoni et al., 2018) follow this design principle to decode calcium signatures. The principle revealed in this work is applicable to study how any CaM-binding TF decodes calcium signals to generate specific gene expression response in plant cells via transcription.

128 **RESULTS**

129 Amplification of calcium signal is an intrinsic property of Ca^{2+} -CaM-TF interactions

The interaction of Ca²⁺, CaM, and another (CaM-binding) protein can form many different 130 binding complexes. CaM has two pairs of Ca²⁺-binding EF-hand domains located at the N-131 and C-termini, respectively (Finn and Forsen, 1995; Valeyev et al., 2008). Experimental 132 measurement showed that 4Ca²⁺-CaM is the active CaM-Ca²⁺ binding complex (Pifl et al., 133 1984). Therefore, this work assumes that the $4Ca^{2+}$ -CaM-TF complex is the active complex 134 for gene expression responses. The cooperative binding between Ca^{2+} and the 4 binding sites 135 of CaM has previously been subjected to both experimental and modelling studies (Fajmut et 136 al., 2005; Shifman et al., 2006; Pepke et al., 2010; Liu et al., 2015) and the kinetic parameters 137 have been experimentally determined (Shifman et al., 2006; Pepke et al., 2010). 138

For any transcription factor with one CaM-binding site, 18 different binding 139 complexes can form via 33 elementary binding processes (Supplemental Information). For 140 example. the binding between Ca²⁺, CaM, and calmodulin-binding transcription activators 141 (CAMTAs), and the binding between Ca^{2+} , CaM and calmodulin binding protein 60g 142 (CBP60g) have been previously described in detail (Liu et al., 2015; Lenzoni et al., 2018). 143 For any CaM-binding transcription factor, and following the previous analysis (Liu et al., 144 2015), there are six adjustable parameters for fully examining the dynamics of Ca^{2+} -CaM-TF 145 interactions after using the experimentally-determined parameters and introducing basic 146 thermodynamic constraints. P describes the cooperative binding between CaM and a TF in 147 the presence of Ca^{2+} . p>, = or <1 represents the binding affinity of Ca^{2+} -CaM complex to the 148 transcription factor being looser than, the same as, or tighter than binding of free CaM to the 149 TF, respectively. K_{14} is the dissociation equilibrium constant for the binding of the Ca²⁺-CaM 150 complex to the TF. $k_{on(14)}$ is the on rate for the binding of Ca²⁺-CaM complex to the TF; Q 151 describes how the cooperative binding between CaM and the TF in the presence of Ca^{2+} is 152 realised by kon, koff or both. [CaMt] describes the total concentration of CaM, which is the 153 summation of free CaM and all CaM complexes. [TF_t] describes the total concentration of the 154 TF, which is the summation of free TF and all TF complexes. 155

Here we consider that a "quasi-equilibrium state" is established for $Ca^{2+}-CaM$ -TF interactions according to the detailed balance principle (Alberty, 2004). Establishing a quasiequilibrium state requires the "on" and "off" rates for all binding reactions of $Ca^{2+}-CaM$ -TF interactions are relatively fast so that each reaction can establish an equilibrium. In the 160 sections "*Case study 1: a simple Ca*²⁺-regulated gene expression system" and "*Case study 2:* 161 *plant immunity gene expression*", we will show that this assumption is valid for 162 experimentally measured parameters of Ca²⁺-CaM-TF interactions. At a quasi-equilibrium 163 state, $k_{on(14)}$ and Q become irrelevant. Thus, there are only four adjustable parameters (i.e., P,

164 K_{14} , $[CaM_t]$, $[TF_t]$) for examining the dynamics of Ca²⁺-CaM-TF interactions.

165 At a quasi-equilibrium state and for any calcium concentration, the concentration of each

166 Ca^{2+} -CaM-TF complex can be analytically derived (Supplemental Information). Equation 1 167 shows the concentration of the active complex, $4Ca^{2+}$ -CaM-TF.

$$[4Ca^{2+} - CaM - TF] = \frac{\frac{[CaM_t][Ca^{2+}]^4[TF]}{K_1K_2K_3K_4K_{14}}}{1 + \frac{P[TF]}{K_{14}} + (1 + \frac{[TF]}{K_{14}})(\frac{[Ca^{2+}]}{K_1} + \frac{[Ca^{2+}]}{K_3} + \frac{[Ca^{2+}]^2}{K_1K_2} + \frac{[Ca^{2+}]^2}{K_1K_2} + \frac{[Ca^{2+}]^2}{K_1K_3} + \frac{[Ca^{2+}]^3}{K_1K_2K_3} + \frac{[Ca^{2+}]^3}{K_1K_2K_3K_4} + \frac{[Ca^{2+}]^4}{K_1K_2K_3K_4} + \frac{[Ca^{2+}]^4}{K_1K_2K_3} + \frac{$$

168 (eq 1)

169 K_1, K_2, K_3 , and K_4 are the dissociation equilibrium constants for binding of first and second 170 Ca^{2+} to the CaM C-terminus; and for binding of first and second Ca^{2+} to the CaM N-terminus, 171 respectively. [TF] is the concentration of the free transcription factor, and it can be calculated 172 using the total concentration of the transcription factor and the concentrations of all CaM-TF 173 complexes. Other symbols in equation 1 are as described above.

At an unperturbed cellular state where a calcium signature has not yet emerged, the 174 calcium concentration settles onto a steady-state value, $[Ca^{2+}]_{ss}$ In this state, expression of a 175 gene, which is regulated by the active signal, 4Ca²⁺-CaM-TF, is at a fixed level, 176 corresponding to $[Ca^{2+}]_{ss}$. Kinetics of different calcium signatures have different temporally 177 changing features of calcium concentration. Due to the innate properties of the Ca²⁺-CaM-TF 178 interactions, different calcium signatures are decoded into different temporally-changing 179 concentrations of the active complex, 4Ca²⁺-CaM-TF, which in turn regulates gene 180 expression. Thus, the first step for elucidating the information flow from a calcium signal to a 181 specific gene expression response is to examine how the signal is decoded into a temporally-182 changing concentration of the active signal, $[4Ca^{2+}-CaM-TF]$. 183

Equation 2 describes the ratio of $[4Ca^{2+}-CaM-TF]$ for any $[Ca^{2+}]$ to that for $[Ca^{2+}]_{ss}$.

185
$$\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{SS}} = \left(\frac{[Ca^{2+}]}{[Ca^{2+}]_{SS}}\right)^4 f = \left(\frac{[Ca^{2+}]}{[Ca^{2+}]_{SS}}\right)^4 \frac{g_{SS} + P + \frac{K_{14}}{[TF]_{SS}}(1+g_{SS})}{g + P + \frac{K_{14}}{[TF]}(1+g)} \quad (eq 2)$$

186 With

$$f = \frac{\frac{1}{[TF]_{ss}} + \frac{P}{K_{14}} + (\frac{1}{[TF]_{ss}} + \frac{1}{K_{14}})(\frac{[Ca^{2+}]_{ss}}{K_1} + \frac{[Ca^{2+}]_{ss}}{K_1} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_3} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_4} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_4} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_3} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_4} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_3} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_4} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_3} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_4} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_3} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2K_4} + \frac{[Ca^{2+}]_{s$$

187 and

188

$$g_{ss} = \frac{[Ca^{2+}]_{ss}}{K_1} + \frac{[Ca^{2+}]_{ss}}{K_3} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_2} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_3} + \frac{[Ca^{2+}]_{ss}^2}{K_1K_4} + \frac{[Ca^{2+}]_{ss}^3}{K_1K_2K_3} + \frac{[Ca^{2+}]_{ss}^3}{K_1K_3K_4} + \frac{[Ca^{2+}]_{ss}^4}{K_1K_2K_3K_4}$$
$$g = \frac{[Ca^{2+}]}{K_1} + \frac{[Ca^{2+}]}{K_3} + \frac{[Ca^{2+}]^2}{K_1K_2} + \frac{[Ca^{2+}]^2}{K_1K_3} + \frac{[Ca^{2+}]^2}{K_1K_3} + \frac{[Ca^{2+}]^3}{K_1K_2K_3} + \frac{[Ca^{2+}]^3}{K_1K_2K_4} + \frac{[Ca^{2+}]^3}{K_1K_2K_$$

Equation 2 shows that, at any calcium concentration, the fold change of calcium signal is 189 always amplified by the power of 4, $\left(\frac{[Ca^{2+}]}{[Ca^{2+}]_{ss}}\right)^4$, multiplied by a modification term, f. In 190 191 order to estimate the magnitude of this amplification, we need to estimate the lower limit of f. First, f has the following property. f is always less than 1, and it decreases when $[Ca^{2+}]$ 192 increases. This is because increasing $[Ca^{2+}]$ increases term g and simultaneously decreases the 193 concentration of free transcription factor, [TF], for a constant total concentration of the 194 transcription factor, $[TF_t]$ Second, the value of f is dependent on both $[TF]_{ss}$ and [TF], both 195 of which increase with [TF_t] . In plant cells, a typical calcium signature can increase 196 cytosolic calcium concentration from its steady state concentration (ca. 0.05 µM) to up to 2.5 197 µM with contrastingly different kinetics (Knight et al., 1996, 1997; Aslam et al., 2008). If we 198 consider that, within this range of $[Ca^{2+}]$, the free TF concentration is only determined by the 199 total concentration of the TF, we are able to deduce that the lower limit of f is $\frac{g_{ss}}{a}$ 200 (Supplemental Information), namely f is always larger than $\frac{g_{55}}{a}$. Thus, when $[Ca^{2+}]$ increases 201 from $[Ca^{2+}]_{ss}$ to $[Ca^{2+}]$, the minimum amplification of the calcium signal into the active 202 signal, $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{sc}}$, is $\left(\frac{[Ca^{2+}]}{[Ca^{2+}]_{sc}}\right)^4 \frac{g_{ss}}{g}$. 203

To determine the values of $\left(\frac{[Ca^{2+}]}{[Ca^{2+}]_{ss}}\right)^4 \frac{g_{ss}}{g}$, we need the values of the four parameters (K₁, K₂, K₃ and K₄). These four parameters have been experimentally determined and their values are $K_1 = 10 \ \mu M$, $K_2 = 0.925 \ \mu M$, $K_3 = 25 \ \mu M$, $K_4 = 5 \ \mu M$ (Linse et al., 1991; Shifman et al., 2006; Kubota et al., 2007; Pepke et al., 2010). To show the ability of Ca²⁺-CaM-TF interaction to amplify a calcium signal, we analysed an example, for which [Ca²⁺] increases to 2.5 \muM from its steady-state value of 0.05 \muM. For [Ca²⁺]_{ss} = 0.05 \muM, g([Ca²⁺]_{ss}, K) = 0.0073. When [Ca²⁺] increases to 0.25 \muM (i.e. 5 fold), 0.5 \muM (i.e. 10 fold), 1.0 \muM (i.e. 20 fold), and 2.5 μ M (i.e. 50 fold), the minimum amplification of these calcium concentrations into the concentrations of their active signals, $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$, is 107 fold, 725 fold, 4390 fold, and 37570 fold, respectively. Thus, the Ca²⁺-CaM-TF interaction possesses an intrinsic property of nonlinearly amplifying any calcium signal, which is quantitatively described by equation 2.

Fig. 1 shows the numerical results that confirm the above theoretical analysis for a 216 wide range of total concentrations of a transcription factor (0.01 µM to 1.0E5 µM). Fig. 1A 217 shows that f is always less than 1, that increasing $[Ca^{2+}]$ decreases the value of f, and that f 218 is always larger than $\frac{g_{ss}}{q}$. Fig. 1B shows that the term f is relatively unimportant and any 219 calcium signal is always amplified. Therefore, numerical analysis confirms theoretical 220 analysis: a calcium signal is always amplified due to Ca²⁺-CaM-TF interaction. In addition, 221 following the derivation of the lower limit of f in the Supplemental Information, we know 222 that decreasing the parameter for the cooperative binding between CaM and a TF in the 223 presence of Ca²⁺, P (Liu et al., 2015; Lenzoni et al., 2018), or increasing the concentration of 224 225 the TF decreases the value of f. Fig. 1, A-D shows that numerical results are in agreement with theoretical analysis. When P is sufficiently small and [TF_t] is sufficiently large, fold 226 amplification of calcium signal is the same as the theoretical minimal fold amplification (Fig. 227 228 1, B and D).

Based on the above analysis, it can be seen that any calcium signal is always 229 amplified by the power of 4 of calcium concentration ratio, $\left(\frac{[Ca^{2+}]}{[Ca^{2+}]_{cc}}\right)^4$, multiplied by a factor 230 that is relatively less important, $\frac{g_{ss}}{q}$. In equation 2, the main factor for amplifying a calcium 231 signal is the term $\left(\frac{[Ca^{2+}]}{[Ca^{2+}]cc}\right)^4$. Derivation of equation 2 reveals that the term $\left(\frac{[Ca^{2+}]}{[Ca^{2+}]cc}\right)^4$ 232 emerges from two pairs of Ca²⁺-binding EF-hand domains and a TF-binding domain in the 233 CaM structure. Therefore, the ability of CaM to bind four Ca²⁺ and one TF molecule results 234 in the amplification of calcium signal. In other words, the Ca²⁺-CaM-TF binding mechanism 235 naturally leads to amplification of calcium signals. As we will show below, this aspect of the 236 underlying design principle, which links the Ca²⁺-CaM-TF binding mechanism with the 237 emerging property of calcium signal amplification, leads to preferential expression of specific 238 calcium-regulated genes. 239

240 Concentration of a CaM-binding TF-specific active signal is insensitive to changes in 241 concentration of other CaM-binding proteins

A variety of experimental data show that there are a large number of CaM-binding proteins in 242 plant cells (Reddy et al., 2011; Poovaiah et al., 2013; Virdi et al., 2015). Thus, when a 243 calcium signature emerges, a specific TF must compete for the binding of CaM with other 244 CaM-binding proteins. An important question, therefore, is how is a CaM-binding TF capable 245 of generating a specific gene expression response by decoding a calcium signature in the 246 context of competing for CaM binding with many other CaM-binding proteins? To address 247 this question, the effects of the existence of a large number of CaM-binding proteins on the 248 concentration of a CaM-binding TF-specific active signal must be examined. 249

When many proteins compete for the binding of CaM, the concentration of the active complex of a transcription factor (TF_i), $4Ca^{2+}-CaM-TF_i$, can be derived following the method used for deriving eq. 1 and is described by equation 3.

 $[4Ca^{2+} - CaM - TF_i]$

$$=\frac{\frac{[CaM_{t}][Ca^{2+}]^{4}[TF_{i}]}{K_{1}K_{2}K_{3}K_{4}K_{i,14}}}{1+\sum_{j=1}^{n}\frac{P_{j}[TF_{j}]}{K_{j,14}}+(1+\sum_{j=1}^{n}\frac{[TF_{j}]}{K_{j,14}})(\frac{[Ca^{2+}]}{K_{1}}+\frac{[Ca^{2+}]^{2}}{K_{3}}+\frac{[Ca^{2+}]^{2}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{2}}{K_{1}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}K_{3}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{3}}{K_{1}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{3}}{K_{1}K_{2}}+\frac{[Ca^{2+}]^{3}}{K_{1}}+\frac{[Ca^$$

253 (eq. 3),

where TF_i and TF_j are the free form of the ith and jth transcription factor, respectively. P_j is 254 the parameter for quantifying the cooperative binding between CaM and TF₁ in the presence 255 of Ca^{2+} . $K_{i,14}$ and $K_{j,14}$ are the dissociation equilibrium constants for the binding of Ca^{2+} -256 CaM complex to TF_i and TF_i, respectively. n is the total number of CaM-binding proteins. In 257 eq. 3, for simplifying notations, TF_i can be any TF or protein that binds with CaM. 258 259 Therefore, following eq. 3, the existence of any CaM-binding TF or protein, TF_i, could affect the concentration of the active complex of a transcription factor TF_i , $4Ca^{2+}-CaM-TF_i$, by 260 competing for the binding of CaM with TF_i. In eq. 3, this competition is described by the two 261 summation terms: $\sum_{j=1}^{n} \frac{P_j[TF_j]}{K_{1,4}}$ and $\sum_{j=1}^{n} \frac{[TF_j]}{K_{1,4}}$. 262

We consider that the total concentration of CaM is $[CaM]_t$ and the concentration of each of the CaM-binding proteins, TF_j , is $[TF_j]_t$ (j=1,...n). When many proteins compete for the binding of CaM, the following constraints must apply. The concentration summation of free CaM and all CaM complexes with different proteins must be equal to $[CaM]_t$ at any calcium concentration. The total concentration for any transcription factor is the concentration summation of free protein, TF_j , and all TF_j -binding complexes $[TF_j]_t$ at any calcium concentration.

Examination of eq. 3 reveals that the existence of a large number of CaM-binding 270 proteins in plant cells can form a buffering system such that the concentration of a CaM-271 binding TF-specific active signal is insensitive to change in the concentration of another 272 CaM-binding protein. This is because of the two summation terms, $\sum_{j=1}^{n} \frac{P_j[TF_j]}{K_{j+1}}$ and 273 $\sum_{j=1}^{n} \frac{[TF_j]}{K_{j+1}}$, in the denominator of eq. 3. Firstly, the existence of any CaM-binding protein, 274 TF_i, always reduces the concentration of the active complex of transcription factor, TF_i. This 275 is because when CaM binds with TF_i, the concentration of CaM available for binding with 276 TF_i will become smaller. In eq.3, this corresponds to $\sum_{j=1}^{n} \frac{P_j[TF_j]}{K_{j,14}}$ and $\sum_{j=1}^{n} \frac{[TF_j]}{K_{j,14}}$ always being 277 larger than $\frac{P_i[TF_i]}{K_{i,14}}$ and $\frac{[TF_i]}{K_{i,14}}$, respectively. Secondly, since each of the two terms is the 278 summation of the contribution of all CaM-binding proteins, the TF or protein that contributes 279 a larger value of $\frac{P_j[TF_j]}{K_{i,14}}$ and $\frac{[TF_j]}{K_{i,14}}$ is quantitatively more important. Thirdly, as the number of 280 CaM-binding proteins increases, the contribution of each protein to both summation terms 281 becomes less important. When there are only relatively few CaM-binding proteins, changing 282 the concentration of one can change the value of both terms to a relatively large extent. 283 However, if there are many CaM-binding proteins, changing the concentration of one will 284 change the value of both terms to a much lesser extent. For example, we consider that 285 $P_j = 1.0, K_{j,14} = 1.0 \ \mu\text{M}, \ [TF_j] = 100 \ \mu\text{M}$ with j = 1...n. When one TF, TF_i, coexists with 286 another TF, TF_j, increasing $[TF_i]$ from 10 μ M to 100 μ M leads to that $\sum_{j=1}^{n} \frac{P_j[TF_j]}{K_{j,1,4}}$ increases 287 to 200 from 110, namely an approximate increase of 82% in $\sum_{j=1}^{n} \frac{P_j[TF_j]}{K_{j,14}}$. However, when one 288 TF, TF_i, coexists with another 100 TF, TF_i, increasing $[TF_i]$ from 10 μ M to 100 μ M leads to 289 that $\sum_{j=1}^{n} \frac{P_j[TF_j]}{K_{j,1,4}}$ increases to 10100 from 10010, namely an approximate increase of 0.9% in 290 $\sum_{j=1}^n \frac{P_j[TF_j]}{K_{j,1,4}}.$ 291

Thus, existence of a large number of CaM-binding proteins forms a buffering system, in which the concentration of a CaM-binding TF-specific active signal is insensitive to changes in the concentration of another CaM-binding TF or protein. An example of this is shown in Fig. 2.

In this example, we assume that $[TF_1]_t$, the total concentration of a CaM-binding 296 transcription factor, TF₁ is 10 μ M. We compare how [4Ca²⁺-CaM-TF₁], which is the 297 concentration of the active signal of TF₁, depends upon the concentration of a CaM-binding 298 protein when different numbers of other CaM-binding proteins coexist. Fig. 2A represents an 299 experimentally measured calcium signature (Whalley et al., 2011). Fig. 2B shows that, when 300 the transcription factor, TF_1 , competes for CaM binding with one CaM-binding protein, TF_2 , 301 changing the total concentration of TF_2 , $[TF_2]_t$, from 1 μ M to 10 μ M and 100 μ M markedly 302 affects [4Ca²⁺-CaM-TF₁]. Thus, when the calcium signature, as shown in Fig. 2A, emerges, 303 although the total concentration of the CaM-binding transcription factor TF_1 , $[TF_1]_t$, 304 remains unchanged (i.e. 10 µM), changing the total concentration of the CaM-binding protein 305 TF_2 , $[TF_2]_t$, alters the capability of the transcription factor TF_1 for generating an active 306 307 calcium signal. This is because the concentration of the active signal of the transcription factor TF₁, [4Ca²⁺-CaM-TF₁], has changed due to the competition between the CaM-binding 308 transcription factor, TF₁,and the CaM-binding protein, TF₂, for binding with CaM. In Fig. 309 2C, the number of CaM-binding proteins TF_i increases to 11 (i.e. j=2,...12). Since the 310 number of CaM-binding proteins has increased, changing the total concentration of one CaM-311 binding protein, [TF₂]_t (the concentrations of other 10 CaM-binding proteins remain 312 unchanged), from 1 μ M to 10 μ M and 100 μ M only slightly affects [4Ca²⁺-CaM-TF₁]. 313 Moreover, when the number of CaM-binding proteins TF_i further increases to 101 (i.e. 314 i=2,...102), the effects of changing the total concentration of one CaM-binding protein, $[TF_1]_t$ 315 , from 1 μ M to 10 μ M and 100 μ M on [4Ca²⁺-CaM-TF₁] becomes negligible (Fig. 2D). Thus, 316 when a large number of CaM-binding proteins coexist, a calcium signature, as shown in Fig. 317 2A, can generate a TF specific active signal, [4Ca²⁺-CaM-TF₁], to mediate specific changes 318 319 in gene expression. The concentration of such an active signal is insensitive to changes in the concentration of other CaM-binding proteins. Therefore, the existence of a large number of 320 321 CaM-binding proteins results in the fidelity of a calcium signature to its TF specific active signal. 322

In addition, Fig. 2E shows that the concentration of the active calcium signal of TF_1 , [4Ca²⁺-CaM-TF₁], is always amplified regardless of the number of CaM-binding proteins. Therefore, the coexistence of a large number of CaM-binding proteins in plant cells does not affect the intrinsic property of amplifying calcium signatures for Ca²⁺-CaM-TF interactions. In this way, the nonlinear amplification of calcium signatures, as demonstrated in Fig. 2E, allows plant cells to effectively distinguish the kinetics of different calcium signatures to produce specific changes in gene expression, in spite of the coexistence of a large number ofCaM-binding proteins in plant cells.

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332 Specific gene expression responses to calcium signatures require an appropriate 333 relationship between the active signal concentration and DNA binding affinity

Gene expression is a complex process, which involves both transcription and mRNA degradative processes. Both processes can be regulated in response to signalling. For example, transcriptional processes can be regulated by calcium signals (Reddy et al., 2011; Seybold et al., 2014; Fromm and Finkler, 2015; Tsuda and Somssich, 2015; Zhu, 2016). Moreover, gene expression can form a network, in which the expression of one gene can be regulated by other genes (Reddy et al., 2011; Seybold et al., 2014; Fromm and Finkler, 2015; Tsuda and Somssich, 2015; Zhu, 2016).

Here we concentrate on elucidating the mechanism for the information flow from calcium signals to a specific gene expression response. To do so, we consider a simple Ca^{2+} regulated gene expression process: transcriptional rate is regulated by calcium signals. The principle revealed by this simple example can be applied to more complex gene expression processes, as will be demonstrated in the Section "*Case study 2: plant immunity gene expression*".

Eq. 4 describes that the transcription of a gene that is positively regulated by calcium signals.

348
$$\frac{d[mRNA]}{dt} = V - k_{decay}[mRNA] \qquad (eq. 4)$$

349 with $V = k_{base} + \frac{V_{max} \frac{[4Ca^{2+} - CaM - TF_i]}{k_d}}{1 + \frac{[4Ca^{2+} - CaM - TF_i]}{k_d}}$. Here, V is the transcription rate; k_{decay} is the decay

constant of the mRNA; k_{base} is the base rate of transcription; V_{max} is the maximal transcription rate regulated by calcium signals, k_d is the binding affinity between the active complex, $4Ca^{2+} - CaM - TF_i$, and DNA.

As analysed above, when any calcium signature emerges in an environment of multiple proteins competing for CaM binding, $[Ca^{2+}]$ is amplified into a robust TF-specific active complex for any CaM binding transcription factor, $4Ca^{2+} - CaM - TF_i$. Eq. 4 shows that, since $4Ca^{2+} - CaM - TF_i$ is always amplified for any calcium signature, the transcription rate, *V*, will effectively be different for different calcium signatures, leading to a different specific gene expression response in each case. Examination of eq. 4 reveals how

the relationship of k_{base} , k_d , and $[4Ca^{2+} - CaM - TF_i]$ determines Ca²⁺-regulated gene 359 expression. If $k_{base} \gg \frac{V_{max} \frac{[4Ca^{2+} - CaM - TF_i]}{k_d}}{1 + \frac{[4Ca^{2+} - CaM - TF_i]}{k_d}}$, the base rate of transcription is more important

360

than the rate regulated by the calcium signal. Thus, the effects of a calcium signature on gene 361 expression are negligible under these particular conditions. If $k_d \gg [4Ca^{2+} - CaM - TF_i]$, 362 the effects of a calcium signature on gene expression is limited, this is because the term 363

$$[4Ca^{2+}-CaM]$$

 $\frac{V_{max}}{1+\frac{[4Ca^{2+}-CaM-TF_{i}]}{k_{d}}}$ can become very small. If $k_{d} \ll [4Ca^{2+}-CaM-TF_{i}]$, the effects of 364

any calcium signature would become approximately a constant V_{max} . Thus, in this case 365 different calcium signatures induce similar transcription rates, leading to similar levels of 366 mRNA. Therefore, in order for a specific gene expression response to calcium signatures to 367 be generated, $[4Ca^{2+} - CaM - TF_i]$ should be not much larger or smaller (e.g. 2 orders 368 larger or smaller) than k_d . Under this condition, different calcium signatures can be decoded 369 to generate specific gene expression responses. Fig. 3 summarises the design principle that 370 governs how the binding mechanism between Ca²⁺, calmodulin (CaM), and transcription 371 factor (TF), which emerges from two pairs of Ca²⁺-binding EF-hand domains, a TF-binding 372 domain in CaM, and a CaM-binding domain in the TF, leading to specific gene expression. 373

In summary, the design principle of Ca²⁺-CaM-TF interactions includes the following 374 three key aspects for information flow from calcium signals to gene expression: 1) nonlinear 375 amplification of a calcium signal; 2) generation of a Ca^{2+} -induced TF-specific active signal; 376 and 3) once the binding affinity between the active calcium signal and DNA is appropriate, 377 specific gene expression responses can be generated. 378

Below, we use two examples to demonstrate how calcium signatures generate specific 379 gene expression responses following the design principle revealed herein. 380

Case study 1: a simple Ca^{2+} -regulated gene expression system 381

To test how the design principle summarised in Fig. 3 governs the decoding of different 382 calcium signatures to generate specific gene expression responses, we first studied a simple 383 theoretical gene expression system described by equation 4 using artificial calcium 384 signatures. An advantage of artificial calcium signatures is that the parameters of different 385 calcium signatures can be compared with each other so that effects of those parameters of 386 calcium signatures on gene expression can be examined. In addition, investigating both 387 artificial calcium signatures in this case study and examining experimentally measured 388

calcium signatures in *case study 2* below allows us to show that the design principle revealedin this research is generic for any calcium signature.

Fig. 4A shows three calcium signatures with the same type of kinetics. All three 391 calcium signatures take a sinusoidal form with the same period, but their amplitudes are 392 different. For simplicity we study one period of these sinusoidal calcium signatures only. Fig. 393 4B shows that a relatively modest change in the amplitude of these three calcium signatures 394 (0.2 µM to 0.4 µM) is amplified into large fold differences in the concentration of the active 395 signal, $[4Ca^{2+} - CaM - TF_i]$. Subsequently, this large difference in the concentrations of 396 the three active signals leads to different fold changes of mRNA concentration, Fig. 4C. We 397 398 emphasize that the large difference (from ca. max. 6 fold to ca. max. 58 fold) in mRNA concentrations in Fig. 4C stems entirely from the relatively modest difference in the 399 amplitude of the three calcium signatures (0.2µM to 0.4µM), as the kinetics of the three 400 calcium signatures is the same. Derivation of equation 2 in Supplemental Information reveals 401

that the term $\left(\frac{[Ca^{2+}]}{[Ca^{2+}]_{rs}}\right)^4$ emerges from two pairs of Ca²⁺-binding EF-hand domains and a TF-402 binding domain in the CaM structure. Therefore, the ability of CaM to bind four Ca²⁺ and one 403 TF molecule results in the amplification of calcium signal. Fig. 4D further shows that the fold 404 change of $[4Ca^{2+} - CaM]$ is approximately the same as that of $[4Ca^{2+} - CaM - TF_i]$, as 405 shown in Fig. 4B, and this is also confirmed in Fig. 4E. Therefore, Fig. 4B, D, and E together 406 reveal that the amplification of the calcium signatures, shown in Fig. 4A, is originated from 407 two pairs of Ca²⁺-binding EF-hand domains in the CaM structure and that it is further relayed 408 to the binding between $4Ca^{2+} - CaM$ complex and transcription factor. 409

Fig. 4F shows three calcium signatures with the same average calcium concentration 410 $(0.2 \ \mu M)$. The difference between the three calcium signatures is their kinetics. Fig. 4G 411 shows that these relatively slight differences in the kinetics of these three calcium signatures 412 is amplified into the kinetics of the active signal, $[4Ca^{2+} - CaM - TF_i]$. Subsequently, the 413 difference in the kinetics of the three active signals leads to different fold changes of mRNA 414 concentration, Fig. 4H. We emphasize that the difference (from ca. max. 80 fold to ca. max. 415 148 fold) in the fold change of mRNA concentrations in Fig. 4H stems solely from the 416 difference in the kinetics of the three calcium signatures, as the average calcium 417 concentration is the same for the three calcium signatures. Following the analysis represented 418 by Fig. 4D and 4E, Fig. 4G, I, and J together reveal that the amplification of the calcium 419 signatures shown in Fig. 4F also originates from two pairs of Ca²⁺-binding EF-hand domains 420

421 in the CaM structure and that it is further relayed to the binding between $4Ca^{2+} - CaM$ 422 complex and transcription factor.

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Therefore, Fig. 4A-J show that different calcium signatures, displaying only modest differences, can generate very different specific gene expression responses following the design principle.

Another aspect of the design principle is that when a large number of CaM-binding proteins coexist, a calcium signature is able to generate a specific gene expression response, which is not affected by the concentrations of another CaM-binding protein. The numerical analysis shown in Fig. 5 confirms that, when a large number of CaM-binding proteins coexist, the gene expression response of the simple system remains the same even if the concentration of a CaM-binding protein has changed from 0.01 μ M to 10000 μ M.

When the calcium signature shown in Fig. 5A emerges and if one protein and one 433 transcription factor compete for binding with CaM simultaneously, changing the protein 434 concentration affects the TF-specific gene expression, resulting in different fold changes of 435 mRNA, Fig. 5B. However, when a large number of CaM-binding proteins (here 101 proteins) 436 and one transcription factor compete for the binding of CaM, changing the concentration of 437 one CaM-binding protein out of 101 (i.e. the concentration of the remaining 100 CaM-438 binding proteins remains unchanged) does not affect the TF-specific gene expression, 439 resulting in no different fold changes of mRNA, Fig. 5C. Therefore, when many proteins 440 441 compete for CaM binding, specific gene expression responses to calcium signatures are robust, and TF-specific. This is because the concentration of a CaM-binding TF-specific 442 443 active signal is insensitive to changes in another CaM-binding TF or protein concentration when a large number of CaM-binding proteins coexist, as analysed in Fig. 2. 444

Fig. 4 and 5 together explain how the interaction between Ca^{2+} , CaM, and the CaMbinding transcription factor induces specific gene expression responses in the simple Ca^{2+} regulated gene expression process described by equation 4. Therefore, this demonstrates that the design principle, shown in Fig. 3, establishes the link between calcium signatures and specific gene expression responses induced by the signatures.

The dynamics for the interactions between Ca²⁺, CaM, and CaM-binding proteins can be generally examined using differential equations (Pepke et al., 2010; Liu et al., 2015; Lenzoni et al., 2018). If a quasi-equilibrium state for the interactions of Ca²⁺, CaM, and CaMbinding proteins has been established, all differential equations describing the interactions

between Ca²⁺, CaM, and CaM-binding proteins become zero and equations 1-3 can be 454 derived. Fig. 5D further examines the validity and effects of the quasi-equilibrium 455 assumption for deriving equations 1-3. Fig. 5D shows that, for experimentally measured 456 parameters of Ca²⁺-CaM binding constants (Shifman et al., 2006; Pepke et al., 2010), the 457 gene expression response curve computed without the quasi-equilibrium assumption for the 458 interactions of Ca²⁺, CaM, and CaM-binding proteins (i.e. differential equations) overlaps 459 with the gene expression response curve computed with the quasi-equilibrium assumption 460 (i.e. equation 3), indicating that a quasi-equilibrium state of $Ca^{2+}-CaM$ –TF interaction in 461 plant cells has been established. 462

Although the quasi-equilibrium state assumption is valid for experimentally measured 463 parameters of Ca²⁺-CaM binding constants, reducing those parameters may make the 464 assumption invalid. We further test how validity of the assumption affects gene expression 465 responses. When all "on" and "off" rate constants for Ca²⁺-CaM interactions are 466 simultaneously reduced by the same fold from their experimentally measured values 467 (Shifman et al., 2006; Pepke et al., 2010), the equilibrium constants for all Ca^{2+} -CaM binding 468 processes remain the same as the experimental values. This is because an equilibrium 469 constant is the ratio between the "off" rate constant and the "on" rate constant. However, if 470 all "on" and "off" rate constants are simultaneously reduced, the quasi-equilibrium 471 assumption may become invalid due to slow binding rates. Fig. 5D shows that when all "on" 472 and "off" rate constants for Ca²⁺-CaM interactions are simultaneously reduced by 100 fold, 473 the quasi-equilibrium assumption becomes invalid. Once this happens, the calcium signature, 474 475 as shown in Fig. 5A, is less capable of inducing a gene expression response. In addition, Fig. 5D also shows that very small Ca²⁺-CaM "on" and "off" rate constants (i.e. they are reduced 476 by 1.0E4 fold from their experimental values) render gene expression response to calcium 477 signatures impossible. This implies that establishing a quasi- equilibrium state is favourable 478 for a calcium signature to induce gene expression responses. 479

Another important aspect of the design principle, as described in Fig. 3, is that specific gene expression responses to calcium signatures require an appropriate relationship between the active signal concentration, $[4Ca^{2+} - CaM - TF_i]$, and DNA binding affinity. The dissociation equilibrium constant (i.e. the binding affinity) for the binding of the Ca²⁺-CaM complex to a transcription factor is an important parameter. Changing the value of the dissociation equilibrium constant changes $[4Ca^{2+} - CaM - TF_i]$, and therefore affects the relationship between $[4Ca^{2+} - CaM - TF_i]$ and DNA binding affinity. Supplemental Fig. S1

shows the effects of the dissociation equilibrium constant for the binding of the Ca²⁺-CaM 487 complex to a transcription factor, K_{14} , on gene expression regulated by the transcription 488 factor. Supplemental Fig. S1A shows an artificial calcium signature. Supplemental Fig. S1B 489 shows that decreasing the value of K_{14} increases the steady-state value of $[4Ca^{2+} - CaM -$ 490 TF_i]. Similarly, Supplemental Fig. S1C shows that decreasing the value of K₁₄ increases the 491 value of $[4Ca^{2+} - CaM - TF_i]$ responding to the calcium signature. Supplemental Fig. S1D 492 shows that, for the three different values of K_{14} , the calcium signature is always amplified. 493 494 Supplemental Fig. S1E, F, and G show that, although decreasing the value of K₁₄ increases both the steady-state mRNA concentration and the mRNA concentration responding to the 495 496 calcium signature, three different values of K₁₄ lead to three different responses of mRNA concentration to the calcium signature. Therefore, different transcription factors with 497 different values of K_{14} can generate different responses of mRNA concentration to a calcium 498 signature. This indicates that the dissociation equilibrium constant for the binding of the 499 Ca^{2+} -CaM complex to a transcription factor, K_{14} , is an important parameter for specific gene 500 expression responses to a calcium signature. Similarly, analysis in Figure S2 for a different 501 502 artificial calcium signature also supports the above conclusion.

503 In summary, this example shows that, for the simple gene expression system 504 described by equation 4, different calcium signatures can be decoded to generate specific 505 gene expression responses following the design principle, as described in Fig. 3.

506 Case study 2: plant immunity gene expression

The CaM-binding transcription factors CAMTA3 (AtSR1) and CBP60g regulate the 507 expression of two important plant immunity genes: enhanced disease susceptibility 1 (EDS1) 508 and isochorismate synthase 1 (ICS1) (Zhang et al., 2010; Zhang et al., 2014). Recently, we 509 developed a dynamic model to determine how expression of both EDS1 and ICS1 is regulated 510 by different calcium signatures and analysed the model using computer simulation of 511 differential equations (Lenzoni et al., 2018). It was demonstrated that the model was able to 512 predict the expression of both EDS1 and ICS1 (Lenzoni et al., 2018). Here we use this system 513 514 as an example to study how the expression response of both EDS1 and ICS1 to calcium signatures is generated following the design principle, as shown in Fig. 3. 515

Fig. 6A and B show two empirically-derived calcium signatures induced by two calcium agonists: mastoparan and extracellular calcium (Lenzoni et al., 2018). The model developed for studying how expression of both *EDS1* and *ICS1* (Lenzoni et al., 2018) is regulated by different calcium signatures employed experimentally measured parameters for

both Ca²⁺-CaM binding (Shifman et al., 2006; Pepke et al., 2010) and CaM-CAMTA3 520 binding (Bouche et al., 2002; Finkler et al., 2007). Fig. 6C and F show that, for these 521 experimentally measured "on" and "off" rate constants for Ca²⁺-CaM interactions, the curve 522 calculated using differential equations overlaps with the curve calculated using equation 3 for 523 both $[4Ca^{2+} - CaM - CAMATA3]$ and $[4Ca^{2+} - CaM - CBP60g]$, indicating that the 524 quasi-equilibrium assumption for interactions of Ca²⁺-CaM-CAMTA3 and Ca²⁺-CaM-525 CBP60g, as well as the interactions of Ca²⁺, CaM, and 100 other CaM-binding proteins are 526 valid. Thus, the two active signals in Fig. 6C and F, 4Ca²⁺-CaM-CAMTA3 and 4Ca²⁺-CaM-527 CBP60g, are differentially induced by the two calcium signatures (Fig. 6A and B). Moreover, 528 Supplemental Fig. S3C and F show that the two active signals are effectively and 529 differentially amplified. 530

However, when both "on" and "off" rate constants for Ca²⁺-CaM interactions are 531 reduced by 1.0E5 fold from their experimental values, the quasi-equilibrium assumption for 532 533 deriving equation 3 becomes invalid, as evidenced by the differences between the curve calculated using differential equations and the curve calculated using equation 3 (Fig. 6D and 534 G). Moreover, the two active signals in Fig. 6D and G, $4Ca^{2+}-CaM-CAMTA3$ and $4Ca^{2+}-CaM-CAMTA3$ 535 CaM-CBP60g, are both less effectively amplified (Supplemental Fig. S3D and G) than in Fig. 536 6C and F, indicating that a valid quasi-equilibrium assumption makes the amplification of 537 both active signals more favourable. In addition, when the "on" and "off" rate constants are 538 reduced by 1.0E8 fold, the two active signals, 4Ca²⁺-CaM-CAMTA3 and 4Ca²⁺-CaM-539 CBP60g, cannot respond to either of the two calcium signatures (Fig. 6A and B), as 540 evidenced by the overlapping of the two flat curves corresponding to the two calcium 541 signatures in Fig. 6E and H. Furthermore, neither of the two active signals in Fig. 6E and H 542 can be amplified anymore under these conditions (Supplemental Fig. S3E and H), indicating 543 that very small Ca²⁺-CaM "on" and "off" rate constants render amplification of calcium 544 signals impossible. 545

CAMTA3 and CBP60g are the transcription factors that regulate the expression of 546 EDS1 and ICS1, respectively (Zhang et al., 2010; Zhang et al., 2014). These correspond to 547 the two active signals shown in Fig. 6C and F, the two calcium signatures inducing different 548 mRNA levels for both EDS1 and ICS1 genes (Fig. 7A and D), leading to specific gene 549 expression responses for both genes. Moreover, since the curve calculated using differential 550 equations overlaps with the curve calculated using equation 3 for the fold change of mRNA 551 of both EDS1 and ICS1 (Fig. 7A and D), gene expression responses of both EDS1 and ICS1 to 552 the two calcium signatures clearly follow the design principle (Fig. 3 and equations 1-3). 553

When the "on" and "off" rate constants for Ca²⁺-CaM interactions are reduced by 554 1.0E5 fold, Fig. 7B and E show that less effective amplification of both active signals, $4Ca^{2+}$ -555 CaM-CAMTA3 and 4Ca²⁺-CaM-CBP60g (Fig. 6D and G, S3D and G), markedly affects the 556 mRNA level of both ICS1 and EDS1. Furthermore, when the "on" and "off" rate constants 557 for Ca²⁺-CaM interactions are reduced by 1.0E8 fold, no amplification of either of the two 558 active signals, 4Ca²⁺-CaM-CAMTA3 and 4Ca²⁺-CaM-CBP60g, occurs (Fig. 6E and H, S3E 559 and H), leading to no change in expression of either EDS1 or ICS1. This is evidenced by the 560 overlapping of the two flat curves corresponding to the two calcium signatures in Fig. 7C and 561 F, showing no change in gene expression response to either signature. 562

In conclusion, for experimentally measured "on" and "off" rate constants (Shifman et 563 al., 2006; Pepke et al., 2010), the two calcium signatures (Fig. 6A and B) are decoded 564 following design principle to generate specific expression of both EDS1 and ICS1 (Fig. 7A 565 and D). If the "on" and "off" rate constants for Ca²⁺-CaM interactions are largely reduced 566 (e.g. 1.0E8 fold), specific gene expression responses to the two calcium signatures become 567 impossible (Fig. 7C and F). Therefore, the actual values of "on" and "off" rate constants for 568 Ca^{2+} -CaM interactions, as experimentally measured in the literature (Shifman et al., 2006; 569 Pepke et al., 2010), ensure that plant immunity gene expression responses of both EDS1 and 570 ICS1 follow the design principle to decode the two calcium signatures induced by two 571 calcium agonists: mastoparan and extracellular calcium (Fig. 6A and B). 572

573

574 **DISCUSSION**

575 Most stimuli lead to a transient elevation in cellular calcium concentration in plant cells. 576 Importantly, different stimuli produce calcium elevations with different characteristics: a 577 unique "calcium signature". These calcium signatures are decoded to generate specific 578 responses (Edel et al., 2017; Yuan et al., 2017; Bender et al., 2018; Kudla et al., 2018). An 579 intriguing question is how can one messenger (Ca²⁺) be decoded by so many decoders 580 (transcription factors and proteins) in plant cells (Edel et al., 2017)?

Design principles are the underlying properties of network structures that have 581 evolved to endow the network functions. This work reveals the design principle for decoding 582 calcium signals to generate specific gene expression response in plant cells via transcription. 583 The design principle links the structural characteristics of CaM and TF with the capability of 584 decoding calcium signatures in plant cells, and it therefore reveals how the mechanism of 585 Ca²⁺, CaM, and TF interactions leads to specific gene expression. It includes the following 586 three important aspects: Firstly, the binding mechanism between Ca²⁺, CaM, and TF, which 587 emerges from two pairs of Ca²⁺-binding EF-hand domains and a TF-binding domain in the 588 CaM structure, possesses an intrinsic property of amplifying calcium signals in the format 589

of $\left(\frac{[Ca^{2+}]}{[Ca^{2+}]s}\right)^4$ being multiplied by a factor that is relatively less important. We derived the 590 equations for describing the amplification of calcium signals (equations 1 and 2) and 591 mathematically proved that calcium signals are always amplified (Supplemental 592 593 Information). Since any calcium signature is always amplified, small differences in the 594 kinetics or parameters of calcium signatures can be read out to generate relatively much larger specific gene expression responses (Fig. 4 and 5). Secondly, the existence of a large 595 596 number of CaM-binding TFs or proteins in plant cells (Reddy et al., 2011; Poovaiah et al., 2013; Virdi et al., 2015; Edel et al., 2017; Yuan et al., 2017; Bender et al., 2018; Kudla et al., 597 2018) can form a buffering system such that the concentration of a CaM-binding TF-specific 598 active signal is insensitive to changes in the concentration of another CaM-binding TF or 599 protein (Fig. 2D). Thus, although many proteins compete for the binding of CaM, Ca²⁺-600 induced TF-specific gene expression will not in fact be affected by the concentration of 601 602 another CaM-binding TF or protein (Fig. 5C) in plant cells. Although a TF-specific gene expression event must be controlled by the concentration of this transcription factor, it would 603 not be advantageous if it can also be altered by changes in the concentrations of other 604 proteins. This is a clear example of inbuilt robustness of the network endowed by the design 605 principle. Our results also show that when a CaM-binding TF competes for CaM binding 606

with one or a few CaM-binding TFs and proteins, gene expression regulated by a CaM-607 binding TF will be interfered with by another CaM-binding TF or protein (Fig. 5C). Thus, 608 competition of CaM-binding TFs or proteins for CaM binding may have a role in the 609 relationship between calcium signals and gene expression response if a small number of 610 CaM-binding TFs or proteins exist in plant cells. Interestingly, for postsynaptic cells, a model 611 in which 6 proteins compete for CaM binding, competition plays a role in setting the 612 frequency-dependence of Ca^{2+} -dependent proteins (Romano et al., 2017), and therefore it was 613 suggested that competitive tuning could be an important dynamic process underlying synaptic 614 615 plasticity. Therefore, both our work and the results in the literature (Romano et al., 2017) suggest that competition of a small number of CaM-binding proteins will cause that the 616 response of one CaM-binding protein to calcium signals to be affected by other CaM-binding 617 proteins. Thirdly, an appropriate relationship between a Ca²⁺-induced TF-specific active 618 signal concentration and its DNA binding affinity is important for a Ca²⁺-induced TF-specific 619 gene expression response. For a Ca²⁺-induced TF-specific active signal to generate gene 620 expression responses, its concentration needs to be similar to the binding affinity between the 621 signal and DNA. In general, for any binding to perform biological functions, the affinity 622 between a ligand and its binding partner should not be very different from the concentration 623 624 of the ligand (e.g. the differences not larger than 2 orders) (Kuriyan et al., 2013). Our analysis reveals this aspect is also applicable to Ca^{2+} -induced gene expression systems. 625

We used two examples to show how gene expression follows the design principle to 626 decode different calcium signatures. Gene expression is generally regulated in a complex way 627 628 (Karlebach and Shamir, 2008). The simplest gene expression process includes: (1) gene transcription is activated or supressed by a transcription factor; and (2) the mRNA decays. 629 630 Our first example tested how a simple gene expression system decodes different calcium signatures. We found that different kinetics or different parameters (here testing amplitudes 631 of a sinusoidal calcium signature) could be decoded following the design principle. 632 Therefore, this example demonstrated that different calcium signatures, even if their 633 differences are modest (Fig. 4A and F), can generate specific gene expression responses (Fig. 634 4C and H) following the design principle. Experimentally any, even a modest, calcium 635 signature (e.g. in response to ozone (Clayton et al., 1999)) is able to induce gene expression. 636 Therefore, our results, shown in Fig. 4 and 5, imply that the design principle is a general 637 principle for governing the decoding of calcium signatures in simple gene expression 638 systems, in which transcription rates are regulated by calcium signals. 639

The second example showed that expression of two plant immunity genes (EDS1 and 640 *ICS1*) follows the design principle to decode two empirical calcium signatures induced by 641 two calcium agonists (mastoparan and extracellular calcium). Calcium signals regulate the 642 expression of EDS1 and ICS1 at two levels. First, CAMTA3 and CBP60g are well 643 characterized Ca²⁺/CaM-regulated transcription factors and both have a CaM binding domain 644 (Finkler et al., 2007; Galon et al., 2008; Kim et al., 2009; Wang et al., 2009; Zhang et al., 645 2010; Reddy et al., 2011; Wang et al., 2011; Bickerton and Pittman, 2012; Poovaiah et al., 646 2013). Thus, calcium signals regulate the activities of both CAMTA3 and CBP60g. Second, 647 648 expression of EDS1 and ICS1 forms a regulatory network (Zhang et al., 2014; Lenzoni et al., 2018) and their expression is regulated by each other via this network (Zhang et al., 2014; 649 Lenzoni et al., 2018). In spite of this complexity in regulating the expression of *EDS1* and 650 ICS1, the design principle still governs the expression of both EDS1 and ICS1. Thus, our 651 results, shown in Fig. 6 and 7, imply that design principle is a general principle for governing 652 the decoding of calcium signature in complex gene expression systems, in which multiple 653 transcription factors are regulated by calcium signals and gene expression itself forms a 654 655 regulatory network.

The design principle, as described in Fig. 3 and summarised above, is generic for 656 657 elucidating the decoding of calcium signals which generate specific gene expression responses via transcription. Therefore, it can be integrated with a wide range of experimental 658 659 analysis. For example, we have shown how to study gene expression for both simple and complex systems that are regulated by any calcium signatures (Fig. 4-7). Arabidopsis genes 660 661 responding to simultaneous biotic and abiotic stresses have been experimentally identified (Atkinson et al., 2013). Following the analysis shown in Fig. 6 and 7, any genes that are 662 regulated by calcium signals under both biotic and abiotic conditions could be theoretically 663 investigated based on the experimental measurements of gene expression corresponding to 664 the relevant calcium signatures. In addition, the role of CaM binding to CAMTA3 in 665 regulating immunity genes was experimentally investigated (Kim et al., 2017). The design 666 principle could be used to quantitatively analyse this role for different binding domains 667 within CAMTA3. It should be noted that this requires experimental inputs to provide 668 parameters. For example, the binding affinity constant of CaM to CAMTA3 in the presence 669 of Ca2+ had been experimentally measured (Bouche et al., 2002; Finkler et al., 2007). 670 671 Therefore, it is important that future experiments measure such parameters for the binding between CaM and other (than CAMTA3) CaM-binding proteins. CaM and other calcium-672 binding proteins have the potential to regulate and modify calcium signatures themselves. We 673

could address this important aspect of calcium signalling in the future. Some genes regulated 674 by calcium signatures encode proteins with roles in transporting/binding calcium in plant 675 cells (Kudla et al., 2010; Delormel and Boudsocq, 2019). To further study the effects of gene 676 expression on the generation of calcium signatures, the design principle established in this 677 work could in the future be combined with the processes for generation of calcium signature 678 (Medvedev, 2018). This may be important in understanding alterations in calcium signatures 679 as a result of acclimation to stress, and due to interaction between different stresses. For 680 example, the design principle developed in this work can be used to study the effects of the 681 682 concentrations of CaM and transcription factors on the mRNA levels of gene expression, which can be linked with the processes of calcium transport to quantitatively examine the 683 effects of mRNA levels on generation of calcium signature in the future. In order to further 684 validate the design principle we present here, the plant immunity system would be a good 685 model. Future experiments could involve complementation of *camta3* and *cbp60g* mutants 686 with CAMTA3 and CBP60g in which the protein coding regions have been modified to alter 687 binding constants to DNA and CaM. The effect of these altered affinities could be predicted 688 using our mathematical model, and tested empirically in the complemented lines by 689 690 measuring *ICS1/EDS1* gene expression in response to applied calcium signatures.

691

Calcium signals are the lead currency of plant information processing (Dodd et al., 692 2010; Kudla et al., 2010), and they regulate many different responses in plant cells. However, 693 little is known about the underlying principle for how information flows from calcium signals 694 695 to specific gene expression responses in plant cells. This work reveals the underlying principles for linking the structure of CaM and TF molecule with calcium-regulated gene 696 expression response through Ca²⁺-CaM-TF binding mechanism and the emerging property of 697 calcium signal amplification. The design principle indicates that the existing interaction 698 network of Ca²⁺, CaM, and proteins, which may have been evolutionarily tuned (Edel et al., 699 2017), effectively navigates calcium signatures to generate specific gene expression responses 700 in plant cells. Experimental data have shown multiple levels of complexities in decoding 701 calcium signals in plant cells (Edel et al., 2017; Yuan et al., 2017; Bender et al., 2018; Kudla 702 et al., 2018). Plants cells possess four main types of Ca^{2+} sensor proteins to relay or decode 703 Ca2+ signalling: CaM, CaM-like proteins (CMLs), calcineurin B-like proteins (CBLs), and 704 Ca²⁺-dependent protein kinases (CDPKs or CPKs) (Yuan et al., 2017). These proteins relay 705 or decode calcium signals at both the transcriptional and post-translational levels (Yuan et al., 706 2017). This work has focused on the interactions between Ca^{2+} , CaM, and TFs at 707

708 transcriptional level and revealed that transcriptional decoding of calcium signals follows a general design principle. Other Ca²⁺ sensor proteins can have different numbers of Ca²⁺-709 binding sites or possess complex molecular structures. For example, CMLs may have one to 710 six EF-hands and one to four Ca²⁺-binding sites (La Verde et al., 2018). A Ca²⁺/CaM-711 dependent protein kinase (CCaMK) possesses three additional Ca²⁺-binding sites in addition 712 to its CaM-binding site (Miller et al., 2013). Our methodology for unravelling the design 713 principle for transcriptional decoding of calcium signals may be further developed to study 714 the underlying general principle for other Ca^{2+} -regulated signalling systems in the future. 715 716

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717 MATERIALS AND METHODS

718 Ca^{2+} -CaM-protein interactions

The interaction between Ca^{2+} , CaM, and any protein can form different binding complexes. 719 CaM has two pairs of Ca²⁺-binding EF-hand domains located at the N-and C-terminus, 720 respectively (Finn and Forsen, 1995; Valevev et al., 2008). Thus, for a protein with one 721 calmodulin binding site, 18 different binding complexes can form via 33 elementary binding 722 processes. A detailed description of these interactions is previously presented in detail (Liu et 723 al., 2015; Lenzoni et al., 2018), and the 33 elementary binding processes are included in 724 Table S1 in Supplemental Information. Experimentally measured parameters for the 725 interactions between Ca²⁺ and CaM are included in Table S2. 726

727 Modelling expression of plant immunity genes

The model used to examine expression of plant immunity genes (*ICS1* and *EDS1*) was previously described in detail (Lenzoni et al., 2018). The differential equations and parameters of the model were included in the previous work (Lenzoni et al., 2018). This work uses this model to study how expression of both *ICS1* and *EDS1* decodes calcium signatures following the design principle.

733 Numerical Method

734 All computational results are generated using simulator Berkeley Madonna (www.berkeleymadonna.com). For differential equations, Rosenbrock (Stiff) method is used 735 736 with a tolerance of 1.0e-5. Much smaller tolerances (1.0E-6 to 1.0E-8) are also tested and the numerical results show that further reduction of tolerances does not improve the accuracy of 737 738 numerical results.

739

740 Accession Numbers

- 741 *EDS1*: AT3G48090 (https://www.arabidopsis.org/servlets/TairObject?id=39706&type=locus)
- 742 *ICS1*: AT1G74710 (https://www.arabidopsis.org/servlets/TairObject?id=28521&type=locus)
- 743

744 SUPPLEMENTAL DATA

Supplemental Figure S1. . Effects of K_{14} , the dissociation equilibrium constant for the binding of the Ca²⁺-CaM complex to the ith TF, on gene expression regulated by the TF for calcium signature shown in Figure S1A.

- Supplemental Figure S2. Effects of K_{14} , the dissociation equilibrium constant for the binding of the Ca²⁺-CaM complex to the ith TF, on gene expression regulated by the TF for calcium signature shown in Figure S2A.
- 751 Supplemental Figure S3. Two calcium signatures are decoded to generate specific expression
- of *EDS1* and *ICS1* following design principle: responses of two active signals, $4Ca^{2+}-CaM^{-1}$
- 753 CAMTA3 and $4Ca^{2+}$ -CaM-CBP60g, to two experimentally measured calcium signatures.
- 754
- Supplemental Table S1. Interactions of Ca^{2+} , calmodulin (CaM), and one transcription factor.
- 757 Supplemental Table S2. Experimentally measured parameters for the interactions between 758 Ca^{2+} and CaM.
- 759
- 760

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764 FIGURE LEGENDS

Figure 1. Ca²⁺-CaM-TF interactions always amplify calcium signals. The parameter for the 765 cooperative binding between CaM and a TF in the presence of Ca^{2+} is P. A. value of function 766 f for P=0.1. Scatter crosses are the theoretical minimum value of f. Blue, red, and green 767 curves correspond to the total concentration of TF, $[TF]_t$, to be 0.01µM, 10 µM, and 1.0E5 768 μ M, respectively. The blue and red curves overlap, indicating that the numerical values of f 769 are always the same for the two concentrations of TF. B. Corresponding to Fig. 1A, , 770 $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$ value for P=0.1 is calculated using equation 2. C. Value of function f for 771 P=1.0E-4. Blue, red, and green curves correspond to total concentration of TF, $[TF]_t$, to be 772 0.01 µM, 10 µM, and 1.0E5 µM, respectively. The green curve and the scatter crosses 773 overlap, indicating that the numerical values of f for $[TF]_t = 1.0E5 \ \mu M$ are always the same 774 as the theoretical minimum value of f. D. Corresponding to Fig. 1C, $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$ value 775 for P=1.0E-4 is calculated using equation 2. 776

Figure 2. Effects of changing the concentration of a CaM-binding protein on the concentration of a CaM-binding TF-specific active signal when the TF and different numbers of CaM-binding proteins coexist. A. An experimentally measured calcium signature (Whalley

et al., 2011). The calcium signature is used to calculate $[4Ca^{2+}-CaM-TF_1]$ following equation 780 3. B. The TF coexists with one protein. Blue, red, and green curves correspond to the 781 concentration of the protein to be 1 µM, 10 µM, and 100 µM, respectively. C. The TF 782 coexists with 11 proteins. Concentrations of 10 proteins are fixed to be 100 µM. Blue, red, 783 and green curves correspond to the concentration of the remaining protein to be 1 µM, 10 784 μM, and 100 μM, respectively. D. The TF coexists with 101 proteins, 100 proteins of which 785 have the same fixed concentration: 100 µM. Blue, red, and green curve corresponds to the 786 concentration of the remaining protein to be 1 µM, 10 µM, and 100 µM, respectively. The 787 788 three curves overlap, indicating that changing the concentration of the remaining protein does not affect [4Ca²⁺-CaM-TF₁]. E. $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$ for all nine curves shown in Fig. 2B and C, 789 indicating that, for all nine cases, the maximum of $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$ reaches at least 9000 790 fold. 791

Figure 3. Diagram showing the design principle for transcriptional decoding calcium signatures to generate specific gene expression. A. The binding mechanism between Ca^{2+} , calmodulin (CaM), and transcription factor (TF), which emerges from two pairs of Ca^{2+} binding EF-hand domains, and a TF-binding domain in CaM and a CaM-binding domain in TF. B. Nonlinear amplification of Ca^{2+} signal emerges from A. C. An amplified, Ca^{2+} induced, TF-specific active signal for each of CaM-binding TFs emerges from A and B.

Figure 4. Three similar calcium signatures are decoded to generate specific gene expression 798 responses for a simple Ca^{2+} -regulated gene expression process. A. Three artificial calcium 799 signatures with the same sinusoidal kinetics (the period is fixed to be 80 s, and amplitudes are 800 0.2 µM, 0.3 µM, and 0.4 µM, respectively. Only one period of the sinusoidal kinetics is 801 used.) B. $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{sc}}$ calculated using the three calcium signatures in Fig. 4A as the 802 input of equation 3. C. Fold change of mRNA corresponding to the three calcium signatures 803 in Fig. 4A. D. $\frac{[4Ca^{2+}-CaM]}{[4Ca^{2+}-CaM]_{ss}}$ calculated using the three calcium signatures in Fig. 4A as the 804 input of equation 3. E. The ratio of $\frac{[4Ca^{2+}-CaM]}{[4Ca^{2+}-CaM]_{ss}}$ to $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$. This ratio is always 805 equal to 1, indicating that $\frac{[4Ca^{2+}-CaM]}{[4Ca^{2+}-CaM]_{ss}}$ is always the same as $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$. F. Three 806 artificial calcium signatures with the same average calcium concentration (the average of 807 $[Ca^{2+}]$ is 0.2 µM for each of the three curves). G. $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$ calculated using the three 808

calcium signatures in Fig. 4F as the input of equation 3. H. Fold change of mRNA corresponding to the three calcium signatures in Fig. 4F. I. $\frac{[4Ca^{2+}-CaM]}{[4Ca^{2+}-CaM]_{ss}}$ calculated using the three calcium signatures in Fig. 4F as the input of equation 3. J. The ratio of $\frac{[4Ca^{2+}-CaM]}{[4Ca^{2+}-CaM]_{ss}}$ to $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$. This ratio is always equal to 1, indicating that $\frac{[4Ca^{2+}-CaM]}{[4Ca^{2+}-CaM]_{ss}}$ is always the same as $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$.

Figure 5. Effects of the number of CaM-binding proteins or the binding rates on specific 814 gene expression responses for a simple Ca²⁺-regulated gene expression process. A. An 815 artificial calcium signature. B. Effects of the number of CaM-binding proteins on specific 816 gene expression responses. The TF coexists with one protein. Green, red, and blue curve 817 corresponds to the concentration of the protein to be 1 μ M, 10 μ M, and 100 μ M, respectively. 818 C. Effects of the number of CaM-binding proteins on specific gene expression responses. The 819 820 TF coexists with 101 proteins, 100 proteins of which have the same fixed concentration: 100 μ M. Green, red, and blue curve corresponds to the concentration of the remaining protein to 821 822 be 1 µM, 10 µM, and 100 µM, respectively. The three curves overlap, indicating that changing the concentration of the remaining protein does not affect fold change of mRNA. D. 823 Effects of the binding rates on specific gene expression responses. Wide orange curve is 824 calculated using equation 3. Blue curve is calculated using differential equations with all 825 experimentally determined "on" and "off" binding rates (Shifman et al., 2006; Pepke et al., 826 2010). The wide orange curve and the blue curve overlap, indicating a quasi-equilibrium state 827 has established. The red and green curves correspond to the "on" and "off" binding rates are 828 reduced by 100 fold and 1.0E4 fold, respectively. 829

Figure 6. Responses of two active signals, $4Ca^{2+}$ -CaM-CAMTA3 and $4Ca^{2+}$ -CaM-CBP60g, 830 to two experimentally measured calcium signatures. A. Two empirical calcium signatures 831 induced by two calcium agonists: mastoparan and extracellular calcium (Lenzoni et al., 832 2018). B. Enlargement of Fig. 6A, showing the details of the two calcium signatures. C. 833 Response of 4Ca²⁺-CaM-CAMTA3 to the two calcium signatures. Wide solid orange curve 834 and wide dashed orange curve are calculated using the two calcium signatures as the input of 835 equation 3, respectively. Experimentally measured parameters are used. Black and blue 836 curves are calculated using the two calcium signatures as the input of differential equations, 837 respectively. The wide orange curve overlaps with the black curve. The wide dashed orange 838

curve overlaps with the blue curve. These results indicate a quasi-equilibrium state is 839 established. D. Same as Fig. 6C, but both "on" and "off" rate constants for Ca²⁺-CaM 840 interactions are reduced by 1.0E5 fold from their experimental values. E. Same as Fig. 6C, 841 but both "on" and "off" rate constants for Ca²⁺-CaM interactions are reduced by 1.0E8 fold 842 from their experimental values. Black and blue curves are flat and they also overlap, 843 indicating that neither calcium signature can induce changes in $[4Ca^{2+}-CaM-CAMTA3]$. F. 844 Same as Fig. 6C, but it is the response of $4Ca^{2+}$ -CaM-CBP60g to the two calcium signatures. 845 G. Same as Fig. 6F, but both "on" and "off" rate constants for Ca²⁺-CaM interactions are 846 reduced by 1.0E5 fold from their experimental values. H. Same as Fig. 6F, but both "on" and 847 "off" rate constants for Ca²⁺-CaM interactions are reduced by 1.0E8 fold from their 848 experimental values. Black and blue curves are flat and they also overlap, indicating that 849 neither calcium signature can induce changes in [4Ca²⁺-CaM-CBP60g]. 850

Figure 7. Fold change of both *EDS1* and *ICS1* mRNA responding to two experimentally
measured calcium signatures. A. Same as Fig. 6C and F, but it is the fold change of *ICS1*mRNA. B. Same as Fig. 6D and G, but it is the fold change of *ICS1* mRNA. C. Same as Fig.
6E and H, but it is the fold change of *ICS1* mRNA. D. Same as Fig. 6C and F, but it is the
fold change of *EDS1* mRNA. E. Same as Fig. 6D and G, but it is the fold change of *EDS1*mRNA. F. Same as Fig. 6E and H, but it is the fold change of *EDS1* mRNA.

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Figure 1. Calcium signals are always amplified. The parameter for the cooperative binding between CaM and a TF in the presence of Ca²⁺ is P. A. value of function f for P=0.1. Scatter crosses are the theoretical minimum value of f. Blue, red, and green curves corresponds to the total concentration of TF, $[TF]_t$, to be 0.01µM, 10 µM and 1.0E5 µM, respectively. The blue and red curves overlap, indicating that the numerical values of f are always the same for the two concentrations of TF. B. Corresponding to Fig. 1A, , $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]_{ss}}$ value for P=0.1 is calculated using equation 2. C. Value of function f for P=1.0E-4. Blue, red, and green curves correspond to total concentration of TF, $[TF]_t$, to be 0.01 µM, 10 µM and 1.0E5 µM, respectively. The green curve and the scatter crosses overlap, indicating that the numerical values of f for $[TF]_t = 1.0E5 \mu$ M are always the same as the theoretical minimum ovalue option 2D. 2009 responding to Fig. All rights reserved $a^{2+}-CaM-TF$ value for P=1.0E-4 is calculated using equation 2.



Figure 2. Effects of changing the concentration of a CaM-binding protein on the concentration of a CaM-binding TFspecific active signal when the TF and different numbers of CaM-binding proteins coexist. A. an experimentally measured calcium signature (Whalley et al., 2011). The calcium signature is used to calculate [4Ca²⁺-CaM-TF₁] following equation 3. B. The TF coexists with one protein. Blue, red and green curves correspond to the concentration of the protein to be 1 µM, 10 µM and 100 µM, respectively. C. The TF coexists with 11 proteins. Concentrations of 10 proteins are fixed to be 100 μ M. Blue, red and green curves correspond to the concentration of the remaining protein to be 1 μ M, 10 μ M and 100 µM, respectively. D. The TF coexists with 101 proteins, 100 proteins of which have the same fixed concentration: 100 μ M. Blue, red and green curve corresponds to the concentration of the remaining protein to be 1 μ M, 10 μ M and 100 µM, respectively. The three curves overlap, indicating that changing the concentration of the remaining protein does not affect $[4Ca^{2+}-CaM-TF_1]$. E. $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-G6M \cap IGE]}$ for all nine curves shown in Fig. 2B and C, indicating that, for all nine cases, the maximum of $\frac{[4Ca^{2+}-CaM-TF]}{[4Ca^{2+}-CaM-TF]}$ copyright © 2019 American Society of Plant Biologists. All rights reserved.



Figure 3. A diagram schematically describes the design principle for transcriptional decoding calcium signatures to generate specific gene expression. A. The binding mechanism between Ca²⁺, calmodulin (CaM) and transcription factor (TF), which emerges from two pairs of Ca²⁺-binding EF-hand domains and a TF-binding domain in CaM and a CaM-binding domain in TF. B. Nonlinear amplificedopylight © 2019 American Society of Plant Biologists. All fights reserved. TF-specific active signal for each of CaM-binding TFs emerges from A and B.



Figure. 4. A simple Ca²⁺-regulated gene expression process governed by design principle: calcium signatures, even if the differences of their kinetics or amplitudes are modest, are decoded to generate specific gene expression responses. A. Three artificial calcium signatures with the same sinusoidal kinetics (the period is fixed to be 80s, and amplitudes are 0.2 μ M, 0.3 μ M and 0.4 μ M, respectively. Only one period of the sinusoidal kinetics is used.) B. $\frac{[4Ca^{2+}-CaM-TF]_{ss}}{[4Ca^{2+}-CaM-TF]_{ss}}$ calculated using the three calcium signatures in Fig. 4A as the input of equation 3. C. Fold change of mRNA corresponding to the three calcium signatures in Fig. 4A. D. $\frac{[4Ca^{2+}-CaM]_{ifCa^{2+}-CaM]_{ss}}}{[4Ca^{2+}-CaM]_{ifCa^{2+}-CaM}]_{ifCa^{2+}-CaM}}$ calculated using the three calcium signatures in Fig. 4A as the input of equation 3. E. The ratio of $\frac{[4Ca^{2+}-CaM]_{ifCa^{2+}-CaM-TF]_{ss}}}{[4Ca^{2+}-CaM-TF]_{ss}}$. This ratio is always unity, indicating that $\frac{[4Ca^{2+}-CaM]_{ifCa^{2+}-CaM]_{ss}}}{[4Ca^{2+}-CaM-TF]_{ifCa^{2+}-CaM}-TF]_{ss}}$. F. Three artificial calcium signatures with the same average calcium concentration (the average of $[Ca^{2+}]$ is 0.2 μ M for each of the three curves). G. $\frac{[4Ca^{2+}-CaM-TF]_{ifCa^{2+}-CaM-TF]_{ss}}}{[4Ca^{2+}-CaM]_{ifCa^{2+}-CaM}-TF]_{ss}}$ calculated using the three calcium signatures in Fig. 4F as the input of equation 3. H. Fold change of mRNA corresponding to the three calcium signatures in Fig. 4F. I. $\frac{[4Ca^{2+}-CaM]_{iss}}{[4Ca^{2+}-CaM]_{iss}}$ calculated using the three calcium signatures in Fig. 4F as the input of equation 3. H. Fold change of mRNA corresponding to the three calcium signatures in Fig. 4F. I. $\frac{[4Ca^{2+}-CaM]_{iss}}{[4Ca^{2+}-CaM]_{iss}}}$ calculated using the three calcium signatures in Fig. 4F as the input of equation 3. J. The ratio of $\frac{[4Ca^{2+}-CaM]_{iss}}{[4Ca^{2+}-CaM]_{iss}}}$ to $\frac{[4Ca^{2+}-CaM-TF]_{iss}}{[4Ca^{2+}-CaM]_{iss}}}$ to $\frac{[4Ca^{2+}-CaM-TF]_{iss}}}{[4Ca^{2+}-CaM]_{iss}}}$ as always unity, indi



Figure 5. A simple Ca²⁺-regulated gene expression process governed by design principle: effects of the number of CaMbinding proteins or the binding rates on specific gene expression responses. A. An artificial calcium signature. B. Effects of the number of CaM-binding proteins on specific gene expression responses. The TF coexists with one protein. Green, red and blue curve corresponds to the concentration of the protein to be 1 μ M, 10 μ M and 100 μ M, respectively. C. Effects of the number of CaM-binding proteins on specific gene expression responses. The TF coexists with 101 proteins, 100 proteins of which have the same fixed concentration: 100 μ M. Green, red and blue curve corresponds to the concentration of the remaining protein to be 1 μ M, 10 μ M and 100 μ M, respectively. The three curves overlap, indicating that changing the concentration of the remaining protein does not affect fold change of mRNA. D. Effects of the binding rates on specific gene expression responses. Wide orange curve is calculated using equation 3. Blue curve is calculated using differential equations with aben pacient rates of the protein specific differential equations with aben pacient rates of the proteins of the remaining by the orange curve is calculated using equation 3. Blue curve is calculated using differential equations with aben pacient rates of the protein specific differential equations with aben pacient rate of the proteins of the remaining by the orange that the orange curve is calculated to the field of the protein specific differential equations with aben pacient rates of the protein specific differential equations with aben pacient rate of the proteins of the protein specific differential equations with aben pacient rate of the protein specific difference of



Figure. 6. Two calcium signatures are decoded to generate specific expression of EDS1 and ICS1 following design principle: responses of two active signals, 4Ca²⁺-CaM-CAMTA3 and 4Ca²⁺-CaM-CBP60g, to two experimentally measured calcium signatures. A. Two empirical calcium signatures induced by two calcium agonists: mastoparan and extracellular calcium (Lenzoni et al., 2018). B. Enlargement of Fig. 6A, showing the details of the two calcium signatures. C. Response of 4Ca²⁺-CaM-CAMTA3 to the two calcium signatures. Wide solid orange curve and wide dashed orange curve are calculated using the two calcium signatures as the input of equation 3, respectively. Experimentally measured parameters are used. Black and blue curves are calculated using the two calcium signatures as the input of differential equations, respectively. The wide orange curve overlaps with the black curve. The wide dashed orange curve overlaps with the blue curve. These results indicate a quasi-equilibrium state is established. D. Same as Fig. 6C, but both "on" and "off" rate constants for Ca²⁺-CaM interactions are reduced by 1.0E5 fold from their experimental values. E. Same as Fig. 6C, but both "on" and "off" rate constants for Ca²⁺-CaM interactions are reduced by 1.0E8 fold from their experimental values. Black and blue curves are flat and they also overlap, indicating that neither calcium signature can induce changes in [4Ca²⁺-CaM-CAMTA3]. F. Same as Fig. 6C, but it is the response of 4Ca²⁺-CaM-CBP60g to the two calcium signatures. G. Same as Fig. 6F, but both "on" and "off" rate constants for Ca2+-CaM interactions are reduced by 1.0E5 fold from their experimental values. H. Same as ნეფორნეკის სისირიორიოთალის რელის და არის სისის სისის სისის სისის სისის სისის ს 1.0E8 fold from their experimenta CVANUEST BISER SATISTICE SUFFICE STREET STATES ALISE ALISE ALISE ALISE AND STREET AND A calcium signature can induce changes in [4Ca²⁺-CaM-CBP60g].



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