The Bolometric Quasar Luminosity Function at z = 0 - 7

Xuejian Shen^{1*}, Philip F. Hopkins¹, Claude-André Faucher-Giguère², D. M. Alexander³, Gordon T. Richards⁴, Nicholas P. Ross⁵, R. C. Hickox⁶

²Department of Physics and Astronomy and Center for Interdisciplinary Exploration and Research in Astrophysics (CIERA), Northwestern University,

2145 Sheridan Road, Evanston, IL 60208, USA

³Centre for Extragalactic Astronomy, Department of Physics, Durham University, South Road, Durham DH1 3LE, UK

⁵Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK

⁶Department of Physics and Astronomy, Dartmouth College, 6127 Wilder Laboratory, Hanover, NH 03755, USA

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ABSTRACT

In this paper, we provide updated constraints on the bolometric quasar luminosity function (QLF) from z = 0to z = 7. The constraints are based on an observational compilation that includes observations in the rest-frame IR, B band, UV, soft and hard X-ray in past decades. Our method follows Hopkins et al. 2007 with an updated quasar SED model and bolometric and extinction corrections. The new best-fit bolometric quasar luminosity function behaves qualitatively different from the Hopkins et al. 2007 model at high redshift. Compared with the old model, the number density normalization decreases towards higher redshift and the bright-end slope is steeper at $z \gtrsim 2$. Due to the paucity of measurements at the faint end, the faint end slope at $z \gtrsim 5$ is quite uncertain. We present two models, one featuring a progressively steeper faint-end slope at higher redshift and the other featuring a shallow faint-end slope at $z \gtrsim 5$. Further multi-band observations of the faint-end QLF are needed to distinguish between these models. The evolutionary pattern of the bolometric QLF can be interpreted as an early phase likely dominated by the hierarchical assembly of structures and a late phase likely dominated by the quenching of galaxies. We explore the implications of this model on the ionizing photon production by quasars, the CXB spectrum, the SMBH mass density and mass functions. The predicted hydrogen photoionization rate contributed by quasars is subdominant during the epoch of reionization and only becomes important at $z \leq 3$. The predicted CXB spectrum, cosmic SMBH mass density and SMBH mass function are generally consistent with existing observations.

Key words: cosmology: observations – quasars: general – galaxies: active – galaxies: nuclei – ultraviolet: galaxies – X-rays: galaxies – infrared: galaxies

1 INTRODUCTION

Luminous quasars and active galactic nuclei (AGN) in general ¹ are observable manifestations of accreting supermassive black holes (SMBHs) at galaxy centers. Gas accreted onto the SMBH forms an accretion disk from which thermal emission is generated through dissipative processes (e.g., Shakura & Sunyaev 1973; Rees 1984). Due to their high radiative efficiency, such objects can be extremely luminous and are detected at z > 7 (Mortlock et al. 2011; Venemans et al. 2015; Bañados et al. 2018). The evolution of quasars is crucial to understand the formation and evolution of SMBHs in the Universe. Apart from that, quasars are one of the most important radiation sources in the Universe. They are luminous in almost all

accessible bands and their radiation has a significant impact in the Universe. For example, quasar emission is important for the build-up of cosmic infrared (IR) and X-ray radiation backgrounds. Quasar emission in the extreme ultraviolet (UV) is believed to dominate the reionization of helium in the Universe and may have a nonnegligible contribution to the reionization of hydrogen, although star-forming galaxies dominate hydrogen reionization in most current models (e.g., Faucher-Giguère et al. 2008a,b, 2009; Kuhlen & Faucher-Giguère 2012; Robertson et al. 2015; Haardt & Salvaterra 2015; Giallongo et al. 2015; Onoue et al. 2017; Parsa et al. 2018). Furthermore, observations have demonstrated that galaxies and SMBHs co-evolve (see reviews of Alexander & Hickox 2012; Fabian 2012; Kormendy & Ho 2013; Heckman & Best 2014, and references therein). For example, the masses of the SMBHs are correlated with the masses, luminosities and velocity dispersions of their host galaxy spheroids (e.g., Magorrian et al. 1998; Ferrarese & Merritt 2000; Gebhardt et al. 2000; Gültekin et al. 2009). AGN

¹TAPIR, California Institute of Technology, Pasadena, CA 91125, USA

⁴Department of Physics, Drexel University, 32 S. 32nd Street, Philadelphia, PA 19104, USA

^{*} E-mail: xshen@caltech.edu

¹ We use the phrase "quasar" across the paper. We are not just referring to the optically bright and unobscured systems but the entire AGN population.

are also widely believed to impact star formation in their host galaxies via a "feedback" mechanism that helps quench galaxies (e.g., Sanders & Mirabel 1996; Springel et al. 2005; Bower et al. 2006; Croton et al. 2006; Sijacki et al. 2007; Somerville et al. 2008; Hopkins et al. 2008; Feruglio et al. 2010; Fabian 2012; Cicone et al. 2014) and solve the classical "cooling flow" problem (e.g., Cowie & Binney 1977; Fabian & Nulsen 1977; Fabian et al. 1984; Tabor & Binney 1993; Fabian 1994; Croton et al. 2006). Therefore, studying the evolution of quasar populations along cosmic time is of great importance in cosmology and galaxy formation.

The quasar luminosity function (QLF), which is the comoving number density of quasars as a function of luminosity, is perhaps the most important observational signature of quasar populations. The study of the OLF goes back decades in the rest-frame optical/UV (e.g., Schmidt 1968; Schmidt & Green 1983; Koo & Kron 1988; Boyle et al. 1988; Hartwick & Schade 1990; Hewett et al. 1993; Warren et al. 1994; Schmidt et al. 1995a; Kennefick et al. 1995; Pei 1995; Boyle et al. 2000; Fan et al. 2001c, 2004; Richards et al. 2006a; Croom et al. 2009; Willott et al. 2010; Glikman et al. 2011; Ross et al. 2013; McGreer et al. 2013; Kashikawa et al. 2015; Jiang et al. 2016), soft X-ray (e.g., Maccacaro et al. 1991; Boyle et al. 1993; Jones et al. 1997; Page et al. 1997; Miyaji et al. 2000; Hasinger et al. 2005), hard X-ray (e.g., Ueda et al. 2003; La Franca et al. 2005; Barger et al. 2005; Silverman et al. 2008; Ebrero et al. 2009; Yencho et al. 2009; Aird et al. 2010; Ueda et al. 2014; Aird et al. 2015a) and IR (e.g., Brown et al. 2006; Matute et al. 2006; Assef et al. 2011; Lacy et al. 2015). These studies have conclusively shown that the observed QLF exhibits a strong redshift evolution. This is not simply an evolution in the normalization (number density) but also in the slope of the QLF. For instance, the number density of low luminosity AGN peaks at lower redshift than that of bright quasars indicating the "cosmic downsizing" of AGN (e.g., Cowie et al. 1996; Barger et al. 2005; Hasinger et al. 2005). AGN feedback that shuts down the supply of gas for accretion may be responsible for this phenomenon. Both optical and X-ray studies have argued that the faint-end slope of the QLF gets steeper from z = 2 to z = 0 (e.g., Aird et al. 2015a; Kulkarni et al. 2018). These investigations of the QLF have also found that both the typical spectral shape (e.g., Wilkes et al. 1994; Green et al. 1995; Vignali et al. 2003; Strateva et al. 2005; Richards et al. 2006b; Steffen et al. 2006; Just et al. 2007; Lusso et al. 2010; Kashikawa et al. 2015; Lusso & Risaliti 2016) and the obscuring column density distribution of quasars (e.g., Hill et al. 1996; Simpson et al. 1999; Willott et al. 2000; Steffen et al. 2003; Ueda et al. 2003; Grimes et al. 2004; Sazonov & Revnivtsev 2004; Barger et al. 2005; Hao et al. 2005; Ueda et al. 2014) have a dependence on quasar luminosity. For example, fainter quasars tend to be more obscured and their emission is more dominated by the X-rays.

In the last decade, the redshift frontier of the observations of quasars have been pushed up to z > 7 (Mortlock et al. 2011; Bañados et al. 2018; Wang et al. 2018b) and about 40 quasars are now known at $z \gtrsim 6.5$ (e.g., Willott et al. 2010; Venemans et al. 2013, 2015; Jiang et al. 2016; Reed et al. 2017; Mazzucchelli et al. 2017; Matsuoka et al. 2018; Ross & Cross 2019). These quasars reveal the early growth of SMBHs and also pinpoint the locations for the assembly of massive galaxies in the early Universe. The absorption spectra of these high redshift quasars are important to study the reionization history of the Universe (e.g., Miralda-Escudé 1998; Madau & Rees 2000; Fan et al. 2002, 2006). However, due to the rapid decline in the quasar number density at high redshift, detecting quasars and constraining the QLF is currently very difficult at $z \gtrsim 6$. The next generation deep, wide-field infrared surveys

will help push the detection of quasars to $z \approx 9 - 10$ and deeper optical/UV surveys will provide better constraints on the faint end of the QLF.

Interpreting the observational findings, however, is complicated by the fact that observations in a single band are always subject to selection effects, host galaxy contamination and reddening and obscuration all in a complicated, wavelength-dependent manner. Although quasars are intrinsically very luminous in the optical/UV, dust extinction along some viewing angles (e.g., Antonucci 1993; Urry & Padovani 1995) can make quasars much more difficult to detect. Heavily obscured AGN can easily be contaminated with the UV stellar light from their host galaxies (e.g., see review of Hickox & Alexander 2018). Even in the X-ray, which is much less affected by dust, the Compton-thick (CTK) AGN, which account for 20% - 50% (e.g., Burlon et al. 2011; Ricci et al. 2015) of the total AGN population, are still severely blocked and current observations remain largely incomplete. In the mid-IR, due to the strong absorption in the terrestrial atmosphere, observations are more limited and also can be contaminated by the hot dust emission in star forming galaxies. In far-IR to millimeter wavelengths ($30\mu m - 10 \text{ mm}$), the majority of AGN are contaminated by emission from dust heated by star formation in host galaxies, which limits the effectiveness of AGN identification. Furthermore, measurements of the QLF based on a single survey are limited in their luminosity coverage and volume probed and are subjected to various biases and uncertainties in completeness corrections.

Given these limitations, what physical models for AGN demographics, SMBH growth and AGN feedback, really require is the bolometric QLF over all redshifts. The bolometric quasar luminosity is the quantity tightly related to the accretion rate of the SMBH and is the ideal quantity to study the physical evolution of quasars. Hopkins et al. (2007) developed a bolometric QLF model that simultaneously fitted the accessible measurements at the time, in different bands. The model has been widely used but has several important shortcomings: First, the model was poorly constrained at $z \gtrsim 3$ due to limited available data at the time and has been shown to deviate significantly from recent observations. Second, the integrated bolometric luminosity at the bright end predicted by this model actually diverges when extrapolating to high redshift ($z \sim 7 - 8$). Third, the number density normalization of the QLF was assumed to be a constant over redshifts, which does not agree with newer observations at high redshift.

In this paper, we provide a new model for the bolometric QLF at z = 0 - 7 constrained by emerging observations of the QLF in the optical, UV, IR and X-ray in the last decade. The paper is organized as follows: In Section 2, we introduce our observational data compilation. In Section 3, we introduce our model linking the observed QLFs with the bolometric QLF. The model includes new bolometric and extinction corrections. In Section 4, we perform a fit to the data and constrain the bolometric QLF. In Section 5, the evolution of the bolometric QLF is analyzed. In Section 6, we present several predictions from our best-fit bolometric QLF model and demonstrate its consistency with observations from independent channels.

We employ the following cosmological parameters: $\Omega_{\rm m} = 0.30$, $\Omega_{\Lambda} = 0.70$, $H_0 = 100h \,\rm km \, s^{-1} \, Mpc^{-1} = 70 \,\rm km \, s^{-1} \, Mpc^{-1}$. The code of all the analysis in this paper along with the observational data compiled are publicly available (see Appendix C for details).

Band name	Definition of luminosity	Bolometric correction parameters (c_1,k_1,c_2,k_2)	Dispersion parameters $(\sigma_1, \sigma_2, \log L_0, \sigma_3)$
B band	$ u_{ m 4400 \AA} L_{ u_{ m 4400 \AA}}$	(3.759, -0.361, 9.830, -0.0063)	(-0.383, 0.405, 42.39, 2.378)
UV	the AB magnitude measured in a top-hat filter centering at rest-frame 1450Å with bandwidth 100Å or almost equivalently in terms of luminosity $\nu_{1450Å}L\nu_{1450Å}$	(1.862, -0.361, 4.870, -0.0063)	(-0.372, 0.405, 42.31, 2.310)
Soft X-ray	the integrated luminosity in $0.5 - 2 \text{ keV}$	(5.712, -0.026, 17.67, 0.278)	(0.080, 0.180, 44.16, 1.496)
Hard X-ray	the integrated luminosity in 2 - 10 keV	(4.073, -0.026, 12.60, 0.278)	(0.193, 0.066, 42.99, 1.883)
Mid-IR	$v_{15\mu \mathrm{m}} L_{v_{15}\mu \mathrm{m}}$	(4.361, -0.361, 11.40, -0.0063)	(-0.338, 0.407, 42.16, 2.193)

Table 1. Definitions of the luminosities in the bands considered in this paper and best-fit parameters of their bolometric corrections and dispersions.

2 OBSERVATIONAL DATA SETS

In this section, we briefly introduce the observations compiled in this work and emphasize the corrections adopted. A full list of the observations compiled is shown in Table A1. We note that some observations used overlapping quasar samples in their binned estimations and are thus not fully independent. We do not include older observations if all the quasar samples used there were covered by later work. For all the observational data, we correct all relevant quantities (distances, luminosities, volumes) to be consistent with our adopted cosmological parameters.

2.1 Optical/UV

We define "optical" wavelengths as $2500\text{\AA} \le \lambda \le 1\mu\text{m}$ and "UV" wavelengths as $600\text{\AA} \le \lambda \le 2500\text{\AA}^2$. We unify the luminosities measured in rest-frame optical (UV) wavelengths in observations to the B band (UV) luminosity defined in Table 1. The optical/UV QLF observations compiled in this work are largely based on the observations listed in Hopkins et al. (2007); Giallongo et al. (2012); Manti et al. (2017) and Kulkarni et al. (2018) (along with their QLF data shared online ³). The observational compilation from Kulkarni et al. (2018) includes: Bongiorno et al. (2007); Siana et al. (2008); Jiang et al. (2009); Willott et al. (2010); Glikman et al. (2011); Masters et al. (2012); Palanque-Delabrouille et al. (2013); Ross et al. (2013); McGreer et al. (2013); Kashikawa et al. (2015). In the Kulkarni et al. (2018) compilation, the poisson errors in several works were recomputed using the Gehrels (1986) formula. The Kcorrections have been unified to that in Lusso et al. (2015), which is based on the stacked spectra of 53 quasars observed at $z \sim 2.4$. In fact, the uncertainty in K-corrections owing to different spectral assumptions was estimated to be within 0.2 mag (Lusso et al. 2015) which is smaller than the uncertainties of the binned estimation itself. The uncertainties in conversion factors between luminosities of different rest-frame bands were also estimated to be smaller than other sources of errors. Other specific corrections have been made in the Kulkarni et al. (2018) compilation are: (1) bins with severe incompleteness from Ross et al. (2013) were discarded; (2) binned estimations in Palanque-Delabrouille et al. (2013) at z > 2.6 were discarded since Lyman-alpha forest enters g band for those redshifts; (3) data from McGreer et al. (2013) was restricted to M_{1450} > -26.73 to avoid overlapping with Yang et al. (2016); (4) for Willott et al. (2010) and Kashikawa et al. (2015), the redshift intervals were recomputed using consistent completeness estimations.

Outside the Kulkarni et al. (2018) compilation, we include measurements from Fontanot et al. (2007); Croom et al. (2009); Shen & Kelly (2012); Jiang et al. (2016); Palanque-Delabrouille et al. (2016); Yang et al. (2016); Akiyama et al. (2018); Matsuoka et al. (2018); McGreer et al. (2018); Wang et al. (2018a); Yang et al. (2018). Observed optical band luminosities are all converted to UV luminosity either with corrections made in these papers or with the formula in Ross et al. (2013) if no corrections had already been made. Matsuoka et al. (2018) and Yang et al. (2018) have binned estimations that correspond to only one object in the bin, which were interpreted as upper limits there. However, their Poisson error estimations were not correct and we recalculate the Poisson errors using the table in Gehrels (1986). After the correction, these data points have proper upper and lower limits and can be included into our standard fitting procedure. For the observations compiled in Hopkins et al. (2007) (Kennefick et al. 1995; Schmidt et al. 1995a; Fan et al. 2001a,b, 2003, 2004; Wolf et al. 2003; Cristiani et al. 2004; Croom et al. 2004; Hunt et al. 2004; Richards et al. 2005, 2006b; Siana et al. 2006), we include only those whose quasar samples are not completely covered by the more recent work discussed above. The details of all the observations compiled in this paper are listed in Table A1.

2.2 X-ray

We define "X-ray" wavelengths as $\lambda \leq 50$ Å ($E \gtrsim 0.25$ keV) which covers the typical soft X-ray and hard X-ray bands defined in Table 1. In the X-ray, in addition to the observations compiled in Hopkins et al. (2007) (Miyaji et al. 2000, 2001; Ueda et al. 2003; Sazonov & Revnivtsev 2004; Barger et al. 2005; La Franca et al. 2005; Hasinger et al. 2005; Nandra et al. 2005; Silverman et al. 2005), we include new observational data from Ebrero et al. (2009); Aird et al. (2008); Silverman et al. (2008); Yencho et al. (2009); Aird et al. (2010); Fiore et al. (2012); Ueda et al. (2014); Aird et al. (2015a,b); Miyaji et al. (2015); Khorunzhev et al. (2018). Among them, Aird et al. (2008) is an update based on Nandra et al. (2005) and Silverman et al. (2008) is an extension to Silverman et al. (2005). Aird et al. (2015a) and Ueda et al. (2014) derived binned estimation of the hard X-ray luminosity functions separately based on soft or hard X-ray selected samples. We include both of them in our compilation. Aird et al. (2015b) is an observation of the 10 – 40 keV X-ray luminosity function. The luminosities are converted to the hard X-ray luminosities with our SED model which will be discussed in the following section. Some observational works (Ebrero et al. 2009; Ueda et al. 2014; Aird et al. 2015b; Miyaji et al. 2015) have done their own "absorption" corrections and presented the "de-absorbed" compton

² The quasar SED at rest-frame 50Å $\leq \lambda \leq$ 600Å is almost inaccessible in optical/UV observations due to strong extinction at these wavelengths. In the construction of our SED model in Section 3.1, we directly connect the 600Å flux with the X-ray SED.

³ https://github.com/gkulkarni/QLF/blob/master/Data/allqlfs.dat

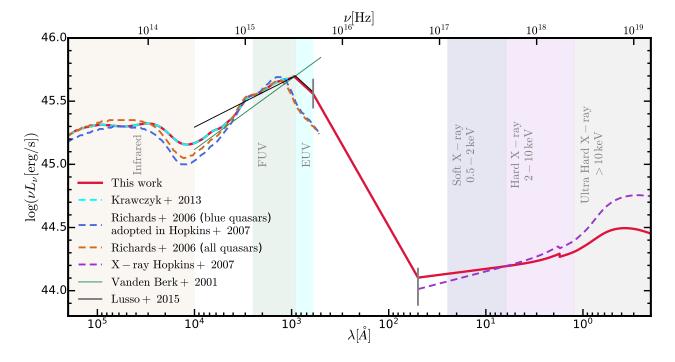


Figure 1. Mean SED template of quasars constructed in this work. The template SED shown here has the normalization $\nu L_{\nu} \simeq 45.5 \text{ erg s}^{-1}$ at 2500Å. The solid red line represents our fiducial SED model. SED templates from other works are presented: Richards et al. (2006b), the blue and orange dashed lines; Hopkins et al. (2007) X-ray SED, the purple dashed line; Krawczyk et al. (2013), the cyan dashed line. The power-law models for optical/UV SED are shown in the green (Vanden Berk et al. 2001) and black (Lusso et al. 2015) thin lines. The common bands for the measurements of quasar luminosities are shown with shaded regions. In this paper, the bolometric luminosity is defined as the integrated luminosity from 30 μ m to 500 keV.

thin QLFs. This would potentially generate double-counting of the extinction effects since we also intend to do extinction corrections in our model. We address this by reintroducing the extinction effect (only in the compton thin regime) for these data points using our extinction model which will be discussed in Section 3.2.

2.3 Infrared (IR)

We define "IR" wavelengths as $\lambda \ge 1\mu$ m. We unify the luminosities measured in rest-frame IR wavelengths to the mid-IR luminosity defined in Table 1. In the IR, in addition to the observations compiled in Hopkins et al. (2007) (Brown et al. 2006; Matute et al. 2006), we include new observations from Assef et al. (2011) and Lacy et al. (2015). The luminosities are converted to the mid-IR (15 μ m) luminosity with our SED model. These observations have extended the redshift coverage of the IR QLF up to z = 5.8. However, there is still an apparent deficiency in IR observations compared with other wavelengths. Deep and large field IR surveys are an urgent need in the study of the QLF at high redshift. Though the total number of IR data points are limited and thus they have low statistical significance in the fit of the bolometric QLF, they do provide an independent check for our bolometric QLF model.

3 MODEL

3.1 SED model and bolometric corrections

In this section, we construct the mean SED model for quasars. With the mean SED, we will calculate the bolometric corrections for the rest-frame B band, UV, soft & hard X-ray and mid-IR, respectively.

3.1.1 Optical/UV

In the optical/UV, we start with the SED template in Krawczyk et al. (2013), which was based on 108184 luminous broad-lined quasars observed at 0.064 < z < 5.46. Among these sources, 11468 showing sign of dust reddening ($\Delta(g-i) > 0.3$) had been discarded by Krawczyk et al. (2013) in deriving the mean SED template. Therefore, this SED template can be considered not strongly affected by reddening and obscuration. The extinction corrections on the quasar luminosities will be considered separately in the next section. This SED template starts at ~ 30μ m and truncates at 912Å. We extend the SED to the extreme UV (here defined as $\lambda < 912$ Å) using the power-law model $f_V = v^{\alpha_V}$ with index $\alpha_V = -1.70$ reported by Lusso et al. (2015). We truncate this extension at 600Å where Lusso et al. (2015)'s measurement ended and directly connect the flux at 600Å with the X-ray template which will be discussed then.

Historically, the optical/UV SED was often modelled as a power-law $f_{\nu} = \nu^{\alpha_{\nu}}$. In the UV, Vanden Berk et al. (2001) found that the 1300Å to 5000Å continuum roughly has a power-law index $\alpha_{\nu} = -0.44 \pm 0.10$. Telfer et al. (2002) found $\alpha_{\nu} = -0.69 \pm 0.06$ at 1200Å $\leq \lambda \leq 2200$ Å. Shull et al. (2012) found $\alpha_{\nu} = -0.68 \pm 0.14$ at 1200Å $\leq \lambda \leq 2000$ Å. Lusso et al. (2015) found $\alpha_{\nu} = -0.61 \pm 0.01$ at 912Å $\leq \lambda \leq 2500$ Å. The differences between Vanden Berk et al. (2001) and other updated measurements arise from different continuum regions used to measure the slope. In the extreme UV, Telfer et al. (2002) found $\alpha_{\nu} = -1.76 \pm 0.12$ at 500Å $\leq \lambda \leq 1200$ Å. Scott et al. (2004) found $\alpha_{\nu} = -0.56^{+0.38}_{-0.28}$ at 630Å $\leq \lambda \leq 1155$ Å. Lusso et al. (2015) found $\alpha_{\nu} = -1.70 \pm 0.61$ at ~ 600 Å $\leq \lambda \leq 912$ Å. The update of break point from ~ 1200 Å to ~ 912 Å mainly attributes to more careful correction on IGM absorption (Lusso et al. 2015). We do not consider the potential redshift/luminosity dependence of

the break point, since it has almost no influence on the bolometric corrections. In Figure 1, we show that our optical/UV SED template is generally consistent with the most recent power-law models.

3.1.2 IR

In the IR, we adopt the SED template in Krawczyk et al. (2013). We extend the template in the long wavelength end to 100μ m using the Richards et al. (2006b) SED which behaves almost the same as the Krawczyk et al. (2013) SED at $\lambda > 10\mu$ m. We note that this IR SED has already included dust emission. No additional dust emission model will be required.

3.1.3 X-ray

The X-ray SED template is generated with a cut-off power-law model $f(E) \sim E^{1-\Gamma} \exp(-E/E_c)$ with the photon index $\Gamma = 1.9$ and the cut-off energy $E_c = 300$ keV (e.g., Dadina 2008; Ueda et al. 2014; Aird et al. 2015a). An additional reflection component is added using the PEXRAV model (Magdziarz & Zdziarski 1995) assuming the reflection relative strength R = 1, the inclination angle $i = 60^{\circ}$ and solar abundances. Then, we have to properly normalize the X-ray SED relative to the optical SED. Previous studies have reported a correlation between $L_{\nu}(2 \text{ keV})$ and $L_{\nu}(2500\text{ Å})$ (the unit of L_{ν} is erg s⁻¹ Hz⁻¹):

$$\log L_{\nu}(2 \,\text{keV}) = \beta \log L_{\nu}(2500 \text{\AA}) + C, \tag{1}$$

where β is found to be 0.7 – 0.8 suggesting a non-linear correlation between the X-ray and optical luminosities. Defining α_{ox} as:

$$\alpha_{\rm ox} = \frac{\log L_{\nu}(2\,\text{keV}) - \log L_{\nu}(2500\text{\AA})}{\log \nu(2\,\text{keV}) - \log \nu(2500\text{\AA})} = 0.384 \log \left(\frac{L_{\nu}(2\,\text{keV})}{L_{\nu}(2500\text{\AA})}\right)$$
(2)

Then Equation 1 can be rewritten as:

$$\alpha_{\rm ox} = -A \log \left(\frac{L_{\nu} (2500 \text{\AA})}{\text{erg s}^{-1} \text{Hz}^{-1}} \right) + C', \tag{3}$$

where $A = 0.384 (1 - \beta)$ and C' = 0.384C. These prefactors have been measured through observations. However, since there is scatter in this relation, treating $L_{\nu}(2500\text{\AA})$ or $L_{\nu}(2 \text{ keV})$ as the independent variable will lead to different results if quasars are not perfectly selected in observations. The bisector of the two fitted relation treating either $L_{\nu}(2500\text{\AA})$ or $L_{\nu}(2 \text{ keV})$ as the independent variable is usually adopted. For example, Steffen et al. (2006) measured $\beta = 0.721 \pm 0.011$ and $C = 4.531 \pm 0.688$; Just et al. (2007) measured $\beta = 0.709 \pm 0.010$ and $C = 4.822 \pm 0.627$; Lusso et al. (2010) measured $\beta = 0.760 \pm 0.022$ and $C = 3.508 \pm 0.641$. Young et al. (2010); Xu (2011); Lusso & Risaliti (2016) found consistent results with previous works though they treated $L_{\nu}(2500\text{\AA})$ as the independent variable. Dependence of α_{ox} on redshift had been reported in Bechtold et al. (2003), but was not confirmed in the following studies. Given these observational results, we conclude that the relation constrained by Steffen et al. (2006), which was adopted in Hopkins et al. (2007), is still consistent with updated observations. We continue to use the parameters measured by Steffen et al. (2006) though varying the parameter choices does not have a significant influence on the bolometric corrections. The X-ray SED is then scaled with the α_{ox} with respect to the optical SED.

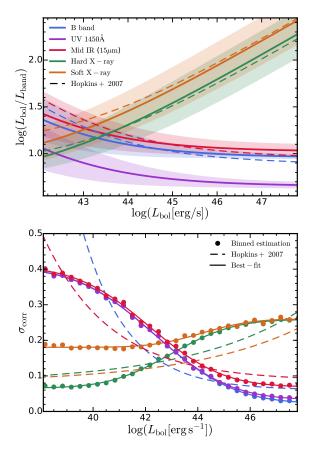


Figure 2. *Top:* Bolometric corrections as a function of bolometric quasar luminosity. We show the bolometric corrections in the rest-frame B band, UV, mid-IR, soft and hard X-ray determined by our fiducial quasar mean SED template. 1σ dispersions are shown with shaded region. The bolometric corrections in Hopkins et al. (2007) are shown in dashed lines. *Bottom:* Magnitude of the dispersions in bolometric corrections as a function of bolometric quasar luminosity. Both binned estimations and best-fit relations are presented.

3.1.4 Bolometric corrections

The direct product of our quasar SED model is the bolometric correction, defined as the ratio between the bolometric luminosity, L_{bol} , and the observed luminosity in a certain band, L_{band} . The definitions of the luminosities in the bands are presented in Table 1. The bolometric luminosity is defined as the integrated luminosity from 30μ m to 500 keV, which represents all the energy budget generated by the accretion of the SMBH. ⁴ Some studies (e.g., Marconi et al. 2004; Krawczyk et al. 2013) have discussed that the reprocessed emission in the IR and > 2 keV X-ray should be excluded in determining the bolometric luminosity to avoid potential double-counting of quasars' intrinsic emission. We have tested that using 1μ m to 2 keV as the range for integration will systematically decrease the bolometric luminosity by ~ 0.2 dex.

However, quasars do not have a single universal SED. There are real variations in the spectral shape, which translate to scatters in the bolometric corrections and influence the observed QLFs in

⁴ Some studies included the emission beyond 30μ m in the bolometric luminosity. But we find that extending the long-wavelength bound to 100μ m will only lead to < 0.02 dex difference in the bolometric luminosity.

the bands. To evaluate this, we first create an ensemble of SEDs. The configuration of these SEDs are similar to our fiducial SED: in the IR, we adopt our fiducial SED; in the optical/UV, for simplicity, we adopt a broken power-law with the break point at 912Å, with a fixed slope -1.70 at $\lambda < 912$ Å and a free slope α_{opt} at $\lambda > 912$ Å; in the X-ray, we adopt our fiducial X-ray SED model but with a free photon index Γ ; the optical/UV and X-ray SEDs are connected with a free α_{ox} . We generate an ensemble of 10⁵ SEDs with randomly sampled $L_{\nu}(2500\text{\AA})$, α_{opt} , Γ and α_{ox} . In sampling α_{opt} , Γ and $\alpha_{\rm ox}$, we adopt a normal distribution around median value with a constant scatter. We adopt $\overline{\Gamma} \pm \sigma_{\Gamma} = 1.9 \pm 0.2$ (e.g., Ueda et al. 2014; Aird et al. 2015a), $\overline{\alpha_{\text{opt}}} \pm \sigma_{\text{opt}} = -0.44 \pm 0.125$ (Vanden Berk et al. 2001; Richards et al. 2003), $\sigma_{ox} \simeq 0.1$ (e.g., Steffen et al. 2006; Lusso et al. 2010). The bolometric luminosity and bolometric corrections for each realization of the SED are calculated. Then we divide the SEDs based on their bolometric luminosities into 30 uniformly log-spaced bins from 10^{38} to 10^{48} erg s⁻¹. We evaluate the standard deviation of the bolometric correction of each band in each bolometric luminosity bin, shown in the bottom panel of Figure 2. Double plateaus show up at the bright and faint ends where a certain band is dominant or negligible in the bolometric luminosity. In Hopkins et al. (2007), the dispersion of the bolometric corrections were fitted with: $\sigma_{\rm corr}(L_{\rm bol}) = \sigma_1 (L_{\rm bol}/10^9 \, {\rm L_{\odot}})^{\beta} + \sigma_2$. However, we find this formula no longer appropriate to fit our results, so we fit the dispersion with an error function:

$$\sigma_{\rm corr}(\log L_{\rm bol}) = \sigma_2 + \sigma_1 \left[\frac{1}{2} + \frac{1}{2} \operatorname{erf}\left(\frac{\log L_{\rm bol} - \log L_0}{\sqrt{2}\sigma_3}\right) \right], \qquad (4)$$

which naturally exhibits a double plateau shape. The best-fit parameters are listed in Table 1. The fitted relations are also shown in the bottom panel of Figure 2. These results indicate a ~ 0.1 dex uncorrelated dispersion in quasar SEDs that is consistent with observations.

In the top panel of Figure 2, we show the bolometric corrections as a function of bolometric luminosity for all bands along with their dispersions shown with shaded regions. The bolometric corrections are generally similar to the Hopkins et al. (2007) model except for the differences at the faint end driven by the updates in the X-ray SED. Following Hopkins et al. (2007), we fit the dependence of the bolometric corrections on bolometric luminosity with a double power-law:

$$\frac{L_{\rm bol}}{L_{\rm band}} = c_1 \left(\frac{L_{\rm bol}}{10^{10} \, \rm L_{\odot}}\right)^{k_1} + c_2 \left(\frac{L_{\rm bol}}{10^{10} \, \rm L_{\odot}}\right)^{k_2}.$$
 (5)

The best-fit parameters are listed in Table 1.

We note that the derivation of the optical/UV and X-ray luminosities using these bolometric corrections has not considered extinction yet. The observed luminosities will be further affected by extinction, which will be discussed in the following section.

3.2 Dust and gas extinction

The absorption and scattering of surrounding gas and dust further modifies the intrinsic emission of quasars. Neutral hydrogen photoelectric absorption is crucial to the extinction in the X-ray while dust is crucial to the extinction in the optical/UV. Here, we first introduce the neutral hydrogen column density ($N_{\rm H}$) distribution model which determines the extinction in the X-ray. Then, $N_{\rm H}$ is converted to the column density of dust assuming a dust-to-gas ratio. The dust abundance determines the extinction in the optical/UV.

In Hopkins et al. (2007), where the constant $N_{\rm H}$ model was

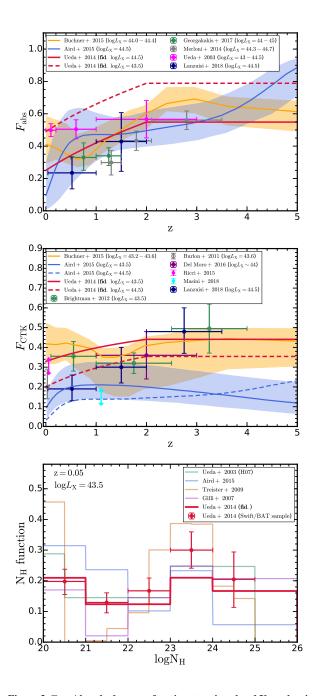


Figure 3. *Top:* Absorbed quasar fraction at a given hard X-ray luminosity as a function of redshift. We present the prediction from our fiducial model, the $N_{\rm H}$ model in Ueda et al. (2014), with red lines. The solid red line is for log $L_{\rm X}$ = 44.5 while the dashed one is for log $L_{\rm X}$ = 43.5. We compare the ficucial model with other observations (labeled). *Middle:* Compton thick quasar fraction at a given hard X-ray luminosity as a function of redshift. We compare the fiducial model with other observations (labeled). Here, the solid red line is for log $L_{\rm X}$ = 43.5 while the dashed one is for log $L_{\rm X}$ = 44.5. *Bottom:* $N_{\rm H}$ distribution at log $L_{\rm X}$ = 43.5 and z = 0.05. We compare our fiducial model with other models (labeled) and the N_H distribution of Swift/BAT samples (Ueda et al. 2014).

shown to fail, the $N_{\rm H}$ distribution model from Ueda et al. (2003) was adopted as the fiducial model. Here, we update the $N_{\rm H}$ distribution with the results from Ueda et al. (2014), which was based on measurements of $N_{\rm H}$ and the intrinsic hard X-ray luminosity for each individual object in their sample. The model provides the probability distribution of $N_{\rm H}$, $f(L_X, z; N_{\rm H})$, at a given intrinsic hard X-ray luminosity (denoted as L_X) and a redshift. $f(L_X, z; N_{\rm H})$ is normalized in the compton thin (CTN, $\log N_{\rm H} \le 24$) regime:

$$\int_{20}^{24} f(L_{\rm X}, z; N_{\rm H}) \,\mathrm{d}\log N_{\rm H} = 1, \tag{6}$$

where the unit of $N_{\rm H}$ is assumed to be cm⁻² and the lower limit of log $N_{\rm H} = 20$ is a dummy value introduced for convenience and Ueda et al. (2014) has assigned log $N_{\rm H} = 20$ for all the quasars with log $N_{\rm H} < 20$.

 $f(L_X, z; N_H)$ is characterized by three parameters: $\psi(L_X, z)$, the fraction of absorbed quasars ($22 \le \log N_H \le 24$) in total CTN quasars; f_{CTK} , the fraction of compton thick (CTK, $\log N_H \ge 24$) quasars relative to the fraction of absorbed CTN quasars; ϵ , the ratio of the quasars with $23 \le \log N_H \le 24$ to those with $22 \le \log N_H \le$ 23. This N_H distribution can then be written as (Ueda et al. 2014):

$$f(L_{\rm X}, z; N_{\rm H}) = \begin{cases} 1 - \frac{2+\epsilon}{1+\epsilon} \psi(L_{\rm X}, z) & [20 \le \log N_{\rm H} < 21] \\ \frac{1}{1+\epsilon} \psi(L_{\rm X}, z) & [21 \le \log N_{\rm H} < 22] \\ \frac{1}{1+\epsilon} \psi(L_{\rm X}, z) & [22 \le \log N_{\rm H} < 23] \\ \frac{1}{1+\epsilon} \psi(L_{\rm X}, z) & [23 \le \log N_{\rm H} < 24] \\ \frac{f_{\rm CTK}}{2} \psi(L_{\rm X}, z) & [24 \le \log N_{\rm H} < 26] \end{cases}$$
(7)

 $1 + \epsilon$

when
$$\psi(L_{\rm X}, z) < \frac{1}{3+\epsilon}$$
 and:

$$f(L_{\rm X}, z; N_{\rm H}) = \begin{cases} \frac{2}{3} - \frac{3+2\epsilon}{3+3\epsilon} \psi(L_{\rm X}, z) & [20 \le \log N_{\rm H} < 21] \\ \frac{1}{3} - \frac{\epsilon}{3+3\epsilon} \psi(L_{\rm X}, z) & [21 \le \log N_{\rm H} < 22] \\ \frac{1}{1+\epsilon} \psi(L_{\rm X}, z) & [22 \le \log N_{\rm H} < 23] \\ \frac{1}{1+\epsilon} \psi(L_{\rm X}, z) & [23 \le \log N_{\rm H} < 24] \\ \frac{f_{\rm CTK}}{2} \psi(L_{\rm X}, z) & [24 \le \log N_{\rm H} < 26] \end{cases}$$
(8)

when $\psi(L_X, z) \ge \frac{1+\epsilon}{3+\epsilon}$. The model assumes $\epsilon = 1.7$, $f_{\text{CTK}} = 1$ and:

$$\psi(L_{\rm X}, z) = \min[\psi_{\rm max}, \max[\psi_{43.75}(z) - 0.24(\log L_{\rm X} - 43.75), \psi_{\rm min}]]$$
(9)

where $\psi_{\min} = 0.2$, $\psi_{\max} = 0.84$, $\psi_{43.75}(z)$ depends on redshift as:

$$\psi_{43.75}(z) = \begin{cases} 0.43(1+z)^{0.48} & [z<2]\\ 0.43(1+2)^{0.48} & [z\geq 2] \end{cases}$$
(10)

The model describes a negative dependence of the absorbed quasar fraction on the intrinsic quasar hard X-ray luminosity as well as redshift at z < 2.

Given this $N_{\rm H}$ distribution model, both the absorbed and the CTK quasar fractions decrease at higher hard X-ray luminosities

and increase at higher redshift with a plateau at $z \ge 2$. The studies of the QLF and extinction properties in the X-ray have many variations in the data used, fitting methods, assumptions of the spectrum form and $N_{\rm H}$ distribution function form, treatments of redshift uncertainties and sources without counterparts. Therefore, it is worth comparing our fiducial extinction model with models determined in other works. In the top and middle panels of Figure 3, we compare the predictions on the absorbed guasar fraction and the CTK quasar fraction from this model with other observational constraints (Ueda et al. 2003; Burlon et al. 2011; Brightman & Ueda 2012; Merloni et al. 2014; Aird et al. 2015a; Buchner et al. 2015; Ricci et al. 2015; Del Moro et al. 2016; Georgakakis et al. 2017; Masini et al. 2018; Lanzuisi et al. 2018). In the comparison, we do not show the hard X-ray luminosity from Ricci et al. (2015) and Masini et al. (2018) since these observations were in harder X-ray bands and the 2 - 10 keV X-ray luminosity was not available. The absorbed fraction F_{abs} in the top panel of Figure 3 is defined as the fraction of absorbed quasars relative to total CTN quasars. The compton thick fraction F_{CTK} in the middle panel of Figure 3 is defined as the fraction of CTK quasars relative to all quasars. We find a good agreement with other observations in the absorbed quasar fraction which monotonically increases towards higher redshift. Our fiducial model (the Ueda et al. (2014) model) is in agreement with the Buchner et al. (2015) and the Aird et al. (2015a) models. Besides, we also find a good consistency in the CTK quasar fraction with most of the observations, except for Aird et al. (2015a) which determined the $N_{\rm H}$ distribution by reconciling the hard X-ray luminosity function of soft X-ray and hard X-ray selected quasars. Compared with the Buchner et al. (2015) model, the Ueda et al. (2014) model is consistent with it except for mild differences at z < 2. We note that some recent studies (Masini et al. 2018; Georgantopoulos & Akylas 2019) using NuSTAR, which is more sensitive in the hard X-ray, found very small lower bounds of F_{CTK} , ~ 10 – 20%. Assuming that the CTK quasars are completely absent in observations, the uncertainty in F_{CTK} can result in $\log \left((1 - F_{\text{CTK}}^{\text{min}}) / (1 - F_{\text{CTK}}^{\text{max}}) \right) \sim 0.2 \text{ dex uncertainty in the binned}$ estimations of the bolometric QLFs. In the bottom panel of Figure 3, we show the $N_{\rm H}$ distribution at log $L_{\rm X}$ = 43.5, z = 0.05 comparing different models (Ueda et al. 2003; Gilli et al. 2007; Treister et al. 2009; Ueda et al. 2014; Aird et al. 2015a).

Given $N_{\rm H}$, we calculate the extinction using the photoelectric absorption cross section in Morrison & McCammon (1983) and the non-relativistic Compton scattering cross section. To determine the dust abundance, a dust-to-gas ratio is required. In Hopkins et al. (2007), a constant dust-to-gas ratio was assumed to convert N_H to dust column density and a SMC-like extinction curve from Pei (1992) was adopted. However, in this work, we find that these assumptions along with our fiducial N_H distribution model result in a systematic inconsistency between UV, B band and X-ray observations. The UV and B band luminosities are under-predicted and the phenomenon is more severe in the UV than in the B band in a luminosity and redshift-dependent manner. This indicates that the extinction in the optical/UV is over-predicted by the model with the constant dust-to-gas ratio and the SMC-like extinction curve. Observations have revealed that the mass-metallicity relation of galaxies has a redshift evolution (e.g., Zahid et al. 2013) with the gas-phase metallicity of typical quasar host galaxies dropping ~ 0.5 dex from z = 0 to z = 2. Similar evolution was also seen in numerical simulations (e.g., Ma et al. 2016). Assuming that the dust-to-metal ratio remains a constant, the decrement in the gas-phase metallicity of quasar host galaxies will lead to a decrement in the dust-to-gas ratio at higher redshift. In addition, some observations have sug-

Name	Redshift	Data	Fitting function	Parameter fixing	
local "free" fit	each individual redshift	data with its redshift bin cover- ing the target redshift	double power-law luminosity function	all free	
local "polished" fit	each individual redshift	data with its redshift bin cover- ing the target redshift	double power-law luminosity function but manually reduced to a single power-law at $z \ge 5.8$	ϕ_* is fixed according to the lin- ear evolutionary trend found in the local "free" fits; other pa- rameters are free all free; uniform priors in the Bayesian inference	
global fit A	all redshifts simulta- neously	all the data compiled	functions of the global evolution model; the faint-end slope has a flexible polynomial evolution- ary pattern		
global fit B	all redshifts simulta- neously	all the data compiled	functions of the global evolution model; the faint-end slope is re- stricted to evolve monotonically with redshift, it has a power-law evolutionary pattern	all free; uniform priors in the Bayesian inference	

Table 2. Overview of the fits we perform in this paper. The results of the local "free" and "polished" fits are presented in Table 3. The results of the global fits A and B are presented in Table 4. Unless otherwise specified, all the predictions and implications presented in this paper are based on the results of the global fits which are highlighted in the table.

gested that the extinction curve of AGN might be shallower than the commonly assumed SMC-like extinction curve (e.g., Maiolino et al. 2001; Gaskell et al. 2004; Gaskell & Benker 2007; Czerny et al. 2004). Given the observational updates, we choose to adopt a redshift-dependent dust-to-gas ratio which scales as the gas-phase metallicity given by the fit in Ma et al. (2016). The value of the dust-to-gas ratio in the local Universe still follows Hopkins et al. (2007) with $(A_{\rm B}/N_{\rm H}) = 8.47 \times 10^{-22} \,{\rm cm}^2$. We adopt the Milky Way-like extinction curve in Pei (1992) which is shallower than the SMC-like curve. Although the extinction curve of quasars does not exhibit the 2175Å bump feature as found in the Milky Way, our results are not affected by this since none of the bands we study in this paper are close to 2175Å.

We note that the extinction in the X-ray would also be affected by the decrement of the gas-phase metallicity. In addition, although the metallicities of quasar host galaxies decrease with redshift, the metallicities of broad line regions do not evolve as strongly. The relative contributions of host galaxies and near quasar obscuration are still largely unknown. Here, our choice in the dust-to-metal ratio empirically prefers the scenario that near quasar obscuration is more important in the X-ray and obscuration in host galaxies contributes more to the extinction in the optical/UV. Our choice is motivated by making the X-ray and optical/UV observations more consistent with each other at all redshifts. Similar argument applies to our choice of the extinction curve. The shallow extinction curves found in some studies are still under debate and our choice here is only for empirical needs.

The extinction model and the bolometric corrections introduced in this and previous sections allow us to link the bolometric QLF with the observed QLF in a certain band, and resolve the discrepancies described above. We note that for all the subsequent analysis in the paper, unless otherwise specified, the QLFs presented include both the obscured and unobscured AGN and the observed QLFs presented take account of dust and gas extinction described in this section.

4 BOLOMETRIC QUASAR LUMINOSITY FUNCTION

4.1 Bolometric quasar luminosity function at a certain redshift

We first study the bolometric QLF at a certain redshift. Following the standard practice, we parameterize the bolometric QLF with a double power-law:

$$\phi_{\text{bol}}(L) = \frac{\mathrm{d}n}{\mathrm{d}\log L} = \frac{\phi_*}{(L/L_*)^{\gamma_1} + (L/L_*)^{\gamma_2}},\tag{11}$$

where ϕ_* is the comoving number density normalization, L_* is the break luminosity, γ_1 and γ_2 are the faint-end and bright-end slopes respectively. We note that the conventions for double power-law are sometimes different. In optical/UV studies, the double power-law is usually defined as:

$$\frac{\mathrm{d}n}{\mathrm{d}L} = \frac{\phi_*'/L_*}{(L/L_*)^{-\alpha} + (L/L_*)^{-\beta}},\tag{12}$$

or per unit absolute magnitude as:

$$\frac{\mathrm{d}n}{\mathrm{d}M} = \frac{\phi_*''}{10^{0.4(\alpha+1)(M-M_*)} + 10^{0.4(\beta+1)(M-M_*)}},\tag{13}$$

where ϕ'_* and ϕ''_* are the comoving number density normalizations with different units, M_* is the break magnitude, α and β are the faint-end and bright-end slopes respectively. In our notation, it gives $\alpha = -(\gamma_1 + 1), \beta = -(\gamma_2 + 1), \phi'_* = \phi_*/\ln 10$ and $\phi''_* = 0.4\phi_*$.

For a given bolometric QLF, we can convolve it with the bolometric corrections and extinction corrections discussed in Section 3 to get the predicted observed QLF in a certain band at the redshift we study. We fit the parameters of the bolometric QLF to match the prediction with the observational binned estimations in all bands at the redshift. We select binned estimations of the QLF from our observation compilation listed in Table A1. A data set is selected if the redshift bin of that observation covers the redshift we study. Since the statistical mean redshift of the quasar samples in the binned estimations in observations does not necessarily perfectly match the redshift we study, we correct the binned estimations with a model-dependent method (referred to as "number density correction" in this paper). To be specific, for each data set in the UV, we first use the UV QLF model constrained by Kulkarni et al. (2018) (the Model 2 of the paper) to calculate the "expected"

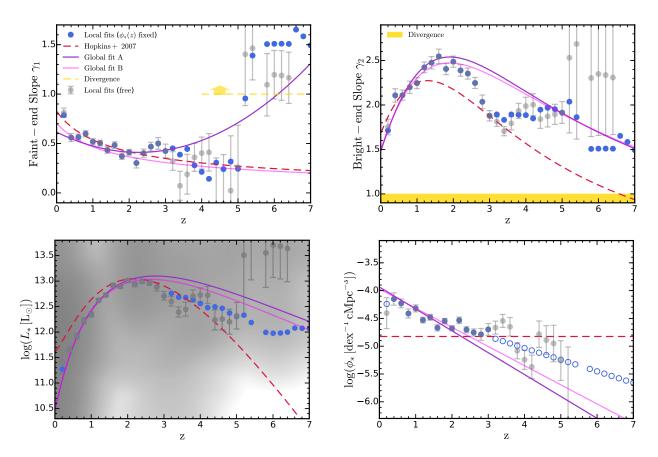


Figure 4. Best-fit double power-law parameters of the bolometric QLF at each redshift. Gray points are the best-fits at individual redshifts (local "free" fits) with error bars indicating 1σ uncertainties. Blue points are the best-fits when the evolution of $\phi_*(z)$ is fixed (local "polished" fits). The blue open circles in the bottom right panel indicate where $\phi_*(z)$ is fixed. For the evolution of the bolometric QLF, the purple (pink) solid lines show the results from the global fit A (B). We compare the evolution of these parameters with that constrained by Hopkins et al. (2007) shown in red dashed lines. In the top left (right) panel, the yellow dashed line (shaded region) indicates where integrated luminosity at the faint (bright) end will diverge. In the bottom left panel, the colormap shows smoothed distribution of the observational data points converted onto the bolometric plane with the bolometric corrections. Darker colors indicate regions with more data points. At $z \gtrsim 5$, the void of data points approaches the break luminosity, indicating that the fits at those redshifts are potentially affected by limited data points at the faint end.

number densities at the redshift we study and at the luminosities where the data points are located. Then, we calculate the mean of the logarithm of the "expected" number densities, representing a mean level of quasar number density. Since the observed quasar samples may center on a slightly different redshift, it is likely that the observed data points exhibit a systematic shift from this "expected" mean level of number density. So we rescale the observed data points to have the "expected" mean value at the redshift we study. We also perform this correction to the X-ray data points with the X-ray QLF model constrained by Miyaji et al. (2015) and to the IR data points with the IR QLF models constrained therein. We note that this correction is model-dependent but the models we choose are representative and have the widest redshift coverage in their bands. They are in good agreement with the observations in their bands. In most of the cases, this correction step improves the clustering of data points from different investigations and reduces the potential bias in redshift estimations of observations. Combining all corrected data points, we can derive the best-fit parameters of the bolometric QLF. The best-fit parameters at some selected redshifts are listed in Table 3. The best-fits at all selected redshifts are shown in Figure 4 with gray points. In the following, we will refer to these

fits as the local "free" fits (see Table 2 for details), since none of the parameters are fixed during fitting.

Since the parameters of the double power-law bolometric QLF have significant degeneracy, which manifests as large covariance in fitting, the best-fit parameters exhibit large coherent fluctuations at some redshifts. The degeneracy prevents us from finding the optimal functional form to describe the redshift evolution of the parameters. To improve the fits, we fix the number density normalization to depend linearly on redshift which is quite clear even in the "free" fits. The linear relation is determined by the best-fits at z = 0.4 - 3.0. We then redo the fitting at redshifts outside z = 0.4 - 3.0 with $\phi_*(z)$ fixed. Apart from that, we find that the bolometric QLF at $z \ge 5.8$ behaves as a single power-law at least in the regime covered by existing observations. Thus we reduce the fitting formula to a single power-law by restricting the faint and bright-end slope to be the same at these redshifts. The fitting procedure with these updates is referred to as the local "polished" fits (see Table 2 for details). The "polished" best-fits are also shown in Figure 4 with blue points. Based on the local "polished" fits, the bright-end slope and break luminosity evolution clearly have a double power-law shape, similar to what was seen in Hopkins et al. (2007), and the faint-end slope has a polynomial-like dependence on redshift.

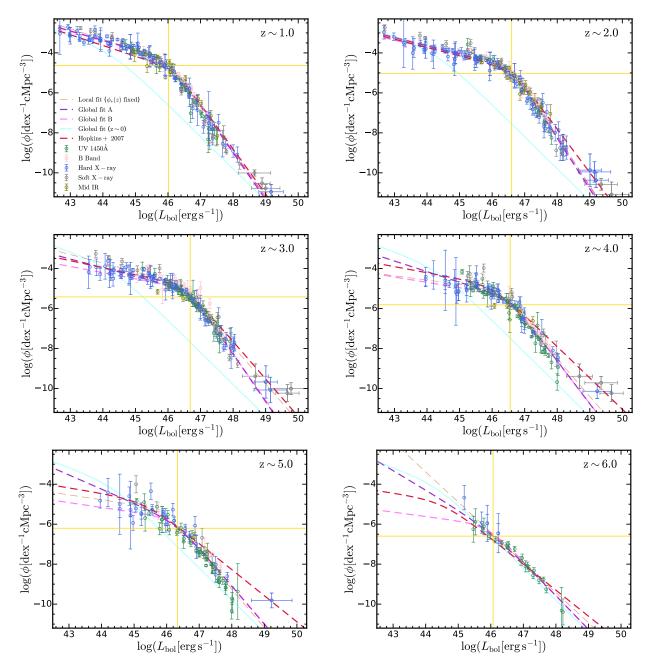


Figure 5. Best-fit bolometric QLFs at 6 selected redshifts. We compare the predictions with the observational binned estimations converted onto the bolometric plane. We present the best-fit bolometric QLFs at individual redshifts (local "free" fits) in orange dashed lines. The bolometric QLFs constrained by our global fit A (B) are shown in purple (pink) dashed lines. The bolometric QLFs from Hopkins et al. (2007) are also presented in red dashed lines for comparison. The z = 0 bolometric QLF constrained by our global fit A is shown in cyan dashed lines. The observational data are converted onto the bolometric plane with the bolometric corrections and the N_{obs}/N_{mod} method. The vertical and horizontal yellow lines show the break luminosity and the number density normalization at each redshift.

4.2 Parameterized evolution model of the bolometric QLF

parameters that evolve with redshift as:

$$\gamma_{1}(z) = a_{0}T_{0}(1+z) + a_{1}T_{1}(1+z) + a_{2}T_{2}(1+z);$$

$$\gamma_{2}(z) = \frac{2b_{0}}{\left(\frac{1+z}{1+z_{\text{ref}}}\right)^{b_{1}} + \left(\frac{1+z}{1+z_{\text{ref}}}\right)^{b_{2}};$$

$$\log L_{*}(z) = \frac{2c_{0}}{\left(\frac{1+z}{1+z_{\text{ref}}}\right)^{c_{1}} + \left(\frac{1+z}{1+z_{\text{ref}}}\right)^{c_{2}};$$

$$\log \phi_{*}(1+z) = d_{0}T_{0}(1+z) + d_{1}T_{1}(1+z),$$

$$(T_{0}(x) = 1, T_{1}(x) = x, T_{2}(x) = 2x^{2} - 1)$$

$$(14)$$

In this section, we aim to describe the evolution of the bolometric QLF with simple formulae and to perform a global fit on all the observational data at all redshifts. Following the discussion in the previous section, we describe the QLF as a double power-law with

Local "free" fits:

z	γ_1	γ_2	$\log \phi_*$	$\log L_*$				
0.2	0.812±0.046	1.753±0.087	-4.405 ± 0.278	11.407 ± 0.223				
0.4	0.561 ± 0.041	2.108 ± 0.075	-4.151 ± 0.111	11.650 ± 0.080				
0.8	0.599 ± 0.031	2.199 ± 0.070	-4.412 ± 0.080	12.223 ± 0.059				
1.2	0.504 ± 0.030	2.423 ± 0.060	-4.530 ± 0.052	12.622 ± 0.036				
1.6	0.484 ± 0.034	2.546 ± 0.082	-4.668 ± 0.058	12.919 ± 0.040				
2.0	0.411 ± 0.029	2.487 ± 0.063	-4.679 ± 0.046	13.011 ± 0.032				
3.0	0.424 ± 0.070	1.878 ± 0.058	-4.698 ± 0.107	12.708 ± 0.086				
4.0	0.403 ± 0.162	1.988 ± 0.099	-5.244 ± 0.174	12.730 ± 0.134				
5.0	0.260 ± 0.425	1.916 ± 0.123	-5.258 ± 0.357	12.319 ± 0.261				
6.0	1.196 ± 0.246	2.349 ± 0.692	-8.019 ± 1.099	13.709 ± 0.639				
Local	Local "polished" fits:							
0.2	0.787 ± 0.024	1.713±0.046	-4.240	11.275 ± 0.023				
0.4	0.561 ± 0.041	2.108 ± 0.075	-4.151 ± 0.111	11.650 ± 0.080				
0.8	0.599 ± 0.031	2.199 ± 0.070	-4.412 ± 0.080	12.223 ± 0.059				
1.2	0.504 ± 0.030	2.423 ± 0.060	-4.530 ± 0.052	12.622 ± 0.036				
1.6	0.484 ± 0.034	2.546 ± 0.082	-4.668 ± 0.058	12.919 ± 0.040				
2.0	0.411 ± 0.029	2.487 ± 0.063	-4.679 ± 0.046	13.011 ± 0.032				
3.0	0.424 ± 0.070	1.878 ± 0.058	-4.698 ± 0.107	12.708 ± 0.086				
4.0	0.213 ± 0.092	$1.885 {\pm} 0.052$	-5.034	12.562 ± 0.027				
5.0	0.245 ± 0.211	1.912 ± 0.086	-5.243	12.308 ± 0.062				
6.0	$1.509 {\pm} 0.058$	$1.509 {\pm} 0.058$	-5.452	11.978 ± 0.055				

Table 3. The best-fit double power-law parameters of the bolometric QLF at selected redshifts. We present the results of the local "free" and the local "polished" fits (see Table 2 for details).

	Parameter	Best-fit A	Best-fit B
γ_1	a_0	$0.8569^{+0.0247}_{-0.0253}$ $-0.2614^{+0.0162}_{-0.0164}$	$\begin{array}{r} 0.3653\substack{+0.0115\\-0.0114}\\-0.6006\substack{+0.0422\\-0.0417}\end{array}$
	a_1	$\substack{-0.2614\substack{+0.0162\\-0.0164}\\0.0200\substack{+0.0011\\-0.0011}$	$-0.6006^{+0.0422}_{-0.0417}$
γ_2	$a_2 \\ b_0$	$2.5375^{+0.0177}_{-0.0187}$	$2.4709^{+0.0163}_{-0.0169}$
	b_1	$2.5375_{-0.0187}^{+0.0177}$ $-1.0425_{-0.0182}^{+0.0164}$ $-1.025_{-0.0182}^{+0.0199}$	$2.4709^{+0.0163}_{-0.0169}$ $-0.9963^{+0.0167}_{-0.0161}$
L_*	$b_2 c_0$	$1.1201^{+0.0199}_{-0.0207}$ $13.0088^{+0.0090}_{-0.0021}$	$\begin{array}{r}1.0716\substack{+0.0180\\-0.0181}\\12.9656\substack{+0.0092\\-0.0089}\\-0.5758\substack{+0.0020\\-0.0019\end{array}$
	c_1	$-0.5759^{+0.0018}_{-0.0020}$	0.400+0.00/2
ϕ_{*}	$c_2 \\ d_0$	$\begin{array}{r} 0.4554\substack{+0.0028\\-0.0027}\\-3.5426\substack{+0.0235\\-0.0209}\end{array}$	$\begin{array}{r} 0.4698\substack{+0.0025\\-0.0026}\\ -3.6276\substack{+0.0209\\-0.0203}\end{array}$
	d_1	$-0.3936^{+0.0070}_{-0.0073}$	$-0.3444^{+0.0063}_{-0.0061}$

Table 4. The best-fit parameters of the global evolution model of the bolometric QLF (see Equation 14 and Equation 16). We present the best-fit parameters of the global fits A and B (see Table 2 for details), respectively.

where T_n is the n-th order Chebyshev polynomial and z_{ref} is chosen to be 2. The evolution of the bolometric QLF is therefore controlled by 11 parameters: $\{a_0, a_1, a_2\}$; $\{b_0, b_1, b_2\}$; $\{c_0, c_1, c_2\}$; $\{d_0, d_1\}$. This parameterization is adequate to describe the evolution of the bolometric QLF parameters. We have tried to extend the parameterization with higher order polynomials and find their contributions are negligible.

In the next step, we perform a global fit (referred to as the global fit A, see Table 2 for details) on all the observational data from the compilation at all redshifts simultaneously. To do this, we adopt a Monte Carlo Markov Chain (MCMC) method using the

emcee ⁵ package (Foreman-Mackey et al. 2013). Given a proposed parameter set of the evolution model, we calculate the resulting observed QLF in bands and compare that with observational data. For a redshift bin of a given data set, the predicted observed QLF is calculated at the center of the redshift bin. The observational data points are also rescaled to the center of the redshift bin with the number density correction discussed in the previous section. The likelihood function is then calculated in a standard way:

$$\ln \mathcal{L} = -\frac{1}{2} \sum_{n} \left[W(z_n) \frac{(\log \phi_{\text{mod}} - \log \phi_{\text{obs}})^2}{\sigma_n^2} + \ln(2\pi\sigma_n^2) \right], \quad (15)$$

where $\log \phi_{mod}$ and $\log \phi_{obs}$ are the predicted and observed number density respectively, σ_n is the uncertainty of the measurement and W(z) is a weighting function introduced to balance the statistical power of high and low redshift data. (Otherwise, the fact that there is more data at low redshifts would skew the fits, sacrificing large discrepancies at high redshifts for marginal improvements at low redshifts.) The summation is taken over all the observational data points at all redshifts. We choose W(z) = 1 when z < 3, W(z) = $\left(\frac{1+z}{1+3}\right)^2$ when $3 \le z < 4$ and $W(z) = \left(\frac{1+z}{1+4}\right)^3 \left(\frac{1+4}{1+3}\right)^2$ when $z \ge 4$. This weighting function makes the weights of data points roughly the same at z = 2 - 6 and helps achieve a converged and decent fit on high redshift data. We adopt uniform priors for all the parameters involved, so that the posterior probability function is the same as the likelihood function given above. The global best-fit parameters of this evolution model are listed in Table 4 and this bestfit model will be referred to as the global fit A. In Figure 5, we show the best-fit bolometric QLFs at 6 selected redshifts compared with the observational data converted onto the bolometric plane with the bolometric corrections and the $N_{\rm obs}/N_{\rm mod}$ method (moving data points across different QLF planes by fixing the ratio between observed and model-predicted number densities). In general, the global fit A does comparably well to the local best-fit at each redshift in matching the observational data. The best-fit bolometric QLFs of the global fit A are qualitatively different from the Hopkins et al. (2007) model. The bright end of the QLF is steeper at $z \gtrsim 2$. The faint end of the QLF is steeper at $z \gtrsim 3$ and becomes progressively steeper at higher redshifts. We achieve a better agreement with observations than the Hopkins et al. (2007) model at $z \gtrsim 3$. The evolution of the double power-law parameters of the bolometric QLF determined by the global fit A is also shown in Figure 4 with purple lines. In the top left (right) panel of Figure 4, we indicate with yellow dashed line (shaded region) the regime where integrated luminosity towards infinite low (high) luminosity will diverge. Compared with Hopkins et al. (2007), extrapolating our new model to z > 7 will not lead to any divergence at the bright end. However, the integrated luminosity at the faint end will diverge at $z \gtrsim 6$ due to the steep faint-end slope constrained in the global fit A. In the bottom left panel of Figure 4, the colormap shows smoothed distribution of the observational data points converted on to the bolometric plane with the bolometric corrections. Darker colors indicate regions with more data points. At $z \gtrsim 5$, the void of data points approaches the break luminosity, indicating that the fits at those redshifts are affected by limited data points at the faint end. For example, in the extreme case that there are no data points fainter than the break luminosity, the fitted faint-end slope will simply be equal to the bright-end slope. The steepening of the faint-end slope at high redshift we find in both the local fits and the global fit A may be seriously affected by

⁵ https://emcee.readthedocs.io/en/stable/

this. So, in parallel to the global fit A introduced above, we perform another independent global fit (referred to as the global fit B, see Table 2 for details) assuming a different evolution model for the faint-end slope. We adopt the function form used in Hopkins et al. (2007):

$$\gamma_1(z) = a_0 \Big(\frac{1+z}{1+z_{\rm ref}}\Big)^{a_1},$$
(16)

where z_{ref} is again chosen to be 2. Different from the function form used in the global fit A, the faint-end slope here is restricted to evolve monotonically as a function of redshift. This will by construction prevent the steepening of the faint-end slope at high redshift. Other double-power-law parameters have the same evolution model as the global fit A. We perform exactly the same fitting procedure for this model and the results are also shown in Figure 4 with pink lines. The best-fit bright-end slopes, break luminosities and number density normalizations of the global fit B are similar to those of the global fit A. However, the faint-end slope in this model remains shallow at $z \gtrsim 5$ on contrary to the global fit A. The best-fit bolometric QLFs of the global fit B are also presented in Figure 5 compared with observational binned estimations. The global fit B is consistent with observations equally well as the global fit A while behaves qualitatively differently at the faint end at $z \gtrsim 5$. Future observations are required to test these two models.

The evolution models of the bolometric QLF we described above are constrained by observational data at 0 < z < 7. Making predictions beyond the redshift frontier certainly requires extrapolations of the model. For the global fit A, the best-fit faint-end slope becomes the same as the bright-end slope at $z \sim 7$ and the double power-law bolometric QLF tends to behave like a single power-law approaching $z \sim 6-7$. Therefore, extrapolating to z > 7, we postulate that the bolometric QLF simply has a single power-law shape. The evolution of the single power-law slope follows the extrapolation of the evolution of the bright-end slope at z < 7. On the other hand, for the global fit B, the faint-end slope remains shallow at z > 7 and we can simply extrapolate the evolution of the parameters to get luminosity functions at z > 7. We note all these extrapolations involve assumptions on the shape of the QLF in the regime where no observational evidence is available. There are serious uncertainties there.

4.3 Tensions in the UV QLF at z = 4 - 6

The measurements of the UV QLF presented in Giallongo et al. (2015), followed by the updates in Giallongo et al. (2019), indicated a high number density of faint AGN at $z \sim 4 - 6$. This has motivated conjectures on whether quasars alone can be responsible for the reionization of hydrogen at z > 6. However, other recent observations (e.g., Akiyama et al. 2018; Matsuoka et al. 2018; McGreer et al. 2018) have presented measurements that are in conflict with the Giallongo et al. (2015) results (as illustrated in Figure 4 in Giallongo et al. (2019)). These tensions serve as a reminder that the potential uncertainties associated with the selection of quasars and host galaxy contamination at high redshift are still substantial.

In the fiducial analysis of this paper, we do not include the Giallongo et al. (2015) data in our fits. In order to check the robustness of our QLF constraints in the UV, we investigate the tensions in the UV QLF at $z \sim 4 - 6$ in Figure 6. We show the UV QLF determinations with various approaches at z = 4.2, 4.8, 5.8 including the Giallongo et al. (2015) measurement, the compiled observational binned estimations in the UV and X-ray and the prediction from the global fits A and B. The redshifts are chosen to be close to the centers

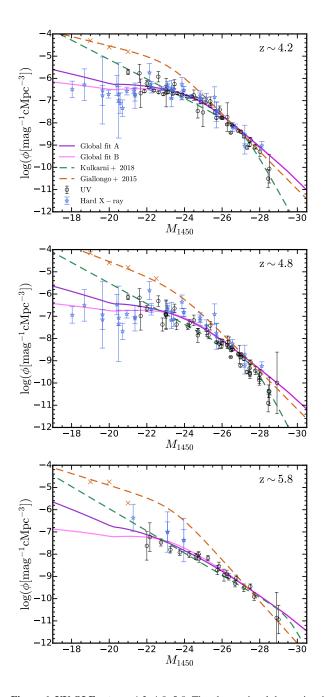


Figure 6. UV QLFs at z = 4.2, 4.8, 5.8. The observational data points in the UV are shown in black circles. The observational data points in the X-ray are moved onto the UV QLF plane with the N_{obs}/N_{mod} method and are shown in blue stars. The predicted UV QLFs from the global fits A and B are shown with purple and pink lines, respectively. The UV QLFs constrained in Kulkarni et al. (2018) is shown with green dashed lines. The UV QLF fitted by Giallongo et al. (2015) and their binned estimations are shown in orange dashed lines with orange crosses. The inferred high number density of quasars at the faint end is disfavored by X-ray observations.

of the redshift bins in Giallongo et al. (2015). The Giallongo et al. (2015) data points (the orange crosses at the faint end) are clearly in tension with other observations in the intermediate luminosity range. The X-ray data points are moved onto the UV QLF plane with the $N_{\rm obs}/N_{\rm mod}$ method. They also disfavor the high number density of faint quasars measured by some UV observations. We

show the UV QLFs constrained by Kulkarni et al. (2018) in green dashed lines. The overall normalization of the Kulkarni et al. (2018) QLFs is consistent with that of the X-ray data, despite a somewhat steeper evolved faint-end slope. Both of the global fits A and B achieve a better agreement with multi-band observational data than the Kulkarni et al. (2018) model, provided that the observational data themselves are internally consistent. At the faint end where observation data is limited, the global fits A and B behave differently. The global fit B predicts shallow faint-end slope at $z \gtrsim 5$ while the global fit A predicts progressively steeper faint-end slope. Given current available observational constraints, we are not able to tell which model is more accurate.

5 EVOLUTION OF THE BOLOMETRIC QLF

In this section, we explore the evolution of the bolometric QLF in detail and investigate the physical interpretation of the evolution based on our global fits discussed in Section 4.

In Figure 7, we compare the bolometric QLFs at different redshifts predicted by the global fits A (solid lines) and B (dashed lines). We divide the evolution of the bolometric QLF into two phases, the early phase at $z \gtrsim 2-3$ and late phase at $z \lesssim 2-3$. In the early phase, the bolometric QLF rises up monotonically following the hierarchical build-up of structures in the Universe. For the global fit A, approaching lower redshift, the relative abundance of faint quasars decreases accompanied by the increased abundance of brighter populations, forming a sharper "break" in the QLF. As a consequence of this change in the relative abundance, the faint-end slope becomes shallower and the bright-end slope becomes steeper. For the global fit B, the relative abundance of faint and bright quasars remains stable towards lower redshift, accompanied by the growth of the break luminosity. In both fits, the evolution at the bright end $(L_{bol} \gtrsim 48)$ is milder than that in the intermediate luminosity range. In the late phase, the bolometric QLF stops rising up. Instead, the bolometric QLF shows a systematic and continuous horizontal shift towards the low luminosity regime. The faint end has almost no evolution in this phase. This indicates processes other than the hierarchical build-up of structures dominating the evolution of the quasar population at late times. AGN feedback is potentially responsible for this evolutionary pattern. AGN feedback is believed to shut down the supply of cold gas to galaxy centers and thus could systematically decrease the bolometric quasar luminosities. Surprisingly, at $z \leq 0.5$, the bright end stops evolving and the bright-end slope becomes slightly shallower again. We note that the global fits A and B give similar evolutionary pattern in the late phase. Across the entire evolution history of the QLF, the evolution at the bright end of the bolometric QLF is apparently milder compared to other luminosity regimes. This suggests potential regulation on the abundance of the most luminous quasars. In Figure 7, we also present the bolometric QLF extrapolated to z = 8, 10. The extrapolations are done as introduced in Section 4.2. The rapidly dropping number density normalization makes the detection of quasars progressively difficult at these redshifts.

In Figure 8, we show the evolution of the cumulative number density of quasars in different luminosity bins in different bands. We show the predictions from the global fits A and B with purple and pink lines, respectively. The cumulative number densities predicted from the two models overlap in the bright luminosity bins. The global fit B predicts lower number density than the global fit A in the faintest UV/X-ray luminosity bin at $z \gtrsim 3$. Apparently, the number density of faint quasars peaks at lower redshift than that

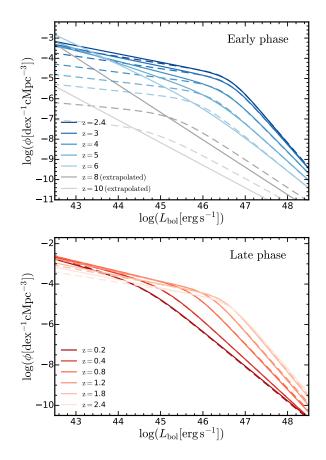


Figure 7. Evolution of the bolometric QLF divided into two phases. The solid (dashed) lines show predictions from the global fit A (B). The lines are color coded to indicate redshifts. The bolometric QLFs at higher redshifts are represented by lighter colors (as labeled). At high redshift ("early phase"), the QLF rises up likely following the hierarchical build-up of structures in the Universe, similar to the halo mass functions. At low redshift ("late phase"), the characteristic luminosity of quasars declines rapidly and the QLF gets systematically shifted to the low luminosity regime, indicating "quenching". The two phases are separated at $z \approx 2 - 3$. We also show the bolometric QLFs extrapolated to z = 8, 10 (see text in Section 4.2).

of bright ones, consistent with the observed "cosmic downsizing" trend (e.g., Cowie et al. 1996; Barger et al. 2005; Hasinger et al. 2005) of AGN at $z \lesssim 2 - 3$. Compared with the Hopkins et al. (2007) model which is shown in red dashed lines, our models agree well at $z \leq 2$ but differences show up at high redshift where new data from the past decade modifies the predictions. Since we predict steeper bright-end slopes than the Hopkins et al. (2007) model at $z \gtrsim 2$, it is not surprising that we predict lower number density at 2 < z < 6 in the most luminous bin of the bolometric luminosity. The lower number density normalization we predict at high redshift gives rise to the lower cumulative number density in the UV, when integrated down to the faint end, compared with the Hopkins et al. (2007) model. In the faintest bin of the UV luminosity, at $z \gtrsim 6$, the prediction of the global fit A in the cumulative number density does not drop as fast as the Hopkins et al. (2007) model and the global fit B primarily because it predicts steeper faint-end slopes at those redshifts. In the UV, we also compare our prediction with the results in Kulkarni et al. (2018) which is an optical/UV-only study. In the bright luminosity bins, we are consistent with their estimations. However, at the faint end, we predict much lower number density

of quasars at $z \gtrsim 2$ primarily driven by the much less steep faintend slope we constrain. We note that the estimations of the number density in Kulkarni et al. (2018) did not reach $M_{\rm UV} \sim -21/-18$, so their predictions on the cumulative number density depends on the extrapolation of their measurements at brighter parts ($M_{\rm UV} \sim -23$) of the QLF. The steeper faint-end slope they constrained results in the higher cumulative number density in their prediction at $z \gtrsim 2$. The steep faint-end slope of UV QLF constrained in Kulkarni et al. (2018) is potentially affected by the paucity of X-ray observations in their study, which provide better constraints at the faint end than present UV observations. Crucially, our models do not have the unphysical upturn at z > 6 in the Kulkarni et al. (2018) model.

In the top left panel of Figure 9, we compare the faint-end slope of our best-fit bolometric QLF with the faint-end slope of the rest-frame UV luminosity function of galaxies observed at z =0-8. The predictions from the global fits A and B are shown in purple and pink lines, respectively. For the galaxy UV luminosity function (GUVLF), constraints on the faint-end slope come from: observations (Duncan et al. 2014; Bowler et al. 2015; Bouwens et al. 2015; Parsa et al. 2016; Finkelstein 2016; Mehta et al. 2017; Atek et al. 2015, 2018; Ishigaki et al. 2018) and theoretical studies (Jaacks et al. 2012; Tacchella et al. 2013; Mason et al. 2015; Wilkins et al. 2017; Tacchella et al. 2018; Yung et al. 2018). The faint-end slopes of the bolometric QLF and the GUVLF are roughly the same at $z \leq 2$. Towards higher redshift, the faint end of the GUVLF starts to become steeper at z = 2 - 3 where the QLF is still flat. For the global fit A, the faint-end slope of the QLF soon catches up that of the GUVLF and become even steeper at $z \gtrsim 5$. For the global fit B, the faint-end slope of the QLF remains shallow at high redshift. Again, these differences are caused by the paucity of observations at the faint end of the QLF.

In the other three panels of Figure 9, we compare the UV QLF with the GUVLF at z = 2, 4, 6. Both the binned estimations and the best-fit luminosity function models are shown. The binned estimations of the GUVLF include: the compilation from Finkelstein (2016) at z = 4 - 10, Alavi et al. (2014); Mehta et al. (2017) at z = 2, Parsa et al. (2016) at z = 2, 4, van der Burg et al. (2010) at z = 4, Bouwens et al. (2017); Atek et al. (2018) at z = 6. We use the best-fit Schechter function in Finkelstein (2016) for the blue curves in the figure. The point where the UV QLF and the GUVLF cross each other becomes progressively higher from z = 6 to z = 2 which indicates enhanced significance of quasars at late times. But at all redshifts, the GUVLF appears to strongly dominate over the faint quasar UVLF at $M_{1450} \gtrsim -23$, wherever data exists. This is true even in models predicting high number density of faint quasars. It is also clear that the global fits A and B only show discrepancies in the regime where no observation is available. For the shaded regions, the two vertical boundaries show the single-visit and final detection limits of the Legacy Survey of Space and Time (LSST, LSST Science Collaboration et al. 2009) which will be conducted with the Simonyi Survey Telescope at the Vera Rubin Observatory. The horizontal boundary shows a reference number density corresponding to one object in the field-of-view of LSST (~ 20000 deg^2) with a survey depth $\Delta z = 1$. As illustrated in the figure, LSST will expand our knowledge by observing faint quasars at high redshift. This will be particularly important in resolving the knee of the QLF at $z \ge 6$, if it exists, and more reliably determine the faint end slope of the QLF at high redshift. Meanwhile, LSST will boost the statistics of both galaxies and quasars at the bright end.

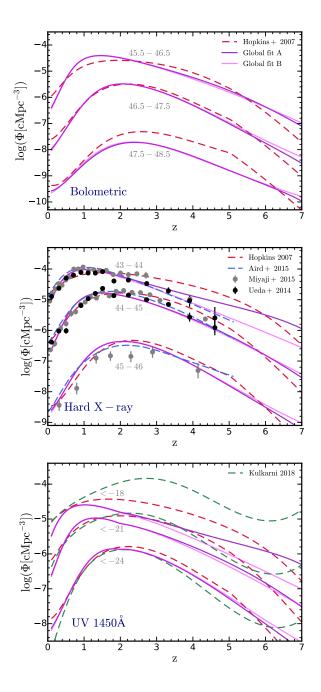


Figure 8. Cumulative number density of quasars in a certain luminosity $(L_{\text{band}} [\text{ erg s}^{-1}])$ or magnitude (M_{1450}) interval as a function of redshift. The predictions from the global fits A and B are shown in purple and pink lines, respectively. The constraints from Hopkins et al. (2007) and Kulkarni et al. (2018) are shown in red and green dashed lines respectively. In the X-ray, we compare our prediction with observations (Ueda et al. 2014; Aird et al. 2015a; Miyaji et al. 2015).

6 IMPLICATIONS AND PREDICTIONS

In this section, we will make predictions based on our global bestfit bolometric QLF models. The predictions involve quasars' cumulative emissivity in the UV and their contribution to hydrogen ionization, the cosmic X-ray radiation background spectrum, the evolution of the cosmic SMBH mass density and the local SMBH mass functions. Comparing the predictions with observations in

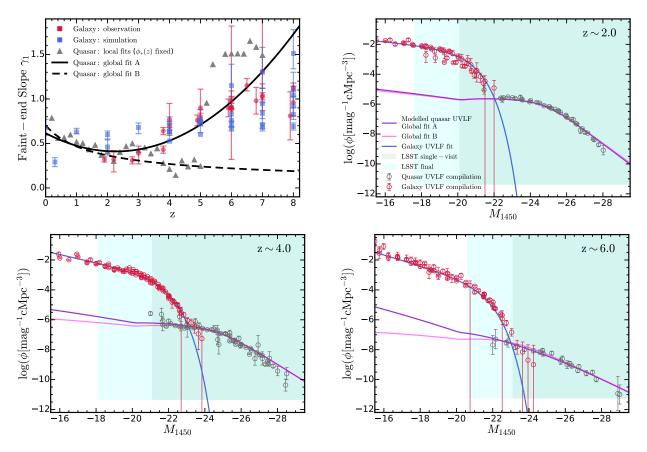


Figure 9. Top left: Comparison between the faint-end slope of the bolometric QLF and the galaxy UV LF (GUVLF). Red (blue) squares represent observational (theoretical) constraints on the GUVLF. Gray triangles represent the best-fit faint-end slopes of the bolometric QLF at individual redshifts. The black solid (dashed) line represents the prediction from the global fit A (B). In the other three panels, we show a detailed comparison between the UV QLF and the GUVLF at z = 2, 4, 6. Binned estimations from observations are shown with points (see text in Section 2 (Section 5) for the sources of the UV QLF (GUVLF) data). The GUVLF always strongly dominates the faint UV population below $M_{1450} \gtrsim -23$. For the shaded regions, the two vertical boundaries show the single-visit and final detection limit of the Legacy Survey of Space and Time (LSST, LSST Science Collaboration et al. 2009). The horizontal boundary shows a reference number density corresponding to one object in the field-of-view of LSST (~ 20000 deg²) with a survey depth $\Delta z = 1$.

these independent channels tests the validity of our bolometric QLF model. We note that, for all the predictions made in this section, the global fits A and B give indistinguishable predictions. The major difference between the global fits A and B is the faint-end slope which does not have strong impact on cumulative luminosities of all quasars, unless the faint-end slope is extremely steep. Therefore, in the following sections, we will only show the result of the global fit A and refer to it as "the global fit" for simplicity.

6.1 Contribution to hydrogen ionization

Faint galaxies have long been considered the dominant source of ionizing photons for the reionization of hydrogen in the Universe (e.g., Kuhlen & Faucher-Giguère 2012; Robertson et al. 2015). However, some observations of high-redshift quasars (e.g., Giallongo et al. 2015, 2019) have inferred much higher number density of quasars at the faint end than other measurements. This suggets the idea that faint quasars could potentially account for the reionization photons (Haardt & Salvaterra 2015). In this section, we quantify the quasar contribution to the photoionization of intergalactic hydrogen using the bolometric QLF derived in this paper.

Following standard modeling of UV background (UVB; e.g., Haardt & Madau 1996, 2012; Faucher-Giguère et al. 2009; FaucherGiguère 2020; Khaire & Srianand 2019), the HI photoionization rate is:

$$\Gamma_{\rm HI}(z) = \int_{\nu_{912}}^{\infty} d\nu \,\sigma_{\rm HI}(\nu) \,c \,n_{\nu}(\nu, z), \tag{17}$$

where $\sigma_{\text{HI}}(v)$ is the HI photoionization cross section and $n_v(v, z)$ is the number density of ionizing photons per unit frequency at redshift *z*. In principle, ionizing photons emitted at all z' > z should contribute to the ionizing background $n_v(v, z)$:

$$n_{\nu}(\nu, z) = \frac{(1+z)^3}{h\nu} \int_{z}^{\infty} dz' \frac{dt}{dz'} \epsilon_{\nu}(\nu_{\rm em}, z') e^{-\tau_{\rm eff}(z, z', \nu)}$$
$$= \frac{(1+z)^3}{h\nu} \int_{z}^{\infty} dz' \frac{1}{H(z')(1+z')} \epsilon_{\nu}(\nu_{\rm em}, z') e^{-\tau_{\rm eff}(z, z', \nu)}.$$
(18)

where $\epsilon_{\nu}(\nu_{em}, z')$ is the comoving emissivity of HI Lyman continuum sources at redshift z' > z at emitting frequency $\nu_{em} = \nu(1+z')/(1+z)$ and $\tau_{eff}(z, z', \nu)$ is the effective optical depth of photons at *z* emitted at *z'*. First, to simplify the calculation, we adopt the "local source" approximation (e.g., Schirber & Bullock 2003; Faucher-Giguère et al. 2008b; Hopkins et al. 2007), which assumes that only ionizing sources with optical depth $\tau_{eff} \leq 1$ contribute to the ionizing background (we will relax this assumption below). Then approximately, Equation 18 is reduced to:

$$n_{\nu}(\nu, z) \simeq \frac{(1+z)^3}{h\nu} \frac{\Delta l(\nu, z)}{c} \epsilon_{\nu}(\nu, z), \qquad (19)$$

where $\Delta l(v, z)$ is the mean free path of ionizing photons defined by $\tau_{\text{eff}}(\Delta l) = 1$. Based on the results in Faucher-Giguère et al. (2008b), the frequency dependence of the mean free path can be described as $\Delta l(v, z) = \Delta l(v_{912}, z) (v/v_{912})^{3(\beta-1)}$, where the β is the power-law index of the intergalactic HI column density distribution. For our local source approximation, we assume that the HI column distribution can be approximated by a single power-law index $\beta \approx 1.5$ (e.g., Madau et al. 1999). Assuming a power-law shape for the extreme UV quasar continuum, we have:

$$\epsilon_{\nu}(\nu, z) = \epsilon_{912}(z) \left(\frac{\nu}{\nu_{912}}\right)^{-\alpha_{\rm UV}}.$$
(20)

Since $\sigma_{\rm HI}(v) \propto v^{-3}$, the $\sigma_{\rm HI}(v) c n_v(v, z)$ term in Equation 17 will be proportional to $v^{-(4+\alpha_{\rm UV}-3(\beta-1))}$. Then integrating Equation 17 gives $\Gamma_{\rm HI}(z) = \frac{\sigma_{\rm HI}(v_{912}) c n_v(v_{912}, z) v_{912}}{3 + \alpha_{\rm UV} - 3(\beta - 1)}$. Plugging in Equation 19, we finally obtain:

$$\frac{\Gamma_{\rm HI}(z)}{10^{-12}} \simeq \frac{0.46}{3 + \alpha_{\rm UV} - 3(\beta - 1)} \left(\frac{1 + z}{4.5}\right)^{3 - \eta} \left(\frac{\Delta l_{z=3.5}^{912}}{50 \,\rm Mpc}\right) \\ \left(\frac{\epsilon_{912}(z)}{10^{24} \,\rm erg s^{-1} \, Hz^{-1} \, cMpc^{-3}}\right).$$
(21)

where we adopt $\alpha_{\rm UV} = 1.7$ (Lusso et al. 2015) and $\Delta l_{z=3.5}^{912} = 50$ Mpc with a power-law index $\eta = 4.44$ for the redshift dependence of Δl (Songaila & Cowie 2010). Here, we only consider the contribution from quasars. The emissivity at Lyman limit $\epsilon_{912}(z)$ can be linked with the UV emissivity $\epsilon_{1450}(z)$ of quasars as:

$$\epsilon_{912}(z) = \epsilon_{1450}(z) \left(\frac{\nu_{912}}{\nu_{1450}}\right)^{-0.61} \tag{22}$$

assuming a power-law shape of the UV continuum with index -0.61 (Lusso et al. 2015), which is in good agreement with our SED model. We note that here we have assumed the escape fraction $f_{\rm esc} = 100\%$ for the ionizing photon produced by quasars. It is common to adopt 100% escape fractions for optically-bright quasars. However, some fraction of quasars have known dust and gas obscuration that would severely limit the escape of ionizing photons. So, the results we derive here should be interpreted as an upper limit of quasars' contribution to ionization. To derive the comoving UV emissivity of quasars, we integrate luminosity over the UV QLF predicted by our global best-fit models:

$$\epsilon_{1450}(z) = \int_{L_{\min}}^{L_{\max}} L_{\nu} \phi(L_{\nu}, z) d\log L_{\nu}$$

=
$$\int_{M_{\min}}^{M_{\max}} L_{\nu}^{0} 10^{-0.4M_{1450}} \phi^{(M)}(M_{1450}, z) dM_{1450}, \quad (23)$$

where L_{ν}^{0} is the zero-point luminosity of the AB magnitude system, M_{\min} and M_{\max} are the magnitude bounds for integration. We adopt $M_{\min} = -18$ and $M_{\max} = -35$.

In the left panel of Figure 10, we present the predicted Lyman limit comoving emissivity ϵ_{912} versus redshift. At low redshifts, our prediction is close to the results of Hopkins et al. (2007) and Kulkarni et al. (2018). At high redshifts, our prediction agrees well with the Haardt & Madau (2012) model and is much lower than the Kulkarni et al. (2018) prediction due to the less steep faint-end

slope we constrain. The prediction is in agreement with observational estimations in narrow redshift bins from Masters et al. (2012); Palanque-Delabrouille et al. (2016); Akiyama et al. (2018). We predict lower emissivity compared to the estimations of McGreer et al. (2018); Parsa et al. (2018). We fit the redshift dependence of the emissivity with a five-parameter functional form (Haardt & Madau 2012):

$$\epsilon_{912} = \epsilon_0 \left(1+z\right)^a \frac{\exp\left(-bz\right)}{\exp\left(cz\right)+d},\tag{24}$$

and we obtain the best-fit as:

$$\epsilon_{912} = (10^{24.108} \text{ erg s}^{-1} \text{Hz}^{-1} \text{ cMpc}^{-3}) (1+z)^{5.865} \\ \times \frac{\exp(0.731z)}{\exp(3.055z) + 15.60}.$$
(25)

In the right panel of Figure 10, we present our prediction for the hydrogen photoionization rate contributed by quasars. We find that the prediction using the local source approximation severely overpredicts the hydrogen photoionization rate at $z \lesssim 2$ where the mean free path of ionizing photons grows comparable to (and eventually larger than) the Hubble radius, so that the local source approximation fails significantly. Therefore, we perform a full UVB calculation using the method described in Faucher-Giguère (2020). The result is also shown in the right panel of Figure 10. The prediction from this full UVB calculation almost overlaps with the prediction with the local source approximation at $z \gtrsim 4$, despite slight differences. The slight differences are due to more physics incorporated in the full UVB calculation that make the UVB spectrum (filtered by IGM absorption and including recombination emission) different from the simple power-law that we have assumed above (see Faucher-Giguère 2020). We compare our predicted hydrogen photoionization rates (from quasars only) with observational inferences of the total rates from Wyithe & Bolton (2011); Calverley et al. (2011); Becker & Bolton (2013); Gaikwad et al. (2017); D'Aloisio et al. (2018). The predicted hydrogen photoionization rate contributed by quasars is an order of magnitude lower than the measured total rate at $z \sim 6$ and only becomes close to the total rate at $z \leq 3$. The results indicate that quasars are subdominant to the hydrogen reionization at $z \gtrsim 6$, but they start to dominate the ionization budget at $z \lesssim 3$. Interestingly, that the hydrogen photoionization rates predicted using our new bolometric QLF are quite similar to the results of Hopkins et al. (2007), which used a different bolometric QLF and adopted a different mean free path model. We have assumed that all ionizing photons produced by the quasar can escape the host galaxy even for faintest quasars. Given this favorable assumption, the predicted contribution of quasars to the hydrogen reionization is still subdominant. Similar conclusion has been reached in Ricci et al. (2017) who adopted a different approach. We have tested that, even including the Giallongo et al. (2015) data in the fit and neglecting all the data points that are incompatible with it, quasars can only have a maximum of $\sim 50\%$ contribution to the ionization budget at $z \sim 5.8$, under the assumption that the escape fraction $f_{esc} = 100\%$ even for quasars much fainter than typical star-forming or Seyfert galaxies.

6.2 Cosmic X-ray background

Since quasars dominate the radiation budget in the X-ray in the Universe, the cosmic X-ray radiation background (CXB) serves as an important channel to cross check our model of the bolometric QLF. The observation of the CXB does not require spatially resolving and

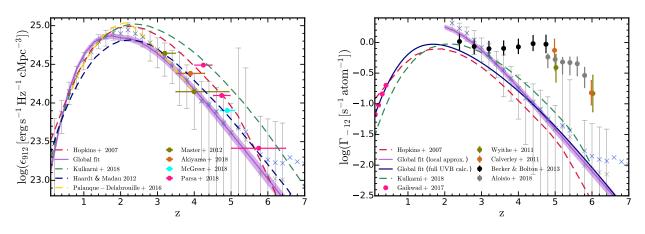


Figure 10. *Left:* **Predicted Lyman limit comoving emissivity of quasars versus redshift.** The prediction from our global best-fit model is shown in the purple line with 1σ confidence interval shown with the shaded region. The predictions from the fits at individual redshifts are shown in the blue (with $\phi_*(z)$ fixed) and gray (leaving $\phi_*(z)$ free) crosses with error bars indicating 1σ uncertainties. The predictions from other models are shown in: Hopkins et al. (2007), the red dashed line; Haardt & Madau (2012), the dark blue dashed line; Kulkarni et al. (2018), the green dashed line. We compare these results with the estimations from observations (labeled). *Right:* **Predicted hydrogen photoionization rate from quasars versus redshift.** The prediction from our global best-fit model, assuming a local source approximation, is shown in the purple line with 1σ confidence interval shown with the shaded region. The prediction from a full UV background calculation (using the code from Faucher-Giguère 2020) is shown with the dark blue line. The predictions from the fits at individual redshifts are shown in the purple line with 1σ confidence interval shown in the green dashed line. We compare these results with the measurements of the total hydrogen photoionization from Kulkarni et al. (2018) is shown in the green dashed line. We compare these results with the measurements of the total hydrogen photoionization rate from observations (labeled). The predicted photoionization rate contributed by quasars is an order of magnitude lower than the measured total rate at $z \sim 6$ and becomes close to the total rate at $z \lesssim 3$. The results indicate that quasars are subdominant to the hydrogen reionization at $z \gtrsim 6$.

identifying quasars and thus can even probe the contribution from faint-end quasars at any redshift.

In general, to get the cosmic radiation background contributed by quasars, we integrate the spectrum of quasars at z = 0 - 7 as:

$$I_{\rm RB}(\nu) = \int_0^7 dz \frac{\epsilon_{\nu}(\nu_{\rm em}, z)}{4\pi d_{\rm L}^2(z)} \frac{dV}{d\Omega dz}(z)$$
$$= \int_0^7 dz \frac{\epsilon_{\nu}(\nu_{\rm em}, z)}{4\pi d_{\rm L}^2(z)} \frac{dV}{d\Omega dz}(z), \tag{26}$$

where $v_{\rm em} = (1 + z)v$ and $\frac{dV}{d\Omega dz}(z)$ is the differential comoving volume element at z. $\epsilon_v(v_{\rm em}, z)$ is derived by integrating over the luminosity function of the emission at $v_{\rm em}$ predicted by our best-fit model.

In practice, we have found that simply adopting the X-ray SED template with the median photon index $\Gamma = 1.9$ leads to an underprediction for the CXB. Considering that the photon index has a significant scatter, ~ 0.2, the stacked SED of quasars should have a very different shape from a simple cut-off power-law. Therefore, in making predictions on the CXB, we adopt the stacked SED of 1000 sampled SEDs with a normal distribution of photon indexes with median value 1.9 and scatter 0.2. In Figure 11, we show the predicted CXB spectrum and compare it with the measurements from Gendreau et al. (1995); Gruber et al. (1999); Churazov et al. (2007); Ajello et al. (2008); Moretti et al. (2009); Cappelluti et al. (2017). For simplicity, we have assumed the galaxies' contribution to the CXB to be a constant $2 \text{ keV}^2 \text{s}^{-1} \text{sr}^{-1} \text{ keV}^{-1}$. We find our predicted CXB spectrum agrees well with observations at high energy end while it is roughly ~ 0.05 dex lower at $E \leq 20$ keV. Imperfectness in the extinction model may be responsible for this though it is hard to argue the source of this level of inconsistency. The Hopkins et al. (2007) model systematically over-predicts the CXB spectrum. We also show separately the contribution to CXB from CTK, absorbed

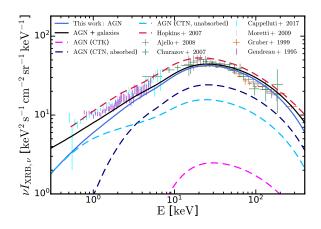


Figure 11. Predicted CXB spectrum. The prediction from our global bestfit model, which only includes the contribution from quasars, is shown with the blue solid line. The prediction that accounts for a simplified constant $2 \text{ keV}^2 \text{s}^{-1} \text{ sr}^{-1} \text{ keV}^{-1}$ contribution from galaxies is shown with the black solid line. The predictions that only include CTK ($\log N_H \ge 24$) or absorbed CTN ($22 \le \log N_H \le 24$) or unabsorbed CTN AGN ($\log N_H \le 22$) are shown in dashed lines. We compare the predictions to the measurements from Gendreau et al. (1995); Gruber et al. (1999); Churazov et al. (2007); Ajello et al. (2008); Moretti et al. (2009); Cappelluti et al. (2017). We also show the prediction from the Hopkins et al. (2007) model with the red dashed line. The prediction from this work is generally in agreement with the observations despite a ~ 0.05 dex lower at $E \lesssim 20$ keV.

CTN and unabsorbed CTN AGN. The absorbed CTN AGN are the major sources of the CXB in the high energy regime while the unabsorbed CTN AGN overtake at $E \leq 3$ keV. The CTK AGN are subdominant to the CXB.

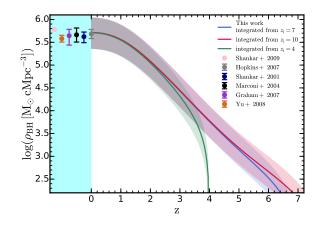


Figure 12. Predicted evolution of the cosmic SMBH mass density at z = 0-7. The red, blue and green lines represent the predictions with starting redshift of integration $z_i = 10, 7, 4$ respectively. We assume the averaged radiative efficiency $\epsilon_r = 0.1$. Shaded regions show the uncertainties when increasing or decreaing ϵ_r by 2 times. The data points show the estimated SMBH mass density in the local Universe from Shankar et al. (2004); Marconi et al. (2004); Graham & Driver (2007); Yu & Lu (2008); Shankar et al. (2009). The local SMBH mass density is mainly dominated by the SMBH growth at z < 4.

6.3 Growth history of SMBHs

The bolometric quasar luminosity is connected with the accretion of the SMBH that powers quasar activities. Thus, based on our bolometric QLF model, constraints can be put on the growth history of SMBHs in the Universe. Here we focus on the evolution of the cosmic SMBH mass density and the SMBH mass function.

6.3.1 Cosmic SMBH mass density

Assuming a constant averaged radiative efficiency $\epsilon_r \simeq 0.1$ for the SMBH accretion, the bolometric quasar luminosity can be related to the accretion rate of the SMBH as:

$$L_{\text{bol}} = \epsilon_{\text{r}} \dot{M} c^2. \tag{27}$$

Therefore, the integrated luminosity density can be translated to the rate of change in the total SMBH mass density as:

$$\frac{\mathrm{d}\rho_{\mathrm{BH}}}{\mathrm{d}z} = \frac{1 - \epsilon_{\mathrm{r}}}{\epsilon_{\mathrm{r}}c^{2}H(z)(1+z)} \int_{L_{\mathrm{min}}}^{L_{\mathrm{max}}} L_{\mathrm{bol}}\,\phi(L_{\mathrm{bol}},z)\,\mathrm{d}\log L_{\mathrm{bol}}.$$
 (28)

where we adopt $\log L_{\min} = 43$, $\log L_{\max} = 48$ here. Starting from an initial redshift for SMBH growth zi and integrating over redshift, we derive the evolution of ρ_{BH} . In Figure 12, we show the redshift evolution of the SMBH mass density with $z_i = 10, 7, 4$ in the red, blue and green lines. Shaded regions show the uncertainties when increasing or decreasing ϵ_r by 2 times. The build-up of the SMBH mass density is completely dominated by the accretion at z < 4. Compared with local constraints (Shankar et al. 2004; Marconi et al. 2004; Graham & Driver 2007; Yu & Lu 2008; Shankar et al. 2009), we predict slightly higher SMBH mass density at z = 0. There are several uncertainties that could impact the comparison made here. These local constraints were calculated by translating galaxy central spheroid properties to the mass of SMBH. New calibrations of the scaling relations between the mass of SMBH and galaxy spheroid properties (e.g., Kormendy & Ho 2013; McConnell & Ma 2013) have generally found higher intercepts and steeper slopes than the

old calibrations. Besides, as discussed in Section 3.1, variations on the definition of the bolometric luminosity could also lead to systematic shift in the estimated radiation energy budget of SMBHs. Both of these two factors could drive the local constraints and our predictions to be more consistent with each other. However, on the other hand, the selection biases in observed scaling relations could result in an over-estimation of the local SMBH mass density (e.g., Shankar et al. 2016). In that case, the discrepancy of our result with local estimations indicates a higher averaged radiative efficiency than the assumed value 0.1.

6.3.2 SMBH mass function

The mass function is one of the most important statistical properties of the SMBH population. In the local Universe, SMBH mass can be determined by various properties of galaxy spheroids, e.g. the velocity dispersion, the bulge mass. Both quiescent and active SMBHs' masses can be estimated in this way. At high redshift, SMBH masses are measured based on direct radiation from the vicinity of active SMBHs. Alternatively, the SMBH mass can be related to the bolometric quasar luminosity with the Eddington ratio. Assuming an Eddington ratio distribution, one can convert the bolometric QLF to the SMBH mass function. Technically, there are two ways to achieve this:

• convolve the bolometric QLF with the measured relation between Eddington ratio and bolometric quasar luminosity. This method is referred to as "convolution".

• assuming an Eddington ratio distribution, fit the parameterized SMBH mass function based on the bolometric QLF. This method is referred to as "deconvolution".

For the first approach, we adopt the scaling relation (Nobuta et al. 2012):

$$\log \lambda_{\rm Edd} = 0.469 \times \log L_{\rm bol} - 22.46, \tag{29}$$

where λ_{Edd} is the Eddington ratio. The relation was measured based on X-ray selected AGN at $z \sim 1.4$ and was demonstrated (Nobuta et al. 2012) to be consistent with what had been found in the SDSS DR5 broad-line AGN (Shen et al. 2009). We also consider the ~ 0.4 dex scatter of this relation (Nobuta et al. 2012). Convolving the bolometric QLF with this relation, we can derive the SMBH mass function for active SMBHs. We further multiply the fraction of unabsorbed CTN AGN $F \sim 0.38$, estimated at the knee of the local X-ray QLF with our fiducial extinction model, to get the SMBH mass function of Type-1 AGN. We present the predicted SMBH mass function of Type-1 AGN in Figure 13 with the blue dashed line which is in good agreement with the observation (Kelly & Shen 2013). In order to further deduce the total SMBH (including quiescent ones) mass function, we need to correct for the fraction of AGN that are in the active phase, f_{duty} . We find that in order to match the observational constrained total SMBH mass function in the local Universe (Vika et al. 2009; Shankar et al. 2009; Marconi et al. 2004), f_{duty} should take the value ~ 0.03. After multiplying $1/f_{duty}$ to the predicted SMBH mass function of active SMBHs, we derive the total SMBH mass function shown with the blue solid line in Figure 13.

For the second approach, we assume a two component Eddington ratio distribution function (ERDF) for AGN (Tucci & Volonteri 2017):

$$P(\log \lambda) = \left[(1 - F)A\lambda^{1 + \alpha} e^{-\lambda/\lambda_1} + \frac{F}{\sqrt{2\pi\sigma^2}} e^{-(\log \lambda - \log \lambda_2)^2/2\sigma^2} \right]$$

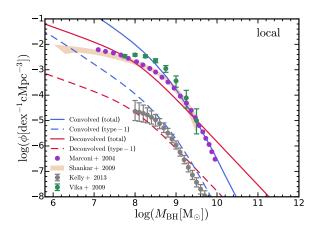


Figure 13. Total SMBH mass function and Type-1 AGN mass function in the local Universe. We show the predictions "convolved" ("deconvolved") from the bolometric QLF in blue (red) lines (see text in Section 6.3.2 for details of the two methods). The total SMBH mass functions are shown in solid lines and the Type-1 AGN mass functions are shown in dashed lines. We compare the predictions for the total SMBH mass function with estimations from Marconi et al. (2004); Shankar et al. (2009); Vika et al. (2009) and compare the predictions on the Type-1 AGN mass function with the estimation from Kelly & Shen (2013).

(30)

The first component takes a Schechter function format and describes the ERDF of Type-2 AGN. The prefactor *A* is set to normalize the total probability of this component to be 1 - F. We choose $\lambda_1 = 1.5$ and $\alpha = -0.6$ which were found in agreement with observations on low redshift Type-2 AGN (Hopkins & Hernquist 2009; Kauffmann & Heckman 2009; Aird et al. 2012). The second component takes a log-normal format and describes the ERDF of Type-1 AGN of which the parameters were determined by fitting the shape of the ERDFs from Kelly & Shen (2013) in different redshift bins and interpolating the results with a linear function (Tucci & Volonteri 2017):

$$\log \lambda_2 = \max[-1.9 + 0.45z, \log 0.03],$$

$$\sigma = \max[1.03 - 0.15z, 0.6)]/\ln 10.$$
(31)

We note that a consensus on the shape of the ERDF has not been reached. However, the potential influence of the ERDF assumptions should be limited (see the Appendix of Weigel et al. (2017)) for our purpose here. We parameterize the total SMBH mass function as a double power-law function. For a proposed total SMBH mass function, multiplying $f_{duty} = 0.03$ where we found through the other method, we can derive the SMBH mass function of the active SMBHs with parameters left for fitting. We can convolve this active SMBH mass function with the assumed ERDF to derive the resulting bolometric QLF. By comparing the result with our bolometric QLF model, we derive the best-fit parameter choice for the SMBH mass function. In Figure 13, we present constraints on the local SMBH mass function from two different methods and compare it with observations of the total SMBH mass function (Marconi et al. 2004; Shankar et al. 2009; Vika et al. 2009) and observations of the Type-1 AGN mass function (Kelly & Shen 2013). The constraints from this work are in decent agreement with all the observations in the range 10^7 to $10^{9.5}$ M $_{\odot}$. The "convolution" method does better at the massive end while the "deconvolution" method does better at the low mass end.

We limit our prediction to the local SMBH mass function, since the uncertainties in the ERDF, the active fraction and the absorbed fraction grow much larger at high redshift. A more comprehensive model of the SMBH population and constraints on the evolution of the SMBH mass function will be explored in future works.

7 SUMMARY AND CONCLUSIONS

In this paper, we update the constraints on the bolometric QLF at z = 0 - 7 and make various predictions based on this model. Our technique follows the method of Hopkins et al. (2007) but with an updated quasar mean SED model and bolometric and extinction corrections. We have also extended the observational compilation in Hopkins et al. (2007) with new binned estimations of the QLF from the recent decade. These new observations allow more robust determination of the bolometric QLF at $z \gtrsim 3$. Our findings on the bolometric QLF can be summarized as:

· We obtain two global best-fit models A and B with different assumptions on the evolution of the faint-end slope at high redshift. As shown in Figure 4 and Figure 5, comparing with the Hopkins et al. (2007) model, we find the bright-end slope steeper at $z \ge 2$ in both the global fits A and B. In the global fit A, the faint-end slope is steeper than the Hopkins et al. (2007) model at $z \gtrsim 3$ and becomes progressively steeper at higher redshift. In the global fit B, where we adopt a monotonically evolved faint-end slope, the faint-end slope remains shallow at high redshift and is close to the prediction of the Hopkins et al. (2007) model. The uncertainties on the faint-end slope arise from the paucity of measurements of the faint-end QLF at high redshift. Apart from that, we have fixed some extrapolation problems of the Hopkins et al. (2007) model. The integrated luminosity of bright-end quasars would not blow up at $z \gtrsim 7$ and the number density normalization exhibits a more natural evolution towards higher redshift.

• We investigate the current tension in the UV QLF at $z \simeq 4 - 6$ shown in Figure 6. We find that the high number density of faint quasars found in Giallongo et al. (2015) is disfavored when compared with current available X-ray observations. Our QLF models achieve a better agreement with the X-ray data at the faint end than the previous QLF models based on optical/UV observations only.

• The evolution of the bolometric luminosity function can be interpreted as two phases separted at $z \simeq 2-3$, illustrated in Figure 7. In the early phase, the bolometric QLF rises up monotonically following the hierarchical build-up of structures in the Universe. In the late phase, the bolometric QLF shows a systematic and continuous horizontal shift towards the low luminosity regime. AGN feedback is potentially responsible for this evolutionary pattern. Surprisingly, in both phases, the evolution at the bright end ($L_{\text{bol}} \gtrsim 48$) of the bolometric QLF is apparently milder compared to other luminosity regimes. This suggests potential regulation on the abundance of the most luminous quasars.

We have made predictions with this new model on the hydrogen photoionization rate contributed by quasars, the CXB spectrum, the evolution of the cosmic SMBH mass density and the local SMBH mass function. We find a general consistency with observations in these channels and our findings can be summarized as:

• We find that quasars are subdominant to the hydrogen photoionization rate during the epoch of reionization at $z \gtrsim 6$. They start to dominate the UV background at $z \lesssim 3$.

• The predicted CXB spectrum shown in Figure 11 agrees well

with observations in the high energy regime while lies slightly lower than observations at $E \lesssim 20$ keV.

• We predict the evolution of the SMBH mass density at z = 0-7 shown in Figure 12. We find that the prediction is consistent with local observations and the evolution is dominated by the growth of SMBHs at z < 4.

• We make predictions on the local total SMBH mass function and the Type-1 AGN mass function shown in Figure 13. We explore two different methods, a "convolution" method and a "deconvolution" method. Both of them can generate consistent results with observations.

The new bolometric QLF model constrained in this paper can simultaneously match the multi-band observations on QLF over a wide redshift range up to $z \sim 7$. The model reveals an evolutionary pattern of the bolometric QLF at high redshift that is qualitatively different from the Hopkins et al. (2007) model. The predictions from the new model is in consistent with observations in various channels. We demonstrate the new bolometric QLF model as a solid basis for future studies of high redshift quasar populations and their cosmological impacts.

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APPENDIX A: COMPILED OBSERVATIONS

In Table A1, we list the observational papers compiled in this work along with the details of their observations, including the survey/fields, the band, the luminosity/redshift coverage and the number of quasar samples adopted.

APPENDIX B: POSTERIOR DISTRIBUTION IN THE GLOBAL FIT

In Figure B1, we show the posterior distribution of the four doublepower-law parameters at z = 5 in our global fit A (see Table 2 for details). The global fit A is originally done in a 11 dimension parameter space of the QLF evolution model. Here, we project the posterior distribution onto the 4 dimension parameter space of the double power-law function at z = 5.

APPENDIX C: CODE AND DATA

The code and data used in this work are publicly available at https://bitbucket.org/ShenXuejian/quasarlf/src/master/. It includes the compiled observational datasets of the QLF, the mean SED model, the pipeline for bolometric and extinction corrections, the global best-fit bolometric QLF models and all other code for the analysis done in this paper.

This paper has been typeset from a TEX/LATEX file prepared by the author.

Reference	Survey/Field	Rest-frame Wavelength/Band	Redshift Range	Luminosity Range ^a [AB mag or erg/s]	N _{AGN}
optical/UV					
Kennefick et al. (1995)	POSS	В	4.0-4.5	$-28.50 < M_{\rm B} < -26.50$	10
Schmidt et al. (1995b)	PTGS	В	~3.5-4.5	$-27.50 < M_{\rm B}^{-} < -25.50$	8
Fan et al. (2001a)	SDSS (equatorial stripe)	1450Å	3.6-5.0	$-27.50 < M_{1450} < -25.50$	39
Fan et al. (2001b, 2003, 2004) ^b	SDSS (Main & Southern Survey)	1450Å	~5.7-6.4	$-28.00 < M_{1450} < -26.50$	9
Wolf et al. (2003)	COMBO-17	1450Å	1.2-4.8	$-28.50 < M_{1450} < -23.50$	192
Cristiani et al. (2004)	GOODS	1450Å	~4-5.2	$-23.50 < M_{1450} < -21.00$	1-4
Croom et al. (2004)	2QZ/6QZ	В	0.4-2.1	$-28.50 < M_{\rm B} < -20.50$	20905
Hunt et al. (2004)	LBG survey	1450Å	~2-4	$-27.00 < M_{1450} < -21.00$	11
Richards et al. (2005)	2dF-SDSS	g	0.3-2.2	$-27.00 < M_{\rm g} < -21.00$	5645
Richards et al. (2006a)	SDSS DR3	i(z=2)	0.3-5.0	$-29.00 < M_{i}^{s} < -22.50$	15343
Siana et al. (2006)	SWIRE	1450Å	~2.8-3.4	$-26.50 < M_{1450} < -23.50$	~100
Bongiorno et al. (2007)	VVDS	B→1450Å	1-4	$-25.69 < M_{1450} < -20.69$	130
Fontanot et al. (2007)	SDSS DR3 & GOODS/ACS	1450Å	3.5-5.2	$-28.00 < M_{1450} < -21.00$	13
Siana et al. (2008)	SWIRE	r→1450Å	2.83-3.44	$-26.11 < M_{1450} < -23.61$	100
Croom et al. (2009)	2SLAQ & SDSS DR3	g(z=2)	0.4-2.6	$-29.75 < M_{g(z=2)} < -20.25$	10637
Jiang et al. $(2009)^{b}$	SDSS Main & Deep	1450Å	5.7-6.6	$-27.63 < M_{1450} < -25.10$	6
Willott et al. (2010)	CFHQS	1450Å	5.75-6.45	$-26.05 < M_{1450} < -22.15$	19
Glikman et al. (2011)	NDWFS & DLS & SDSS DR3	1450Å	3.8-5.2	$-28.45 < M_{1450} < -21.61$	24+314
Ikeda et al. (2012)	COSMOS	1450Å	5.07	$-23.52 < M_{1450} < -22.52$	1
Masters et al. (2012)	COSMOS	1450Å	3.1-5.0	$-24.50 < M_{1450} < -21.00$	128
Shen & Kelly (2012)	SDSS DR7	i(z=2)	~0.3-5	$-29.25 < M_{i(z=2)} < -22.65$	~58000
McGreer et al. (2013)	SDSS DR7 & Stripe 82	1450Å	4.7-5.1	$-27.98 < M_{1450} < -24.18$	103+59
Palanque-Delabrouille et al. (2013)	BOSS & MMT	g(z=2)	0.68-4.0	$-28.80 < M_{\rm g} < -21.60$	1367
Ross et al. (2013)	BOSS DR9	i(z=2)→1450Å	2.2-3.5	$-27.53 < M_{1450} < -23.00$	22301
1055 et al. (2015)	BOSS Stripe82	$i(z=2) \rightarrow 1450\text{\AA}$	2.2-3.5	$-28.42 < M_{1450} < -23.59$	5476
Giallongo et al. (2015) ^d	CANDELS GOODS-S	1450Å	4.0-6.5	$-22.50 < M_{1450} < -19.00$	22
Kashikawa et al. (2015)	UKIDSS-DXS	1450Å	5.85-6.45	$M_{1450} \sim -22.84$	2
Jiang et al. (2016)	SDSS	1450Å	5.7-6.4	$-29.00 < M_{1450} < -24.50$	52
Palanque-Delabrouille et al. (2016)	SDSS-IV/eBOSS	g(z=2)	0.68-4.0	$-28.80 < M_{g(z=2)} < -22.00$	13876
Yang et al. (2016)	SDSS & WISE	1450Å	4.7-5.4	$-29.00 < M_{1450} < -26.80$	99
Akiyama et al. (2018)	HSC-SSP	1450Å	3.6-4.3	$-25.88 < M_{1450} < -21.88$	1666
Matsuoka et al. (2018)	SDSS & CFHQS & SHELLQs	1450Å	5.7-6.5	$-30.00 < M_{1450} < -22.00$	110
McGreer et al. (2018)	CFHTLS	1450Å	4.7-5.4	$-26.35 < M_{1450} < -22.90$	25
Wang et al. (2018a)	DELS & UHS & WISE	1450Å	6.45-7.05	$-27.60 < M_{1450} < -25.50$	17
Yang et al. (2018)	Deep CFHT Y-band & SDSS & VVDS	1450Å	0.5-4.5	$-27.00 < M_{1450} < -20.50$ $-27.00 < M_{1450} < -20.50$	109
Soft X-ray					
Miyaji et al. (2000, 2001)	ROSAT	0.5-2 keV	0.015-4.8	$10^{41} < L_{0.5-2} < 10^{47}$	691
Hasinger et al. (2005)	ROSAT & CDF-N/S	0.5-2 keV	0.015-4.8	$10^{42} < L_{0.5-2} < 10^{48}$	2566
Silverman et al. (2005)	CHAMP & ROSAT	0.5-2 keV	0.1-5	$10^{44.5} < L_{0.5-2} < 10^{46}$	217
Ebrero et al. (2009)	XMS & RBS & RIXOS8 & RIXOS3 & UDS & CDF-S	0.5-2 keV	0.01-3	$10^{40.50} < L_{0.5-2} < 10^{46.81}$	1009
Hard X-ray					
Ueda et al. (2003)	HEAO-1 & AMSS-n/s & ALSS & ASCA & CDF-N	2-10 keV	0.015-3.0	$10^{41.5} < L_{2-10} < 10^{46.5}$	247
Sazonov & Revnivtsev (2004)	RXTE	3-20 keV	0.0-0.1	$10^{41} < L_{3-20} < 10^{46}$	77
Barger et al. (2005)	CDF-N/S+CLASXS+ASCA	2-8 keV	~0.1-1.2	$10^{42} < L_{2-8} < 10^{46}$	601
La Franca et al. (2005)	HELLAS2XMM	2-10 keV	0.0-4.0	$10^{42} < L_{2-10} < 10^{46.5}$	508
Nandra et al. (2005) ^b	GWS & HDF-N	2-10 keV	2.7-3.2	$10^{43} < L_{2-10} < 10^{44.5}$	15
Silverman et al. (2005)	CHaMP	0.3-8 keV	0.2-4.0	$10^{42} < L_{0.3-8} < 10^{45.5}$	368
Aird et al. (2008)	GWS & HDF-N & Lynx & LALA CETUS & EGS1	2-10 keV	2.5-3.5	$10^{42.5} < L_{2-10} < 10^{48.0}$	~1000

^a The minimum and maximum luminosity that binned luminosity function data ever reach. One should not expect that this luminosity range holds for all redshift bins.

^b Old observations that are not included in constraining the QLF. There are more recent works using exactly the same or more extended quasar samples.

^c Data sets presented in a way that an apple-to-apple comparison cannot be made. But we still list them here for references.

^d Giallongo et al. (2015) data is not included in our fiducial analysis.

Table A1. Observations compiled.

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Ebrero et al. (2009)	XMS & AMSS & CDF-S	2-10 keV	0.01-3	$10^{41.83} < L_{2-10} < 10^{45.87}$	435
Aird et al. (2010)	CDF-S & CDF-N & AEGIS &	2-10 keV	0-3.5	$10^{41.3} < L_{2-10} < 10^{45.8}$	130
	ALSS & AMSS				
Fiore et al. (2012)	CDF-S	2-10 keV	3-7.5	$10^{42.75} < L_{2-10} < 10^{44.5}$	54
Ueda et al. (2014)	BAT9 & MAXI7 & AMSS & ALSS & SXDS & LH/XMM & H2X & XBS & CLASXS &	2-10 keV	0.002-5	$10^{41.8} < L_{2-10} < 10^{46.5}$	4039
Aird et al. (2015a)	CLANS & CDF-N & CDF-S & ROSAT surveys CDF-S & CDF-N & EGS & COS-	2-10 keV	0-7	$10^{38.25} < L_{2-10} < 10^{47.5}$	2957+435
	MOS & Boötes field & AMSS & ALSS & ROSAT surveys				
Aird et al. (2015b)	NuSTAR	10-40 keV	0.1-3	$10^{42.75} < L_{10-40} < 10^{45.75}$	94
Miyaji et al. (2015)	Swift BAT & CDF-S	2-10 keV	0.015-5.8	$10^{42} < L_{2-10} < 10^{46}$	~3200
Khorunzhev et al. (2018)	XMM-NEWTON Serendipitous	2-10 keV	3.0-5.1	$10^{45} < L_{2-10} < 7.5 \times 10^{45}$	101
Near-IR & Mid-IR					
Brown et al. (2006)	NDWFS Boötes field	8µm	~1-5	$10^{45} < \nu L_{8\mu m} < 10^{47}$	183
Matute et al. (2006)	RMS & ELIAS & HDF-N/S	15µm	~0.1-1.2	$10^{42} < \nu L_{15\mu m} < 10^{47}$	148
Assef et al. (2011)	NDWFS Boötes field	J	0-5.85	$-28.5 < M_{\rm J} < -18.5$	1838
Lacy et al. (2015)	SWIRE & XFLS	5μ m	0.05-3.8	$10^{43.5} < \nu L_{5\mu m} < 10^{46.5}$	479
Singal et al. (2016) ^c	SDSS DR7 & WISE	$22\mu m$	0.08-4.97		>20000
Emission Lines					
Hao et al. (2005)	SDSS (main galaxy sample)	Hα	0-0.33	$10^5 \mathrm{L}_\odot < L_{\mathrm{H}\alpha} < 10^9 \mathrm{L}_\odot$	~3000
		[O _{II}]		$10^{5} L_{\odot} < L_{[O_{II}]} < 10^{8} L_{\odot}$	
		[O III]		$10^{5} L_{\odot} < L_{[O III]} < 10^{9} L_{\odot}$	

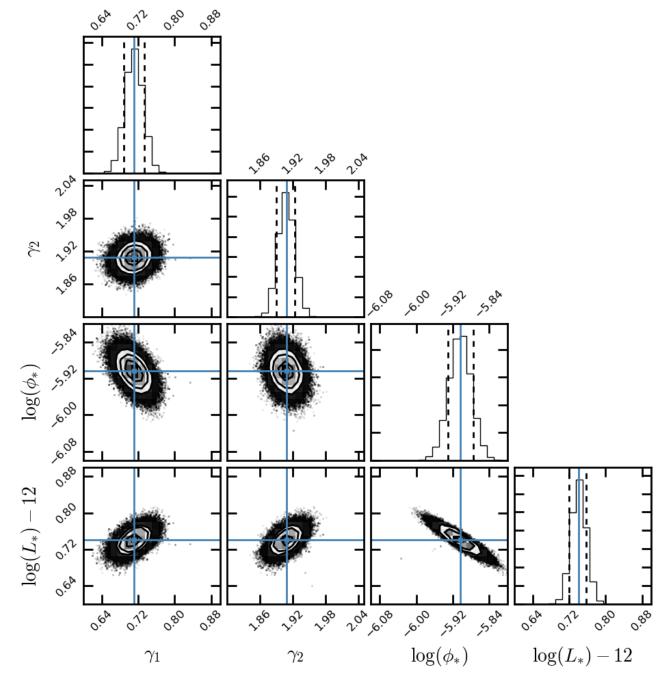


Figure B1. Posterior distribution of the four double-power-law parameters at z = 5 in our global fit A (see Table 2 for details). The global fit A is originally done in a 11 dimension parameter space of the QLF evolution model. Here, we project the posterior distribution onto the 4 dimension parameter space of the double power-law function at z = 5. The blue lines and squares indicate the best-fit values of the global fit A at this redshift. The black dashed lines indicate 1σ dispersions. Similar behaviour of the posterior distribution is seen at other redshifts.