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QWIND code release: a non-hydrodynamical approach to modelling line-driven winds in active galactic nuclei

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ABSTRACT

Ultraviolet (UV) line-driven winds may be an important part of the active galactic nucleus (AGN) feedback process, but understanding their impact is hindered by the complex nature of the radiation hydrodynamics. Instead, we have taken the approach pioneered by Risaliti & Elvis, calculating only ballistic trajectories from radiation forces and gravity but neglecting gas pressure. We have completely rewritten their QWIND code using more robust algorithms and can now quickly model the acceleration phase of these winds for any AGN spectral energy distribution spanning UV and X-ray wavebands. We demonstrate the code using an AGN with black hole mass $10^8 \, \mathrm{M}_\odot$ emitting at half the Eddington rate and show that this can effectively eject a wind with velocities $\simeq (0.1-0.2) \, c$. The mass loss rates can be up to $\simeq 0.3 M_\odot$ per year, consistent with more computationally expensive hydrodynamical simulations, though we highlight the importance of future improvements in radiation transfer along the multiple different lines of sight illuminating the wind. The code is fully public and can be used to quickly explore the conditions under which AGN feedback can be dominated by accretion disc winds.

Key words: acceleration of particles – galaxies: active – quasars: general.

1 INTRODUCTION

Almost every galaxy in the Universe hosts a supermassive black hole (BH) at its centre. It is observationally well grounded that the BH mass ($M_{\rm BH}$) correlates with different galactic-scale properties such as the bulge's stellar mass (Häring & Rix 2004) and velocity dispersion (Ferrarese & Merritt 2000; Gebhardt et al. 2000), which suggests a joint evolution of the BH and its host galaxy (Magorrian et al. 1998; Kormendy & Ho 2013). Nonetheless, the nature of the physical coupling between the BH and its host galaxy is not entirely understood, though winds from the accretion discs of supermassive BHs are a strong candidate to explain how the accretion energy can be communicated to much larger galactic scales. Observations show that (10–20) per cent of quasars (QSOs) exhibit broad blueshifted absorption lines with velocities of $v \sim (0.03-0.3)c$ (Weymann et al. 1991; Pounds et al. 2003a,b; Reeves et al. 2009; Tombesi et al. 2010; Crenshaw & Kraemer 2012). Many physical mechanisms

have been proposed to explain the launching and acceleration phases of these outflows. Magnetic fields control the accretion process of the disc through the magnetorotational instability (Balbus & Hawley 1998; Ji et al. 2006), enabling the transport of angular momentum outwards. It is therefore possible that they also play a key role in generating disc winds (Proga 2003; Fukumura et al. 2017), as well as being responsible for the production of radio jets (Blandford & Znajek 1977; Blandford & Payne 1982). Another plausible force that can accelerate a disc wind is radiation pressure on to spectral lines. The ultraviolet (UV) luminosity from the accretion disc can resonantly interact with the disc's surface gas through boundbound line transitions, effectively boosting the radiative opacity by several orders of magnitude with respect to electron scattering alone, provided that the material is not overionized (Stevens & Kallman 1990, hereafter SK90). This acceleration mechanism is also strongly supported by the observation of line-locking phenomena (Bowler et al. 2014).

The physical principles of radiatively line-driven winds were extensively studied by Castor, Abbott & Klein (1975), hereafter CAK, and Abbott (1982) in the context of O-type stars. Two decades later,

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the same approach was extended to accretion discs around active galactic nuclei (AGNs) (Murray et al. 1995), using the classical thin disc model of Shakura & Sunyaev (1973) (hereafter SS). A few years later, the first results of hydrodynamical simulations of line-driven winds using the ZEUS2D code (Stone & Norman 1992) were released (Proga, Stone & Kallman 2000; Proga & Kallman 2004, hereafter P00 and P04) and continue to be extensively improved (Nomura et al. 2016, hereafter N16), and also Nomura & Ohsuga (2017), Nomura, Ohsuga & Done (2018), Dyda & Proga (2018a), and Dyda & Proga (2018b).

However, full radiation hydrodynamic calculations are very computationally intensive. Another approach is to study only ballistic trajectories, i.e. neglect the gas pressure forces. This non-hydrodynamic approach was started by Risaliti & Elvis (2010), hereafter RE10, as the radiation force from efficient UV line driving can be much stronger than pressure forces. Their QWIND code calculated the ballistic trajectories of material from an accretion disc illuminated by both UV and X-ray flux. The neglect of hydrodynamics means that the code can be used to quickly explore the wind properties across a wide parameter space, showing where a wind can be successfully launched and accelerated to the escape velocity and beyond.

Here, we revisit the QWIND code approach, porting it from C to PYTHON, and improving it for better numerical stability and correcting some bugs. We show that this non-hydrodynamic approach does give similar results to a full hydrodynamic simulation. We illustrate how this can be used to build a predictive model of AGN wind feedback by showing the wind mass loss rate and kinetic luminosity for a typical quasar. The new code, QWIND2, is now available as a public release on GitHub.¹

2 METHODS

In this section, we include for completeness the physical basis of the code and its approach to calculating trajectories of illuminated gas parcels (RE10). In sub-Section 2.1, we describe the geometrical setup of the system. The treatment of the X-ray and UV radiation field is explained in sub-Section 2.2, and we conclude by presenting the trajectory evolution algorithm in sub-Section 2.3.

2.1 Geometry setup

We use cylindrical coordinates (R, ϕ, z) , with the BH and the X-ray-emitting source considered as a point located at the centre of the grid, at R=z=0. The disc is assumed to emit as a Novikov–Thorne (Novikov & Thorne 1973) (NT) disc, but is assumed to be geometrically razor thin, placed in the plane z=0, with its inner radius given by $R_{\rm isco}$ and outer radius at $R_{\rm out}$. We model the wind as a set of streamlines originating from the surface of the disc between radii $R_{\rm in} \geq R_{\rm isco}$ and $R_{\rm out}$, where the freedom to choose $R_{\rm in}$ allows wind production from the very inner disc to be suppressed by the unknown physical structure, which gives rise to the X-ray emission.

The trajectory of a gas element belonging to a particular streamline is computed by solving its equation of motion given by $\mathbf{a} = \mathbf{f}_{\text{grav}} + \mathbf{f}_{\text{rad}}$, where \mathbf{a} is the acceleration and \mathbf{f}_{grav} and \mathbf{f}_{rad} are the force per unit mass due to gravity and radiation pressure, respectively, using a time-adaptive implicit differential equation system solver (Section 2.3). The computation of the trajectory stops when the

fluid element falls back to the disc or it reaches its terminal velocity, escaping the system. Since the disc is axisymmetric, it is enough to consider streamlines originating at the $\phi=0$ disc slice.

2.2 Radiation field

The radiation field consists of two spectral components.

2.2.1 The X-ray component

The central X-ray source is assumed to be point-like, isotropic, and is solely responsible for the ionization structure of the disc's atmosphere. The X-ray luminosity, $L_{\rm X}=f_{\rm X}\,L_{\rm bol}$. The ionization parameter is

$$\xi = \frac{4\pi F_{\rm X}}{n},\tag{1}$$

where F_X is the ionizing radiation flux, and n is the number density. The X-ray flux at the position (R, z) is computed as

$$F_{\rm X} = \frac{L_{\rm X} \exp\left(-\tau_{\rm X}\right)}{4\pi r^2},\tag{2}$$

where $r = \sqrt{R^2 + z^2}$, and τ_X is the X-ray optical depth, which is calculated from

$$\tau_{\mathbf{X}} = \int_{R_{\mathrm{in}}}^{r} n_0(r') \, \sigma_{\mathbf{X}}(\xi) \, \mathrm{d}r', \tag{3}$$

where $n_0(r)$ is the number density measured at the base of the wind by projecting the distance r' to the disc (see Appendix A). This assumption overestimates both the UV and the X-ray optical depth far from the disc surface. Since most of the acceleration is gained very close to the disc, the impact of this assumption is small; however, it will be improved in a future improvement of the radiative transfer model. $\sigma_X(\xi)$ is the cross-section to X-rays as a function of ionization parameter, which we parametrize following the standard approximation from Proga et al. (2000),

$$\sigma_{\rm X}(\xi) = \begin{cases} 100 \, \sigma_{\rm T} & \text{if } \xi < 10^5 \, {\rm erg \, cm \, s^{-1}}, \\ \sigma_{\rm T} & \text{if } \xi \ge 10^5 \, {\rm erg \, cm \, s^{-1}}, \end{cases} \tag{4}$$

where the step function increase in opacity below $\xi = 10^5 {\rm erg~cms^{-1}}$ very approximately accounts for the increase in opacity due to the bound electrons in the inner shells of metal ions, and $\sigma_{\rm T}$ is the Thomson cross-section.

2.2.2 The ultraviolet component

The UV source is the accretion disc, emitting according to the NT model in an anisotropic way due to the disc geometry. The UV luminosity is $L_{\rm UV}=f_{\rm UV}\,L_{\rm bol}$. Currently, the code makes the simplifying assumption that $f_{\rm UV}$ is constant as a function of radius. The emitted UV-radiated power per unit area by a disc patch located at $(R_{\rm d},\phi_{\rm d},0)$ is

$$\mathcal{F} = f_{\text{UV}} \frac{3GM\dot{M}}{8\pi R_{\text{d}}^3} f(R_{\text{d}}, R_{\text{isco}}). \tag{5}$$

The SS equations as used by RE10 are non-relativistic, with $f(R_d, R_{\rm isco}) = [1 - (R_{\rm isco}/R_{\rm d})^{1/2}]$, which leads to the standard Newtonian disc bolometric luminosity of $L_{\rm d} = \frac{1}{12} \dot{M} c^2$, i.e. an efficiency of ≈ 0.08 for a Schwarzschild BH, with $R_{\rm isco} = 6R_{\rm g}$. We use instead the fully relativistic NT emissivity, where f is explicitly a function of BH spin, a, and the efficiency is the correct value of $\eta(a=0) = 0.057$ for a Schwarzschild BH. This is important, as the standard

¹https://www.github.com/arnauqb/qwind

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input parameter, $\dot{m} = L_{\rm bol}/L_{\rm Edd}$, is used to set \dot{M} via $L_{\rm bol}/(\eta(a)c^2)$. The relativistic correction reduces the radiative power of the disc by up to 50 per cent in the innermost disc annuli, compared to the Newtonian case.

Assuming that the radiative intensity (energy flux per solid angle) $I(R_d)$ is independent of the polar angle over the range $\theta \in [0, \pi/2]$, we can write

$$I(R_{\rm d}) = \frac{\mathcal{F}}{\pi},\tag{6}$$

thus the UV radiative flux from the disc patch as seen by a gas blob at a position (R, 0, z) is

$$dF = f_{\rm UV} \frac{I(R_{\rm d})}{\Lambda^2} \cos \theta \ R_{\rm d} \ dR_{\rm d} d\phi_{\rm d}, \tag{7}$$

where

$$\Delta = (R^2 + R_d^2 + z^2 - 2RR_d\cos\phi_d)^{1/2}.$$
 (8)

(The flux received from an element of area $dA = R_d dR_d d\phi_d$ at distance Δ seen at angle θ is $Id\Omega$, where the solid angle subtended is $d\Omega = (dA \cos \theta)/\Delta^2$, and $\cos \theta = z/\Delta$.)

The average luminosity-weighted distance is $\Delta \approx r$, so attenuation by electron scattering along all the UV lines of sight is approximately that along the line of sight to the centre i.e. analogously to equation (3) but considering only the electron-scattering cross-section (see Appendix A). A more refined treatment that considers the full geometry of the disc will be presented in a future paper. The corresponding radiative acceleration due to electron scattering is then

$$d\mathbf{a}_{rad} = \frac{\sigma_{T}}{c} \hat{\mathbf{n}} dF \exp(-\tau_{UV}), \tag{9}$$

with $\hat{\mathbf{n}}$ being the unit vector from the disc patch to the gas blob,

$$\hat{\mathbf{n}} = \frac{(R - R_{\rm d}\cos\phi_{\rm d}, -R_{\rm d}\sin\phi_{\rm d}, z)}{\Delta}.$$
 (10)

2.2.3 Radiative line acceleration

The full cross-section for UV photons interacting with a moderately ionized gas is dominated by line absorption processes, implying potential boosts of up to 1000 times the radiation force caused solely by electron scattering. To compute this, we use the force multiplier M proposed by Stevens & Kallman (1990) hereafter SK90, which is a modified version of Castor et al. (1975) that includes the effects of X-ray ionization. Ideally, one should recompute the force multiplier considering the full AGN spectral energy distribution (SED) (Dannen et al. (2019)), which is different than the B0 star spectrum considered in SK90; however, this is out of the scope of this paper. The full opacity is then $\sigma_{\rm total} = (1 + M)\sigma_{\rm T}$, with the force multiplier M depending on the ionization parameter, and on the effective optical depth parameter t,

$$t = \sigma_{\rm T} \, n \, v_{\rm th} \, \left| \frac{\mathrm{d}v}{\mathrm{d}l} \right|^{-1},\tag{11}$$

which takes into account the Doppler shifting resonant effects in the accelerating wind and depends on the gas number density n, the gas thermal velocity $v_{\rm th}$, and the spatial velocity gradient along the light ray, ${\rm d}v/{\rm d}l$. In general, the spatial velocity gradient is a function of the velocity shear tensor and the direction of the incoming light ray at the current point. In this work, we approximate the velocity gradient as the gradient along the gas element trajectory, allowing the force multiplier to be determined locally. A full velocity gradient

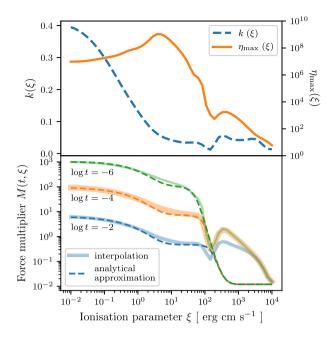


Figure 1. Top panel: Best-fitting values for the force multiplier parameters k and η_{max} as a function of ionization parameter ξ , taken from SK90. Bottom panel: Force multiplier as a function of the ionization parameter and the effective optical depth, showing the discrepancy between the analytical approximation derived in SK90 and the direct interpolation at the range $10^2 \le \xi \le 10^4$. Note that, for the analytical approximation, M is independent of t for $\xi > 10^2$.

treatment in the context of hydrodynamical simulations of linedriven winds in CV systems has been studied in Dyda & Proga (2018a), who find that the inclusion of non-spherically symmetric terms results in the formation of clumps in the wind. Our nonhydrodynamical approach is insensitive to this kind of gas feature. It is convenient to rewrite the spatial velocity gradient as

$$\frac{\mathrm{d}v}{\mathrm{d}l} = \frac{\mathrm{d}v}{\mathrm{d}t} \frac{\mathrm{d}t}{\mathrm{d}l} = \frac{a_t}{v_t},\tag{12}$$

where $a_t = \sqrt{a_R^2 + a_z^2}$, and $v_t = \sqrt{v_R^2 + v_z^2}$. This change of variables avoids numerical roundoff errors as it avoids calculating small finite velocity differences. The force multiplier is parametrized as

$$M(t,\xi) = k(\xi) t^{-0.6} \left[\frac{(1+t \, \eta_{\text{max}}(\xi))^{0.4} - 1}{(t \, \eta_{\text{max}}(\xi))^{0.4}} \right] \approx k(\xi) t^{-0.6}, \quad (13)$$

where the latter expression holds when $\eta_{\rm max}(\xi)\,t\gg 1$, which is the case for all cases of interest here. We extract the best-fitting values for k and $\eta_{\rm max}$ directly from fig. 5 of SK90, as opposed to using the usual analytic approximation given in equations (18) and (19) of SK90. The reason we fit directly is because the analytical fitting underestimates the force multiplier in the range $10^2 \le \xi \le 10^4$, as we can see in Fig. 1. In RE10, the analytical approximation was used, but we note that the step function change in X-ray opacity at $\xi=10^5$ means that these intermediate ionization states are not important in the current handling of radiation transfer, since the gas quickly shifts from being very ionized to being neutral; thus, this change has negligible effect on the code results.

With all this in mind, the total differential radiative acceleration is

$$d\mathbf{a}_{\text{rad}} = \frac{\sigma_{\text{T}} (1 + M(t, \xi))}{c} \hat{\mathbf{n}} dF \exp(-\tau_{\text{UV}}), \tag{14}$$

and the contribution from the whole disc to the radial and vertical radiation force is found by performing the two integrals

$$\mathcal{I}_{R} = \int_{R_{\rm min}}^{R_{\rm max}} dR_{\rm d} \, \frac{f(R_{\rm d}, R_{\rm isco})}{R_{\rm d}^2} \int_{0}^{\pi} d\phi_{\rm d} \frac{(R - R_{\rm d} \cos \phi_{\rm d})}{\Delta^4}, \tag{15}$$

and

$$\mathcal{I}_z = \int_{R_{\text{min}}}^{R_{\text{max}}} dR_d \frac{f(R_d, R_{\text{isco}})}{R_d^2} \int_0^{\pi} d\phi_d \frac{1}{\Delta^4}.$$
 (16)

The angular contribution is zero because of the cylindrical symmetry. Evaluating these integrals is not straightforward due to the presence of poles at $\Delta=0$. The original QWIND code used a fixed grid spacing, but this is not very efficient, and led to inaccuracies with convergence of the integral (see Section 3.2). Instead, we use the QUAD integration method implemented in the SCIPY (Virtanen et al. 2019) PYTHON package to compute them. Appendix B shows that this converges correctly.

2.3 Trajectories of fluid elements

Gas trajectories are initialized at a height z_0 , with launch velocity v_0 . This can be different to the assumed thermal velocity as there could be additional mechanisms that help launch the wind from the disc, such as convection and/or magnetic fields, thus we keep this as a free parameter in the code so that we can explore the effect of this. The equation of motion is $\mathbf{a}_{tot} = \mathbf{a}_{grav} + \mathbf{a}_{rad}$, with

$$\mathbf{a}_{\text{grav}}(R,z) = -\frac{GM_{\text{BH}}}{r^2} \left(\frac{R}{r}, 0, \frac{z}{r}\right). \tag{17}$$

In cylindrical coordinates, the system to solve is

$$\frac{\mathrm{d}R}{\mathrm{d}t} - v_R = 0,$$

$$\frac{\mathrm{d}z}{\mathrm{d}t} - v_z = 0,$$

$$\frac{\mathrm{d}v_R}{\mathrm{d}t} - a_R^{\mathrm{grav}} - a_R^{\mathrm{rad}} - \frac{\ell^2}{R^3} = 0,$$

$$\frac{\mathrm{d}v_z}{\mathrm{d}t} - a_z^{\mathrm{grav}} - a_z^{\mathrm{rad}} = 0,$$
(18)

where ℓ is the specific angular momentum, which is conserved along a trajectory. The radiative acceleration depends on the total acceleration and the velocity at the evaluating point through the force multiplier [see equations (13) and (12)]; therefore, the system of differential equations cannot be written in an explicit form, and we need to solve the more general problem of having an implicit differential algebraic equation (DAE), $\mathbf{F}(t, \mathbf{x}, \dot{\mathbf{x}}) = 0$, where **F** is the left hand side of equation (18), $\mathbf{x} = (R, z, v_R, v_z)$, and $\dot{\mathbf{x}} = (v_R, v_z, a_R, a_z)$. We use the IDA solver (Hindmarsh et al. 2004) implemented in the ASSIMULO simulation software package (Andersson, Führer & Åkesson 2015), which includes the backward differentiation formula (BDF) and an adaptive step size to numerically integrate the DAE system. We choose a BDF of order 3, with a relative tolerance of 10⁻⁴. In RE10, a second-order Euler method was used without an adaptive time-step. We do not find significant differences in the solutions found by both solvers, as RE10 used a very small step size, keeping the algorithm accurate. Nonetheless, the time-step adaptiveness of our new approach reduces the required number of time-steps by up to four orders of magnitude, making the algorithm substantially faster. For an assessment on the solver's convergence, refer to Appendix B.

The gas density is calculated using the mass continuity equation, $\dot{M}_{\text{line}}(t) = \dot{M}_{\text{line}}(0)$. If the considered streamline has an initial width

 ΔL_0 , assuming that the width changes proportionally to the distance from the origin, $\Delta L \propto r$, we can write

$$\dot{M}_0 = \rho_0 \, v_0 \, A_0 = \rho_0 \, v_0 \, 2 \, \pi \, r_0 \, \Delta L_0 = \rho \, v \, 2 \, \pi \, r \, \Delta L = \dot{M}, \tag{19}$$

where $\rho_i = n(r_i) m_p$, with m_p being the proton mass. From here, it easily follows, using $\Delta L/\Delta L_0 = r/r_0$, that

$$n(r_i) v_i r_i^2 = n(r_0) v_0 r_0^2, (20)$$

which we use to update the density at each time-step. The simulation stops either when the fluid element falls back to the disc or when it leaves the grid ($r = 10^5 R_g$).

3 THE QWIND2 CODE

Algorithm 1: Fluid element trajectory initialization and evolution

input: R_0, z_0, n_0, v_0

Read initial parameters;

Set initial angular velocity to Keplerian;

Initialise IDA solver;

while (material not out of grid) or (material not fallen to the disc) do

IDA solver iteration. At each step, take current value of x, and \dot{x} , and do:

Compute local velocity gradient $\frac{dv}{dl}$ using equation (12):

Compute gas density using equation (20);

Compute X-ray and UV optical depth (see Appendix A);

Compute ionization parameter using equations (1) and (2);

Compute force multiplier using equation (13);

Compute radiative acceleration using the computed force multiplier and integrating equations (16) and (15);

Compute gravitational acceleration using equation (17):

Update fluid element position, velocity, and acceleration:

Estimate solver error and update time-step;

end

if gas escaped then

Compute mass loss using mass flux conservation equation (24);

Compute kinetic luminosity using equation (25);

In the code, we organize the different physical phenomena into three PYTHON classes: wind, radiation, and streamline. The wind class is the main class of the code and it handles all the global properties of the accretion disc and launch region, such as accretion rate, atmospheric temperature/velocity/density etc. The radiation class implements all the radiative physics, such as the calculation of optical depths and the radiation force. Finally, the streamline class represents a single-fluid element, and it contains the ASSIMULO's IDA solver that solves the fluid element equation of motion, evolving it until it falls back to the disc or it exceeds a distance of $r=10^5\,R_{\rm g}$. It takes about 10 s on average on a single CPU to calculate one fluid element trajectory; thus, we are able to simulate an entire wind in a few minutes, depending on the number of streamlines wanted.

Table 1. QWIND baseline parameters.

Parameter	Value
R _{in}	$200R_{ m g}$
R_{out}	$1600 R_{\rm g}$
$M_{ m BH}$	10^8M_\odot
m	0.5
a	0
v_0	10^{7}cms^{-1}
n_0	$2 \times 10^{8} \text{ cm}^{-3}$
<i>z</i> ₀	$1 R_{\rm g}$
T	$2.5 \times 10^{4} \text{ K}$
$f_{\rm UV}$	0.85
$f_{\rm X}$	0.15

The system is initialized with the input parameters (see Table 1), and a set of fluid elements is launched and evolved between $R_{\rm in}$ and $R_{\rm out}$ following Algorithm 1. As an illustrative example, we define our baseline model with the parameter values described in Table 1. These parameter values are the same as used in RE10, except for the BH mass that we take to be $M=10^8~{\rm M}_{\odot}$, rather than $2\times10^8~{\rm M}_{\odot}$, to be able to compare with the hydrodynamic simulations of P04 and N16. We also launch the wind from closer to the disc at $z_0=1R_{\rm g}$ rather than the default $z_0=5R_{\rm s}=10R_{\rm g}$ of RE10. We do this to highlight the effect of the new integration routine.

To determine the number of streamlines N to simulate, we notice that the mass flow along a streamline with initial radius R_0 is

$$\dot{M}_{\text{wind}} = 2\pi R_0 \rho_0 v_0 \Delta L_0,$$
 (21)

where $\Delta L_0 = (R_{\rm out} - R_{\rm in})/N$. The streamline with the highest mass flow is, thus, the one with the highest initial radius. We expect that the outermost escaping streamline will satisfy, at its base, $\tau \simeq R_0 \, n_0 \, \sigma_T \simeq 1$. We set N such that this streamline carries, at most, the 0.05 per cent of the mass accretion rate. This implies that the chosen number of streamlines is independent of the initial density,

$$N = \frac{2\pi \ m_{\rm p} \ v_0 \ (R_{\rm out} - R_{\rm in})}{5 \times 10^{-4} \ \dot{M} \ \sigma_T}.$$
 (22)

For the parameter values of the baseline model (Table 1), we have $N \simeq 53$.

3.1 Improvements in the OWIND code

We first run the original QWIND code using the SS disc model with an efficiency $\eta = 0.0313$, and a wind temperature of $T = 2 \times 10^6$ K. The rest of the parameters are fixed to the default values shown in Table 1. We plot the resulting streamlines in Fig. 2. The structure of the wind can be divided into three distinct regions: an inner failed wind (green), an escaping wind (blue), and an outer failed wind (orange), also delimited by the separating vertical dashed lines. The inner failed region corresponds to streamlines that have copious UV irradiation but where the material is too highly ionized for the radiation force to counter gravity. On the other hand, the outer failed wind comprises trajectories where the material has low enough ionization for a large force multiplier, but the UV flux is not sufficient to provide enough radiative acceleration for the material to escape. Finally, the escaping wind region consists of streamlines where the material can escape as it is shielded from the full ionizing flux by the failed wind in the inner region.

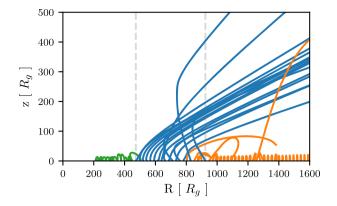


Figure 2. Results of a wind simulation, using the original QWIND code with the Newtonian disc flux equations from SS and a radiative efficiency of $\eta = 0.0313$. The wind temperature is set to $T = 2 \times 10^6$ K. The other parameters are set to the baseline parameter values (Table 1). The inner failed wind, escaping wind, and outer failed wind regions are coloured in green, blue, and orange, respectively, and delimited by the grey dashed vertical lines.

3.1.1 Effect of integration routine

Two of the blue escaping wind streamlines in Fig. 2 (those originating from ${\sim}900R_g$) cross all the other escaping trajectories. We find that these crossing flow lines result from the old integration routine. The original code solved the integrals [equations (15) and (16)] using a non-adaptive method, which led to numerical errors in the radiative force at low heights. The first panel of Fig. 3 shows the results using the same parameters and code with the new integration routine. The behaviour is now much smoother, not just in the escaping wind section but across all of the surface of the disc. The new PYTHON integrator is much more robust and has much better defined convergence (see Appendix B).

3.1.2 Efficiency and disc emissivity

The original code used the Newtonian disc flux equations from SS but then converted from $\dot{m}=L_{\rm bol}/L_{\rm Edd}$ to \dot{M} using an assumed efficiency, with default of $\eta=0.0313$. This is low compared to that expected for the Newtonian SS disc accretion, where $\eta=0.08$, and low even compared to a fully relativistic non-spinning BH, which has $\eta=0.057$. For a fixed dimensionless mass accretion rate \dot{m} , the inferred $\dot{M}\propto 1/\eta$ as a larger mass accretion rate is required to make the same bolometric luminosity if the efficiency is smaller. Since \dot{M} sets the local flux, this means that the local flux is a factor of \sim 2 smaller in the new QWIND2 code for a given $L_{\rm bol}$. The comparison between the first and second panels of Fig. 3 shows that this reduction in the local UV flux means that fewer wind streamlines escape.

3.1.3 Wind thermal velocity

In the absence of an X-ray ionizing source, the force multiplier is independent of the thermal velocity (see Abbott 1982 for a detailed discussion); this, however, does not mean that one can freely choose a thermal velocity value at which to evaluate the effective optical depth t, since the values of the fit parameters in the analytical fit for M(t) depend on the thermal velocity as well (see table 2 in Abbott 1982). If one includes an X-ray source as in SK90, then we expect the temperature of the gas to change depending on how much radiation a gas element is receiving from the X-ray source

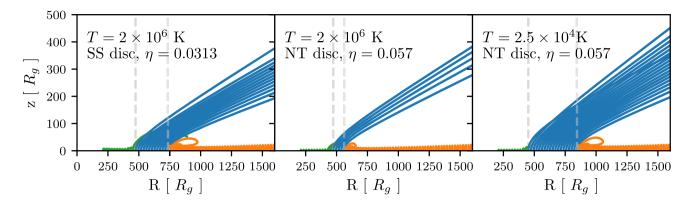


Figure 3. Three wind simulations performed with the updated QWIND code but different physical assumptions. All the non-specified parameters are fixed to the baseline model (Table 1). The leftmost panel shows a simulation run assuming a non-relativistic Newtonian disc with an efficiency of $\eta = 0.0313$, and a temperature of $T = 2 \times 10^6 K$, while the middle one corresponds to the relativistic NT disc model with the correct efficiency $\eta = 0.057$. Finally, for the rightmost panel, we use the relativistic disc model with the correct efficiency and a temperature of $T = 2.5 \times 10^4 K$, consistent with the force multiplier derivation in SK90.

as well as from the UV source. At low values of the ionization parameter, the results from Abbott (1982) hold, and thus it is justified to evaluate the force multiplier using an effective temperature of T $= 2.5 \times 10^4$ K, corresponding to the temperature of the UV source used in SK90. Since the evaluation of the force multiplier is most important in regions of the flow where the gas is shielded from the X-ray radiation, we use this temperature value to compute the force multiplier throughout the code. In the N16 and P04 hydrodynamic simulations, the wind kinetic temperature is calculated by solving the energy equation that takes into account radiative cooling and heating: however, for the purpose of evaluating the force multiplier. a constant temperature of $T = 2.5 \times 10^4 \,\mathrm{K}$ is also assumed. In RE10, the force multiplier is evaluated setting $T = 2 \times 10^6$ K for the kinetic temperature. A higher thermal velocity increases the effective optical depth t, which in turn decreases the force multiplier, given the same spatial velocity gradient and assuming the same parametrization for $k(\xi)$ and $\eta_{\text{max}}(\xi)$, thus resulting on a narrower range of escaping streamlines. We can visualize the impact of this change by comparing the second and third panels of Fig. 3. However, this apparent dependence of the force multiplier on thermal velocity is artificial, as explained above.

We define our baseline model as the one with the parameters shown in Table 1.

3.2 Baseline model in QWIND2

The new code is publicly available online in the author's GitHub account.² It is written purely in PYTHON, making use of the Numba (Lam, Pitrou & Seibert 2015) JIT compiler to speed up the expensive integration calculations.

We now show more results from our new implementation of the QWIND code. The third panel of Fig. 3 shows that the radius range from which escaping lines can be originated is relatively narrow. This can be explained by looking at the radiative acceleration and the force multiplier for each streamline. We plot the maximum radiative acceleration and force multiplier for each of the streamlines as a function of their initial radius in the left-hand panel of Fig. 4. To effectively accelerate the wind, we need both a high-UV flux and a high-force multiplier, which requires that the X-ray flux is

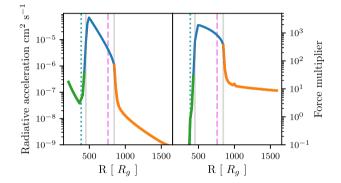


Figure 4. Maximum radiative force and force multiplier as a function of the initial radius of each streamline. Note that escaping lines, plotted in blue and delimited by the two vertical grey lines, require a balance between a sufficiently high-force multiplier (thus low ionization parameter) and a high radiative force. Gas trajectories originating at the green coloured radii (left region delimited by the first vertical grey line) are too ionized, while the orange ones (rightmost region delimited by the second grey line) intercept too few UV photons. The radius at which the gas on the base of the wind becomes optically thick ($\tau=1$) to X-rays and UV is denoted by the dotted blue and the dashed purple lines, respectively.

sufficiently attenuated. Therefore, computing the UV and X-ray optical depths from the centre at the base of the wind can give us an estimate of the escaping region. Indeed, the cyan dotted line shows the radius at which the optical depth along the disc becomes unity for X-ray flux, while the purple dashed line shows the same for the UV flux. Clearly, this defines the radii of the escaping streamlines, i.e. successful wind launching requires that the X-rays are attenuated but the UV is not.

We focus now on the physical properties of an individual escaping streamline. In Fig. 5, we plot the vertical radiative acceleration, the velocity, and the force multiplier of the streamline as a function of its height and radius. We observe that most of the acceleration is achieved very rapidly and very close to the disc; consequently, the wind becomes supersonic shortly after leaving the disc, thus justifying our non-hydrodynamical approach. The sub-sonic part of the wind is encapsulated in the wind initial conditions, and the subsequent evolution is little affected by the gas internal forces. As we are focusing on a escaping streamline, the ionization parameter is low; thus, $\eta_{\rm max}$ will be very high (see top panel of Fig. 1),

²https://github.com/arnauqb/qwind

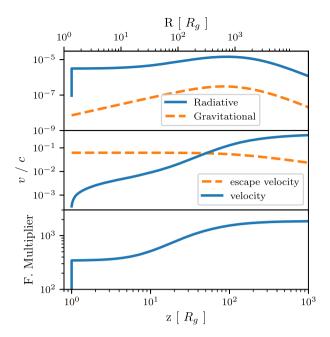


Figure 5. Streamline properties for an escaping gas trajectory. Top panel: Vertical radiative and gravitational acceleration as a function of height and radius. Middle panel: Streamline velocity as a function of radius and height. Bottom panel: Force multiplier as a function of radius and height.

enabling us to write $M(t) \propto t^{-0.6}$ [by taking the corresponding limit in equation (13)]. Additionally, since the motion of the gas element is mostly vertical at the beginning of the streamline, we have from the continuity equation [equation (20)] $n \propto v_t^{-1}$, which combined with equation (12) gives

$$M(t) \propto t^{-0.6} \propto \left(\frac{a_t}{nv_t}\right)^{0.6} \simeq a_t^{0.6}.$$
 (23)

Therefore, as the gas accelerates, the force multiplier increases as well, creating a resonant process that allows the force multiplier to reach values of a few hundred, accelerating the wind to velocities of $v \sim (0.1-0.2)\ c$. At around $z=50\ R_{\rm g}$, the gas element reaches the escape velocity at the corresponding radius, and it will then escape regardless of its future ionization state.

We use mass conservation to calculate the total wind mass loss rate by summing the initial mass flux of the escaping trajectories,

$$\dot{M}_{\text{wind}} = \sum_{i \in \{\substack{\text{escaping} \\ \text{trajectories}}\}} \dot{M}_{\text{wind}}^{(i)}$$

$$= \sum_{i \in \{\substack{\text{escaping} \\ \text{trajectories}}\}} \rho_{i,0} \ v_{i,0} \ 2 \ \pi \ R_{i,0} \ \delta R_i, \tag{24}$$

where $\delta R_{i,0} = R_{i+1,0} - R_i$. For the baseline model, we obtain $\dot{M}_{\rm wind} = 3.01 \times 10^{24} {\rm g s^{-1}} = 0.05 {\rm M}_{\odot} {\rm yr^{-1}}$, which equates to 2.5 per cent of the BH mass accretion rate. We can also compute the kinetic luminosity of the wind,

$$L_{\rm kin} = \frac{1}{2} \dot{M}_{\rm wind} v_{\rm wind}^2, \tag{25}$$

where $v_{\rm wind}$ is the wind terminal velocity, which we take as the velocity at the border of our grid, making sure that it has converged to the final value. The wind reaches a kinetic luminosity of $L_{\rm kin} = 7.83 \times 10^{43}$ erg/s, which equates to 0.62 per cent of the Eddington luminosity of the system. Both these results depend on the choice

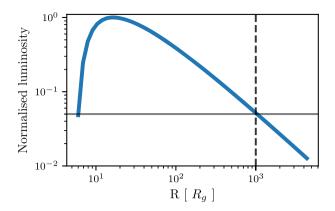


Figure 6. Disc annulus luminosity as a function of annulus radius, normalized to the luminosity of the brightest annulus. We have divided the radius range into 50 logarithmically spaced bins. The dashed black line corresponds to $R \simeq 1000\,R_{\rm g}$ from where the outer annuli contribute less than 5 per cent to the total luminosity compared to the brightest annulus at $R \simeq 16R_{\rm g}$. The sudden drop at $R \lesssim 16R_{\rm g}$ is due to the relativistic NT corrections to the SS disc

of the initial conditions for the wind. In the next section, we scan the parameter range to understand under which parameter values a wind successfully escapes the disc, and how powerful it can be.

3.3 Dependence on launch parameters: R_{in} , n_0 , v_0

We consider variations around the baseline model (Table 1). We fix the BH mass and accretion rate to their default values and vary the initial launching radius $R_{\rm in}$, the initial density n_0 , and the initial velocity v_0 . We can make some physical arguments to guide our exploration of the parameter space:

(i) The initial radius $R_{\rm in}$ at which we start launching gas elements can be constrained by considering the physical scale of the UV-emitting region of the disc. In Fig. 6, we plot the luminosity of each disc annulus normalized to the luminosity of the brightest annulus, using 50 logarithmically spaced radial bins. We observe that radii larger than $\gtrsim 1000\,R_{\rm g}$ contribute less than 5 per cent of the luminosity of the brightest annulus. On the other hand, the effective temperature of the disc drops very quickly below $R\simeq 16\,R_{\rm g}$ due to the NT relativistic corrections. We thus consider that the initial launching radius can vary from $10\,R_{\rm g}$ to $1000\,R_{\rm g}$.

In Fig. 7, we plot the results of changing $R_{\rm in}$ in the baseline model. Increasing the radius at which we start launching gas elements shifts the location of the wind towards higher radii, thus increasing the overall mass loss rate since outer streamlines represent a bigger disc surface [see equation (24)]. For very large initial radii, $R_{\rm in} \geq 1000\,R_{\rm g}$, the wind severely diminishes as the UV flux is too low. To explore the remaining parameters, we fix $R_{\rm in} = 60\,R_{\rm g}$, and $f_x = 0.1$. The reason for this is that we want to compare our results with the hydrodynamic simulations of P04 and N16, which used these parameter values.

(ii) The initial density n_0 of the gas elements needs to be high enough to shield the outer gas from the X-ray radiation, so we need $\tau_X > 1$ at most a few hundred R_g away from the centre (further away the UV flux would be too weak to push the wind). Therefore as a lower limit,

$$\tau_{\rm X} = \int_{R_{\rm in}}^{100 R_{\rm g}} \sigma_{\rm x} n_0 \, {\rm d}r' < \int_0^{100 R_{\rm g}} 100 \, \sigma_{\rm T} \, n_0 \, {\rm d}r' \simeq 10^{-7} \left(\frac{n_0}{\rm cm}^{-3}\right), \tag{26}$$

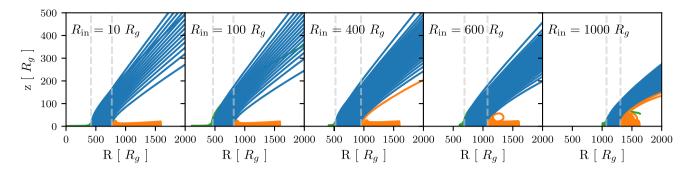


Figure 7. Different runs of the baseline model changing $R_{\rm in}$. The number of escaping streamlines is higher for larger values of $R_{\rm in}$, as the UV optical depth is lower while the shielding is still effective. Furthermore, outer escaping streamlines contribute more to the overall mass loss rate than the inner ones, since they represent larger disc annuli. The wind diminishes at $R_{\rm in} \gtrsim 1000 R_{\rm g}$, where the disc annuli do not emit enough UV radiation.

which implies a minimum shielding density of $n_0 \simeq 10^7 \, \mathrm{cm}^{-3}$. On the other hand, if the density is too high, the gas is also shielded from the UV flux coming from the disc. Even though our treatment of the UV optical depth assumes that the UV source is a central point source (see Appendix A), let us consider now, as an optimistic case for the wind, that the optical depth is computed from the disc patch located just below the wind. In that case, we need $\tau_{\rm UV} < 1$ at a minimum distance of $r \simeq 1 \, R_{\rm g}$,

$$\tau_{\rm UV} = \int_0^{1R_{\rm g}} \sigma_T \, n_0 \, \mathrm{d}r' \simeq 10^{-11} \left(\frac{n_0}{\rm cm^{-3}} \right) \,, \tag{27}$$

so that the maximum allowed value is $n_0 \simeq 10^{11} \, \mathrm{cm}^{-3}$. Thus, we vary the initial density from $10^7 \, \mathrm{cm}^{-3}$ to $10^{11} \, \mathrm{cm}^{-3}$.

(iii) Finally, we estimate the parameter range of the initial velocity v_0 by considering the isothermal sound speed at the surface of the disc. The disc's effective temperature at a distance of a few hundred R_g from the centre computed with the NT disc model is $\simeq 10^6$ cm/s, so we vary the initial velocity from 10^6 cm/s to 10^8 cm/s to account for plausible boosts in velocity due to the launching mechanism. The total number of streamlines is adjusted to ensure enough resolution [see equation (22)].

Fig. 8 shows the resulting scan over the $n_0 - v_0$ parameter space. These results confirm the physical intuition we described at the beginning of this section; initial density values lower than $\simeq 5 \times 10^7$ cm⁻³ do not provide enough shielding against the X-ray radiation, while values higher than $\simeq 10^{10}$ cm⁻³ shield the UV radiation as well

and produce a slower wind. Furthermore, lower initial velocities result into higher final velocities, as the gas parcels spend more time in the acceleration region, and are thus also launched at a higher angle with respect to the disc. The parameter combination that yields the highest wind mass loss rate is $n_0 = 5 \times 10^7 \text{ cm}^{-3}$ and $v_0 = 10^8$ cm/s, which predicts a mass loss rate of 0.3 M_{\odot}/yr, equal to \simeq 17 per cent of the mass accretion rate. The reason why lower initial densities lead generally to higher mass loss rates can be visualized in Fig. 9. Higher initial densities shift the wind-launching region to the inner parts of the accretion disc, since they are able to shield the X-ray more efficiently but the gas also becomes optically thick to UV radiation rapidly. On the other hand, for low values of the initial density, the gas becomes optically thick to X-rays on the outer parts of the disc and the low UV attenuation implies that the range of escaping streamlines is wider. Additionally, outer radii represent annuli with bigger areas, so the mass loss rate is significantly larger [see equation (24)]. The parameter combination $n_0 = 10^{10}$ cm⁻³ and $v_0 = 10^8$ cm/s yields the highest kinetic luminosity value; however, a few of the escaping streamlines have non-physical superluminal velocities. The parameter combination that generates the physical wind with the highest kinetic luminosity is $n_0 = 5 \times 10^9 \text{ cm}^{-3}$ and $v_0 = 10^8$ cm/s with $L_{\rm kin} \simeq 9$ per cent $L_{\rm Edd}$. Following Hopkins & Elvis (2010), this kinetic energy would be powerful enough to provide an efficient mechanism of AGN feedback, as it is larger than 0.5 per cent of the bolometric luminosity. It is also worth noting that the angle that the wind forms with respect to the disc is proportional to the initial density. This can be easily understood,

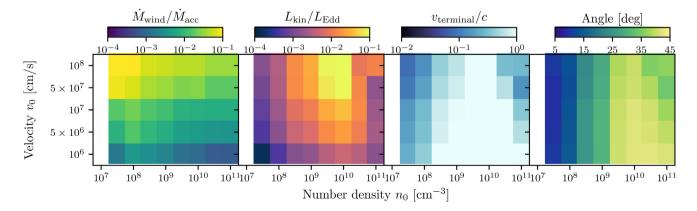


Figure 8. Results of different wind simulations varying the initial density n_0 , and the initial velocity v_0 . The rest of the parameters are fixed to the baseline model values (Table 1), except for $R_{\rm in} = 60 R_{\rm g}$, and $f_x = 0.1$. The first panel shows the mass loss rate normalized to the mass accretion rate, and the second panel shows the wind kinetic luminosity normalized to the Eddington luminosity. Finally, the third and fourth panels show the terminal velocity and angle of the fastest streamline in the wind.

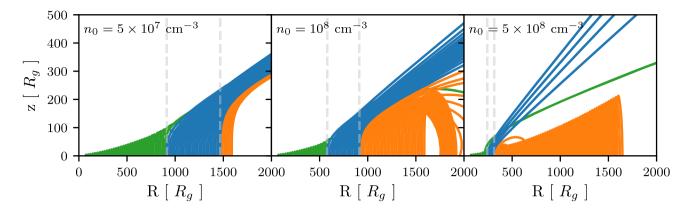


Figure 9. Three wind simulations from the parameter range scan shown in Fig. 8. The initial velocity is fixed to $v_0 = 10^8$ cm/s, while the initial density is varied in the range $n_0 \in (5 \times 10^7, 10^8, 5 \times 10^8)$ cm⁻³. Higher density values shift the escaping region to smaller radii, thus reducing the effective disc surface that produces an escaping wind. Furthermore, the increase in UV shielding narrows the range of escaping streamlines. Note that a high number of streamlines was used to produce Fig. 8, according to the rule in equation (22), but we plot only a fraction of them for clarity.

since, as we discussed before, higher initial densities shift the radii of the escaping streamlines inwards from where most of the UV radiation flux originates. The wind originating from the inner regions of the disc has therefore a higher vertical acceleration, making the escaping angle higher compared to the wind in the outer regions.

3.4 Comparison with hydrodynamic simulations

A proper comparison with the hydrodynamic simulations of N16 and P04 is not straightforward to do, as there is not a direct correspondence of our free parameters with their boundary conditions, and some of the underlying physical assumptions are different (for instance, the treatment of the UV continuum opacity). Nonetheless, with P04 as reference, we have fixed so far $R_{\rm in} = 60~R_{\rm g}$ to match their starting grid radius, and $f_x = 0.1$, as they assume.

Another physical assumption we need to change to compare with P04 is the treatment of the radiative transfer. In P04, the UV radiation field is not attenuated throughout the wind, although line self-shielding is taken into account by the effective optical depth parameter t. Furthermore, the X-ray radiation is considered to only be attenuated by electron-scattering processes, without the opacity boost at $\xi \le 10^5$ erg cm s⁻¹. We thus set $\tau_{\rm UV} = 0$, and $\sigma_x = \sigma_{\rm T}$. Finally, we assume that the initial velocity is $v_0 = 2 \times 10^6$ cm/s, which is just supersonic at $T = 2.5 \times 10^4$ K, and we fix $n_0 =$ 2.5×10^9 cm⁻³, which gives $\tau_X = 1$ at $r = 100 R_g$. The result of this simulation is shown on the top panel of Fig. 10. We notice that not attenuating the UV continuum has a dramatic effect on the wind, allowing much more gas to escape as one would expect. Indeed, the bottom panel of Fig. 10 shows the same simulation but with the standard UV and X-ray continuum opacities used in QWIND. Running the simulation with the normal UV opacity but just electron scattering for the X-ray cross-section results in no wind being produced. For the unobscured simulation that mimics P04, we obtain a wind mass loss rate of 0.3 M_☉/yr, which is in good agreement with the results quoted in P04 ($\dot{M}_{\rm wind} \sim (0.16-0.3)\,{\rm M}_{\odot}/{\rm yr}$). The wind has a kinematic luminosity of $L_{kin} = 0.7$ per cent at the grid boundary, and a terminal velocity ranging (0.016-0.18) c, again comparable to the range (0.006-0.06)c found in P04. Finally, the wind in P04 escapes the disc approximately at an angle between 4° and 21°, while in our case, it flows at an angle in the range of 3°-14°.

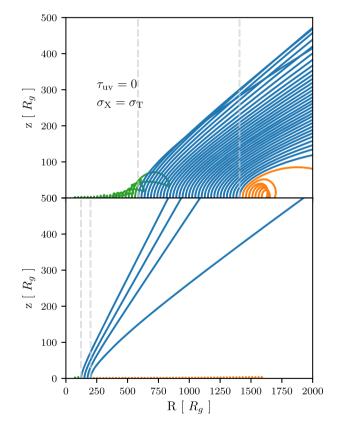


Figure 10. Top panel: Wind simulation with parameter values set to match P04: $f_x = 0.1$, $R_{\rm in} = 60\,R_{\rm g}$, $v_0 = 2\times 10^6$ cm/s, $T = 2.5\times 10^4$ K, and $n_0 = 2.5\times 10^9$ cm⁻³. We also set $\tau_{\rm UV} = 0$, and $\sigma_{\rm X} = \sigma_{\rm T}$ as it is done in P04. Bottom panel: Wind simulation with same parameters as the top panel but using the standard $\tau_{\rm UV}$ and $\tau_{\rm X}$ of QWIND.

4 CONCLUSIONS AND FUTURE WORK

We have presented an updated version of the QWIND code (QWIND2), aimed at modelling the acceleration phase of UV line-driven winds in AGNs. The consistency of our approach with other more sophisticated simulations shows that the non-hydrodynamical treatment is well justified, and that our model has the potential to mimic the results of more expensive hydrodynamical simulations.

The main free parameters of the model are the initial density and velocity of each streamline, and the inner disc radius from which the fluid elements are first launched. Nomura et al. (2013) calibrate the initial wind mass loss using the relation from CAK that links the wind mass loss from O-stars to their gravity and Eddington ratio. However, it is not clear whether this relation holds for accretion discs, where the geometry and the radiation field and sources are quite different (Laor & Davis 2014). To be able to derive these initial wind conditions from first principles, we require a physical model of the vertical structure of the accretion disc. Furthermore, we need to take into account the nature of the different components of the AGN and their impact on the line-driving mechanism. In that regard, we can use spectral models like Kubota & Done (2018) to link the initial conditions and physical properties of the wind to spectral features. We aim to present in an upcoming paper a consistent physical model of the vertical structure of the disc, considering the full extent of radiative opacities involved, that will allow us to infer the initial conditions of the wind.

Another point that needs to be improved is the treatment of the radiation transfer. OWIND and current hydrodynamical simulations compress all of the information about the SED down to two numbers $L_{\rm X}$ and $L_{\rm UV}$; however, the wavelength-dependent opacity can vary substantially across the whole spectrum. This simplification is likely to underestimate the level of ionization of the wind (Higginbottom et al. 2014) and motivates the coupling of OWIND to a detailed treatment of radiation transfer. Higginbottom et al. (2013) construct a simple disc wind model with a Monte Carlo ionization/radiative transfer code to calculate the UV spectra as a function of viewing angle; however, properties of the wind such as its mass flow rate and the initial radius of the escaping trajectories need to be assumed. We will incorporate a full radiative transfer code like CLOUDY or XSTAR to compute the line driving and transmitted spectra together. This also opens the possibility of having a metallicity-dependent force multiplier and studying how the wind changes with different ion populations.

Future development could also include dust opacity to study whether the presence of dust-driven wind can explain the origin of the broad line region in AGN (Czerny & Hryniewicz 2011).

The ability of QWIND to quickly predict a physically based wind mass loss rate makes it very appealing to use as a subgrid model for AGN outflows in large-scale cosmological simulations, as opposed to the more phenomenological prescriptions that are currently employed to describe AGN feedback.

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REFERENCES

Abbott D. C., 1982, ApJ, 259, 282 Andersson C., Führer C., Åkesson J., 2015, MCS, 116, 26

Qwind code release 411 Balbus S. A., Hawley J. F., 1998, Rev. Mod. Phys., 70, 1 Blandford R. D., Payne D. G., 1982, MNRAS, 199, 883 Blandford R. D., Znajek R. L., 1977, MNRAS, 179, 433 Bowler R. A. A., Hewett P. C., Allen J. T., Ferland G. J., 2014, MNRAS, 445, 359 Castor J. I., Abbott D. C., Klein R. I., 1975, ApJ, 195, 157 Crenshaw D. M., Kraemer S. B., 2012, ApJ, 753, 75 Czerny B., Hryniewicz K., 2011, A&A, 525, L8 Dannen R. C., Proga D., Kallman T. R., Waters T., 2019, ApJ, 882, 99 Dyda S., Proga D., 2018a, MNRAS, 475, 3786 Dyda S., Proga D., 2018b, MNRAS, 478, 5006 Ferrarese L., Merritt D., 2000, ApJ, 539, L9 Fukumura K., Kazanas D., Shrader C., Behar E., Tombesi F., Contopoulos I., 2017, Nature, 1, 0062 Gebhardt K. et al., 2000, ApJ, 539, L13 Häring N., Rix H.-W., 2004, ApJ, 604, L89 Higginbottom N., Knigge C., Long K. S., Sim S. A., Matthews J. H., 2013, MNRAS, 436, 1390 Higginbottom N., Proga D., Knigge C., Long K. S., Matthews J. H., Sim S. A., 2014, ApJ, 789, 19 Hindmarsh A., Brown P., Grant K. E., Lee S., Serban R., Shumaker D., Woodward C., 2004, ACM TOMS, 31, 363 Hopkins P. F., Elvis M., 2010, MNRAS, 401, 7 Ji H., Burin M., Schartman E., Goodman J., 2006, Nature, 444, 343 Kormendy J., Ho L. C., 2013, ARA&A, 51, 511 Kubota A., Done C., 2018, MNRAS, 480, 1247 Lam S. K., Pitrou A., Seibert S., 2015, Proceedings of the Second Workshop on the LLVM Compiler Infrastructure in HPC - LLVM '15. ACM Press, Austin, Texas, p. 1 Laor A., Davis S. W., 2014, MNRAS, 438, 3024 Magorrian J. et al., 1998, ApJ, 115, 2285 Murray N., Chiang J., Grossman S. A., Voit G. M., 1995, ApJ, 451, 498 Nomura M., Ohsuga K., 2017, MNRAS, 465, 2873 Nomura M., Ohsuga K., Wada K., Susa H., Misawa T., 2013, PASJ, 65, Nomura M., Ohsuga K., Takahashi H. R., Wada K., Yoshida T., 2016, PASJ, Nomura M., Ohsuga K., Done C., 2018, preprint (arXiv:1811.01966) Novikov I. D., Thorne K. S., 1973, Black Holes (Les Astres Occlus). p. 343 Pounds K. A., Reeves J. N., King A. R., Page K. L., O'Brien P. T., Turner M. J. L., 2003a, MNRAS, 345, 705 Pounds K. A., King A. R., Page K. L., O'Brien P. T., 2003b, MNRAS, 346, 1025 Proga D., 2003, ApJ, 585, 406 Proga D., Kallman T. R., 2004, ApJ, 616, 688 Proga D., Stone J. M., Kallman T. R., 2000, ApJ, 543, 686 Reeves J. N. et al., 2009, ApJ, 701, 493 Risaliti G., Elvis M., 2010, A&A, 516, A89 Shakura N. I., Sunyaev R. A., 1973, A&A, 24, 337

Stevens I. R., Kallman T. R., 1990, ApJ, 365, 321

Stone J. M., Norman M. L., 1992, ApJS, 80, 753

Tombesi F., Cappi M., Reeves J. N., Palumbo G. G. C., Yagoob T., Braito V., Dadina M., 2010, A&A, 521, A57

Virtanen P. et al., 2019, preprint (arXiv:1907.10121)

Weymann R. J., Morris S. L., Foltz C. B., Hewett P. C., 1991, ApJ, 373, 23

APPENDIX A: OPTICAL DEPTH CALCULATION

The computation of the X-ray (and UV analogously) optical depth [equation (3)] is not straightforward, as we need to take into account at which point the drop in the ionization parameter boosts the X-ray opacity. Furthermore, the density is not constant along the light ray. Following the scheme illustrated in Fig. A1, R_X denotes the radius at which the ionization parameter drops below 10^5 erg cm s⁻¹, $R_{\rm in}$ is the radius at which we start the first streamline, and thus the radius from which the shielding starts, and finally R_0 is the initial

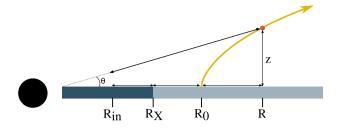


Figure A1. Schematic representation of the geometrical setup to compute the X-ray and UV optical depths. R_0 corresponds to the initial radius of the streamline being considered, and R_x is the radius at which $\xi = 10^5$ erg cm s⁻¹.

radius of the considered streamline. With this notation in mind, we approximate the optical depth by

$$\tau_{\mathbf{X}} = \sec \theta \, \sigma_{\mathbf{T}} \left[n_0 \, \int_{R_{\mathrm{in}}}^{R_0} \kappa(R') \, \mathrm{d}R' + n(R) \, \int_{R_0}^{R} \kappa(R') \, \mathrm{d}R' \right], \quad (A1)$$

with

$$\kappa(R) = \begin{cases} 100 & \text{if } R > R_{\text{X}}, \\ 1 & \text{if } R \le R_{\text{X}}. \end{cases} \tag{A2}$$

The calculation for the UV optical depth is identical but setting the opacity boost factor to unity for all radii.

APPENDIX B: INTEGRAL AND SOLVER CONVERGENCE

B1 Integral convergence

Numerically solving the integrals (15) and (16) can be tricky because the points $\Delta=0$ are singular. We use the QUAD integration method implemented in the SCIPY (Virtanen et al. 2019) PYTHON package to compute them. We fix the absolute tolerance to 0, and the relative tolerance to $10^{-4},$ which means that the integral computation stops once it has reached a relative error of $10^{-4}.$ We have checked that the integrals converge correctly by evaluating the integration error over the whole grid, as can be seen in Fig. B1. The relative errors stays below $10^{-3},$ which is 10 times more the requested tolerance but still a good enough relative error. We thus set a tolerance of 10^{-4} as the code's default.

B2 Solver convergence

To assess the convergence of the IDA solver, we calculate the same gas trajectory multiple times changing the input relative tolerance of the solver from 10^{-15} to 10^{-1} . We take the result with the lowest tolerance as the true value and compute the errors of the computed quantities, R, z, v_R , v_Z relative to our defined true values. As we can see in Fig. B2, the relative error is well behaved and generally accomplishes the desired tolerance. After this assessment, we fix the relative tolerance to 10^{-4} as the code's default.

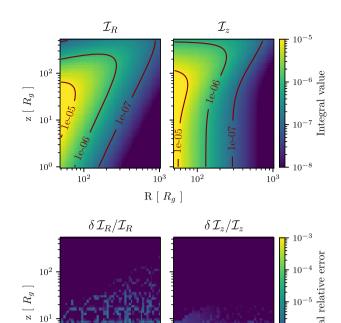


Figure B1. Top panels: Values for the radial and height integrals across the R-z grid. Bottom panels: Relative error of the integrals. Note that the relative error stays well below 10^{-3} for the whole variable range, the low height points being the most difficult to compute.

 $R [R_q]$

 10^{2}

 10^{3}

 10^{0}

 10^{2}

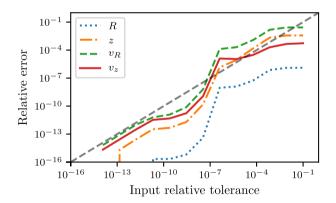


Figure B2. Measured relative error as a function of the input relative tolerance for the ASSIMULO IDA solver. The black dashed line represents equality.

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