

Private Facial Prediagnosis as an Edge Service for Parkinson's DBS Treatment Valuation

Richard Jiang, Paul Chazot, Nicola Pavese, Danny Crookes, Ahmed Bouridane and M Emre Celebi

Abstract—Facial phenotyping for medical prediagnosis has recently been successfully exploited as a novel way for the preclinical assessment of a range of rare genetic diseases, where facial biometrics is revealed to have rich links to underlying genetic or medical causes. In this paper, we aim to extend this facial prediagnosis technology for a more general disease, Parkinson's Diseases (PD), and proposed an Artificial-Intelligence-of-Things (AIoT) edge-oriented privacy-preserving facial prediagnosis framework to analyze the treatment of Deep Brain Stimulation (DBS) on PD patients. In the proposed framework, a novel edge-based privacy-preserving framework is proposed to implement private deep facial diagnosis as a service over an AIoT-oriented *information theoretically secure* multi-party communication scheme, while data privacy has been a primary concern toward a wider exploitation of Electronic Health and Medical Records (EHR/EMR) over cloud-based medical services. In our experiments with a collected facial dataset from PD patients, for the first time, we proved that facial patterns could be used to evaluate the facial difference of PD patients undergoing DBS treatment. We further implemented a privacy-preserving information theoretical secure deep facial prediagnosis framework that can achieve the same accuracy as the non-encrypted one, showing the potential of our facial prediagnosis as a trustworthy edge service for grading the severity of PD in patients.

Index Terms— Facial Prediagnosis, Medical Biometrics, Edge AIoT, Electronic Health and Medical Records, Private Deep learning, Private Biometrics.

I. Introduction

FACIAL diagnosis dates back to 2000 years ago in Traditional Chinese Medicine (TCM) practice [1-2]. Recently, scientists have shown that facial phenotyping [3-8] can be used

to diagnose accurately over 200 rare genetic diseases, reviving this ancient technology as a new method potentially for diagnosing a wide range of diseases. In addition to applying to rare diseases, facial prediagnosis may have a potential to be applied to many common illnesses. In this paper, we will look into the quantifiable modelling on facial prediagnosis of Parkinson's disease (PD) [9-14], while it has been widely reported that PD has an apparent impact on the faces of PD patients, like many other neurodegenerative diseases [11, 12].

PD can affect natural facial expressions in addition to gross motor skills. This phenomenon, called “facial-masking” (hypomimia) [12], is a common sign of early PD, arising prior to major motor and non-motor symptoms. This is due to a reduction of automatic and controlled expressive movement of facial musculature, creating an appearance of apathy, social disengagement or compromised cognitive status. Such facial symptoms can have significant negative effects on mental health, as it distorts the perceived emotional responses of the individual [11], which can lead to misinterpretation by friends, family and the public. Hence, via facial diagnosis, we can expect that a robust computational model can capture subtle variations of facial features, establish quantifiable evidence and measure/predict the developmental stages of Parkinson's Diseases.

Unlike other senescent diseases, PD is featured by two distinct issues [10]. First, there is no cure for Parkinson's diseases.

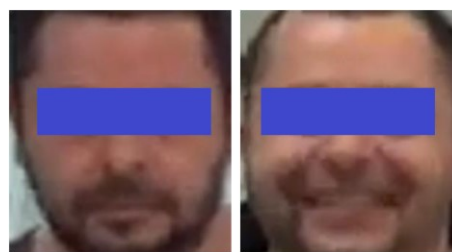


Figure 1. Facial images of a PD patient before and after Deep Brain Stimulation treatment.

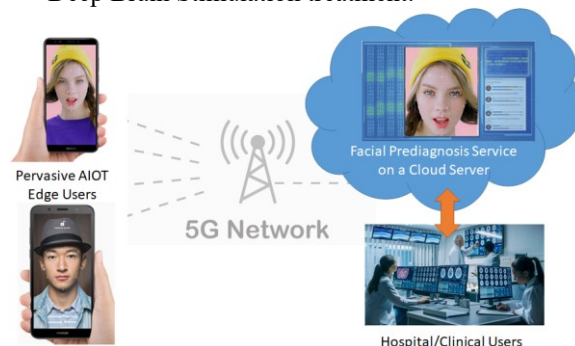


Figure 2. Facial Prediagnosis over 5G AIoT edge service

The manuscript was submitted on xx/05/2021. This work was supported in part by the UK EPSRC under Grant EP/P009727/1, the Leverhulme Trust under Grant RF-2019-492, and the US National Science Foundation under Grant 1946391. (Correspondent e-mail: r.jiang2@lancaster.ac.uk).

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However, early detection can help the adoption of an early intervention to slow down the PD progress. Second, there is no test for Parkinson's diagnosis, making it hard to identify PD at its early stages. Though we can find evidences from EEG or MRI scanning at a developed stage, it is often too late. Instead, Parkinson's diagnosis [10] is often based on the examination by a well-trained expert on tremor at rest, rigidity, slowness and loss of spontaneous movement, a characteristic way of walking, a frozen smile on face, etc.. While such visually observable symptoms can be captured by AI-powered video-based facial analysis, in this work, to save the precious time of doctors, nurses and care staff from examining mass communities, we aim to develop AI-based facial diagnosis for PD.

Parkinson's Diseases [9-14] is a heterogeneous disease (no case being exactly the same), with motor symptoms including tremor, rigidity, bradykinesia, dyskinesia (drug-induced), and non-motor symptoms, including dementia, anxiety, depression, sleep dysfunction, psychosis, persistent pain, delirium, gambling compulsion etc. At the early developmental stage, these symptoms are subtle and occasional. Via automated facial diagnosis, individuals in a range of settings can be monitored and diagnosed quickly and scored on the risk of potential phenotypes of PDs for doctors/caregivers to consider social interventions and palliative therapies. Facial diagnosis [1-8] can provide a cost-effective staff-free automated diagnosis platform via 24/7 real-time online surveillance of patients in care with no waiting time. Potentially, it will enable early diagnosis for preventive treatments over a large population in care and help provide accurate phenotyping for timely precision medicine or treatment. To enable facial prediagnosis for PD analysis, there are two challenges that need to overcome:

- 1) First, we need proof-of-concept experiments to show that facial images can be practically used to classify PD patients with suitable accuracy.
- 2) Secondly, due to privacy issues, the facial biometrics of patients need to be restricted to private use instead of circulating over Internet servers, and a privacy-preserved framework is needed for automated facial diagnosis services over cloud-based networks.

In this paper, taking the PD treatment via Deep Brain Stimulation (DBS) as our case study, we aim to develop a private IoT-based facial prediagnosis framework to evaluate the facial difference of DBS treatment on patients by comparing facial biometrics before and after DBS.

Fig.1 shows the sample facial images of a patient before and after DBS treatment, respectively. Facial images are deformable, and key features are subtle to discriminate. Cross-subject classification becomes more challenging particularly, when the training dataset consists of totally different subjects from the test dataset. Although there are reports that links facial features to PDs [11, 12], up to now it has not been certain if we can use facial images to grade the severity of PD patients via machine learning. In this paper, we will prove this concept using a deep learning based framework.

The scenario of cloud-based automated facial prediagnosis can be depicted in Fig.2. The face photo of a patient can be collected at an Artificial-Intelligence-of-Thing (AIoT) edge device such as a mobile phone, and the face photo is then sent to the server of the service provider. Due to privacy concerns and legislation, patients (or hospitals) may not allow their electronic

health or medical records (EHR or EMR) to upload to a server in an external business. Hence, a privacy-aware framework is then required for the purpose of commercialized facial diagnosis services to offer a widely accessible platform for point-of-care (POC) AIoT end users.

To address the privacy issue in medical prediagnosis, it has been reported to utilize Partial Homomorphic Encryption(PHE) to implement privacy-preserving algorithms such as Support Vector Machine[19] or Naïve Bayesian Classification[15]. However, the implementation of deep neural networks (DNNs) via PHE is yet not applied to medical prediagnosis, while DNNs have nonlinear activation functions that cannot be directly mapped to the encryption domain.

In our proposed solution, we will aim to exploit the multi-party communication architecture and propose an information theoretical secure framework for privacy-preserving deep learning based facial prediagnosis. Our novel contributions in this work include three key aspects, as detailed below:

- 1) *A novel PD prediagnosis method*: Our work presents a novel preclinical assessment method on PD via facial prediagnosis that achieved good accuracy in our experiments, implying a great value of facial prediagnosis for further exploitation on medical purposes.
- 2) *Novel information-theoretical secure implementation*: We implemented a novel AIoT-based framework for privacy-preserving deep learning based facial diagnosis, which is information theoretical secure and achieved the equivalent accuracy in comparison with the original non-privacy-preserving facial diagnosis algorithm.
- 3) *Clinical trial*: we present our experiments with 52 PD patients before and after Deep Brain Stimulation (DBS), which offers a valuable medical trial from our report.

We implemented our initial demo with a PHE library and validated our implementation as the proof-of-concept on a video datasets of 52 PD patients who received the DBS treatments. Our experiments show an accuracy over 95% on discriminating facial features before and after treatment. In comparison, it was reported EEG-based prediagnosis [45] has an accuracy of 85%.

The remainder of the paper is organized as follows. Section 2 reviews the existing relevant work. Section 3 gives background on PHE and describes its implementation. Section 4 presents the proposed AIoT-based privacy-preserving deep learning framework. Section 5 shows the experimental results. Finally, Section 6 concludes the paper.

II. PRELIMINARY ON PRIVATE MACHINE LEARNING

To protect the privacy of shared data over the Internet, it has been widely researched to use various encryption methods [15-30] to secure the data under various hostile or curious conditions. While privacy can be mostly assured by a sophisticated encryption scheme, the data services that need to carry out various computations on the data cannot work due to the encryption. To solve this issue, homomorphic encryption schemes have become a popular way to protect the private data while enabling computation, such as machine learning, to operate on encrypted data.

Partial Homomorphic Encryption, as its name suggests, can maintain only some homomorphic features in its encryption, while full homomorphic encryption is expected to be able to

carry out all equivalence arithmetic operations in its encrypted domain. Typical PHE algorithms include Paillier, ElGamal, and RSA [21]. Well known FHE libraries include SEAL, HELib and TFHE [20]. Table I gives a comparison of several existing open encryption algorithms. We can see that division and comparison are not yet available in PHE or FHE algorithms. Unlike FHE algorithms, PHE algorithms cannot support bitwise operation, exponentiation, negation, and add/subtract with plain texts.

Although PHE does not provide all operations to implement deep learning in the encrypted domain, in this paper, we will demonstrate a new scheme to fulfill the privacy-preserving deep learning without resorting to expensive FHE ones. By taking the Paillier cryptosystem as our encryption method, we will show a full implementation of privacy-preserving deep neural networks using PHE based on an AIoT framework. The reasons for choosing PHE instead of Full Homomorphic Encryption (FHE) include: 1) PHE has been applied for medical applications for years [15–19] and is relatively mature with much lower costs; 2) It is less compute-intensive than full homomorphic encryption (FHE) [19–21] and thus easier to deploy on AIoT devices; 3) PHE based machine learning has recently been successfully utilized on facial images [22–25]. Hence, a PHE based privacy-preserving deep learning framework is a rational choice for our facial prediagnosis application.

There have been a number of reported applications of privacy-preserving machine learning [15]–[30]. The majority of these are developed for distributed setting where different parties hold parts of the training database and securely train a common classifier without each party needing to disclose its own training data to other parties. Recently, Paillier encryption has been applied successfully for facial classification using classic linear machine learning methods [22–25] such as SVM, LDA, etc. In our work, we aim to utilize deep learning for our facial diagnosis service, because deep learning has achieved greater robustness and better accuracy in pattern classification [3, 6–8].

There have been reports of various FHE based deep learning implementations [20, 31–35]. However, it is yet challenging to implement the nonlinear functions in neurons since FHE is fundamentally based on linearization lattice. As shown in Table I, current FHE methods cannot yet cope with divide and compare [20]. Its implementation of exponentiation is based on the repeating squaring algorithm, which causes extra computational complexity and accuracy concerns, and can be applied only to positive number exponentiation [20]. Due to the complexity, most reported implementations assumes the linear approximation of nonlinear functions, with no guarantee of the control of extra errors [29–33]. On the other side, PHE is relatively less compute-intensive [22–24]. Hence, in our application to PD, we choose PHE to implement a lightweight framework for privacy-preserving deep learning.

While the current trend is to provide AI-enabled medical diagnosis as a service [15, 16, 18, 19, 21], the needs to preserve the privacy of the data comes with data sharing over distributed systems, cloud-based services, 5G/6G communication, Internet-of-Things, etc.. There are many reported frameworks to try to meet the various needs. In [29], the encrypted data from clients are decrypted on the server side before feeding into the deep neural networks and the final results are encrypted before sending back to clients. However, this implies the server can know the client’s private data with no privacy protection,

Table I Comparison of FHE and PHE algorithms.

Ops.	FHE			PHE		
	SEAL	HELlib	TFHE	Paillier	ElGamal	RSA
Add/Sub	√	√	√	√	×	×
Multiply	√	√	√	×	√	√
Division	×	×	×	×	×	×
Compare	×	×	×	×	×	×
Matrx Ops	√	√	×	×	×	×
Exp	√	√	×	×	×	×
Square	√	√	√	×	√	√
Negation	√	√	×	×	×	×

though it may be secure to third parties in the communication nodes. In [33], the encryption is performed partially on the layers of deep neural networks. However, asymmetric encryption, although data is hidden from each other, lacks robustness due to the exposure of public keys, leaving it vulnerable if sufficient attempts are made, particularly when the emerging quantum computing becomes available [36–38]. Hence, these proposed schemes over multi-party communication will not be secure in the information theoretical sense.

In this work, we are concerned with facial diagnosis over AIoT services. When patients or hospitals send their data over to the commercial service provider, they may not want to risk compromising the privacy of their patients. On the other side, the service provider wants to keep their learned model safe, and does not want to be exposed to an end user. Hence an information theoretically secure scheme is required for such automated medical data services.

Encrypted facial recognition has been implemented with many algorithms [22–25]. Privacy-preserving data classification algorithms suitable for a client-server model were studied in [39–41]. The client-server model substantially reduces the computational and communication overhead at the client since it needs to interact with only one server compared to a more distributed setting. Outsourcing the clinical decision support system to a third-party server without violating the client’s privacy was studied in [15–19, 21–24, 28–35].

In this paper, in contrast to these previous works, we propose a lightweight privacy-preserving medical diagnosis protocol based on encrypted deep learning over an information theoretically secured AIoT framework. We will demonstrate that our proposed facial diagnosis framework achieves the desired privacy requirements without degrading the classification performance, and the computational and communication complexity are under control.

III. PRIVACY-PRESERVING DNN IMPLEMENTATION

Considering the scenario that AIoT users send their encrypted facial images to the automated medical diagnosis server hosted by a commercial service provider, we need to find a robust privacy-preserving scheme to guarantee data privacy in the system. To achieve this, as detailed in the above sections, we choose the Paillier cryptosystem as our encryption engine, which is partially homomorphic.

A. The Paillier Cryptosystem

Typical PHE algorithms [21–24] include Unpadded RSA, ElGamal encryption, Goldwasser–Micali cryptosystem, Benaloh

cryptosystem, Paillier cryptosystem, etc.. The Paillier cryptosystem [24] is an additive homomorphic encryption method. The Paillier cryptosystem, invented by and named after Pascal Paillier in 1999, is a probabilistic asymmetric algorithm for public key cryptography. The problem of computing n^{th} residue classes is known to be computationally difficult. The decisional composite residuosity assumption is the intractability hypothesis upon which this cryptosystem is based.

Like most other RSA-like algorithms, the Paillier encryption needs a pair of keys, namely public and private keys. The keys are generated via the process below:

- (1) Public keys: Choose two large prime numbers p and q randomly and independently of each other such that: $\gcd(pq, (p-1)(q-1)) = 1$. Compute $n=pq$ and $\lambda=\text{lcm}(p-1, q-1)$.
- (2) Select a random integer $g \in \mathbb{Z}_{n^2}^*$, and calculate the modular multiplicative inverse:

$$\mu = \text{mod}\left(\frac{n}{\text{mod}(g^\lambda, n^2) - 1}, n\right) \quad (1)$$

Here the division gives the integral quotient.

With the above two steps, the generated public keys are $\{n, g\}$ and the private keys are $\{\lambda, \mu\}$.

After keys are produced, the encryption step will be decided by public keys only. Assuming t is the message to encrypted and satisfies $0 \leq t < n$, and r is a random number and satisfies $0 \leq r < n$ and $r \in \mathbb{Z}_n^*$, the cipher text can be obtained as:

$$c = \llbracket t \rrbracket r = \text{mod}(g^{t+r}, n^2), \text{ and } c \in \mathbb{Z}_{n^2}^* \quad (2)$$

Here, $\llbracket * \rrbracket$ denotes the encryption. The random number r will make the Paillier encryption as non-deterministic. Every time with the same keys, the same text t will have different cipher text c .

Inversely, the decipher step will be based on the private keys, and

$$t = \langle c \rangle = \text{mod}\left(\frac{\text{mod}(c^\lambda, n^2) - 1}{n}, \mu, n\right) \quad (3)$$

Here, $\langle * \rangle$ denotes decryption in this paper. As it can be seen pointed out by Paillier in 1999 [21], decryption here is "essentially one exponentiation modulo n^2 ".

B. Homomorphic Properties

A notable feature of the Paillier cryptosystem is its homomorphic properties along with its non-deterministic encryption. The Paillier encryption function is additively homomorphic, and the product of two ciphertexts will decrypt to the sum of their corresponding plaintexts,

$$\llbracket t_1 + t_2 \rrbracket = \text{mod}(\llbracket t_1 \rrbracket \cdot \llbracket t_2 \rrbracket, n^2) \quad (4)$$

With the above equation, we can easily obtain the sum of two encrypted numbers without deciphering them.

Besides the additive homomorphic property, the encrypted numbers in the Paillier cryptosystem can implement the negation homomorphic property as,

$$\llbracket t_1 \times t_2 \rrbracket = \text{mod}(\llbracket t_1 \rrbracket^{t_2}, n^2) \quad (5)$$

Here, it is noted that t_2 must be in its original value. Given the Paillier encryptions of two messages there is no known way to compute an encryption of the product of these messages without knowing the private key.

Based on the above partial multiplicative homomorphic

property, the encrypted numbers in the Paillier cryptosystem can implement a form of the negation homomorphic property,

$$\llbracket -t_1 \rrbracket = \text{mod}(\llbracket t_1 \rrbracket^{-1}, n^2) \quad (6)$$

This is particularly useful since in artificial neurons we have negative weights and bias.

Sometimes we may need to add the ciphertext with a plain text, which could be done simply by,

$$\llbracket t_1 \rrbracket + t_2 = \llbracket t_1 \rrbracket + \text{mod}(\llbracket 1 \rrbracket^{-t_2}, n^2) \quad (7)$$

Here, a plaintext is encoded by taking advantage of the ciphertext $\llbracket 1 \rrbracket$ and Eq.(5), without knowing the encryption keys (including public keys).

C. Encrypted Faces

Consider a pattern or image consisting of $W \times H$ pixels, where each pixel is represented by its intensity value x_i . Using Eq.[2], we can then obtain the encrypted big integer $z_i = \llbracket x_i \rrbracket$ for each pixel. Normalizing $\{z_i\}$ by n^2 , we can obtain the whole encrypted images shown in Fig.3. The original images are on the left, and the corresponding encrypted patterns are visualized on the right.

As we can observe from Fig.3, the encrypted patterns are no longer visually identifiable, though each pattern contains exactly the same amount of information as the original images. However, without knowing the keys, no one can decipher the patterns. Hence, data security and privacy can be safely guaranteed, unlike other alternative arrangements in many private learning methods [15-19] that may compromise the security over shared keys between multiple parties.

D. Encrypted Neurons without Keys

Artificial neurons are a simplified model of biological neurons that contain multiple synaptic inputs and one axon output.

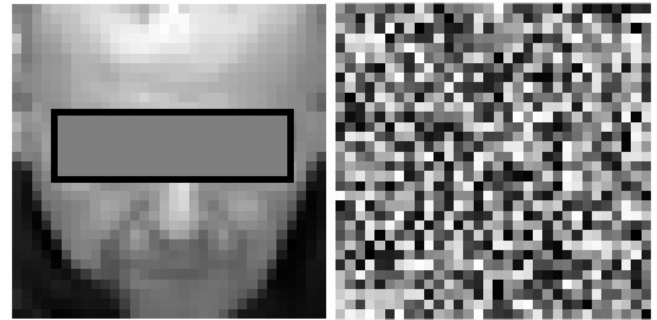


Figure 3. Encrypted digital patterns

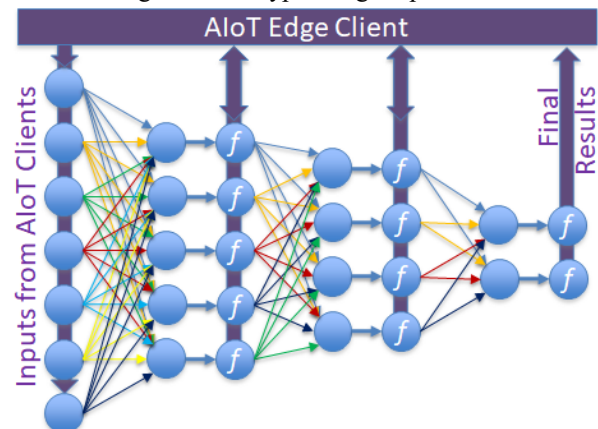


Figure 4. An encryption based private deep neural network running in a server communicating with AIoT edge clients.

The model of an artificial neuron consists of a weighted-sum process that can be described as,

$$y_j = \sum_{i=1}^K w_i x_i + b_j \quad (8)$$

where x_i are the input signals and y_j is the summation result that will be capped by an activation process, typically the sigmoid function,

$$z_j = \frac{1}{1 - e^{-y_j}} \quad (9)$$

z_j denotes the final output from the j -th neuron in a layer.

If we have encrypted inputs $\llbracket x_i \rrbracket$, then the addition process in the above neuron model will be described as,

$$\begin{aligned} \llbracket y_j \rrbracket &= \left\llbracket \sum_{i=1}^K w_i x_i + b_j \right\rrbracket \\ &= \text{mod} \left(\left\llbracket \sum_{i=1}^K w_i x_i \right\rrbracket \cdot \llbracket b_j \rrbracket, n^2 \right) \\ &= \text{mod} \left(\left(\prod_{i=1}^K \llbracket w_i x_i \rrbracket \right) \cdot \llbracket b_j \rrbracket, n^2 \right) \\ &= \text{mod} \left(\left(\prod_{i=1}^K \llbracket x_i \rrbracket^{w_i} \right) \cdot \llbracket b_j \rrbracket, n^2 \right) \end{aligned} \quad (10)$$

Hence, the calculation can be easily carried out directly on the encrypted inputs. Here, we may need to encrypt the bias value in the learned neuron model. To make it simple, we can take advantage of Eq.(5) and obtain,

$$\llbracket b_j \rrbracket = \llbracket 1 \times b_j \rrbracket = \text{mod}(\llbracket 1 \rrbracket^{b_j}, n^2) \quad (11)$$

Hence, we do not need any encryption keys to fulfil the above calculation if the big integer value of $\llbracket 1 \rrbracket$ is given.

The calculation of the activation function in Eq.(9) on encrypted data is a great challenge because it needs to carry out divisions and exponentiations in the encrypted domain. Some attempts adopting various linear approximation have been reported [34, 35]. However, these approximations may introduce unexpected errors. Similarly, the implementation of softmax functions on encrypted data suffers from similar difficulties.

In this paper, we provide an AIoT-based solution to this challenge in privacy-preserving deep learning. Fig.4 shows its schematic view. While the learned model is stored in the server in a layer-wise structure, the activation functions are computed via queries to the AIoT clients in a distributed computing framework, and the computational load is shared by the server and the clients. More details can be found in the following section.

IV. AIOT-BASED INFORMATION THEORETICAL SECURE DEEP FACIAL DIAGNOSIS

With the PHE-enabled encrypted neurons, we can then implement a given neural network layer by layer. Details are described below, based on our proposed AIoT-oriented secure framework.

A. Overall Framework

The overall framework of our proposed AIoT-based facial diagnosis is detailed in the diagram in Fig.5. The central medical service with well-trained deep neural networks resides on a

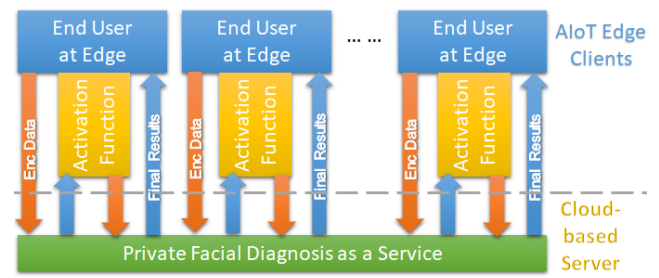


Figure 5. Schematic view of the proposed privacy-protected client-server framework for AIoT edge services.

cloud-based Honest-But-Curious (HBC) server, and AIoT edge clients can upload their encrypted data to the server. The encrypted data is then processed in a layer-wise mode through deep neural networks, and each layer is followed by the activation through the communication with the AIoT clients, as shown in the architecture in Fig.4. The server may host many requests from different AIoT clients in corresponding sessions, as far as it can handle by its computing capability.

The detailed algorithms for the AIoT clients and the facial diagnosis server are listed in List I. In an AIoT server, the Paillier cryptosystem is set up to encrypt the query data for privacy protection. The encrypted data is then sent to the server side for medical diagnosis. The server will then carry out the computation in a layer-wise mode, and at each layer, will send the tentative outputs from each layer back to the client for the computation of activation or softmax, which needs both division and exponential operations. Once the computation at the server side reaches the last layer of deep neural networks, the final result will be sent back to the client and the communication session will be terminated.

In this framework, the server can maintain multiple sessions with different clients, as far as multi-threading is allowed on the cloud server. It is worth noting that all keys (both public and private) are kept only on the client itself, and the computation at the server side is keyless and only needs an encrypted big integer $\llbracket 1 \rrbracket$.

B. Proposed AIoT Edge Service

As shown in Fig.5, the proposed AIoT medical diagnosis framework is based on two-party communication in its computation. Though a server can host many clients, the communication session is based on a client with a communication channel to the server. Hence, there is a need to look into the data privacy issue of the two-party secure computation.

1) Privacy with Information Theoretical Security

An algorithm is defined as information-theoretically secure if its security is proved to match with the derived concept from information theory. The information-theoretical security in communication was termed by Shannon to prove that the one-time pad system achieves perfect security subject to the following two conditions [42]:

- (1) the key which randomizes the data should be random and should be used only once;
- (2) the key length should be at least as long as the length of the data.

If any algorithm randomizes its parameter and satisfies the above conditions, its parameters cannot be unmasked by an adversary even when the adversary has unlimited computing

power. In this case, the system is guaranteed to have information theoretical security. If for example both the plain text and the random ciphertext have 1024 bits, the prior probability (probability for a particular ciphertext out of 2^{1024} possible ciphertexts) and posterior probability (probability of inferring/mapping a ciphertext in a random domain to a plaintext domain) are equal, and there is no advantage for an adversary to get higher posterior probability than prior probability.

In the following sections, we will analyze whether our algorithm in List I is vulnerable to any privacy leakage. Our algorithm is based on two party computation over the AIoT scheme. As defined by Goldreich [43], privacy for secure two-party computation will be achieved if a secure two-party protocol cannot reveal more information to a semi-honest party than the information that can be inferred by looking at that party's input and output. To verify whether the proposed AIoT computation satisfies the privacy definition, we will show the inputs and outputs to and from the client and server, respectively, in the algorithm in List I, and identify what is already known to the client and the server. Following this, if we can prove that nothing else can be inferred other than the known input and output with higher posterior probability than prior probability, the proposed algorithm in List I then satisfies with the privacy definition based on information theory.

The ultimate aim for the client is to keep the test image and the classification result away from the server while the server wants to keep the classification model parameters away from the client. In the communication, the client sends only the encrypted messages to the server with no public keys. From these inputs, the server knows only the size of the test image and the length of encrypted data. This is not a privacy leakage since the server knows the size of the images when training the classifier.

2) Privacy-Preserving Secure Computation at Edge

The overall framework needs its computation to be based on secure operations in both AIoT clients and the server. An honest-but-curious server/client follows the protocol and takes no actions beyond those of an honest server/client. In the proposed framework, let us assume the client knows a vector (data) $\mathbf{a}$ and sends its ciphertext $[\mathbf{a}]$ to the server. The whole system will expect the ciphertext is unbreakable in both the server and any third party. Since the encrypted DNNs at the server side need neither private keys nor public keys, the security of the client data in the proposed AIoT-oriented keyless medical diagnosis system is therefore guaranteed, though asymmetric encryption can be breakable if public keys are available [39, 40].

Theorem 1. The proposed two-party AIoT protocol in List I is information-theoretically secure i.e., the server cannot infer the plaintexts in the client's input vector $[\mathbf{a}]$ and the client will only learn the final result but not the model parameters in the server.

Proof: To validate the security we consider both the client and server are honest-but-curious (HBC) i.e., they will follow the procedures but try to learn about each other's inputs, intermediate values and results. We will then demonstrate that the algorithm in List I is information-theoretically secure for the following two cases in 3) and 4).

3) Honest-But-Curious AIoT-oriented Server

The server computes the results in their encrypted form. Each layer performs a weighted summation, as shown in Eq.(8) and (10). The HBC client sends its encrypted data to the server, and

List I. Algorithms of the proposed framework

Algorithm 1 AIoT Client

Inputs:

- (1) Sample pair D_1 and D_2 for diagnosis
- (2) Client ID uid and password pwd
- (3) Server queries with cmd and XL

Procedure:

- 1: setup bit length Bl and float point length Fl
- 2: setup communication with server using uid and pwd
- 3: **loop** over D_1 & D_2 :
- 4: create public & private keys of Pallier cryptosystem
- 5: encrypt D_k and 1, send to the diagnosis server
- 6: **wait** for the returned data from server: (cmd , XL)
- 7: **if** cmd is "sigmoid"
- 8: calculate $sigm(\langle XL \rangle)$, encrypt & send to server
- 9: **if** cmd is "softmax"
- 10: calculate $softm(\langle XL \rangle)$, encrypt & send to server
- 11: **if** cmd is "results"
- 12: decrypt XL , $R_k = \langle XL \rangle$;
- 13: **end loop**
- 14: **Compare** the scores R_1 and R_2 ;
- 15: **if** $R_1 > R_2$: D_1 is before and D_2 is after DBS;
- 15: **else**: D_2 is before and D_1 is after DBS;
- 16: **close the communication & return**

Algorithm 2 Keyless Private Facial Diagnosis

Inputs:

- (1) Client lists with IDs and Passwords
- (2) Pretrained weights w_{ij} and bias b_j
- (3) From client: Query data $[[D_k]]$ and $[[1]]$

Procedure:

- 1: Setup DNNs with weights w_{ij} and bias b_j ;
- 2: **wait** for the client request;
- 3: verify user and setup the session;
- 4: **wait** for the client data $[[D_k]]$ and $[[1]]$;
- 5: **loop** over layers of the diagnosis DNN:
- 6: calculate $[[y_j]]$ in layer-wise;
- 7: shuffle $[[y_j]]$ over j randomly;
- 8: calculate $[[z_j]]$ by querying the client (*sigmoid*);
- 9: **end loop**
- 10: calculate $[[r_j]]$ by querying the client (*softmax*);
- 11: send the final results back to the client
- 12: **close** the session
- 13: **return** to step 2

the server computes the weighted sum outputs and shuffle them via one time pad, and send them back to the client for the computation. Because the inputs and the outputs are shuffled each time using different one-time pads (step 7 in algorithm 2, List I), the client cannot accumulate the knowledge to solve w_{ij} and b_j in Eq.(8). Hence, there is no privacy leak on model parameters such as weights and bias values in layers, and the communication from the server to the client is perfectly information theoretical secure in term of the server's private model.

4) Honest-But-Curious AIoT-oriented Server

The main purpose in the proposed framework is to protect the data privacy of the individual client from the public medical diagnosis server. In List I, a client encrypts its data and sends the data to the server, and the server carries out its computation

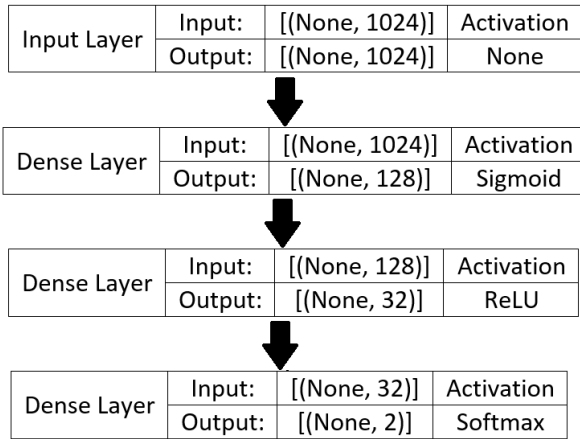
on encrypted data only, and return the encrypted result back to the client, which implies that only the client can know the final results via decryption.

However, as has been suspected [36, 37], asymmetric encryption itself may not be information theoretical secure, since the factorization of a large prime number can be solved via some algorithms [36] in limited time, if the public keys can be known. However, in our proposed algorithms in List I, neither private keys nor public keys are shared with the server. The curious server cannot infer the keys simply from the ciphertext.

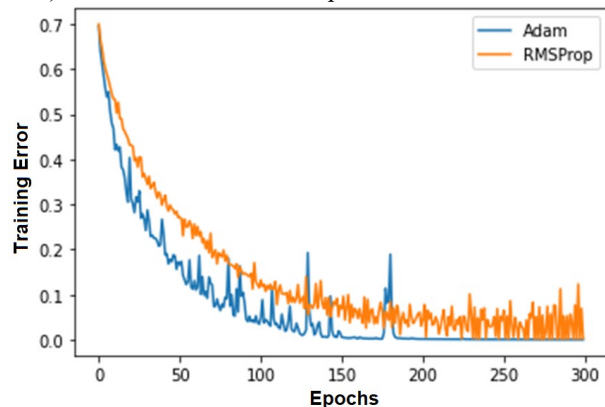
It is worth noting that in the proposed scheme, the encryption



Figure 6. PD DBS facial dataset.



a) The structure of the deep encoder as a classifier



b) Training the classifier in the server side. Two training methods, Adam and RMSProp were used.

Figure 7. Train the deep encoder classifies on the server side.

of 1 needs to be sent to the server. Considering $t=1$, we have

$$c1 = \llbracket 1|r \rrbracket = \text{mod}(gr^n, n^2), \text{ and } c \in Z_{n^2}^* \quad (12)$$

and,

$$1 = \langle c1 \rangle = \text{mod}\left(\frac{\text{mod}(c^\lambda, n^2) - 1}{n} \mu, n\right) \quad (13)$$

In the above equations, g, r, n, c and λ are all unknown to the server side, and these parameters are changed every time based on one time pad strategy. Hence, the server cannot accumulate more knowledge about the encryption parameters from the next ciphertext, and the private data from the client will be information theoretical secure to the server side.

C. Information Theoretical Security in Our Framework

It is noted that though the computation is split between the IoT edge side and the cloud server side, the computation is information secure and neither side can infer from the data for more than necessary information. In the server side, the model weights and bias will not be learned by an edge user because they are randomly shuffled every time in the step 7 in the algorithm 2 in List I. Meanwhile, both public and private keys are unknown to the server side, and therefore a user's own data will not be exposed to the service provider via some cracking algorithms such as Shor's algorithm [36]. Therefore, information theoretical security is guaranteed in both edge client and cloud server sides by our novel implementation.

V. EXPERIMENTS

A. PD DBS Dataset from Youtube

In our experiment, we use a video dataset consisting of 52 PD patients collected from Youtube online resources. Two video shots were taken per patient before and after DBS treatment. From videos, we extract 2345 facial images for our tests, as shown in Fig.6. The facial images were cropped from video shots and resized to 32×32 pixels. The dataset is then split into two subsets – training dataset and test dataset, each having 26 PD patients.

In our experiments, it is assumed that the training dataset is

Table II Evaluation on the cross-subject dataset

Method	Precision	Recall	Acc	F1
Adam	94.88%	94.28%	94.71%	94.54%
RMSProp	96.20%	95.00%	95.22%	95.10%

Confusion Matrix				
Output Class	1	2		
	651 55.6% 32 2.7% 95.3% 4.7%	24 2.0% 464 39.6% 95.1% 4.9%		
	96.4% 3.6%	93.5% 6.5%	95.2% 4.8%	
		Target Class		

Figure 8. Confusion matrix of the facial diagnosis test

owned by the server to train the deep neural networks for medical diagnosis, and the test dataset is owned as private data by AIoT clients. The experiments were set up as a cross-subject facial diagnosis test, while training faces and test faces are from different subjects/patients. Such cross-subject issues are often considered more challenging than the same subject tests (such as recognize a face of a person already in the training dataset).

Our experiments are set up as below. Given two images of a patient, one from before the DBS treatment and one from after the treatment, we want to know:

- (1) Can facial features be used to clearly discriminate which one is before or after DBS treatment?
- (2) Can the proposed lightweight PHE-based solution work properly as an implementation of private deep learning?
- (3) Can our PHE-based solution achieve an accuracy similar to its original non-privacy-preserving peer?

To answer the above questions, our experiments are detailed in the following sections.

B. Facial Diagnosis using Deep Neural Networks

Although facial expression is known to be associated with the degree of Parkinson's, it is yet not used on the evaluation of DBS treatment. To achieve this purpose, we aim to exploit deep neural networks to carry out the facial diagnosis on the patients.

In our experiments, our targets is to demonstrate the proposed PHE based lightweight implementation of deep neural networks over encrypted data. We choose Deep Autoencoder as our classifier because it is the first reported method that enlightened the research on deep learning [44]. Here, we only need the encoder part, as shown in Fig.7-a, a four layer deep neural network architecture with two hidden dense layers. It takes all dimensions of the data as its inputs, and then reduces the number of neurons via the propagation from layer to layer, from 1024, 128 to 32.

In our implementation, the input layer has $32 \times 32 = 1024$ neurons. The 1st hidden layer has 128 neurons with sigmoid activation, and the 2nd hidden layer has 32 neurons with ReLU activation. The output layer with softmax activation has two neurons standing for two classes: before DBS treatment (with apparent PD symptoms) and after DBS treatment (with little PD symptoms).

We used the training dataset (facial images of 26 patients) trained the four layer encoder, and obtained the model parameters. Fig.7-b) shows the convergence of loss rates in the training process. Here, two training methods were applied, Adam and RMSProp. We can see the model trained by RMSProp achieved better accuracy.

Table II shows the valuation on two trained models in term of accuracy, recall, precision and F1 score based on the output likelihoods on two classes. We can see the RMSProp based model achieved a bit better results consistently on all measures. Hence, we use the RMSProp model as our facial diagnosis service model.

Fig.8 shows the confusion matrix of the test results. We can clearly see that the model achieved a nice accuracy over 95%, implying that there are sufficiently explicit facial features to discriminate a PD patient form a recovered patient.

It is worth to note that the diagnosis is based on a single facial photo instead of long shot videos, and the test subjects are all new to the trained model. From the test results, we can

Table III. Prediagnosis using face vs using MRI.

Method	Clinical Cases	Accuracy
EEG Prediagnosis by Oxford [42]	13 Patients	84.62%
Our Facial Prediagnosis	52 Patients	95.22%

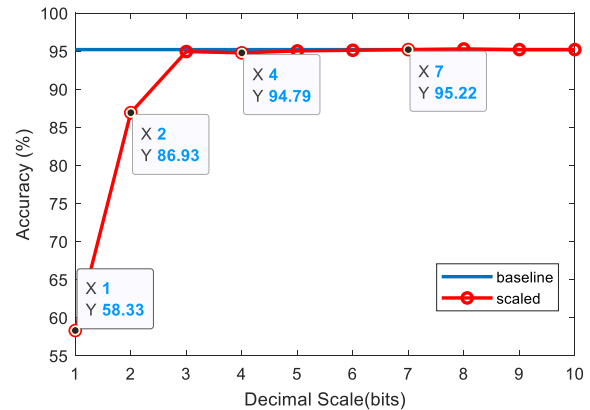


Figure 9. Test accuracy over the decimal precision of the encrypted DNN model parameters.

Table IV. Computational time versus the bit length on server and client, measured in seconds averaged per test image in our experiment.

Bits	256	512	768	1024
Server (s)	42	64	101	146
Clients (s)	1	2	5	9
Total (s)	43	66	106	155

Table V. The estimated computational complexity

Layers	Server	Client
Input	0	$m_0(2C_e + C_m)$
Layer 1	$m_1m_0(C_e + C_m)$	$3m_1(C_e + C_m)$
Layer 2	$m_2m_1(C_e + C_m)$	$3m_2(C_e + C_m)$
Layer 3	$m_3m_2(C_e + C_m)$	$3m_3(C_e + C_m)$
Total	$(m_3m_2 + m_2m_1 + m_1m_0) \times (C_e + C_m)$	$(2m_0 + 3m_1 + 3m_2 + 3m_3)C_e + (m_0 + 3m_1 + 3m_2 + 3m_3)C_m$

Table VI. The communication complexity

Layers	S2C	C2S
Input layer	0	m_0C_{Big}
Layer 1	m_1C_{Big}	m_1C_{Big}
Layer 2	m_2C_{Big}	m_2C_{Big}
Layer 3	m_3C_{Big}	0
Total	$(m_1 + m_2 + m_3) \times C_{Big}$	$(m_0 + m_1 + m_2) \times C_{Big}$

clearly see the trained model can explicitly discriminate the faces of patients before and after DBS treatment, suggesting its potential as an automated medical diagnosis tool for evaluating the severity of PD patients.

In Table III, we compared the facial prediagnosis against the MRI-based prediagnosis in clinical trials. MRI-based preclinical assessment achieved its accuracy around 85%, as reported by an Oxford team from their clinical trial with 13 patients. In comparison, our facial prediagnosis on 52 patients achieved an initial accuracy around 95.22%. It is also worth to highlight that unlike the expensive EEG based diagnosis, facial prediagnosis

could be low-cost, non-interrupting, and available 24/7 remotely with little needs of staff intervention, demonstrating a great potential as a new prediagnosis tool on PD for medical caring services.

C. Encrypted Facial Diagnosis over AIoT Edge

Following the test in the above section, we implemented the encrypted counterpart of the above facial diagnosis model and compare the test results on the encrypted test dataset. Here, a concern issue is about the number of decimal digits that may scale down the model parameters (weights, bias, etc.). The encrypted data from a client was fed to the encrypted DNN model on the server side, and we want to examine if the algorithms in List I can achieve similar accuracy as the original non-privacy-preserving model even with a reduced or limited number of decimal digits.

Fig.9 shows the comparison of the results of the encrypted implementation with different decimal precisions. The decimal precision varies from 1 bit to 10 bit, and we valuated the classification accuracy on the encrypted data. We can see that when decimal bits were reduced to 1 bit (2^{-1} or 0.5), the accuracy was only 58.33%. When the decimal bits were increased to 7 bits, the encryption-based model achieved the same accuracy (95.22%) as its non-privacy preserving original model. Compared with the length of big integer, 7 bits for decimal digits could be a small cost for the overall encryption scheme.

Table IV also gives the experimental results on the computational time in the client and the server, respectively, over various bit lengths of the big integer. Here both client and server were running on a GPU-powered laptop with 3.6GHz CPU. The results show that in the same session, most computational work load (~95%) was assigned to the server side, which is a benefit for AIoT end users offered by the service provider. Typically, the computational time can be linked to the computational complexity, as analyzed below.

D. Computational Complexity

The computational complexity of the algorithm in List I can be estimated as the costs of two types of big integer operations: multiplication operations and modulo exponentiation as C_m and C_e , respectively. Table V list out the estimated complexity of the proposed schemes for both the server (S) and client (C) with regards to the number of neurons per layer (m_0, m_1 , etc.) and the number of synaptic inputs to each neuron (namely the number of neurons in the previous layer, in the architecture illustrated in Fig.4).

In our implementation, the input layer has 32×32 neurons, layer 1 has 128 neurons, layer 2 has 32 neurons and the final layer has 2 neurons. Hence, the total computational costs can be estimated as:

Server side: $(1024 \times 128 + 128 \times 32 + 32 \times 2) \rightarrow 135232 \times (C_e + C_m)$

Client side: $2534 \times C_e + 1510 \times C_m$

We can see most computational workload is assigned to the server side. Assuming $C_e \approx C_m$, the ratio of the workload between the server and a client is $135232/4044 \approx 36.1$, which implies the server copes with 97% of the total computation. This theoretical analysis matches well with the experimental results (~95%) in Table V. Since the cloud-based server has much better computation resources, such a client-server split is reasonable for an AIoT edge-oriented framework.

Besides the computation on the cipher texts, the computational cost on encryption is a constant that is proportional to the number of pixels per facial photo. In this experiment, each photo has $32 \times 32 = 1024$ pixels. Assuming the encryption on each pixel has an encryption cost C_E , the extra computation cost per facial photo will then be $1024C_E$.

E. Communication Complexity

We can measure the total communication complexity in terms of data being communicated between the server and client. In our algorithm, the transferred data between client and server are all in the form of big integer, such as 1024-bit format, as detailed in the secure two-party algorithm proposed in List I. The estimated communication load is summarized in Table VI based on a layer-wise estimation in term of the communication costs of a single 1024-bit big integer, C_{Big} .

Similarly, since the input layer has 32×32 neurons, layer 1 has 128 neurons, layer 2 has 32 neurons and the final layer has 2 neurons, the total communication costs can be estimated as:

Server to client: $162 \times C_{Big}$

Client to server: $1184 \times C_{Big}$

In total, the communication bandwidth needs to cope with $1346 \times C_{Big} = 1346 \times 1024 \text{bits} = 1.378 \text{Mbits}$. If we process video streams at 25 frames per seconds, the highest bandwidth needs to be around 35 Mbps. Currently 5G-based AIoT can easily achieve 100+ Mbps. Hence, the communication complexity in our proposed AIoT framework is achievable even in the case of considering real-time video streaming, although our facial diagnosis carries out on single image based classification.

VI. CONCLUSION AND FUTURE WORK

In conclusion, we have demonstrated a novel AIoT-oriented medical diagnosis framework using deep learning and PHE that can achieve Shannon's information theoretical security. In our proposed scheme, the encrypted DNNs at the server side were implemented without the needs for encryption keys, guaranteeing the client data has information theoretical security; the intermediate results from the server to a client were shuffled randomly, making the model unknown to the client, too. Hence, the information theoretical security at both server and client ends is guaranteed via our proposed framework, showing a promising merit toward the privacy protection on exploiting EHR/EMR data for wide medical services.

It is also worth noting that, with the 95.22% accuracy of our facial prediagnosis model, we verified that facial prediagnosis could be a valuable medical tool with a potential to evaluate the severity of PD patients. Consequently, we offered a novel low-cost method for the preclinical assessment on PD with an initial proof-of-concept test showing the underlying links between facial features and PD symptoms. One of our future tasks is to explicitly expand our deep facial prediagnosis to an explainable model, to help identify which part of facial features are linked to the severity of PDs.

Besides, we reported our facial prediagnosis model with a clinical trial on 52 PD patients before and after DBS treatment, which could also be valuable and interesting for many medical researchers, doctors, or clinical consultants. In the future work, a more clear evaluation on how facial features can be linked to evaluate the improvement of PD treatments can be further

studied, aiming to bring Explainable AI and Fair AI into this privacy-sensitive topic [46].

ACKNOWLEDGMENT

This work was supported in part by Grant (EP/P009727/1) from the EPSRC and Grant (RF-2019-492) from the Leverhulme Trust, and the Grant 1946391 by the US National Science Foundation.

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